

# Scheduling and Analysis of Limited-Preemptive Malleable Gang Tasks

Joan Marcè i Igual

Geoffrey Nelissen

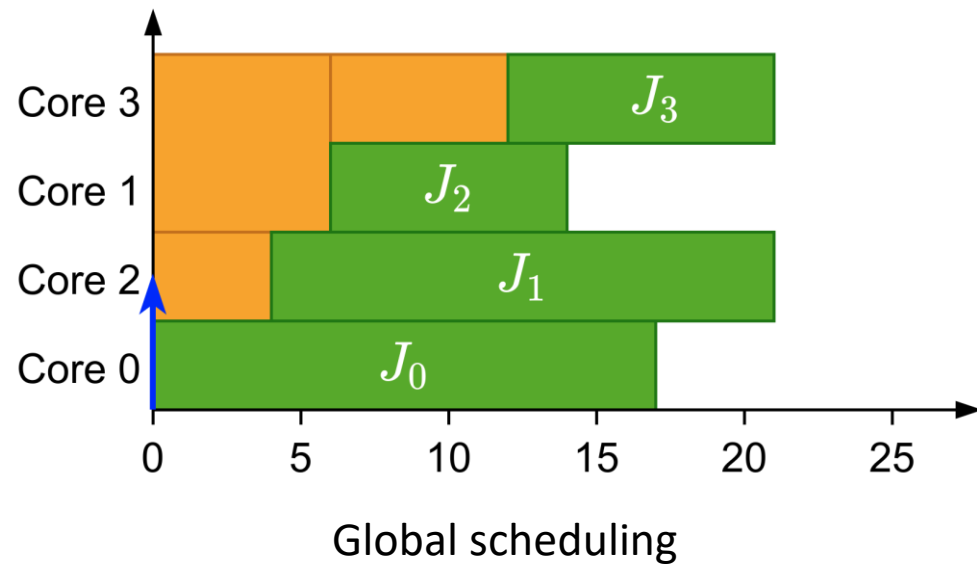
Mitra Nasri

Paris Panagiotou

24<sup>th</sup> of February, 2020

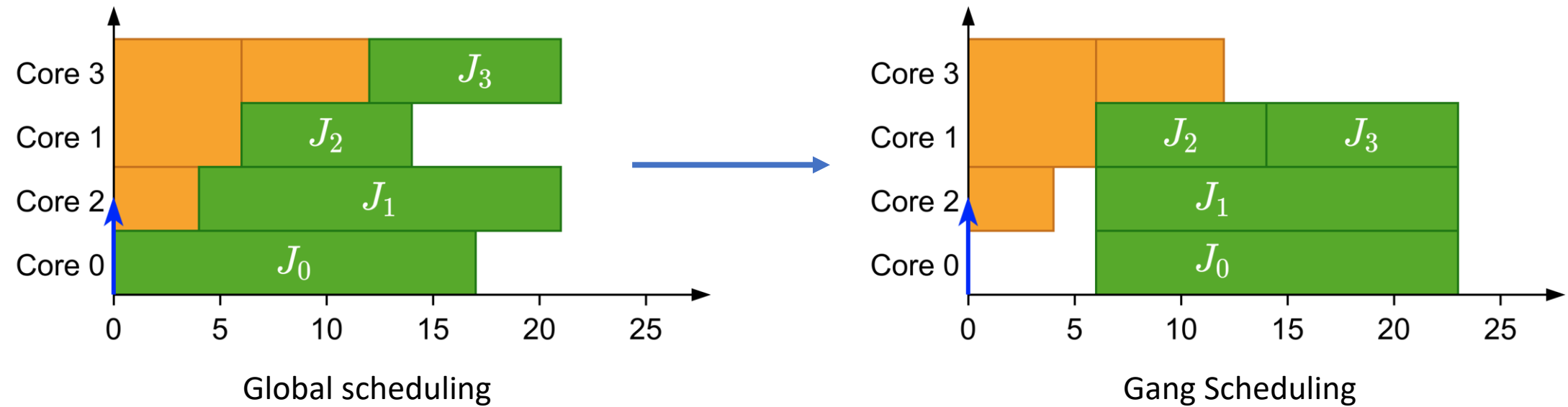
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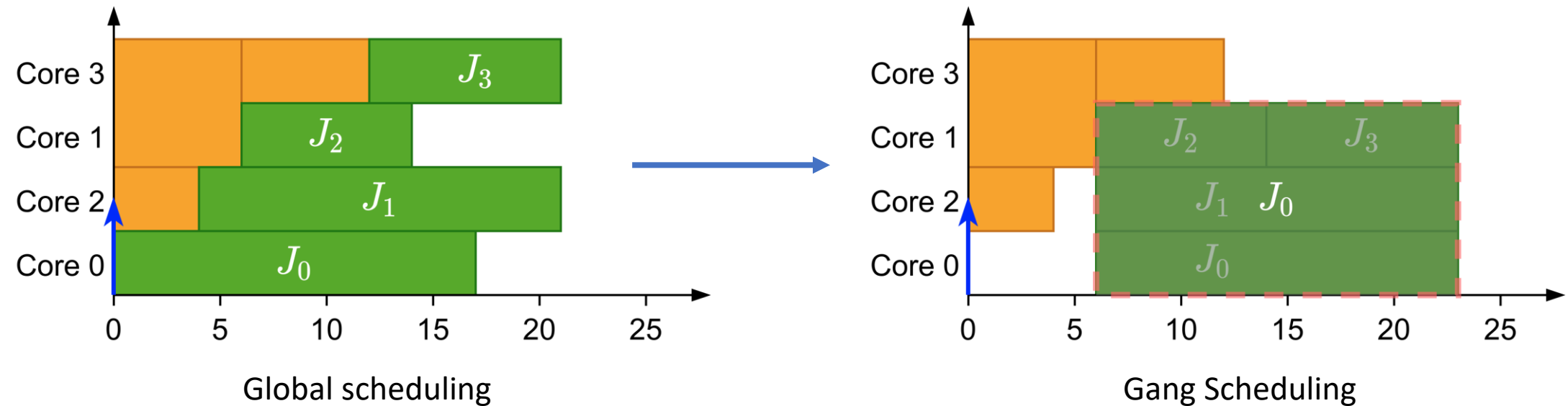
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- Parallel threads executed together as a “gang”



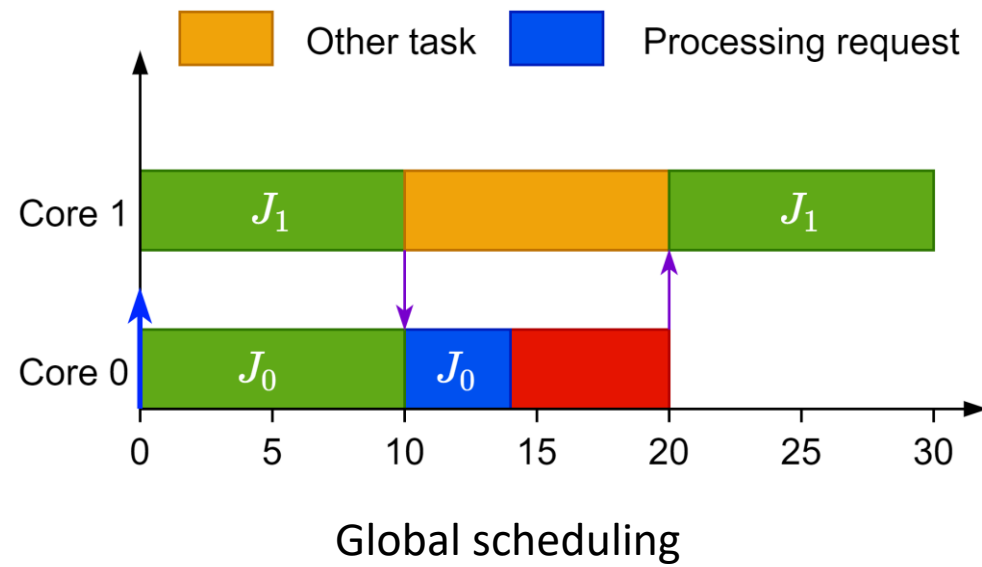
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- Parallel threads executed together as a “gang”
- Execution does not start until there are enough free cores



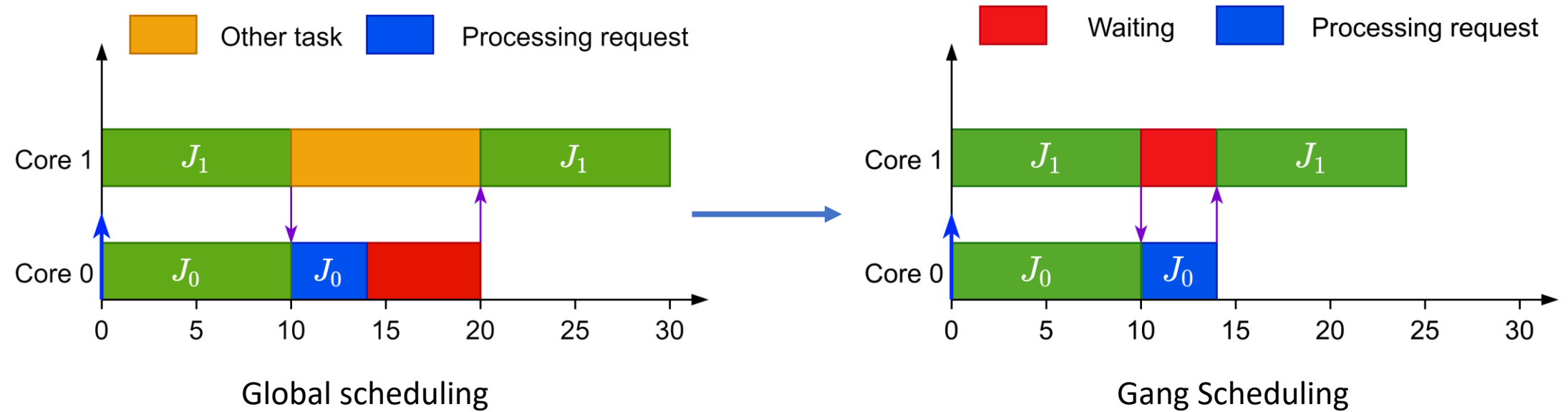
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- Efficient synchronization



