

## Phase 12 : Sequences , Bags , and Tuple Projection

### Example 1 : Sequence Literals

(a)

Empty sequence

$\langle \rangle$

(b)

Single element

$\langle a \rangle$

(c)

Multiple elements

$\langle 1, 2, 3, 4, 5 \rangle$

(d)

Sequence of identifiers

$\langle x, y, z \rangle$

### Example 2 : Sequence Operators

(a)  $\langle 1, 2, 3 \rangle$

(b)  $\langle 1, 2, 3 \rangle$

(c)  $\langle 1, 2, 3 \rangle$

(d)  $\langle 1, 2, 3 \rangle$

(e)  $\langle 1, 2, 3 \rangle$

### Example 3 : Sequence Concatenation

(a)  $\langle 1, 2 \rangle \cap \langle 3, 4 \rangle$

(b)  $s \cap t \cap u$

(c)  $\langle a \rangle \cap \langle b, c \rangle \cap \langle d \rangle$

### Example 4 : Tuple Projection

(a)  $x.1$

(b)  $x.2$

(c)  $(a, b, c).1$

(d)  $(a, b, c).2$

### Example 5 : Bag Literals

(a)  $[\![x]\!]$

- (b)  $\llbracket 1, 2, 3 \rrbracket$
- (c)  $\llbracket a, b, c \rrbracket$
- (d)

Bags with duplicates

$\llbracket 1, 2, 2, 3, 3, 3 \rrbracket$

#### Example 6 : Sequences in Expressions

- (a)  $x \in \langle 1, 2, 3 \rangle$
- (b)  $s = a$
- (c)  $\langle 1, 2, 3 \rangle = \langle 2, 3 \rangle$

#### Example 7 : Complex Expressions

- (a)  $\forall i: \mathbb{N} \bullet i \in \langle 1, 2, 3 \rangle \Rightarrow i > 0$
- (b)  $\exists s: seq[\mathbb{N}] \bullet s = 1$
- (c)  $\{x: \mathbb{N} \mid x > 0 \bullet \langle x, x^2 \rangle\}$

#### Example 8 : Real Examples

- (a)

From Solution 37

- $\langle a \rangle$
- (b)

Tuple projection from Solution 38

- $trains(x).2$
- (c)

Bags from Solution 39

$\llbracket d \rrbracket$