

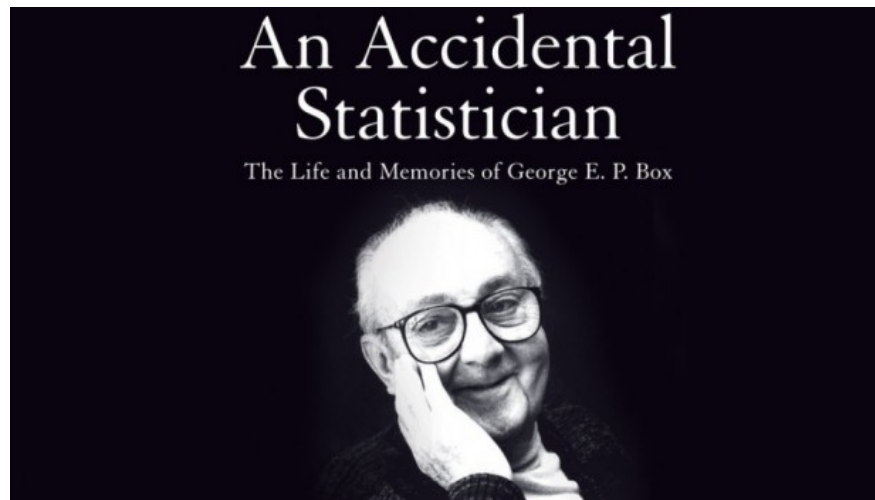
# Stochastic Thinking and Random Walks, Segment 3

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# Simulation Models

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- A description of computations that provide useful information about the possible behaviors of the system being modeled
- Descriptive, not prescriptive
- Only an approximation to reality
- “All models are wrong, but some are useful.” – George Box



# Simulations Are Used a Lot

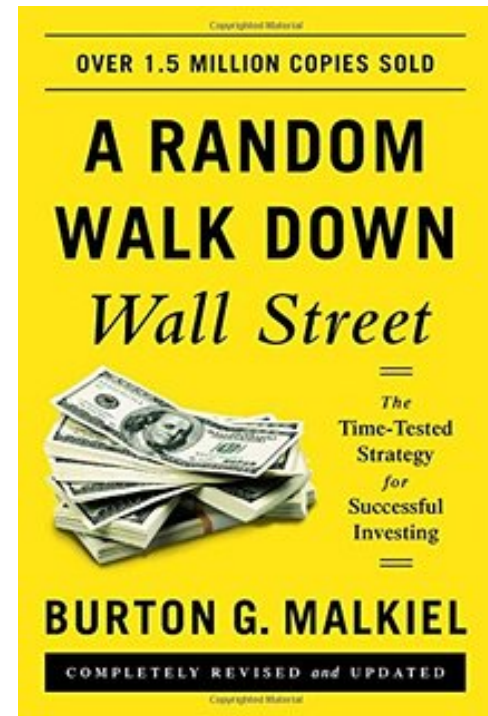
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- To model systems that are mathematically intractable
- To extract useful intermediate results
- Lend themselves to development by successive refinement and “what if” questions
- Start by simulating random walks

# Why Random Walks?

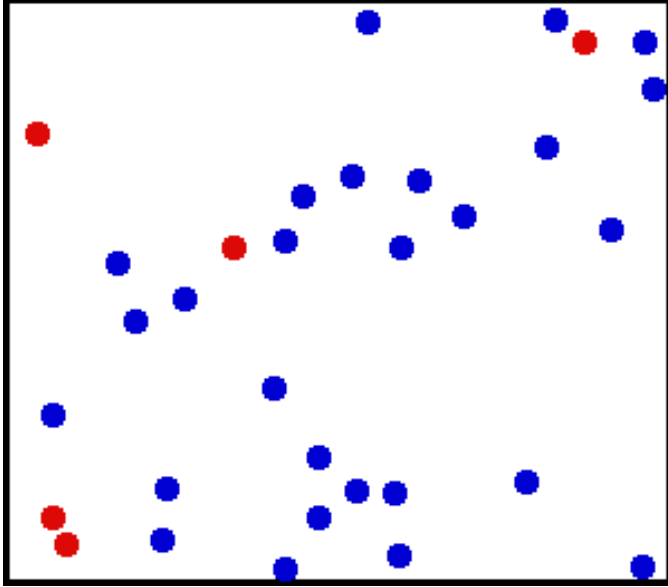
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- Random walks are important in many domains
  - Understanding the stock market
  - Modeling diffusion processes
  - Etc.
- Good illustration of how to use simulations to understand things
- Excuse to cover some important programming topics
  - Using inheritance mechanisms
  - More about plotting



