

## Phase 18 Demo : Partial Function Operators

### Example 1 : $\text{---}_i$ operator ( partial injection )

Basic function type with  $\text{---}_i$  operator:

$$\left| \begin{array}{l} f : N \rightsquigarrow N \\ \hline \text{dom } f = \{1, 2, 3\} f(1) = 10 f(2) = 20 f(3) = 30 \end{array} \right|$$

### Example 2 : $\text{+}_i$ operator ( partial function )

Basic function type with  $\text{+}_i$  operator:

$$\left| \begin{array}{l} g : N \rightarrowtail N \\ \hline \text{dom } g = \{1, 2\} g(1) = 100 g(2) = 200 \end{array} \right|$$

### Example 3 : Complex types with $\text{---}_i$

Using  $\text{---}_i$  with custom types:

$$[Year, Entry]$$

*abbrev*

Table == seq *Entry*

$$\left| \begin{array}{l} records : Year \rightsquigarrow Table \\ \hline \text{dom } records = \{1993, 1994, 1995\} \end{array} \right|$$

### Example 4 : Mixed function type operators

Different function type operators:

$$\left| \begin{array}{l} total : N \rightarrow N \\ partial : N \rightarrowtail N \\ injection : N \rightsquigarrow N \end{array} \right|$$