

## Phase 18 Demo : Partial Function Operators

### Example 1 : $\dashv\!\!\rightarrow$ operator ( partial injection )

Basic function type *with*  $\dashv\!\!\rightarrow$  operator:

$$\frac{\left| \begin{array}{l} f : \mathbb{N} \dashv\!\!\rightarrow \mathbb{N} \end{array} \right.}{\text{dom } f = \{1, 2, 3\} f(1) = 10 f(2) = 20 f(3) = 30}$$

### Example 2 : $\dashv\!\!\rightarrow$ operator ( partial function )

Basic function type *with*  $\dashv\!\!\rightarrow$  operator:

$$\frac{\left| \begin{array}{l} g : \mathbb{N} \dashv\!\!\rightarrow \mathbb{N} \end{array} \right.}{\text{dom } g = \{1, 2\} g(1) = 100 g(2) = 200}$$

### Example 3 : Complex types with $\dashv\!\!\rightarrow$

*Using*  $\dashv\!\!\rightarrow$  *with* custom types:

$[Year, Entry]$

Table == seq *Entry*

$$\frac{\left| \begin{array}{l} records : Year \dashv\!\!\rightarrow Table \end{array} \right.}{\text{dom } records = \{1993, 1994, 1995\}}$$

### Example 4 : Mixed function type operators

Different function type operators:

$$\left| \begin{array}{l} total : \mathbb{N} \rightarrow \mathbb{N} \text{partial} : \mathbb{N} \rightarrow \mathbb{N} \text{injection} : \mathbb{N} \dashv\!\!\rightarrow \mathbb{N} \end{array} \right|$$