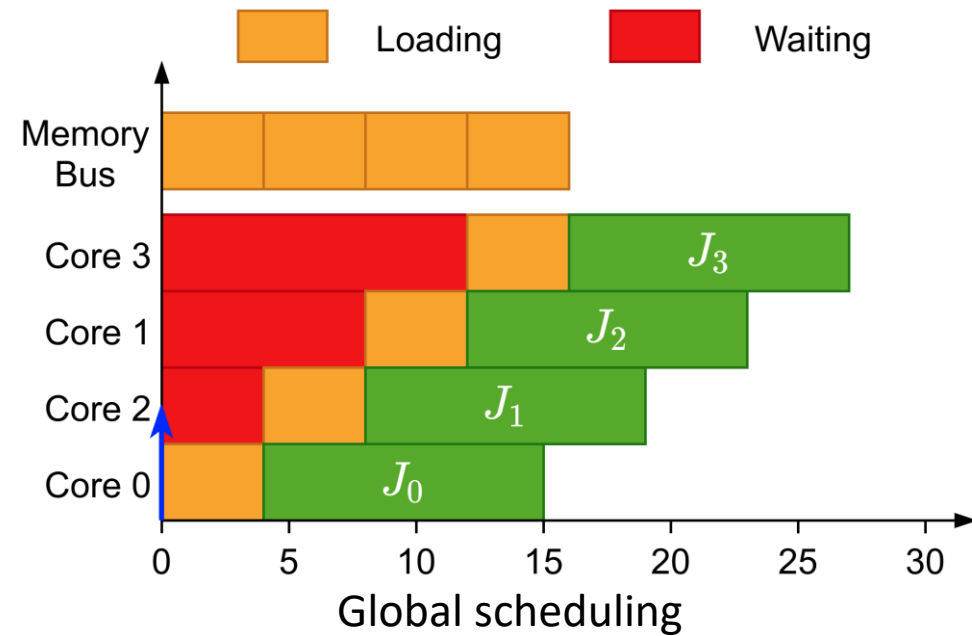


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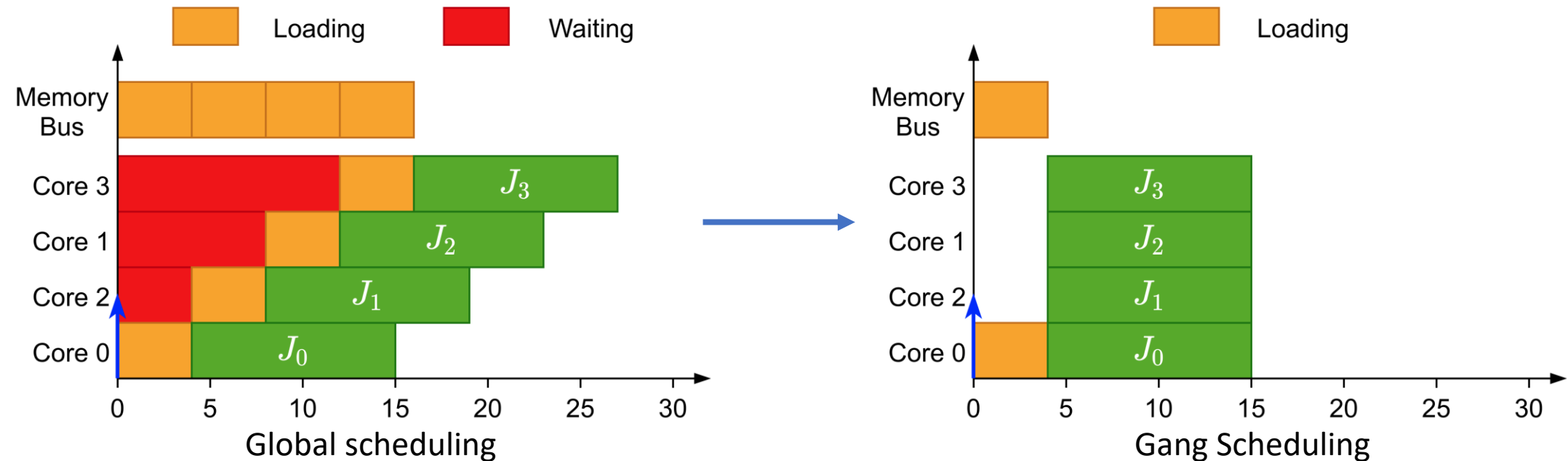
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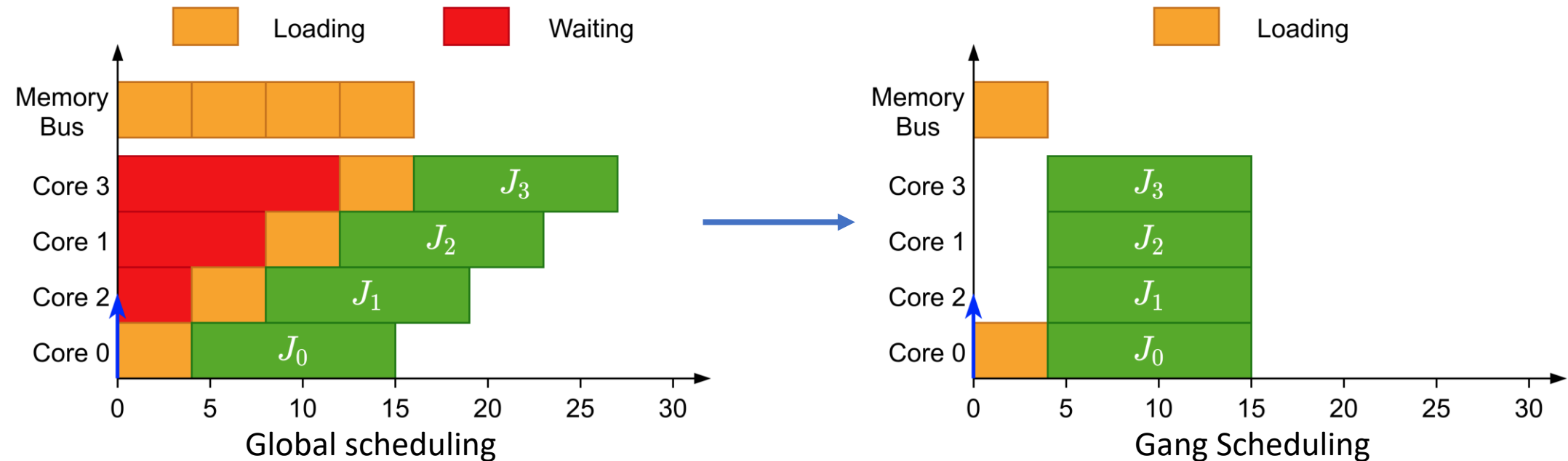
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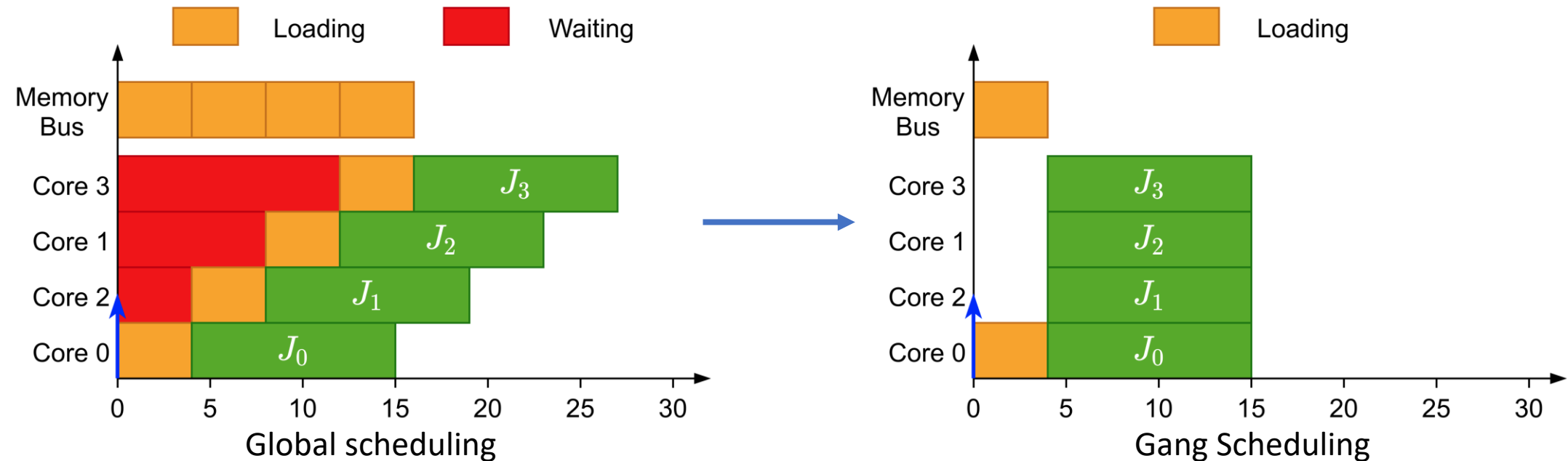
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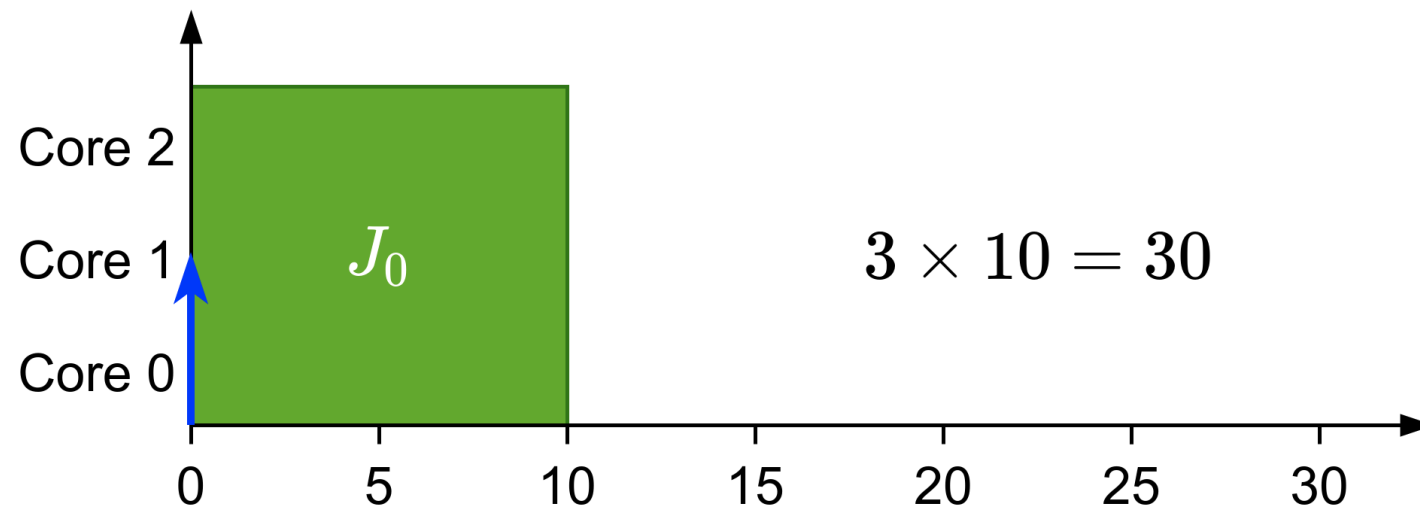
# Why gang?

- Efficient synchronization
- Avoids overhead when loading initial data
- Shows its full potential when executed non-preemptively



