

## Phase 9 : Generic Parameters

This example demonstrates Z notation definitions with generic (polymorphic) type parameters.

Basic generic abbreviation for a Pair type:

$$\text{Pair}[X] == X \times X$$

Generic abbreviation with two type parameters:

$$\text{Product}[X, Y] == X \times Y$$

Generic axiomatic definition with constraints:

$$\begin{array}{c} \overline{[T]} = \\ \overline{\text{identity} : T} \\ \hline \text{identity} = \text{identity} \end{array}$$

Generic schema for a collection:

$$\begin{array}{c} \overline{\text{Collection}[X]} = \\ \overline{\text{items} : \text{seq } X} \\ \overline{\text{count} : \mathbb{N}} \\ \hline \text{count} = \#\text{items} \end{array}$$

Generic schema with multiple parameters:

$$\begin{array}{c} \overline{\text{Tuple}[X, Y]} = \\ \overline{\text{first} : X} \\ \overline{\text{second} : Y} \\ \hline \end{array}$$

Non-generic definitions still work as before:

$$\text{Naturals} == \mathbb{N}$$

$$\begin{array}{c} \overline{\text{zero} : \mathbb{N}} \\ \hline \text{zero} = 0 \end{array}$$

$$\begin{array}{c} \overline{\text{Counter}} = \\ \overline{\text{value} : \mathbb{N}} \\ \hline \text{value} \geq 0 \end{array}$$