

## Phase 18 Demo : Partial Function Operators

**Example 1 : ---; operator ( partial injection )**

Basic function type *with*  $\leftrightarrow$  operator:

$$\frac{f : \mathbb{N} \leftrightarrow \mathbb{N}}{\text{dom } f = \{1, 2, 3\} f(1) = 10 f(2) = 20 f(3) = 30}$$

**Example 2 : +-; operator ( partial function )**

Basic function type *with*  $\rightarrow$  operator:

$$\frac{g : \mathbb{N} \rightarrow \mathbb{N}}{\text{dom } g = \{1, 2\} g(1) = 100 g(2) = 200}$$

**Example 3 : Complex types with ---;**

*Using*  $\leftrightarrow$  *with* custom types:

$[Year, Entry]$

Table == seq *Entry*

$$\frac{\text{records} : Year \leftrightarrow Table}{\text{dom records} = \{1993, 1994, 1995\}}$$

**Example 4 : Mixed function type operators**

Different function type operators:

$$total : \mathbb{N} \rightarrow \mathbb{N} \\ partial : \mathbb{N} \rightarrow \mathbb{N} \\ injection : \mathbb{N} \leftrightarrow \mathbb{N}$$