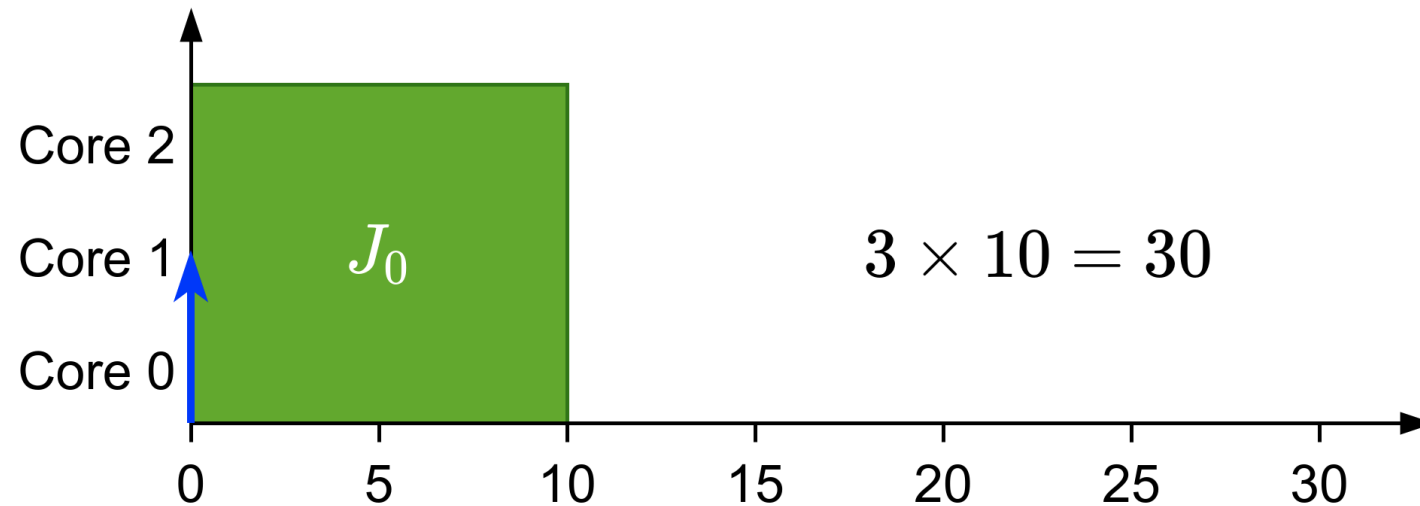
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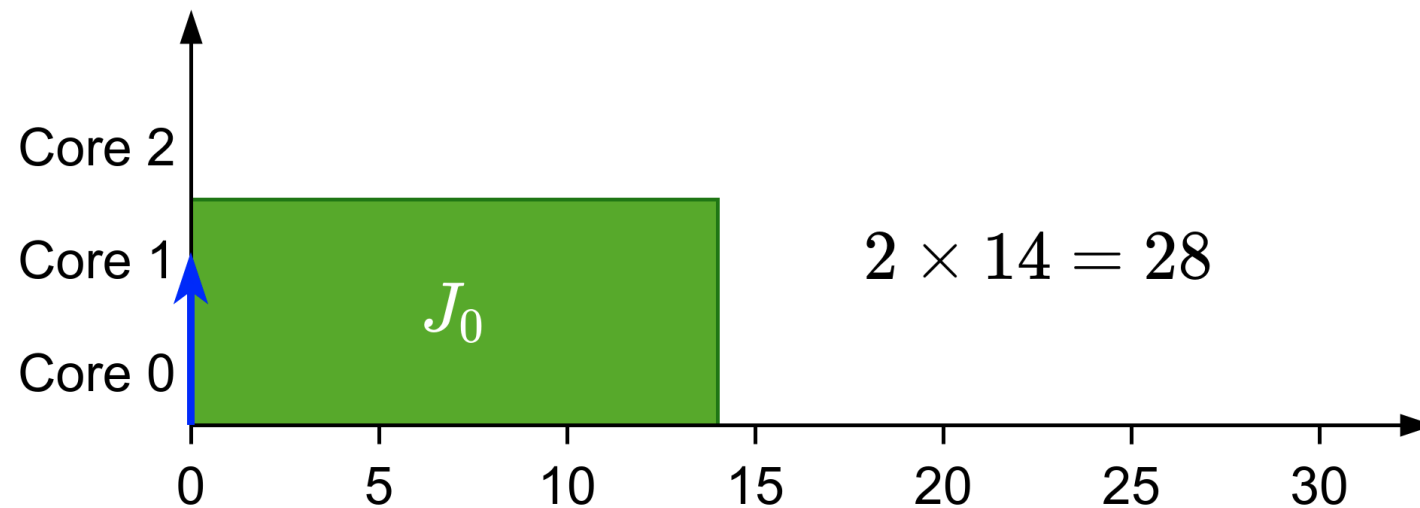
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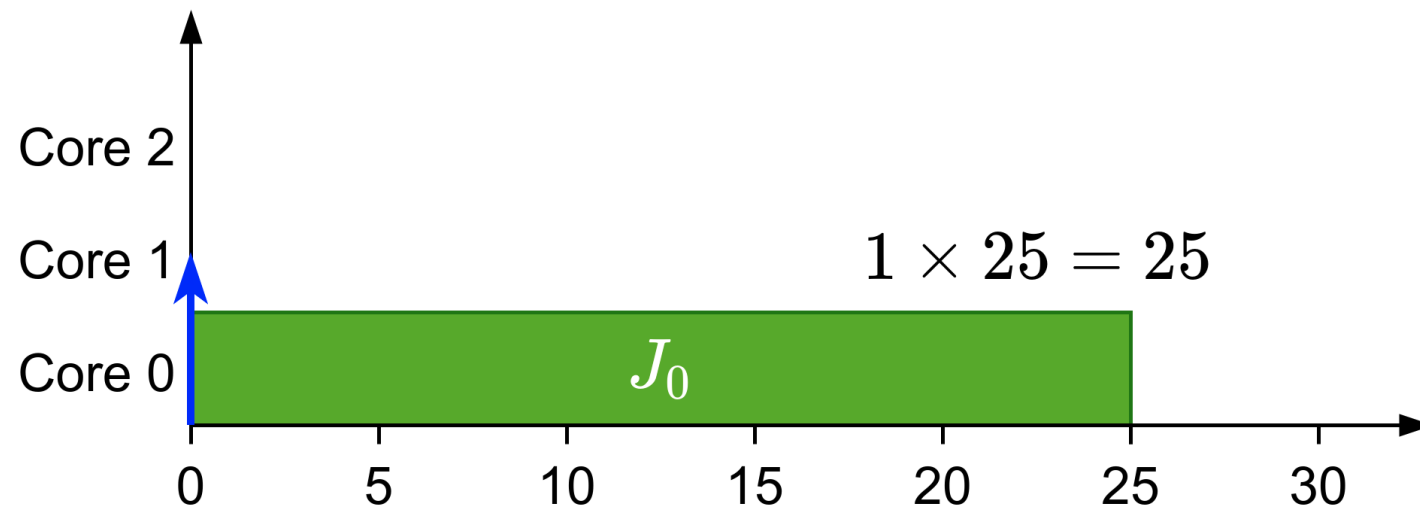
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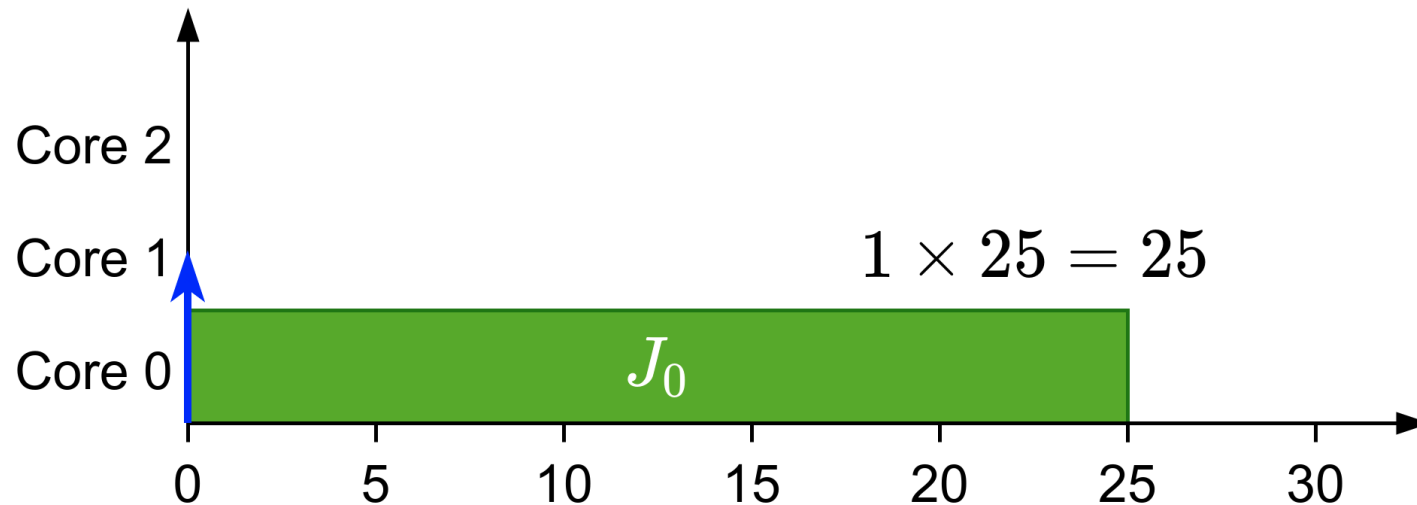
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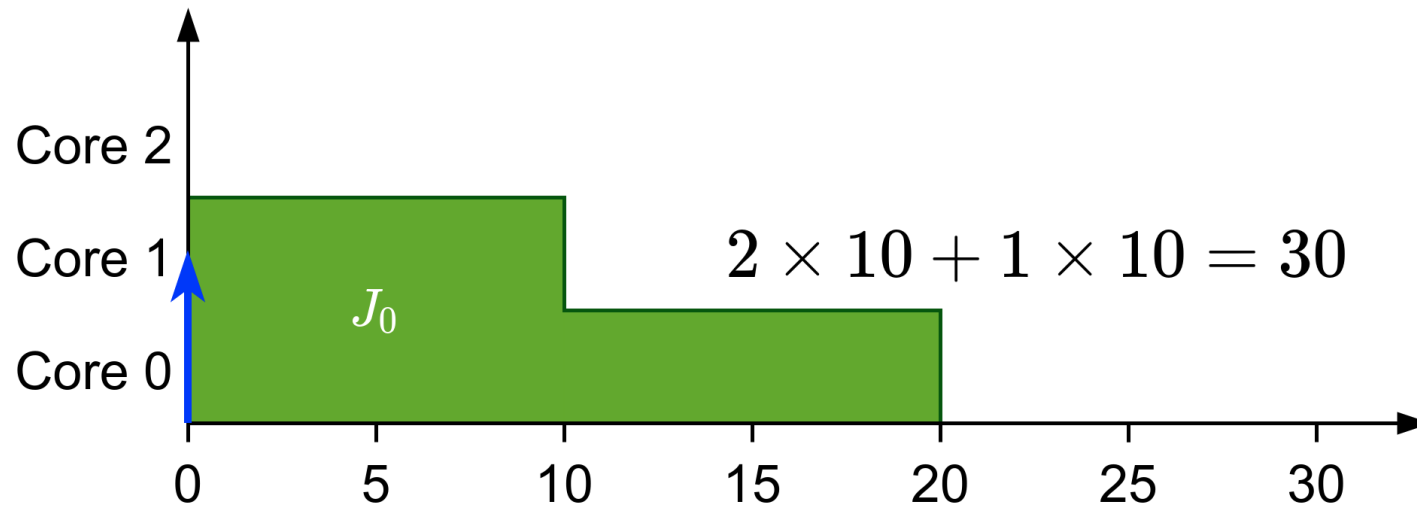
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- **Rigid:** number of cores set by programmer
- **Moldable:** number of cores assigned during scheduling



