

1. Jacobi method

$$x^{(k+1)} = D^{-1} \left(\underbrace{b}_{n \times 1} - \underbrace{C}_{n \times n} \underbrace{x^{(k)}}_{n \times 1} \right)$$

$2n^2 + 3n$ per iteration

for n rows so

Gauss Seidel method

$$2n^3 + 3n^2$$

$$x_i^{(k+1)} = \frac{1}{a_{ii}} \left(b_i - \sum_{j=1}^{i-1} a_{ij} x_j^{(k+1)} - \sum_{j=i+1}^n a_{ij} x_j^{(k)} \right)$$

$$n^2 \text{ for } i=1 \text{ to } n \text{ } + n^2 \text{ for } i=1 \text{ to } n$$

$$n (2n^2 + 3n - n_j) \quad 2n^2 + 3n - n_j$$

$$2n^3 + 3n^2 - n^2 j$$

Cholesky Decomp

$$L_{ii} = \sqrt{A_{ii} - \sum_{k=1}^{i-1} L_{ik}^2}$$

\downarrow
 $(i-1)$

\downarrow
 $n(i-1)$

$$L_{ij} = \frac{1}{L_{ii}} \left(A_{ji} - \sum_{k=1}^{i-1} L_{jk} L_{ik} \right)$$

\downarrow
 n^2

\downarrow
 n

$$n^3 + ni - n + 3$$