CS181 Assignment 3

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1 Problem 1

1. The probability that all of the M dimensions of $x - y$ are between $-\epsilon$ and ϵ is
2. The probability of $max_m|x_m - y_m| \leq \epsilon$ is at most p
3. If x is any point in χ, and y is a point in χ drawn randomly from a uniform distribution on χ, then the probabilty that $||x - y|| \leq \epsilon$ is also at most p
4. Lowerbound on number N of points needed to guarantee
5. We can conclude that the effectiveness of the hierarchical agglomerativ clustering algorithm in high dimensional spaces

2 Problem 2

1. Given a prior distribution $Pr(\theta)$ and likelihood $Pr(D|\theta)$, the predictive distribution $Pr(x|D)$ for a new datum,
   (a) ML: $Pr(x|D) = Pr(x|\theta) = \arg\max_{\theta}(\ln(Pr(D|\theta)))$
   (b) MAP: $Pr(x|D) = Pr(x|D) = Pr(x|\theta) = \arg\max_{\theta}(\ln(P(D|\theta)P(\theta)))$
   (c) FB: $Pr(x|D) = \int \theta P(\theta|D)d\theta$
2. MAP can be considered "more Bayesian" than ML because
3. One advantage the MAP method enjoys over the Ml method
4. The Beta distribution ins the conjugate prior of the Bernoulli
5. Under the ML approach

3 Problem 3

1. The K -means clustering objective is to minimize the sum of squared distances between prototype and data.
2. PCA relates to K-means

4 Problem 4