

# 1 Introduction

This is a simple document to get you up and running with L<sup>A</sup>T<sub>E</sub>X. See the *fuzz* manual (<http://spivey.orient.ox.ac.uk/mike/fuzz/fuzzman.pdf>) for a good introduction to the symbols we use.

# 2 Maths

We drop into math-font simply: the variable,  $x \in \{1, 2, 3\}$ .

# 3 Types, etc.

This is a basic definition:

$[A]$

This is a free type definition:

$B ::= b1 \mid b2$

This is an axiomatic definition:

$$\frac{\mid \quad var_1, var_2 : B}{\mid \quad var_1 \neq var_2}$$

This is an abbreviation:

$Pair == A \times B$

And here's a generic axiomatic definition:

$[X, Y]$
$first : (X \times Y) \rightarrow X$
$second : (X \times Y) \rightarrow Y$
$\forall x : X; y : Y \bullet first(x, y) = x$
$\forall x : X; y : Y \bullet second(x, y) = y$

# 4 Proofs

This is how to format a proof:

$(1 \times 2) + 3$	
$= 2 + 3$	[definition of multiplication]
$= 5$	[definition of addition]

## 5 Proof trees

$$\frac{\frac{[p \wedge p]^{[1]}}{p} [\wedge\text{-elim}]}{(p \wedge p) \Rightarrow p} [\Rightarrow\text{-intro}^{[1]}]$$

$$\frac{p \vee q \quad \frac{[p]^{[1]}}{q \vee p} [\vee\text{-intro}] \quad \frac{[q]^{[1]}}{q \vee p} [\vee\text{-intro}]}{q \vee p} [\vee\text{-elim}^{[1]}]$$

Here's an example from the solutions.  
In one direction:

$$\frac{\frac{\frac{[p \wedge q]^{[4]}}{p} [\wedge\text{-elim1}] \quad \frac{\frac{[p \wedge q]^{[4]}}{q} [\wedge\text{-elim2}] \quad \frac{q}{q \vee r} [\vee\text{-intro1}]}{q \vee r} [\wedge\text{-intro}]}{p \wedge (q \vee r)} \quad \frac{\frac{\frac{[p \wedge r]^{[4]}}{p} [\wedge\text{-elim1}] \quad \frac{\frac{[p \wedge r]^{[4]}}{r} [\wedge\text{-elim2}]}{q \vee r} [\vee\text{-intro2}]}{p \wedge (q \vee r)} [\wedge\text{-intro}]}{[(p \wedge q) \vee (p \wedge r)]^{[3]} \quad p \wedge (q \vee r)} [\vee\text{-elim}^{[4]}] \\ ((p \wedge q) \vee (p \wedge r)) \Rightarrow (p \wedge (q \vee r))} [\Rightarrow\text{-intro}^{[3]}]$$

and the other:

$$\begin{array}{c}
\frac{\frac{[p \wedge (q \vee r)]^{[1]}}{p} [\wedge\text{-elim1}] \quad \frac{[r]^{[2]}}{[\wedge\text{-intro}]} \quad \frac{p \wedge r}{(p \wedge q) \vee (p \wedge r)} [\vee\text{-intro2}]}{\frac{[p \wedge (q \vee r)]^{[1]}}{p} [\wedge\text{-elim1}] \quad \frac{[q]^{[2]}}{[\wedge\text{-intro}]} \quad \frac{p \wedge q}{(p \wedge q) \vee (p \wedge r)} [\vee\text{-intro1}]} \\
\frac{\frac{[p \wedge (q \vee r)]^{[1]}}{q \vee r} [\wedge\text{-elim2}] \quad \frac{(p \wedge q) \vee (p \wedge r)}{(p \wedge (q \vee r)) \Rightarrow ((p \wedge q) \vee (p \wedge r))} [\Rightarrow\text{-intro}^{[1]}]}{\frac{(p \wedge q) \vee (p \wedge r)}{(p \wedge (q \vee r)) \Rightarrow ((p \wedge q) \vee (p \wedge r))} [\vee\text{-elim}^{[2]}]}
\end{array}$$