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1 # Groundwater Modeling Coding Assignment #2
2 # Jim Finnegan
3 # 1D Transport Equation
4 # Finite Difference Method
5 import numpy as np
6 from scipy.sparse import diags
7 from matplotlib import pyplot as plt
8
9 # user inputs
10 D = float(input('Enter D (m^2/d): '))
11 R = float(input('Enter R: '))
12
13 # other parameters
14 v, L, dx, t, dt = 0.1, 200, 2, 400, 10
15 # matrix dimensions
16 rows = int(t / dt) + 1
17 cols = int(L / dx) + 1
18
19 # initial conditions
20 C = np.zeros((rows, cols))
21 C[:, 0] = 1 # boundary condition: C/C0 = 1 at x=0
22
23 # simplified variables from central difference derivation
24 G = (D * dt) / (2 * R * dx**2)
25 H = (v * dt) / (4 * R * dx)
26 lam_1, lam_2, lam_3, lam_4 = G + H, 2*G + 1, G - H, 2*G - 1
27
28 # CENTERED DIFFERENCE SCHEME
29 # Left hand side - k+1
30 A_diagonals = [np.ones(cols-1)*lam_1, np.ones(cols)*-lam_2, np.ones(cols-1)*
    lam_3]
31 A = diags(A_diagonals, offsets=[-1, 0, 1], shape=(cols, cols)).toarray()
32 # Right hand side - k
33 B_diagonals = [np.ones(cols-1)*-lam_1, np.ones(cols)*lam_4, np.ones(cols-1)*
    lam_3]
34 B = diags(B_diagonals, offsets=[-1, 0, 1], shape=(cols, cols)).toarray()
35
36
37 for k in range(1, rows):
38     b = np.dot(B, C[k-1, :]) # solve RHS
39     b[0] = -(1 + lam_1) # boundary condition
40     C[k, :] = np.linalg.solve(A, b) # solve LHS
41
42 x = np.linspace(0, L, num=cols)
43 plt.plot(x, C[0, :])
44 plt.plot(x, C[10, :])
45 plt.plot(x, C[20, :])
46 plt.plot(x, C[30, :])
47 plt.plot(x, C[40, :])
48
49 title_string = 'Finite difference solution\n' + 'D = ' + str(D) + ', R = ' +
    str(R)
50 plt.title(title_string)
51 plt.xlabel('distance (m)')
52 plt.ylabel('C/C0')
53 plt.legend(['0 days', '100 days', '200 days', '300 days', '400 days'])
54 plt.show()
55

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