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1  # Groundwater Modeling Coding Assignment #2
2  # Jim Finnegan
3  # 1D Transport Equation
4  # Finite Element Method
5
6  # SETUP
7  import numpy as np
8  from matplotlib import pyplot as plt
9
10 # PARAMETERS
11 # user inputs
12 D = float(input('Enter D (m^2/d): '))
13 R = float(input('Enter R: '))
14 # other parameters
15 v, L, dx, t, dt = 0.5, 200, 2, 400, 10
16 # matrix dimensions
17 rows = int(t / dt) + 1
18 n_el = int(L / dx)
19 cols = n_el + 1
20 # initial conditions
21 C = np.zeros((rows, cols))
22 C[:, 0] = 1 # boundary condition: C/C0 = 1 at x=0
23
24 # CONSTRUCT STIFFNESS AND STORAGE MATRICES
25 # element matrices
26 alpha = (R * dx) / 6
27 lam_1 = D / dx
28 lam_2 = v / 2
29 Ae = [[lam_1 - lam_2, -lam_1 + lam_2], [-lam_1 - lam_2, lam_1 + lam_2]] #
    element stiffness matrix
30 Be = [[2 * alpha, alpha], [alpha, 2 * alpha]] #
    element storage matrix
31 # global matrices
32 A = np.zeros((cols, cols))
33 B = np.zeros((cols, cols))
34 for i in range(1, cols):
35     A[i, i] += Ae[1][1] # assemble Ae elements
36     A[i, i - 1] += Ae[1][0]
37     A[i - 1, i] += Ae[0][1]
38     A[i - 1, i - 1] += Ae[0][0]
39     B[i, i] += Be[1][1] # assemble Be elements
40     B[i, i - 1] += Be[1][0]
41     B[i - 1, i] += Be[0][1]
42     B[i - 1, i - 1] += Be[0][0]
43 LH = (A/2 + B/dt)
44 RH = (-A/2 + B/dt)
45
46 # TIME STEPPING
47 for k in range(1, rows):
48     b_f = np.dot(RH, C[k-1, :]) # solve RHS
49     b_f[0] = LH[0][0] + LH[0][1]*C[k-1][1] # boundary condition
50     C[k, :] = np.linalg.solve(LH, b_f) # solve LHS
51
52 # PLOT
53 x = np.linspace(0, L, num=cols)
54 plt.plot(x, C[0, :])
55 plt.plot(x, C[10, :])
56 plt.plot(x, C[20, :])
57 plt.plot(x, C[30, :])
58 plt.plot(x, C[40, :])

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59
60 title_string = 'Finite element solution\n' + 'D = ' + str(D) + ', R = ' +
    str(R)
61 plt.title(title_string)
62 plt.xlabel('distance (m)')
63 plt.ylabel('C/C0')
64 plt.legend(['0 days', '100 days', '200 days', '300 days', '400 days'])
65 plt.show()
66
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