# Brownian Motion Is a Random Walk

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Brown



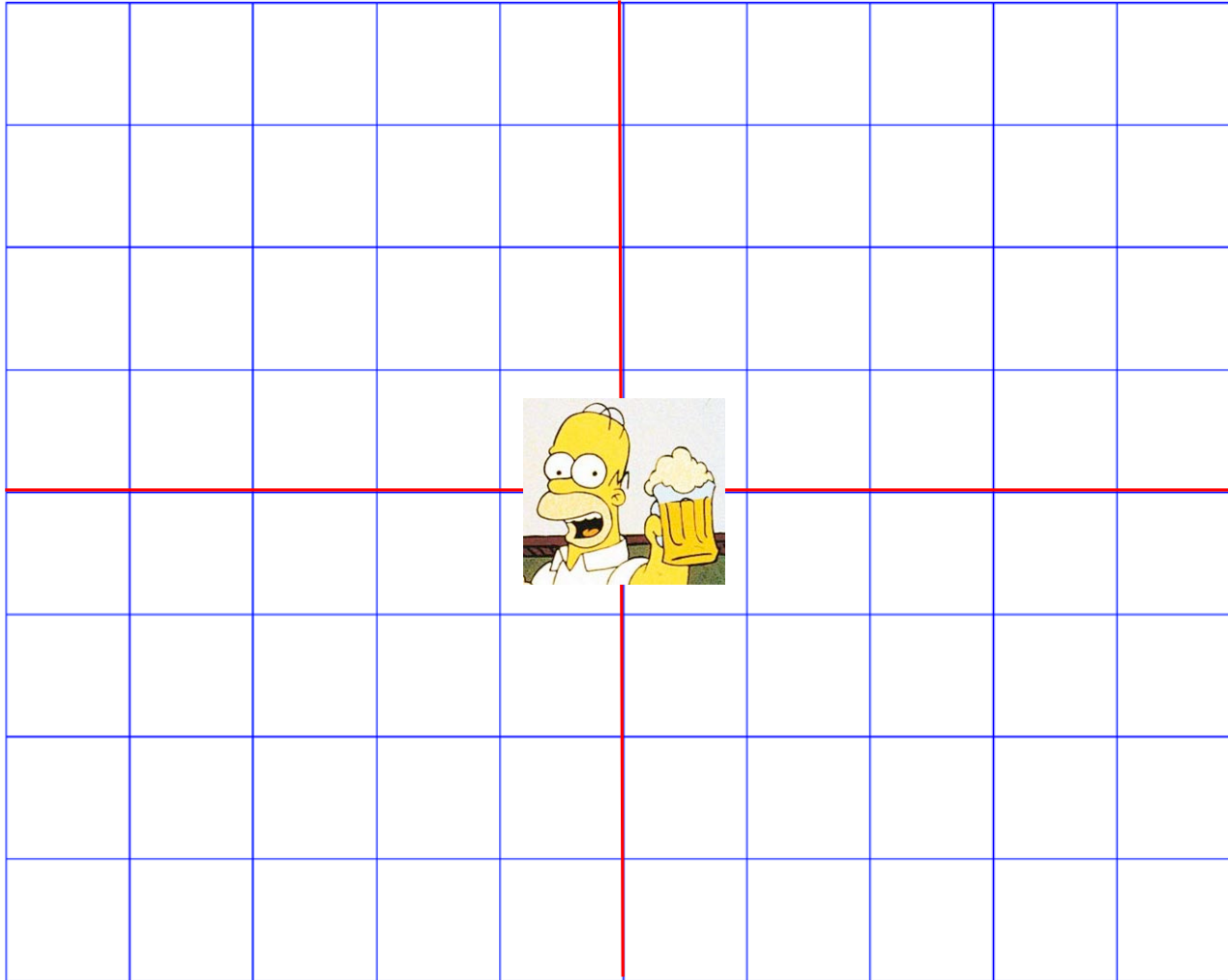