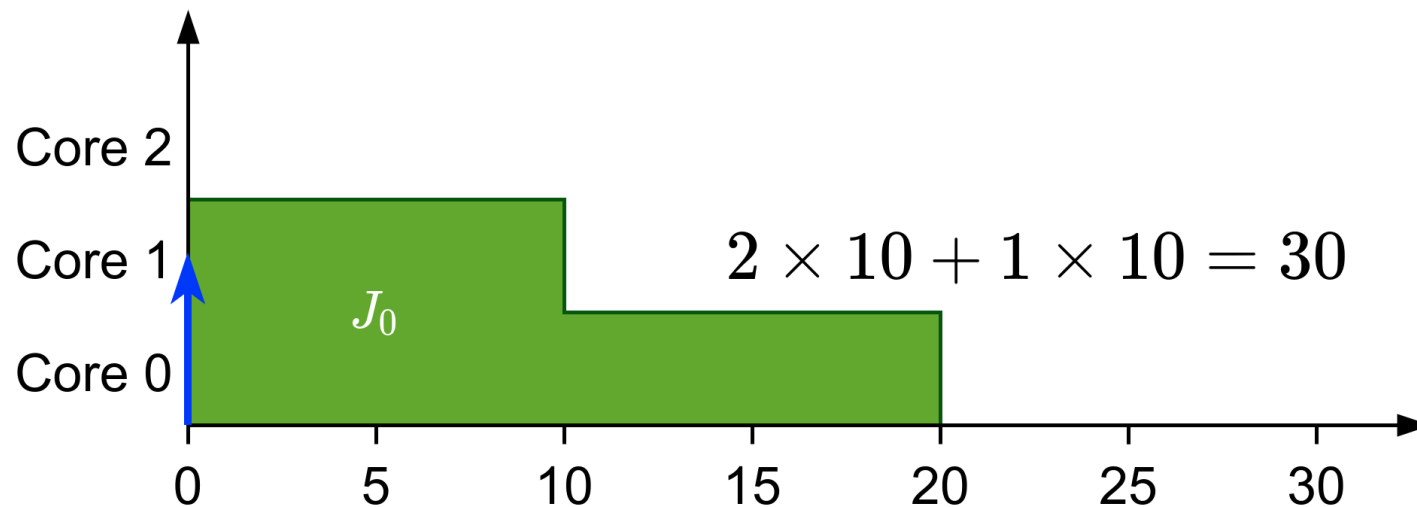
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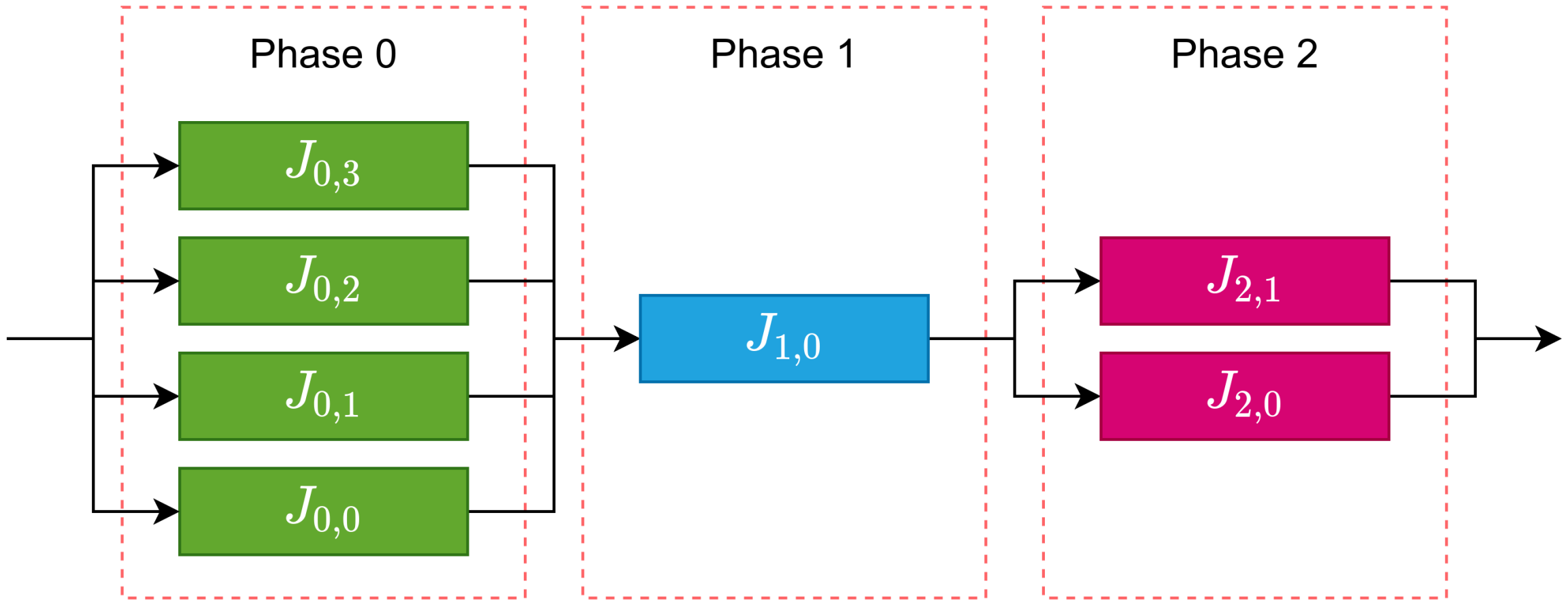
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    - Optimal scheduler for rigid gang (DP-Fair)<sup>[3]</sup>
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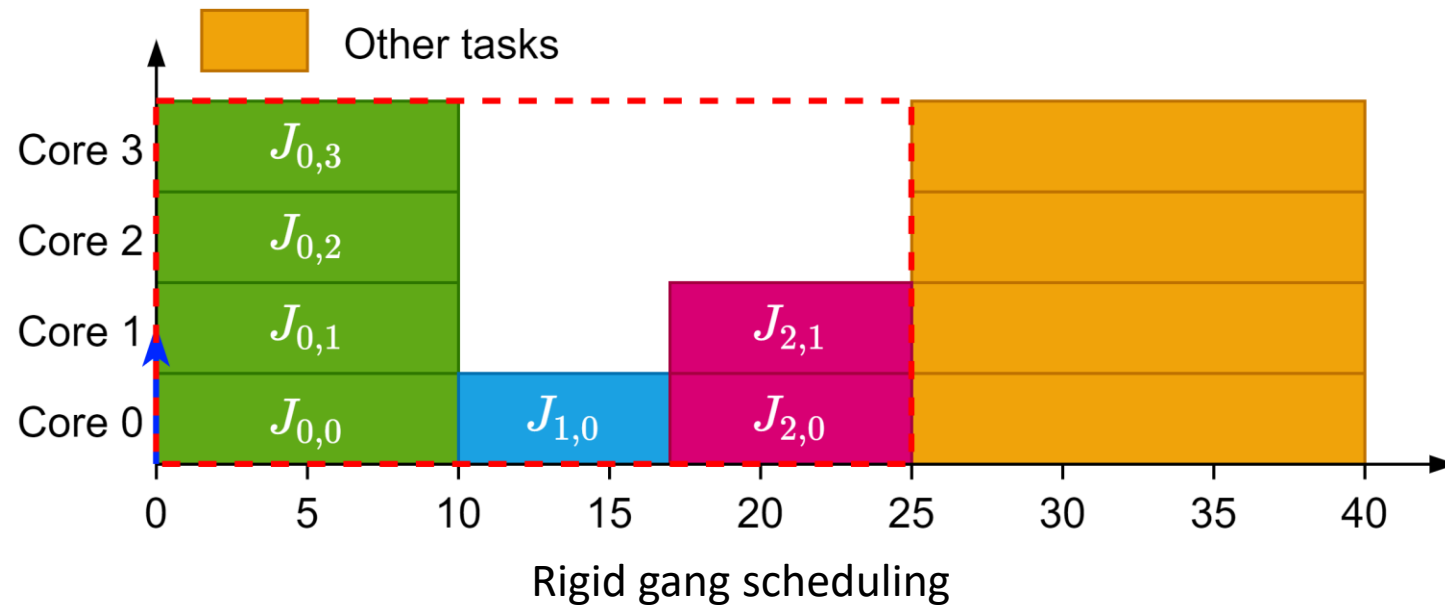
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    - Optimal scheduler for rigid gang (DP-Fair)<sup>[3]</sup>
    - Moldable scheduler<sup>[4]</sup>
  - Bundled scheduling<sup>[5]</sup>
    - Tasks with precedence constraints modelled as a succession of bundles
    - Our limited-preemptive definition comes from here

# Summarizing

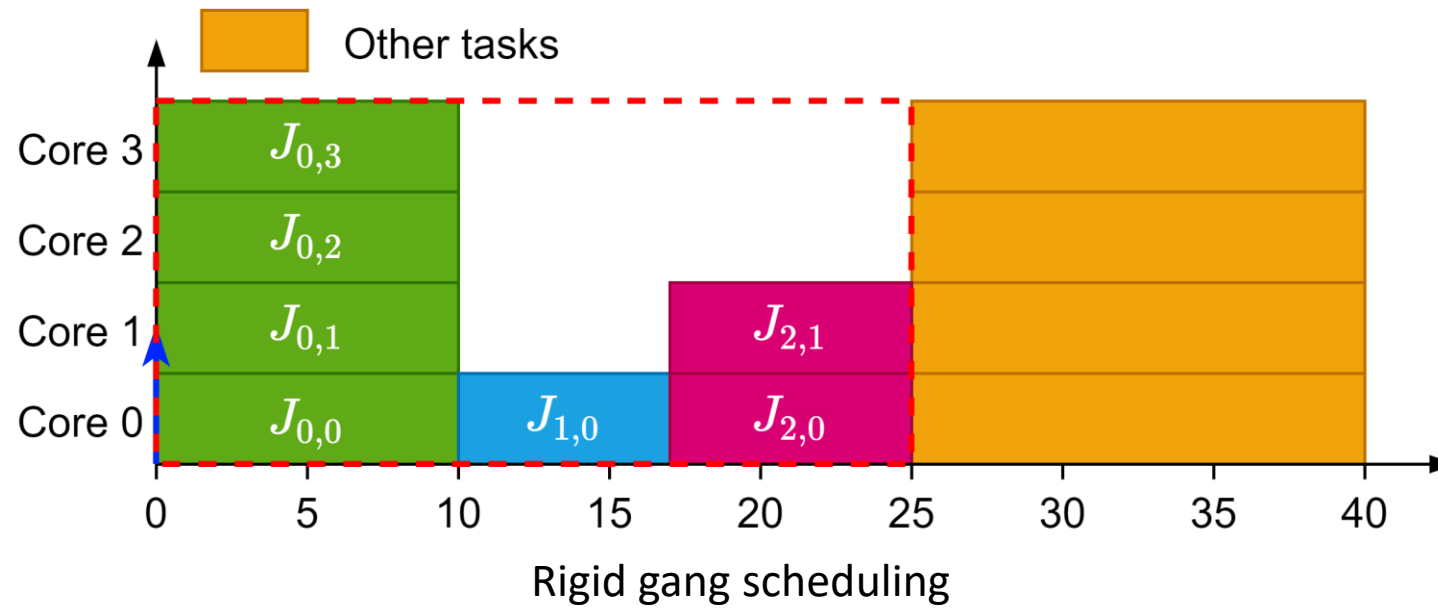


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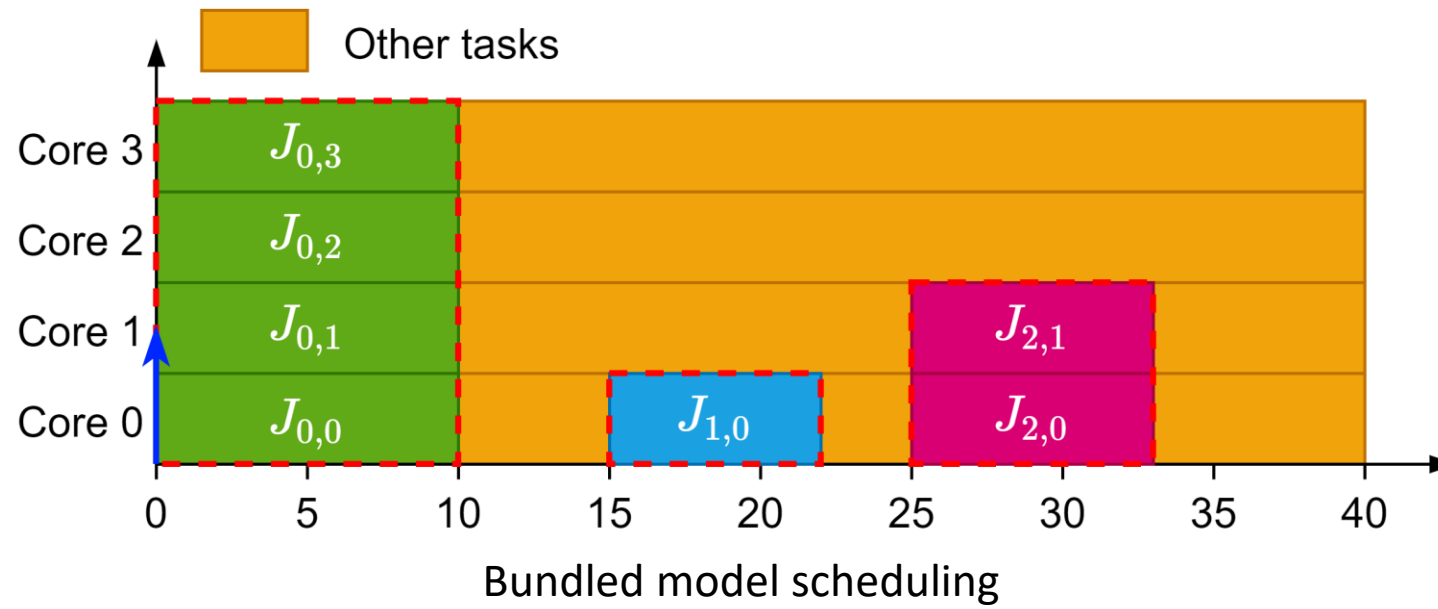
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- Rigid gang reserves the whole block



