

## 2 ebatze-modoa

Multzo makrokanonikoan dagoen sistema

$$\sum_{r,s} n_{r,s} = \mathcal{N}$$

$$\sum_{r,s} n_{r,s} N_r = \mathcal{N} \bar{N}$$

$$\sum_{r,s} n_{r,s} E_s = \mathcal{N} \bar{E}$$

$$W\{n_{r,s}\} = \frac{\mathcal{N}!}{\prod_{r,s} (n_{r,s}!)}$$

edozein banaketarekin lotutako sup  
max!!

$$(i) \quad \frac{n_{r,s}^*}{\mathcal{N}} = \frac{\exp(-\alpha N_r - \beta E_s)}{\sum_{r,s} \exp(-\alpha N_r - \beta E_s)}$$

$$(ii) \quad \langle n_{r,s} \rangle = \frac{\sum_{\{n_{r,s}\}} n_{r,s} W\{n_{r,s}\}}{\sum_{\{n_{r,s}\}} W\{n_{r,s}\}}$$

$$\lim_{\mathcal{N} \rightarrow \infty} \frac{\langle n_{r,s} \rangle}{\mathcal{N}} \simeq \frac{n_{r,s}^*}{\mathcal{N}} = \frac{\exp(-\alpha N_r - \beta E_s)}{\sum_{r,s} \exp(-\alpha N_r - \beta E_s)}$$

PROBABILITATEA

TERMODINAMIKA

$$\rightarrow \bar{N} = \frac{\sum_{r,s} N_r \exp(-\alpha N_r - \beta E_s)}{\sum_{r,s} \exp(-\alpha N_r - \beta E_s)} \equiv - \frac{\partial}{\partial \alpha} \left\{ \ln \sum_{r,s} \exp(-\alpha N_r - \beta E_s) \right\}$$

$$\rightarrow \bar{E} = \frac{\sum_{r,s} E_s \exp(-\alpha N_r - \beta E_s)}{\sum_{r,s} \exp(-\alpha N_r - \beta E_s)} \equiv - \frac{\partial}{\partial \beta} \left\{ \ln \sum_{r,s} \exp(-\alpha N_r - \beta E_s) \right\}$$

SISTEMAREN LOTUTAKO FISIKA