$$S(N, V, E) = k \ln \Omega(N, V, E) = k \ln \left[\sum_{\{n_i\}} W\{n_i\} \right]$$
$$S(N, V, E) \approx k \ln W\{n_i^*\}$$

$$\left\{ egin{aligned} h_i
ight\} & oxed{max} \ \delta \ln W\{n_i\} - \left[lpha \sum_i \delta n_i + eta \sum_i \epsilon_i \delta n_i
ight] \end{aligned}$$

$$\ln W\{n_i\} = \sum_{i} \ln w_i$$

$$\approx \sum_{i} \left[n_i \ln \left(\frac{g_i}{n_i} - a \right) - \frac{g_i}{a} \ln \left(1 - a \frac{n_i}{g_i} \right) \right]$$

$$\sum_{i} \left[\ln \left(\frac{g_i}{n_i} - a \right) - \alpha - \beta \epsilon_i \right]_{n_i = n_i^*} \delta n_i = 0$$

$$\ln\left(\frac{g_i}{n_i^*} - a\right) - \alpha - \beta\epsilon_i = 0$$

$$a = \begin{cases} -1 & B.E. \\ 0 & M.B. \\ 1 & F.D. \end{cases}$$