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1 # Groundwater Modeling Coding Assignment #2
2 # Jim Finnegan
3 # 1D Transport Equation
4 # Analytical Solution
5
6 import numpy as np
7 from math import exp, sqrt
8 from scipy.special import erfc
9 from matplotlib import pyplot as plt
10
11 # initial conditions
12 # for R = 1
13 v = 0.1
14 D = float(input('Enter D (m^2/d): '))
15 L, dx = 200, 2
16 dist = np.linspace(2, L, num=int(L/dx))
17 dist = [int(x) for x in dist]
18 # print(dist)
19 t, dt = 400, 10
20 time = np.linspace(10, t, num=int(t/dt))
21 time = [int(t) for t in time]
22 # print(time)
23
24 # initialize grid for C
25 # x is distance (one column is 2 ft), y is time (one row is 10 days)
26 C = np.zeros((len(time)+1, len(dist)+1))
27 C[:, 0] = 1 # boundary condition: C/C0 = 1 at x=0
28
29 # calculate C using analytical solution for all x>0
30 for x in range(len(dist)):
31     for t in range(len(time)):
32         C[t+1][x+1] = (1/2)*(exp(v*dist[x]/D)*erfc((dist[x]+v*time[t])/(2*
            sqrt(D*time[t])))+erfc((dist[x]-v*time[t])/(2*sqrt(D*time[t]))))
33
34 # plot
35 dist.insert(0, 0)
36 plt.plot(dist, C[0, :])
37 plt.plot(dist, C[10, :])
38 plt.plot(dist, C[20, :])
39 plt.plot(dist, C[30, :])
40 plt.plot(dist, C[40, :])
41
42 title_string = 'Analytical solution\n' + 'D = ' + str(D) + ', R = 1'
43 plt.title(title_string)
44 plt.xlabel('distance (m)')
45 plt.ylabel('C/C0')
46 plt.legend(['0 days', '100 days', '200 days', '300 days', '400 days'])
47 plt.show()
48

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