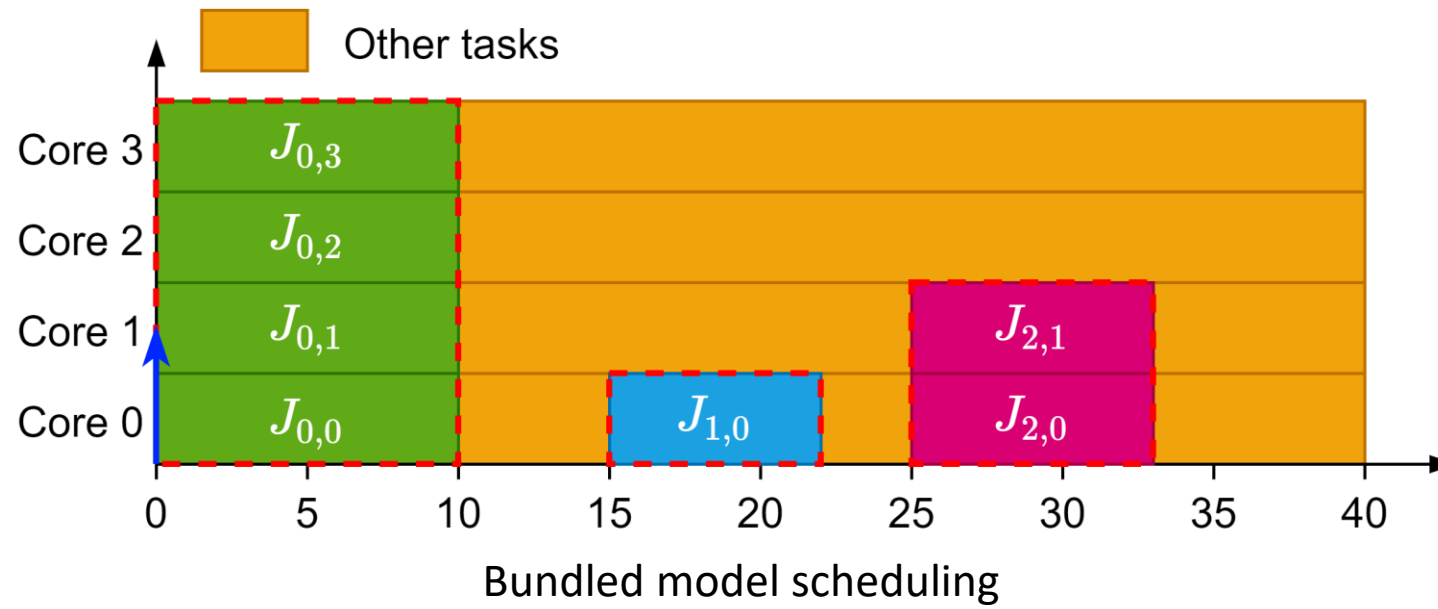
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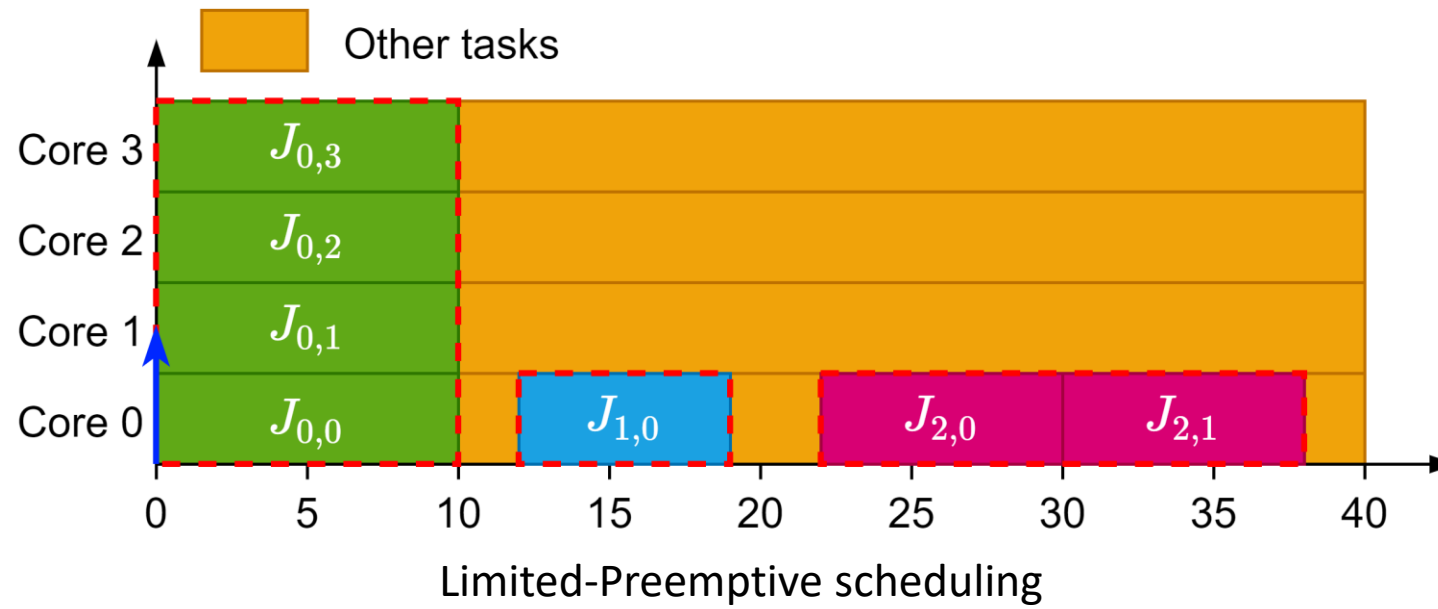
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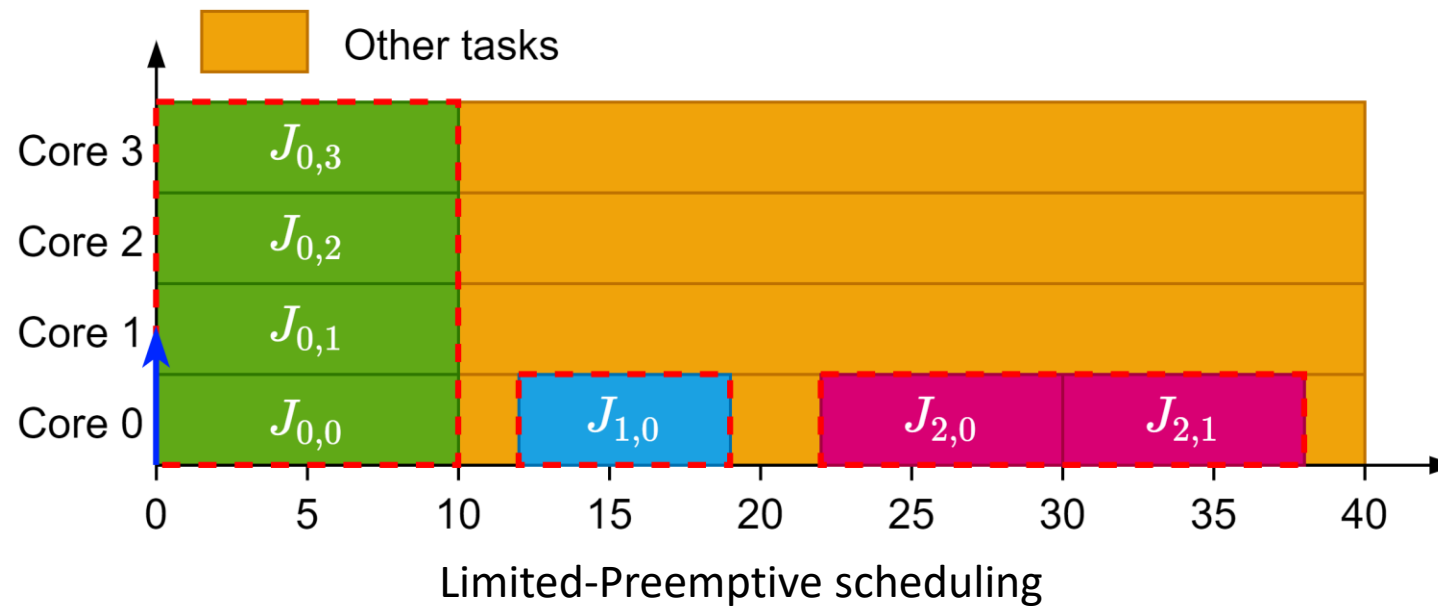
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# Summarizing

- Rigid gang reserves the whole block
- Bundled creates multiple rigid blocks with dependencies
- Limited-Preemptive tries to schedule these blocks in a moldable way



# Our work

# Project goals

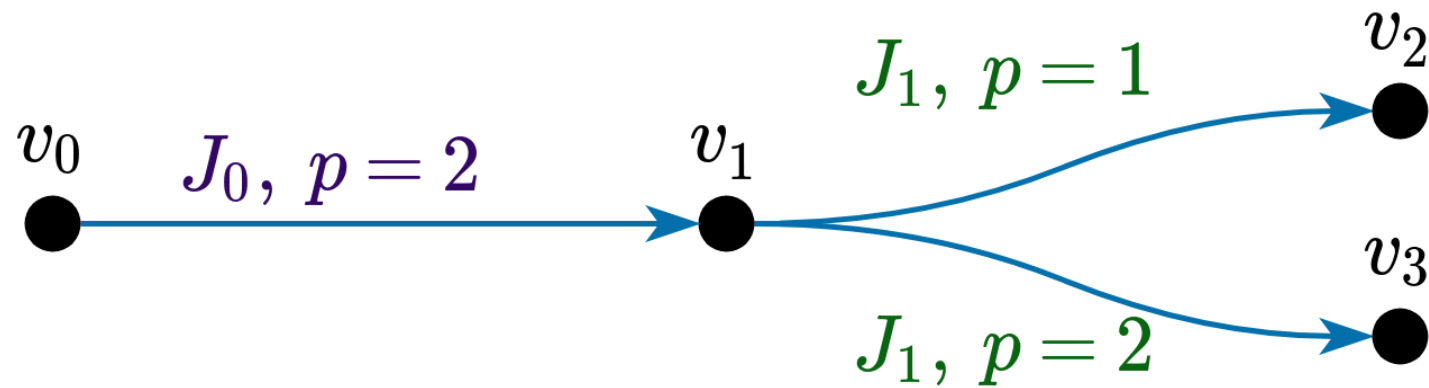
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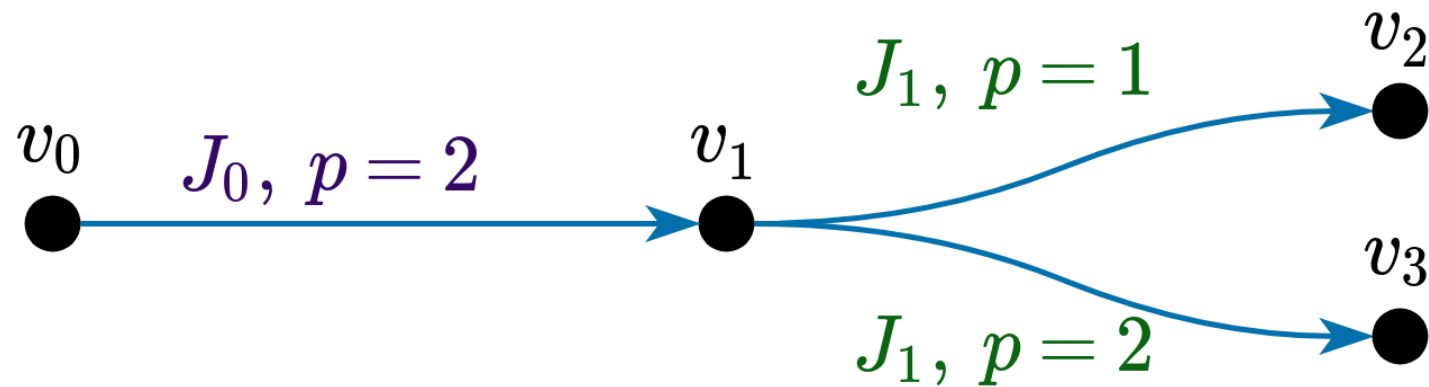
- Design an accurate schedulability analysis for limited-preemptive moldable gang tasks
- Propose a new scheduling algorithm to improve the schedulability of limited-preemptive moldable gang tasks

