

## Phase 19 Demo : Finite Set Types

### Example 1 : F ( finite sets )

$F X$  denotes all finite subsets of  $X$ :

$$[SongId, UserId]$$

$$\mid songs : F SongId users : F UserId$$

### Example 2 : F1 ( non - empty finite sets )

$F1 X$  denotes all non-empty finite subsets of  $X$ :

$$\mid \begin{array}{l} activeUsers : F_1 UserId \\ \hline activeUsers(subseteq)(users) \end{array}$$

### Example 3 : Combined with function types

Using  $F$  and  $F1$  with partial functions:

$$[PlaylistId, Playlist]$$

$$\mid \begin{array}{l} playlists : PlaylistId \rightarrow \text{Playlist} \\ \text{playlistOwner} : PlaylistId \rightarrow UserId \\ \text{playlistSubscribers} : PlaylistId \rightarrow F_1 UserId \\ \hline \text{dom playlistOwner}(subseteq)(\text{dom playlists}) \text{ dom playlistSubscribers}(subseteq)(\text{dom playlists}) \forall i : \text{dom playlistSubscribers} \end{array}$$

### Example 4 : Comparison with P ( power set )

$F X$  is a subset of  $P X$  (all finite subsets are subsets):

$$\mid \begin{array}{l} \overline{\mathbb{F} users(subseteq)(\mathbb{P} users)} \\ \mathbb{F}_1 users(subseteq)(\mathbb{F} users) \end{array}$$