Bachelier



Einstein

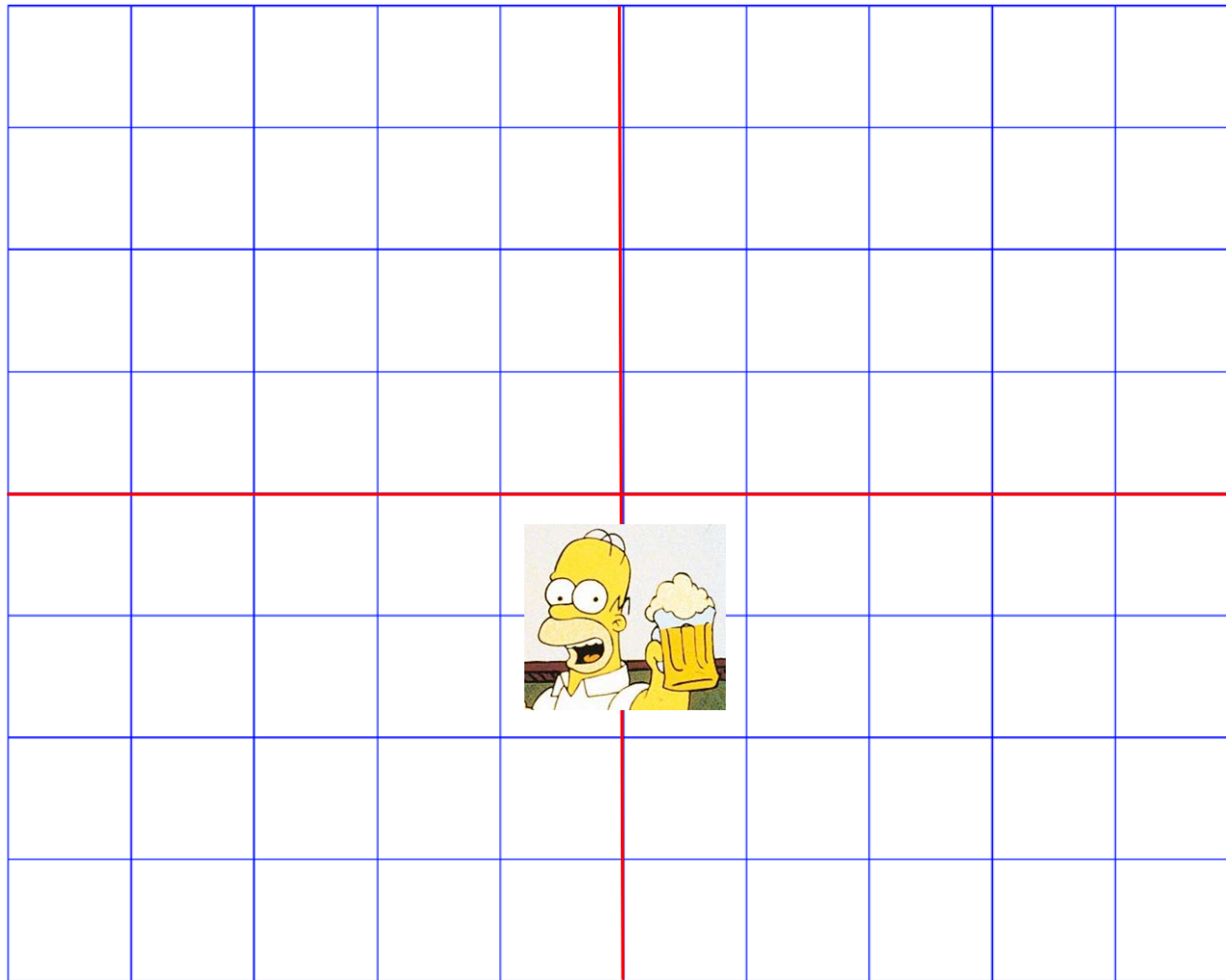
# Drunkard's Walk

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