# Schedule Abstraction Graph



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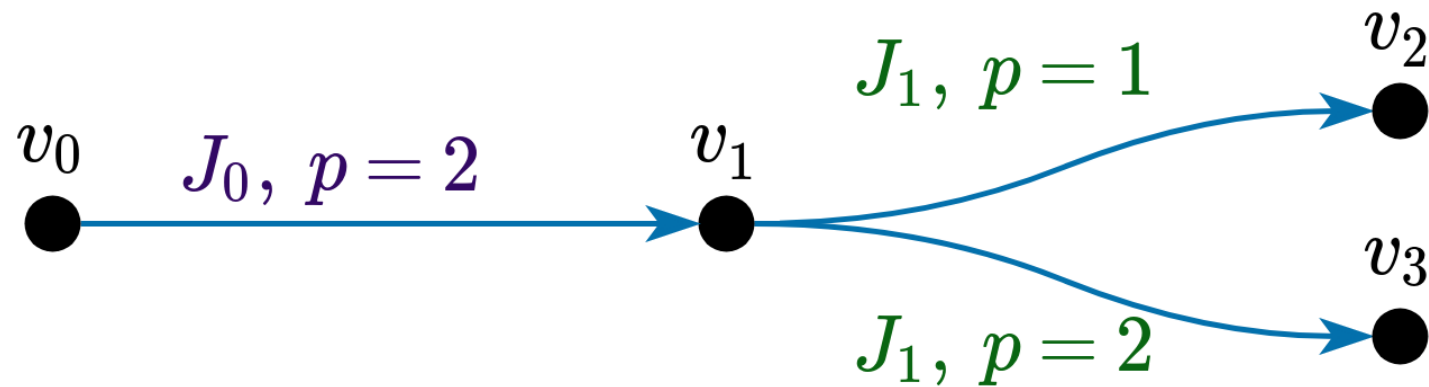
- Accurate and relatively fast analysis
  - Faster than an exact analysis
  - Not as pessimistic as closed-form analyses





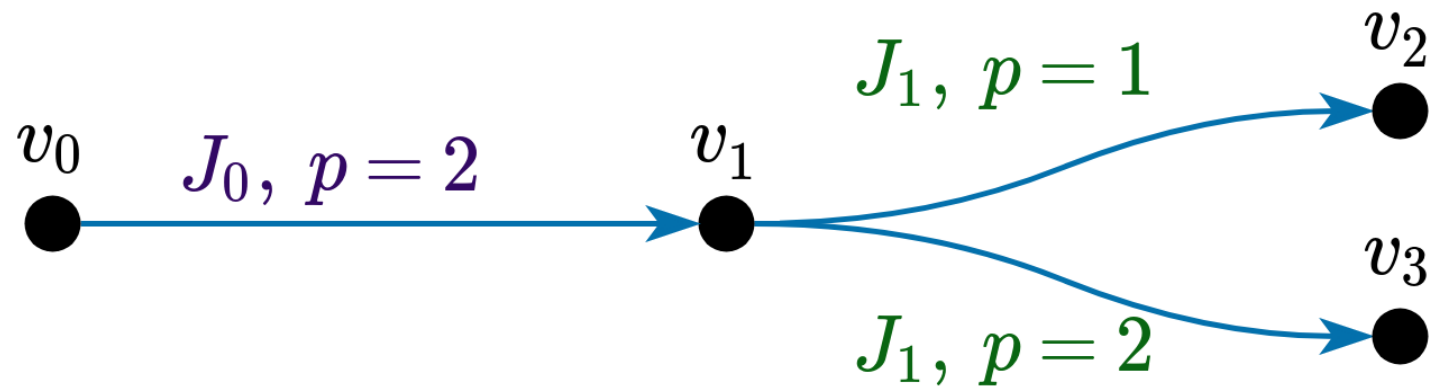
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# Schedule Abstraction Graph

- Accurate and relatively fast analysis
  - Faster than an exact analysis
  - Not as pessimistic as closed-form analyses
- Models scheduler decisions
- Encodes core availability after every transition



# Job-Level Fixed Priority Scheduler for Gang

- Based on Global JLFP scheduler
- Work conserving scheduler
- Job with highest priority goes first
- Assigns maximum cores available between  $s_i^{\min}$  and  $s_i^{\max}$

# Difficulties related to SAG

- We have to consider all scenarios.
- The scheduler has to decide:
  - When to release a job
  - How many cores to assign to this job

# Analysis

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- $LST_i$  Latest Start Time
- $EFT_i$  Earliest Finishing Time
- $LFT_i$  Latest Finishing Time

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$$EST_i \leq LST_i$$



# Analysis

- $A_c^{\min}$  time at which we have  $c$  cores possibly available
- $A_c^{\max}$  time at which we have  $c$  cores certainly available
- $EST_i^p$  Earliest Start Time
- $LST_i^p$  Latest Start Time
- $EFT_i^p$  Earliest Finishing Time
- $LFT_i^p$  Latest Finishing Time

$$EST_i^p \leq LST_i^p$$

# Analysis

$$EST_i^p = \max\{r_i^{\min}, A_p^{\min}\}$$

- Job cannot start before
  - Being released
  - Enough cores are available

$$LST_i^p = \min\{t_{p+1}, t_{wc}, t_{high} - 1\}$$

- Job cannot start with  $p$  cores after:
  - $p + 1$  cores are available as JLFP would schedule it with  $p + 1$  cores
  - A lower priority task is ready because JLFP is work-conserving
  - A higher priority task is ready

# Analysis

- Obtain  $EFT_i^p$  and  $LFT_i^p$  from:

$$EFT_i^p = EST_i^p + c_i^{\min}(p)$$

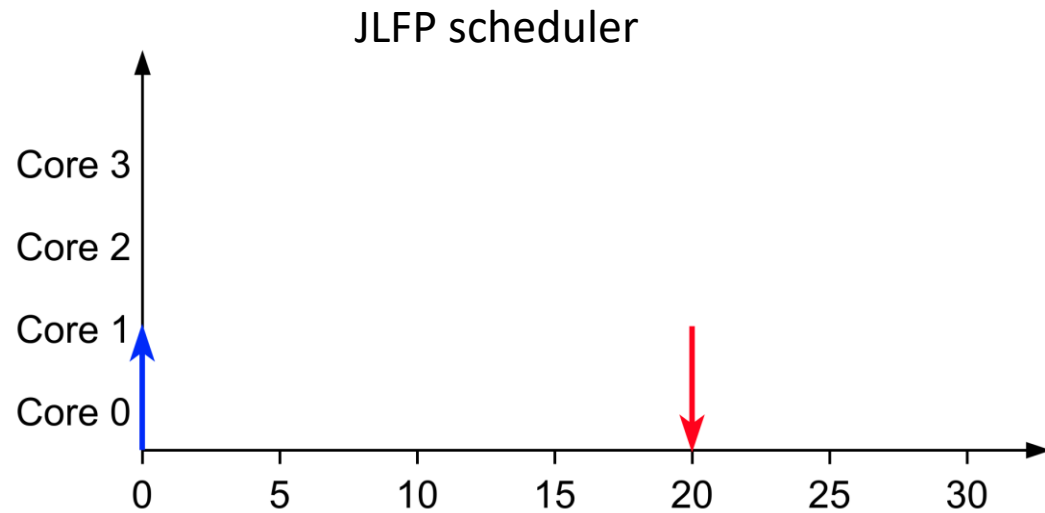
$$LFT_i^p = LST_i^p + c_i^{\max}(p)$$

- And compute new  $A_c^{\min}$  and  $A_c^{\max}$

# New scheduler

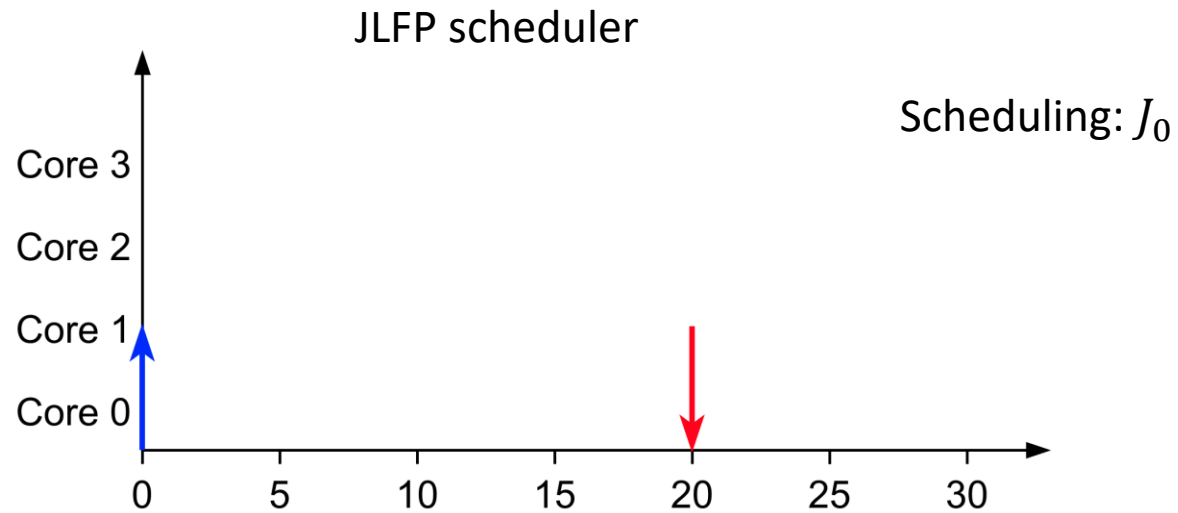
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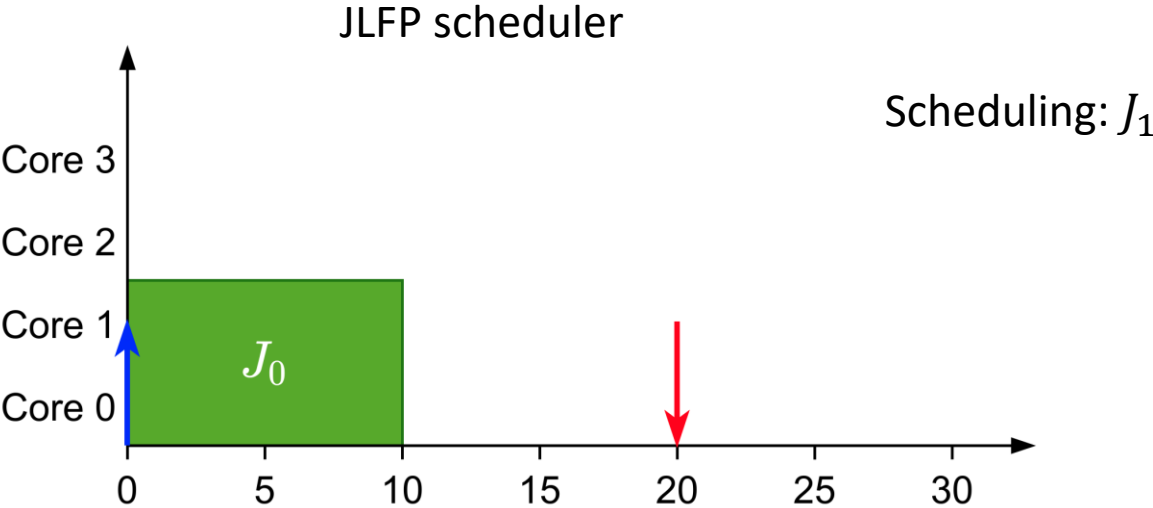
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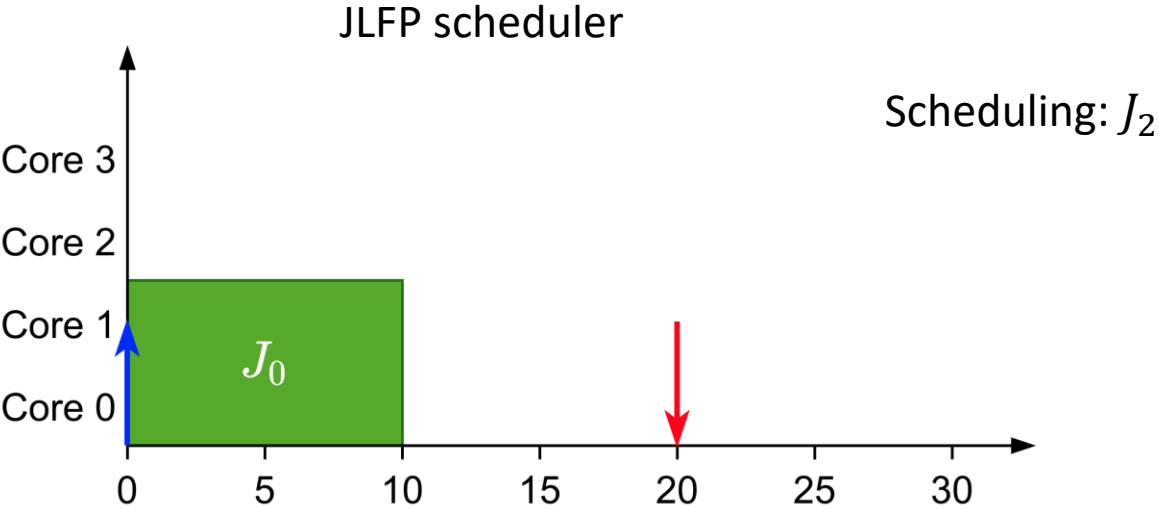
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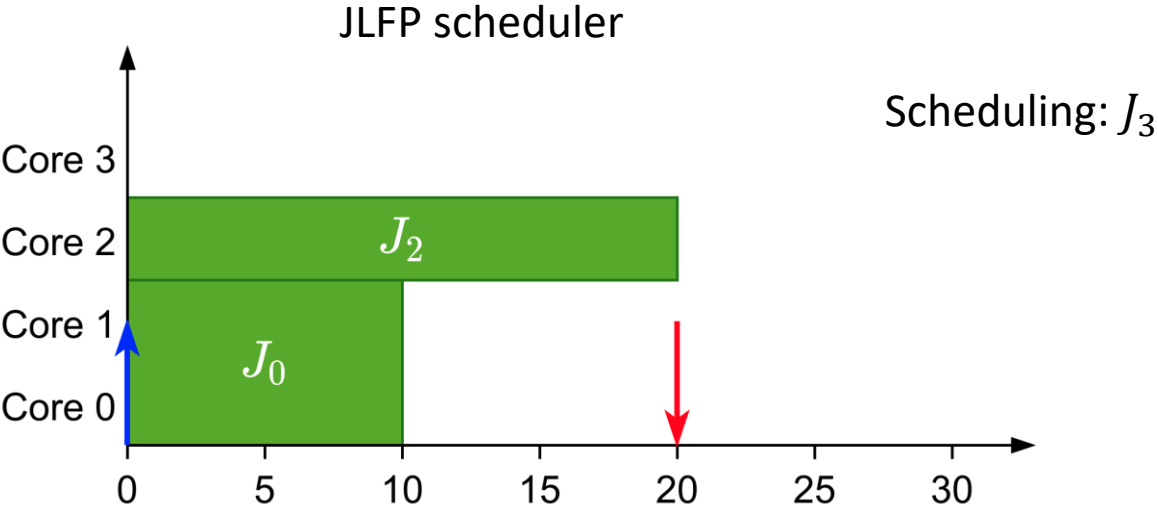


