



**Figure 3.9** Heat capacity at constant volume of one molecule of  $\text{H}_2$  in the gas phase. The vertical scale is in fundamental units; to obtain a value in conventional units, multiply by  $k_B$ . The contribution from the three translational degrees of freedom is  $\frac{3}{2}$ ; the contribution at high temperatures from the two rotational degrees of freedom is 1; and the contribution from the potential and kinetic energy of the vibrational motion in the high temperature limit is 1. The classical limits are attained when  $\tau \gg$  relevant energy level separations.

applies to the harmonic oscillator in the classical limit. The quantum results for the harmonic oscillator and for the diatomic rotator are derived in Problems 3 and 6, respectively. At high temperatures the classical limits are attained, as in Figure 3.9.

**Example: Entropy of mixing.** In Chapter 1 we calculated the number of possible arrangements of A and B in a solid made up of  $N - t$  atoms A and  $t$  atoms B. We found in (1.20) for the number of arrangements:

$$g(N, t) = \frac{N!}{(N - t)! t!} \quad (78)$$

The entropy associated with these arrangements is

$$\sigma(N, t) = \log g(N, t) = \log N! - \log(N - t)! - \log t! , \quad (79)$$

and is plotted in Figure 3.10 for  $N = 20$ . This contribution to the total entropy of an alloy