



Figure 5.9 The reservoir is in thermal and diffusive contact with the system. In (a) the system is in quantum state 1, and the reservoir has $g(N_0 - N_1, U_0 - \epsilon_1)$ states accessible to it. In (b) the system is in quantum state 2, and the reservoir has $g(N_0 - N_2, U_0 - \epsilon_2)$ states accessible to it. Because we have specified the exact state of the system, the total number of states accessible to $\mathcal{R} + \mathcal{S}$ is just the number of states accessible to \mathcal{R} .

Here g refers to the reservoir alone and depends on the number of particles in the reservoir and on the energy of the reservoir.

We can express (42) as a ratio of two probabilities, one that the system is in state 1 and the other that the system is in state 2:

$$\frac{P(N_1, \epsilon_1)}{P(N_2, \epsilon_2)} = \frac{g(N_0 - N_1, U_0 - \epsilon_1)}{g(N_0 - N_2, U_0 - \epsilon_2)}, \quad (43)$$

where g refers to the state of the reservoir. The situation is shown in Figure 5.9. By definition of the entropy

$$g(N_0, U_0) \equiv \exp[\sigma(N_0, U_0)], \quad (44)$$

so that the probability ratio in (43) may be written as

$$\frac{P(N_1, \epsilon_1)}{P(N_2, \epsilon_2)} = \frac{\exp[\sigma(N_0 - N_1, U_0 - \epsilon_1)]}{\exp[\sigma(N_0 - N_2, U_0 - \epsilon_2)]}, \quad (45)$$

or

$$\begin{aligned} \frac{P(N_1, \epsilon_1)}{P(N_2, \epsilon_2)} &= \exp[\sigma(N_0 - N_1, U_0 - \epsilon_1) - \sigma(N_0 - N_2, U_0 - \epsilon_2)] \\ &= \exp(\Delta\sigma). \end{aligned} \quad (46)$$

$$T \equiv \frac{S}{k_B}$$

$$g \equiv \Omega$$

$$k_B T = \sigma \quad S = k_B \ln \Omega$$