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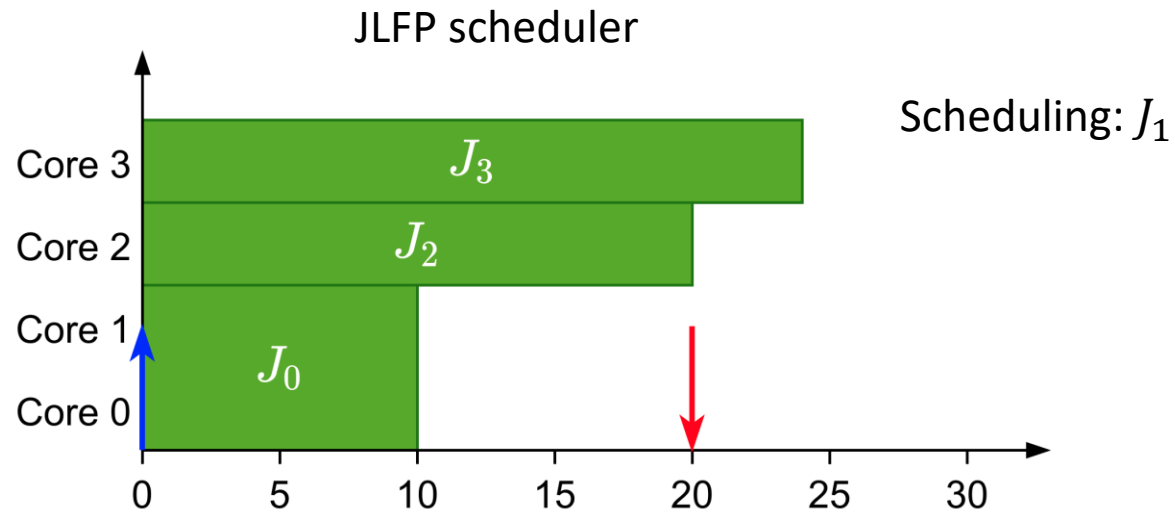
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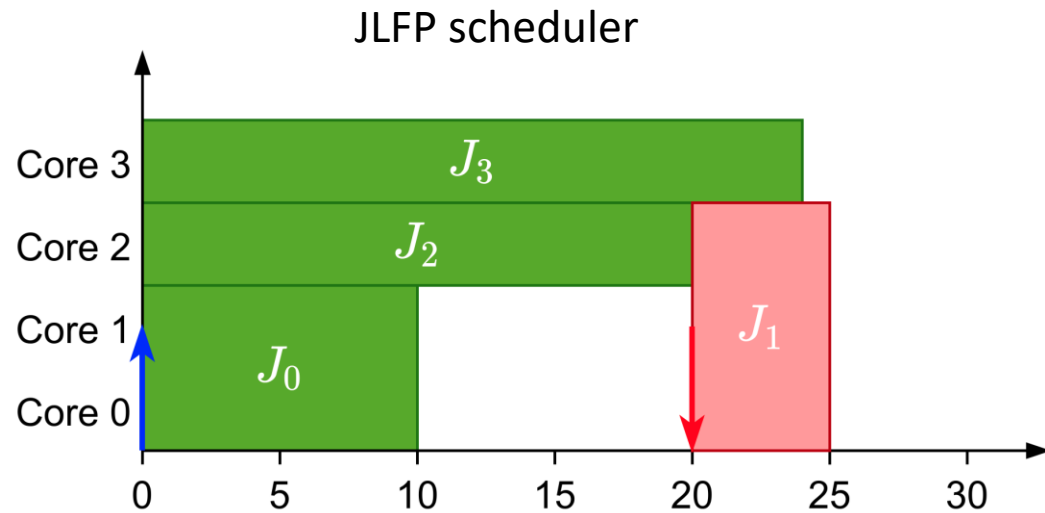
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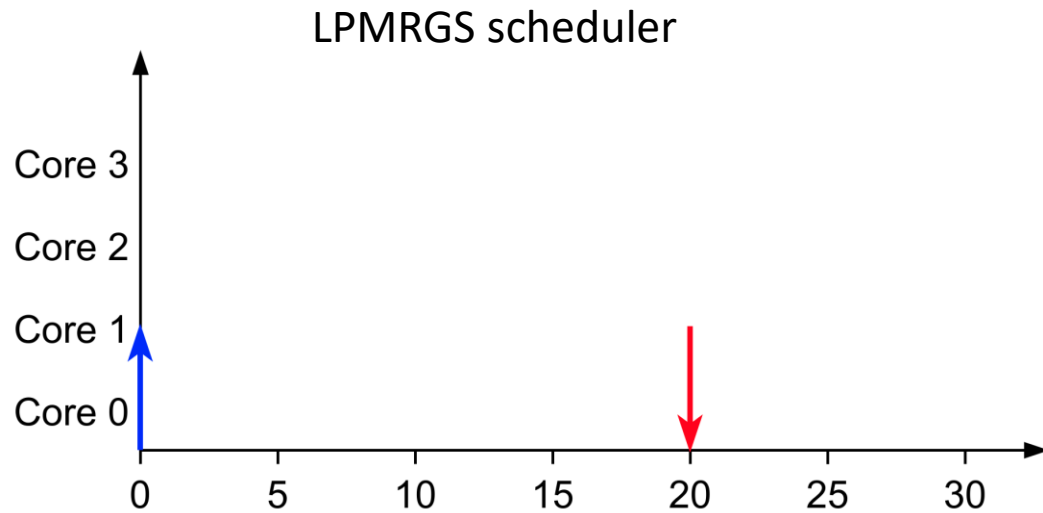
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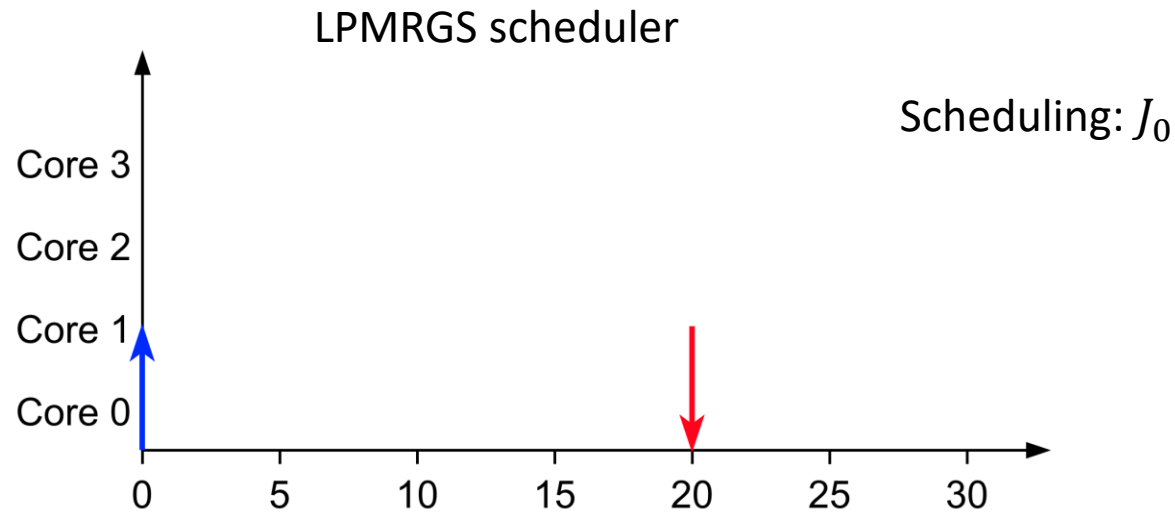
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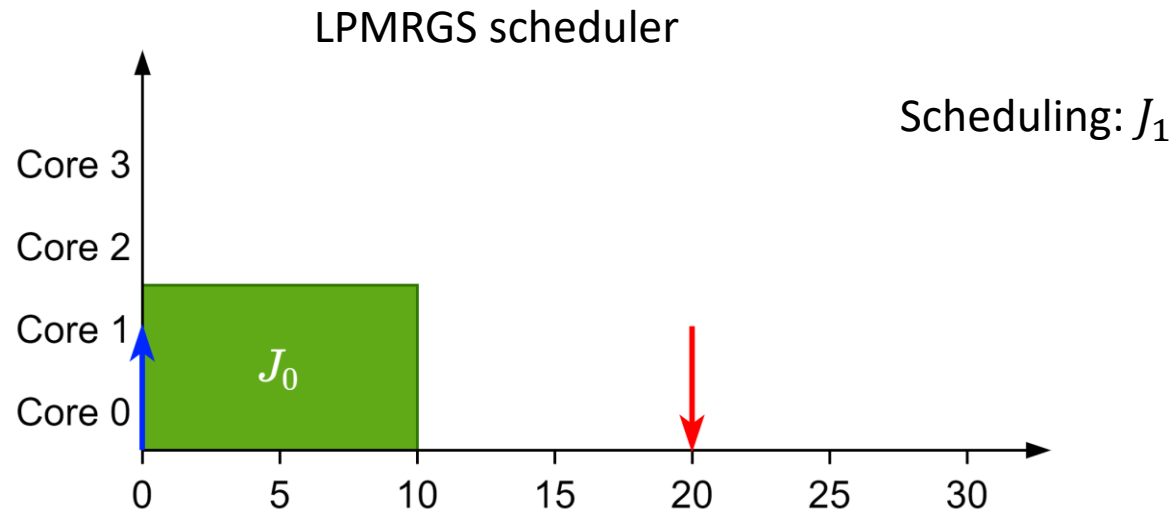
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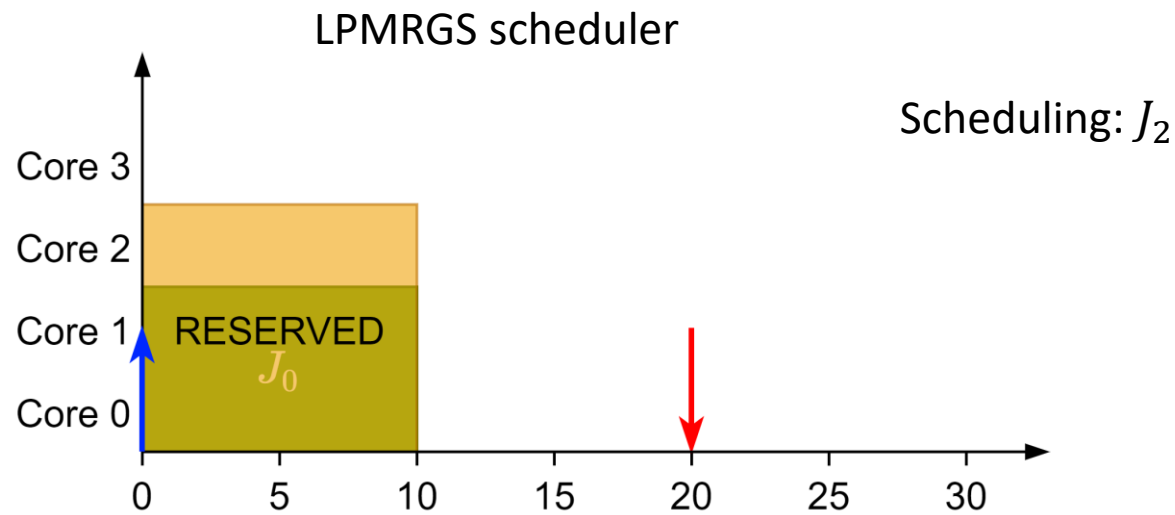


