

Zenbait kantitate estatistikoren esangura fisikoa

$$q \equiv \ln \left\{ \sum_{r,s} \exp(-\alpha N_r - \beta E_s) \right\}$$

$$q = q(\alpha, \beta, E_s)$$

Kalkula dezagun haren diferentziala:

$$dq = -\bar{N}d\alpha - \bar{E}d\beta - \frac{\beta}{\mathcal{N}} \sum_{r,s} \langle n_{r,s} \rangle dE_s$$

$$d(q + \alpha\bar{N} + \beta\bar{E}) = \beta \left(\frac{\alpha}{\beta} d\bar{N} + d\bar{E} - \frac{1}{\mathcal{N}} \sum_{r,s} \langle n_{r,s} \rangle dE_s \right)$$

Lehenengo Printzipioaren adierazpen diferentzialarekin alderatuz...

$$\delta Q = d\bar{E} + \delta W - \mu d\bar{N}$$

Hauexek dira egin daitezkeen "identifikazioak"...

$$\delta W = -\frac{1}{\mathcal{N}} \sum_{r,s} \langle n_{r,s} \rangle dE_s, \quad \mu = -\frac{\alpha}{\beta}$$

$$d(q + \alpha\bar{N} + \beta\bar{E}) = \beta\delta Q$$

$$\boxed{\begin{aligned} \beta &= \frac{1}{k_B T} \\ \alpha &= -\frac{\mu}{k_B T} \end{aligned}}$$