

# \* 1D oscillator hamiltonian

hamiltonian of a harmonic oscillator

$$h(q, p) = \frac{1}{2} k q^2 + \frac{1}{2m} p^2$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$E = \frac{1}{2} m \omega^2 A^2$$

$$\begin{cases} q \equiv A \cos(\omega t + \phi) \\ p \equiv m \dot{q} = -m[\omega A \sin(\omega t + \phi)] \end{cases}$$

\*w!!

Mechanik

$$\frac{q^2}{\left(\frac{2E}{m\omega^2}\right)} + \frac{p^2}{(2mE)} = 1$$

phase space is valid

interpretation E = constant

$$\begin{array}{ccc} \text{circle} & \Rightarrow & \text{ring} \\ E < E_0 & & E_0 - \frac{\Delta}{2} \leq E \leq E_0 + \frac{\Delta}{2} \\ \Downarrow & \text{order?} & \Downarrow \\ \frac{2\pi E}{\omega} & & \frac{2\pi \Delta}{\omega} \end{array}$$

$$E_n = \left(n + \frac{1}{2}\right) \hbar \omega \quad \omega = \sqrt{\frac{k}{m}}$$

$$n = 0, 1, 2, \dots, \infty$$

$$\left[ \frac{2\pi \Delta}{\omega} \right] \equiv h$$

$\Delta = \hbar \omega$

$\hbar \omega \equiv \text{quantum}$

multiresolution system better than  
classical mechanics

$$\omega_0 \equiv h^N$$

Heisenberg's uncertainty principle