

# 1 Introduction

This is a simple document to get you up and running with L<sup>A</sup>T<sub>E</sub>X. See the *fuzz* manual (<http://spivey.oriel.ox.ac.uk/mike/fuzz/fuzzman.pdf>) for a good introduction to the symbols we use.

## 2 Maths

We drop into math-font simply: the variable,  $x \in \{1, 2, 3\}$ .

## 3 Types, etc.

This is a basic definition:

[A]

This is a free type definition:

$B ::= b1 \mid b2$

This is an axiomatic definition:

$$\frac{\begin{array}{c} var_1, var_2 : B \\ \hline var_1 \neq var_2 \end{array}}{var_1 \neq var_2}$$

This is an abbreviation:

$Pair == A \times B$

And here's a generic axiomatic definition:

$$\frac{\begin{array}{c} [X, Y] \\ \hline \begin{array}{c} first : (X \times Y) \rightarrow X \\ second : (X \times Y) \rightarrow Y \end{array} \\ \hline \begin{array}{c} \forall x : X; y : Y \bullet first(x, y) = x \\ \forall x : X; y : Y \bullet second(x, y) = y \end{array} \end{array}}{\forall x : X; y : Y \bullet first(x, y) = x \wedge second(x, y) = y}$$

## 4 Proofs

This is how to format a proof:

$$\begin{aligned} & (1 \times 2) + 3 \\ &= 2 + 3 \quad [\text{definition of multiplication}] \\ &= 5 \quad [\text{definition of addition}] \end{aligned}$$

## 5 Proof trees

$$\frac{\frac{[p \wedge p]^{[1]}}{p} [\wedge\text{-elim}]}{(p \wedge p) \Rightarrow p} [\Rightarrow\text{-intro}^{[1]}]$$

$$\frac{p \vee q \quad \frac{[p]^{[1]}}{q \vee p} [\vee\text{-intro}] \quad \frac{[q]^{[1]}}{q \vee p} [\vee\text{-intro}]}{q \vee p} [\vee\text{-elim}^{[1]}]$$

Here's an example from the solutions.

In one direction:

$$\frac{\frac{\frac{\frac{[p \wedge r]^{[4]}}{p} [\wedge\text{-elim1}] \quad \frac{[p \wedge r]^{[4]}}{r} [\wedge\text{-elim2}]}{p \wedge (q \vee r)} [\wedge\text{-intro}]}{\frac{[p \wedge q]^{[4]}}{p} [\wedge\text{-elim1}] \quad \frac{[p \wedge q]^{[4]}}{q} [\wedge\text{-elim2}]} [\wedge\text{-intro}]}{\frac{[(p \wedge q) \vee (p \wedge r)]^{[3]}}{\frac{p \wedge (q \vee r)}{((p \wedge q) \vee (p \wedge r)) \Rightarrow (p \wedge (q \vee r))} [\Rightarrow\text{-intro}^{[3]}]}} [\vee\text{-elim}^{[4]}]$$

and the other:

$$\frac{\frac{\frac{\frac{[p \wedge (q \vee r)]^{[1]}}{p} [\wedge\text{-elim1}] \quad [r]^{[2]} [\wedge\text{-intro}]}{p \wedge r} [\vee\text{-intro2}]}{(p \wedge q) \vee (p \wedge r)} \quad \left| \begin{array}{c} \frac{\frac{[p \wedge (q \vee r)]^{[1]}}{p} [\wedge\text{-elim1}] \quad [q]^{[2]} [\wedge\text{-intro}]}{p \wedge q} [\vee\text{-intro1}] \\ \left| \frac{[p \wedge (q \vee r)]^{[1]}}{q \vee r} [\wedge\text{-elim2}] }{q \vee r} \end{array} \right. }{(p \wedge (q \vee r)) \Rightarrow ((p \wedge q) \vee (p \wedge r))} [\vee\text{-elim}^{[2]}] \quad [\Rightarrow\text{-intro}^{[1]}]$$