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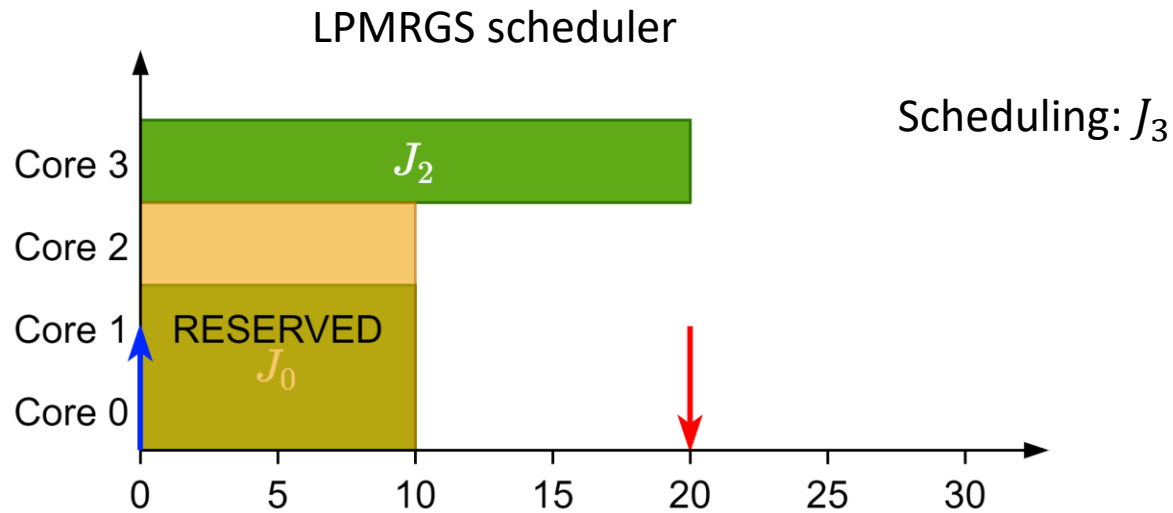
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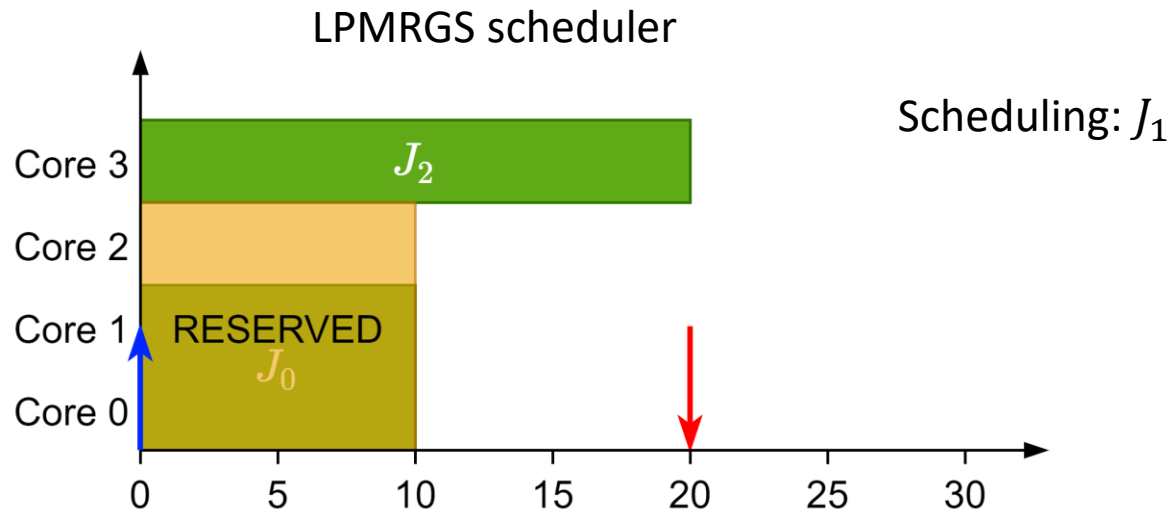
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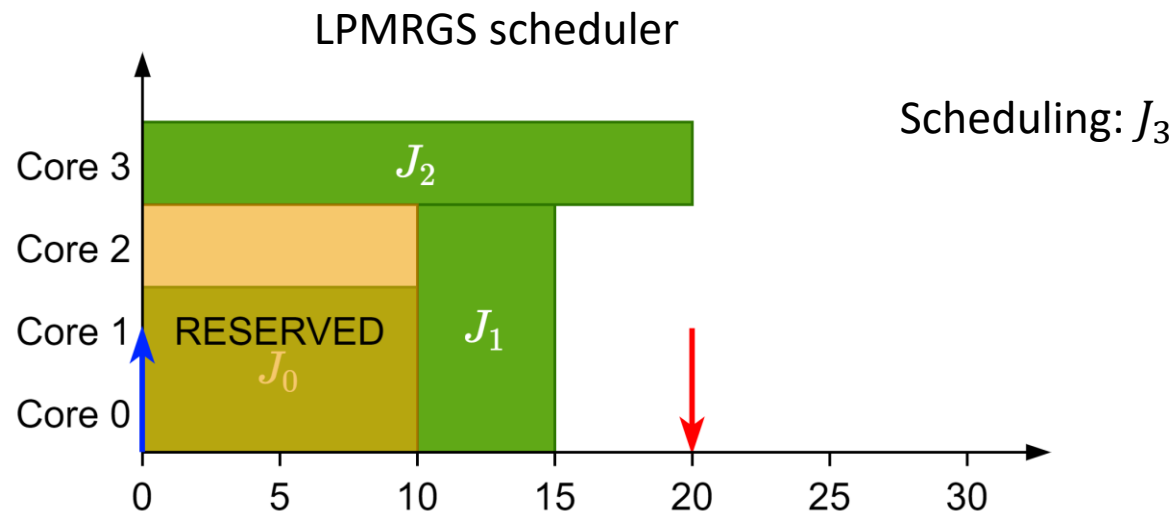
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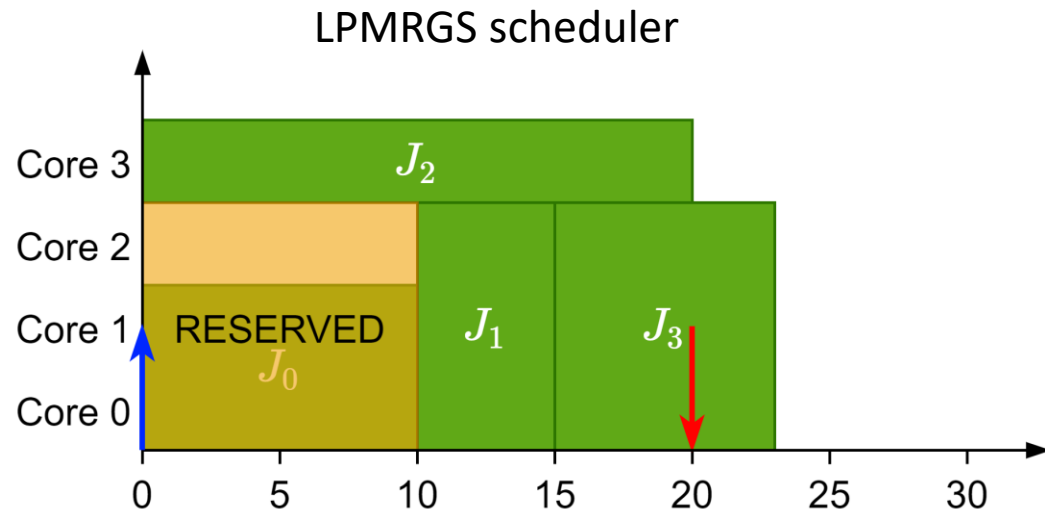
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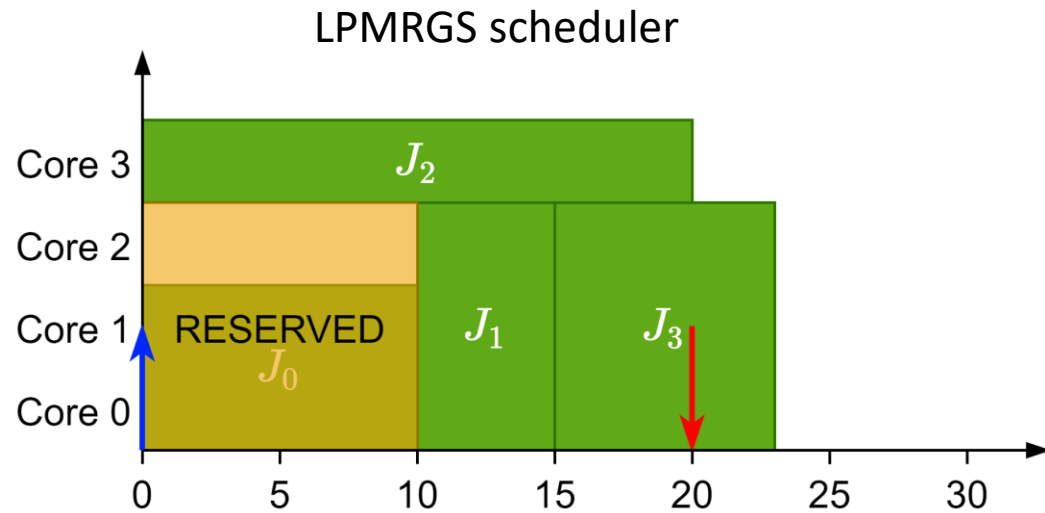
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- Limited-Preemptive Moldable Reservation Gang Scheduler
- Non-work conserving scheduler
- Reserve cores of higher-priority tasks and distribute the remaining ones among lower priority tasks



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# Results

# Questions?