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1 # Groundwater Modeling Coding Assignment #2
2 # Jim Finnegan
3 # 1D Transport Equation
4 # Finite Difference Method
5 import numpy as np
6 from scipy.sparse import diags
7 from matplotlib import pyplot as plt
8
9 # user inputs
10 D = float(input('Enter D (m^2/d): '))
11 R = float(input('Enter R: '))
12
13 # other parameters
14 v, L, dx, t, dt = 0.1, 200, 2, 400, 10
15 # matrix dimensions
16 rows = int(t / dt) + 1
17 cols = int(L / dx) + 1
18
19 # initial conditions
20 C0 = np.zeros(cols)
21 C = np.zeros((rows, cols))
22 C[:, 0] = 1 # boundary condition: C/C0 = 1 at x=0
23
24 # simplified variables from central difference derivation
25 G = (D * dt) / (2 * R * dx**2)
26 H = (v * dt) / (4 * R * dx)
27 lam_1, lam_2, lam_3, lam_4 = G + H, 2*G + 1, G - H, 2*G - 1
28
29 # CENTERED DIFFERENCE SCHEME
30 # Left hand side - k+1
31 A_diagonals = [np.ones(cols-1)*lam_1, np.ones(cols)*-lam_2, np.ones(
    cols-1)*lam_3]
32 A = diags(A_diagonals, offsets=[-1, 0, 1], shape=(cols, cols)).
    toarray()
33 # Right hand side - k
34 B_diagonals = [np.ones(cols-1)*-lam_1, np.ones(cols)*lam_4, np.ones(
    cols-1)*-lam_3]
35 B = diags(B_diagonals, offsets=[-1, 0, 1], shape=(cols, cols)).
    toarray()
36
37
38 for k in range(1, rows):
39     b = np.dot(B, C[k-1, :]) # solve RHS
40     C[k, :] = np.linalg.solve(A, b) # solve LHS
41     C[k][0] = 1 # boundary condition
42 print('Centered difference results: ')
43 print(C)
44
45 x = np.linspace(0, L, num=cols)
46 plt.plot(x, C[0, :])
47 plt.plot(x, C[10, :])
48 plt.plot(x, C[20, :])
49 plt.plot(x, C[30, :])
50 plt.plot(x, C[40, :])
51

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52 plt.xlabel('distance (m)')
53 plt.ylabel('C/C0')
54 plt.legend(['0 days', '100 days', '200 days', '300 days', '400 days'
    ])
55 plt.show()
56
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