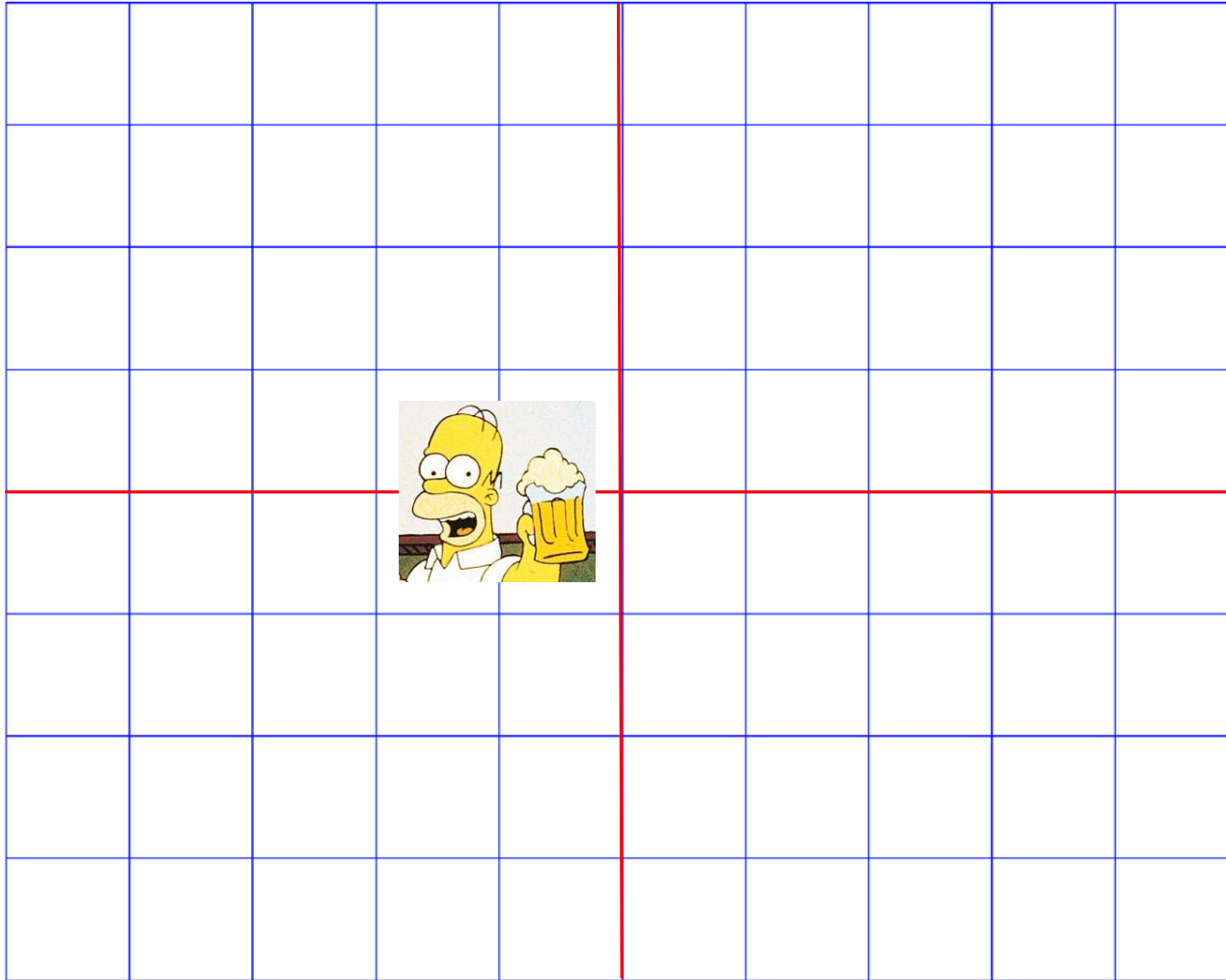
# One Possible First Step

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# Another Possible First Step

