

$$variables = \begin{array}{c} \mathbf{Bid} \quad P_H \quad P_G \quad P_P \quad E \quad d \quad T \quad P_{DL} \\ \left[\begin{array}{cccccccc} x0 & x1 & x2 & x3 & x4 & x5 & x6 & x7 \end{array} \right] \end{array}$$

$$\begin{array}{l|ll|l} Bid_i & 0 & & x_0 \\ P_{Hs} & 1 & s & x_1 \\ P_{Gs} & s+1 & 2s & x_2 \\ P_{Ps} & 2s+1 & 3s & x_3 \\ E_s & 3s+1 & 4s & x_4 \\ d_s & 4s+1 & 5s & x_5 \\ T_s & 5s+1 & 6s & x_6 \\ P_{DLs} & 6s+1 & 7s & x_7 \end{array}$$

Equations:

Eq. 0: Market Bid for period $i \Rightarrow [0 : s - 1]$

$$Bid_i = P_{Hs,i} + P_{Gs,i}$$

$$Eq. 0 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 1 & -1 & -1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$b = [0]$$

Eq. 1: Initial Reservoir Level $\Rightarrow [s : 2s - 1]$

\hookrightarrow 1st hour

$$E_{s,1} = past_reservoir_level$$

$$Eq. 1 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

$$b = [e_begin]$$

Eq. 2: Reservoir level $\Rightarrow [2s : 3s - 1]$

\hookrightarrow remaining hours

$$E_{s,i} = E_{s,i-1} + t \cdot \left[\eta_P \cdot P_{Ps,i-1} - \frac{P_{Hs,i-1}}{\eta_H} \right]$$

$$Eq. 2 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 1_{t-1} \cdot \frac{t}{\eta_H} & 0 & -1_{t-1} \cdot \eta_P \cdot t & -1_{t-1} & 0 & 0 & 0 \end{bmatrix}$$

$$b = [0]$$

Eq. 3: Imbalance for every scenario $\Rightarrow [3s : 4s - 1]$

$$d_{s,i} = P_{Gs,i} - P_{Ws,i} + P_{Ps,i} + P_{DLs,i}$$

$$Eq. 4 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \end{bmatrix}$$

$$b = [P_{Ws,i}]$$

Inequalities:

Ine. 0: Hydro Generation $\Rightarrow [0 : s - 1]$

$$P_{Hs,i} \leq \eta_H \cdot \left[\frac{E_{s,i}}{t} + \eta_P \cdot P_{Ps,i} \right]$$

$$Ad. 0 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 1 & 0 & -t \cdot \eta_H \cdot \eta_P & -\frac{\eta_H}{t} & 0 & 0 & 0 \end{bmatrix}$$

$$bd = [0]$$

Ine. 1: Epigraph Form (1) $\Rightarrow [s : 2s - 1]$

$$d_{s,i} \cdot (p_i - p_i^+) \leq T_{s,i}$$

$$Ad. 1 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 0 & 0 & 0 & 0 & p - p_{plus} & -1 & 0 \end{bmatrix}$$

$$bd = [0]$$

Ine. 2: Epigraph Form (2) $\Rightarrow [2s : 3s - 1]$

$$-d_{s,i} \cdot (p_i^- - p_i) \leq T_{s,i}$$

$$Ad. 2 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 0 & 0 & 0 & 0 & p_{minus} - p & -1 & 0 \end{bmatrix}$$

$$bd = [0]$$

Ine. 3: Hydro + Pump Constraint $\Rightarrow [3s : 4s - 1]$

$$P_{Hs,i} + P_{Ps,i} \leq P_H^M$$

$$Ad. 3 = \begin{bmatrix} Bid_i & P_{Hs,i} & P_{Gs,i} & P_{Ps,i} & E_{s,i} & d_{s,i} & T_{s,i} & P_{DLs,i} \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$bd = [P_H^M]$$