# **Exam 1 Review**

#### Question 1

The piecewise-defined function below represents the shipping charges, C(x), for packages based on the package weight, x (in pounds).

$$C(x) = \begin{cases} 4.50, & 0 < x \le 3 \\ 0.5(x-3) + 4.50, & 3 < x \le 10 \\ 0.5(x-10)^2 + 7.50, & 10 < x \le 12. \end{cases}$$

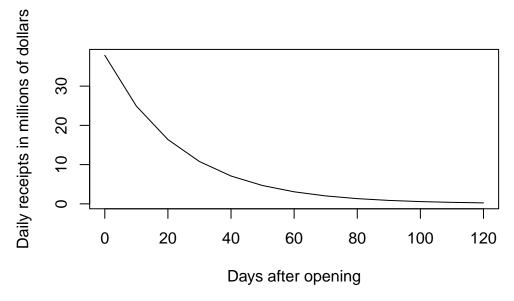
- a. Find C(2) and interpret its meaning in context.
- b. Find C(5) and interpret its meaning in context.
- c. Use a table to find the left limit of the function at x=3 (i.e.,  $\lim_{x\to 3^-}C(x)$ ).

d. Use a table to find the right limit of the function at x=3 (i.e.,  $\lim_{x\to 3^+}C(x)$ ).

e. Based on your work in parts (c) and (d), state whether the limit  $\lim_{x\to 3} C(x)$  exists and explain why. If the limit exists, find its value.

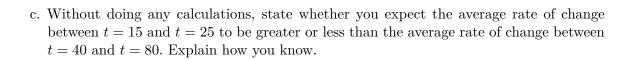
### Question 2

The daily receipts f(t) in millions of dollars of the movie "The Hunger Games" after its opening on 23 March 2012 had an exponential model shown below:



a. Estimate the value of f(20) and state its meaning in context.

b. Without doing any calculations, state whether you expect f(25) to be greater or less than f(30). Explain how you know.



d. Without doing any calculations, state whether you expect f'(30) to be negative or positive. Explain how you know.

e. Without doing any calculations, state whether you expect f''(30) to be positive or negative. Explain how you know.

#### Question 3

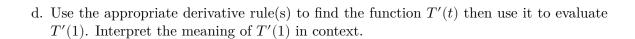
A climate model predicts that the average global temperature rise (in degrees Celsius) above pre-industrial levels can be approximated by the function  $T(t) = 0.008t^3 - 0.06t^2 + 0.5t + 0.2$ , where t represents time in decades since 2000.

a. Find T(2) and interpret its meaning in context.

b. Estimate the average rate of change in the global temperature rise between t=0 and t=1. Include units in your answer.

c. The expression below is for finding the *instantaneous rate of change* in the global temperature rise at t=1 using the limit definition of the derivative. Write down the next step. No need to evaluate the limit.

$$T'(1)=\lim_{h\to 0}\frac{T(1+h)-T(1)}{h}$$



e. Calculate T''(3) and interpret its meaning in context.

## Question 4

Use derivative rules to find the derivative function for each of the following functions:

a. 
$$f(x) = 3x^2 - 4x + 5$$

b. 
$$g(x) = \frac{x^5 + x^3}{x^2}$$

c. 
$$h(x) = \sqrt{x} + x^2$$

d. 
$$k(x) = 5^x + x^5$$

e. 
$$q(x) = e^x + 5x^4$$