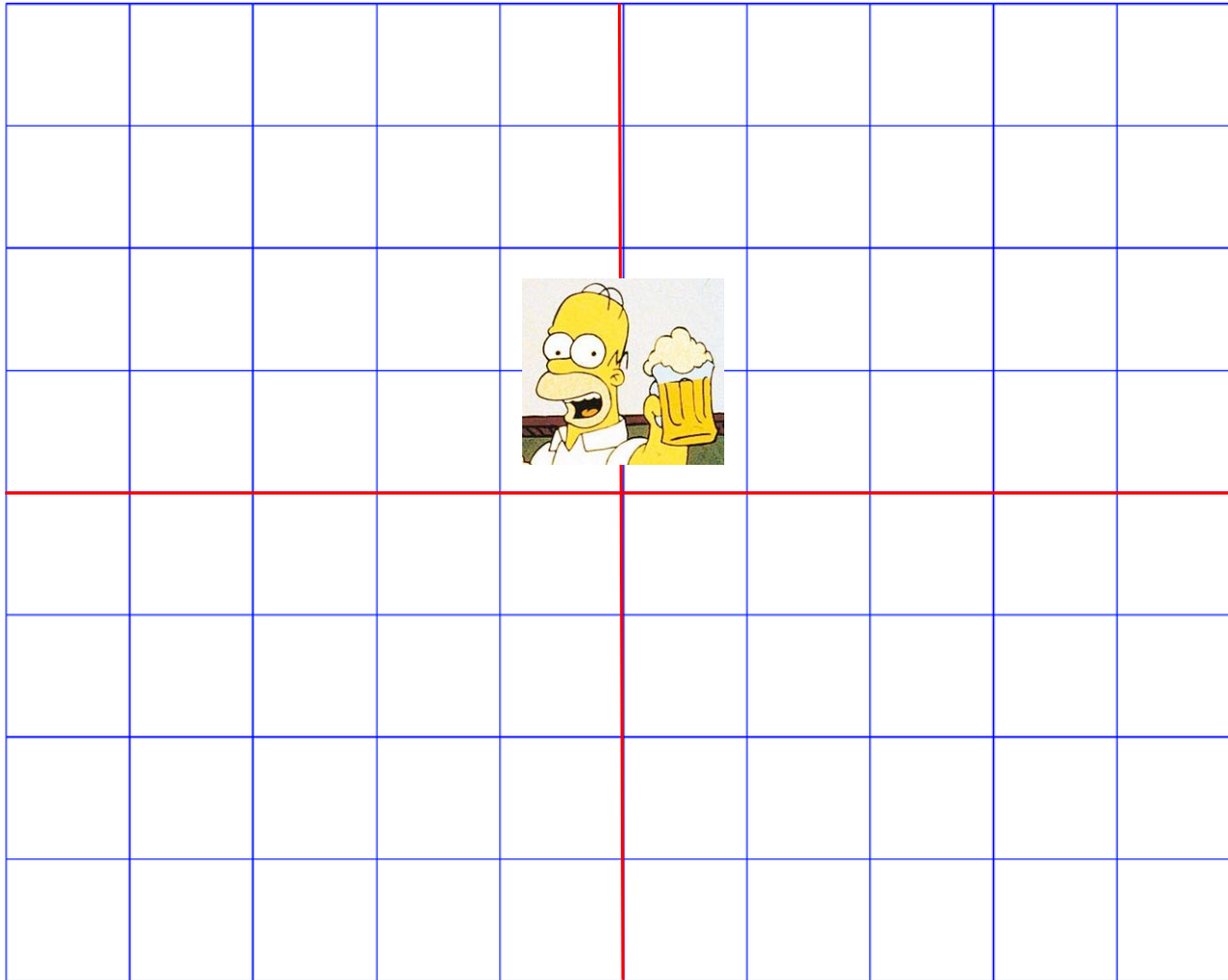
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