

Phase 3 : Quantifiers and Mathematical Notation

Example 1 : Quantifiers

(a)

$$\forall x: N \bullet x \geq 0$$

(b)

$$\exists y: N \bullet y = 0$$

(c)

$$\forall n: N \bullet n \geq 0 \wedge n < 100$$

Example 2 : Subscripts and Superscripts

(a)

$$x^2$$

(b)

$$a_1$$

(c)

$$x_i^2$$

Example 3 : Comparison Operators

(a)

$$x < 10$$

(b)

$$x \geq 0 \wedge x \leq 100$$

(c)

$$y > 5 \vee y = 0$$

Example 4 : Set Operators

(a)

$$x \in N$$

(b)

$$A \subseteq B$$

(c)

$$A \cup B \cap C$$

Example 5 : Complex Expressions

(a)

$$\begin{aligned} \forall x: N \bullet x \in N \wedge x \geq 0 \\ \Leftrightarrow \forall x: N \bullet x \geq 0 \end{aligned}$$

(b)

$$\forall i: N \bullet a_i > 0 \Rightarrow a_i^2 > 0$$

(c)

$$\frac{\begin{array}{ccc} p & q & p \Rightarrow q \\ \hline t & t & t \\ t & f & f \\ f & t & t \\ f & f & t \end{array}}{}$$