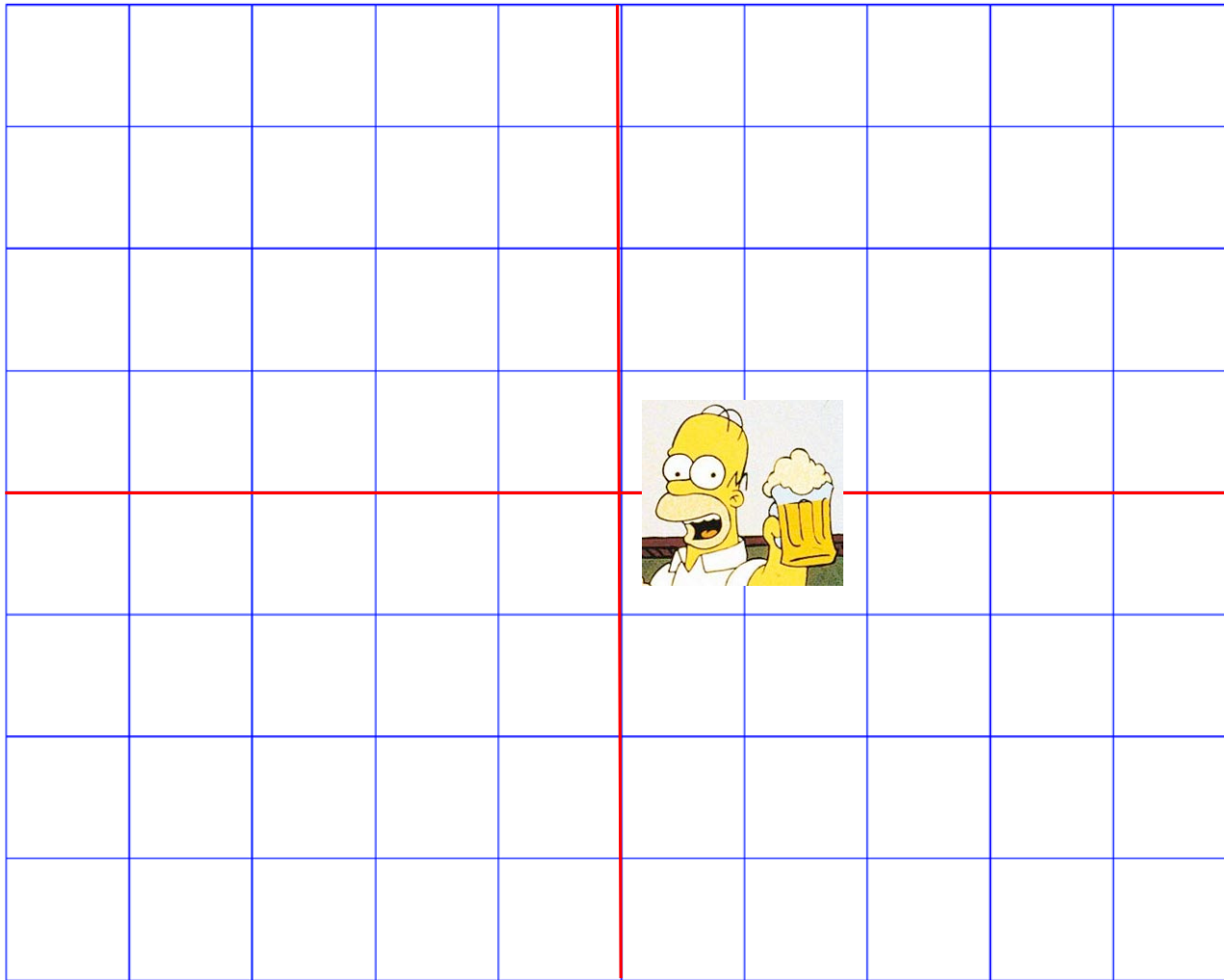
# Yet Another Possible First Step

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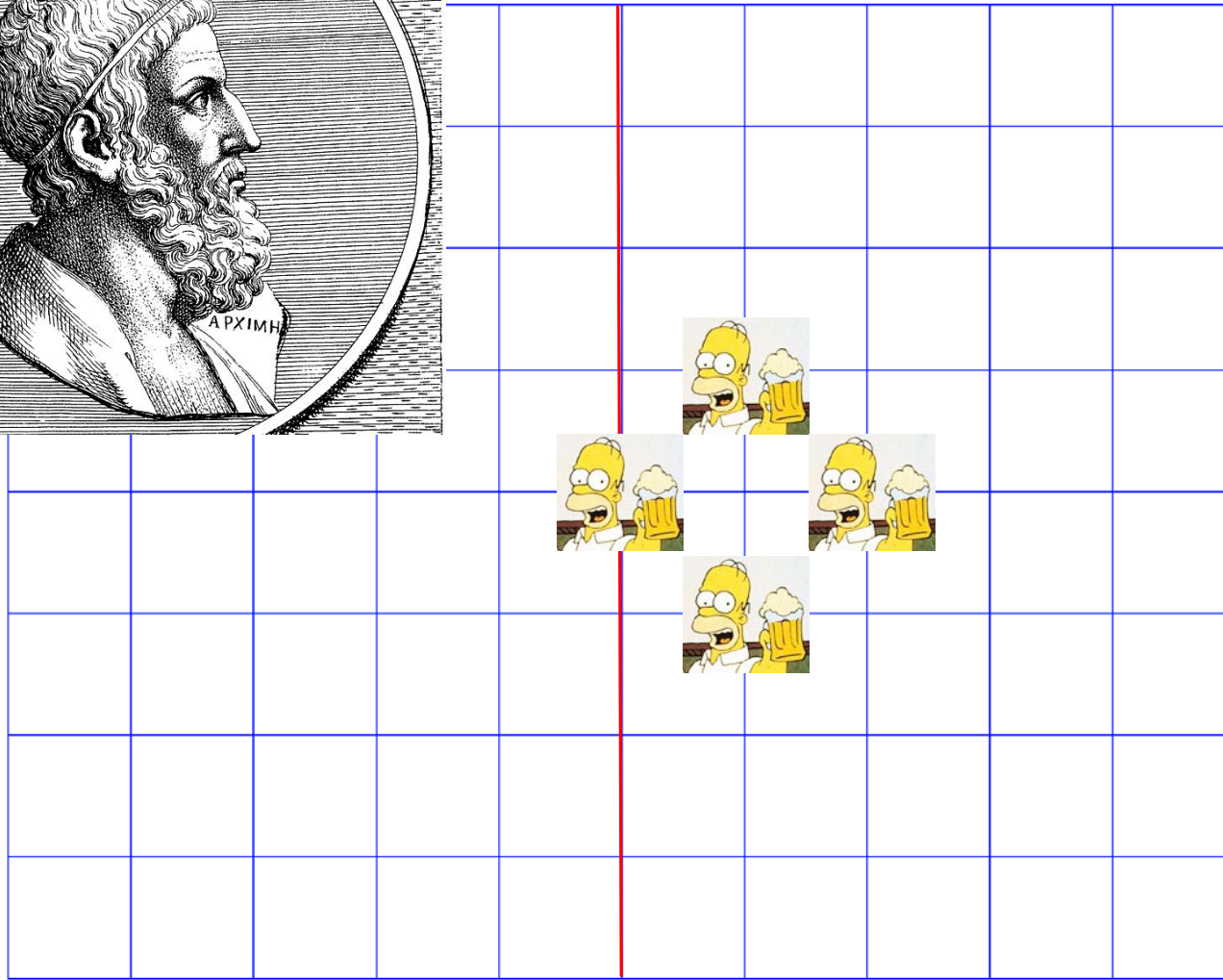
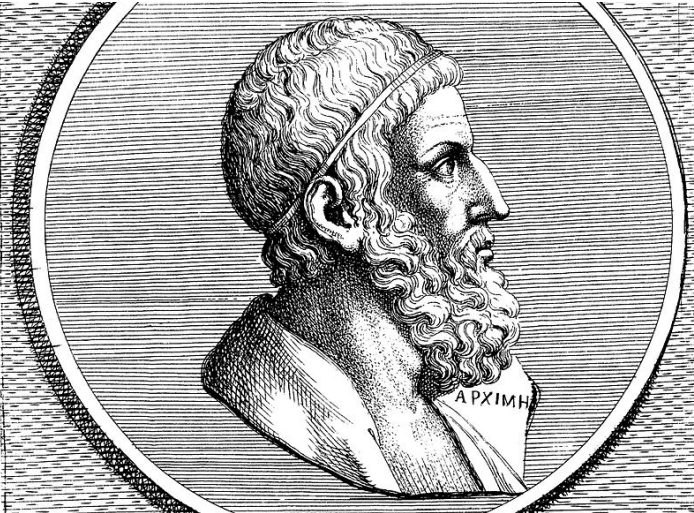


# Last Possible First Step

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# Possible Distances After Two Steps



# Expected Distance After 100,000 Steps?

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- Need a different approach to problem
- Will use simulation
- But not until the next lecture