

CIS6060 Assignment 2: Performance of Logistic Regression and Support Vector Machines Classifiers on Three Datasets

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I chose to add the popular Pima Indians diabetes dataset to the pipeline (<https://www.kaggle.com/uciml/pima-indians-diabetes-database>). These data were previously obtained and additional features were generated in R using an existing script (`make_diabetes_data.R`).

Results

The performance of logistic regression and support vector machines (SVM) classifiers were compared for three datasets: abalone (n = 4177, 7 variables, 3 classes); cancer (n = 79, 7129 genes, binary outcome, PCA transform was applied); and the Pima Indians diabetes dataset with interaction and quadratic terms (n = 768, 45 predictors, binary outcome). Performance metrics of interest (accuracy, precision, recall, and f1 score) were collected for analysis and hypothesis testing by paired t-tests. Two evaluations were performed for each classifier with the three dataset: from a single training-testing split (table 1), and from 5-fold cross-validation (table 2 and fig. 1).

In terms of dataset-specific performance, both classifiers achieved near-perfect accuracy on the cancer data (except SVM on the single test/train split), had good performance on the diabetes data (~0.8), and struggled with the abalone data (~0.55; tables 1 & 2). In evaluations with a single test-train split, both algorithms had similar performance with the various datasets except was on the cancer dataset, where logistic regression performed better in terms of recall (table 1).

Table 1: Performance estimates of logistic regression and support vector machines classifiers on the Abablone, Cancer, and Diabetes sets from a single train-test split.

data	Classifier	Accuracy	Precision	Recall	F1
Abalone	Logistic regression	0.54	0.53	0.53	0.47
Abalone	SVM	0.6	0.59	0.6	0.59
Cancer	Logistic regression	1	1	1	1
Cancer	SVM	0.83	1	0.5	0.67
Diabetes	Logistic regression	0.74	0.76	0.51	0.61
Diabetes	SVM	0.73	0.74	0.51	0.6

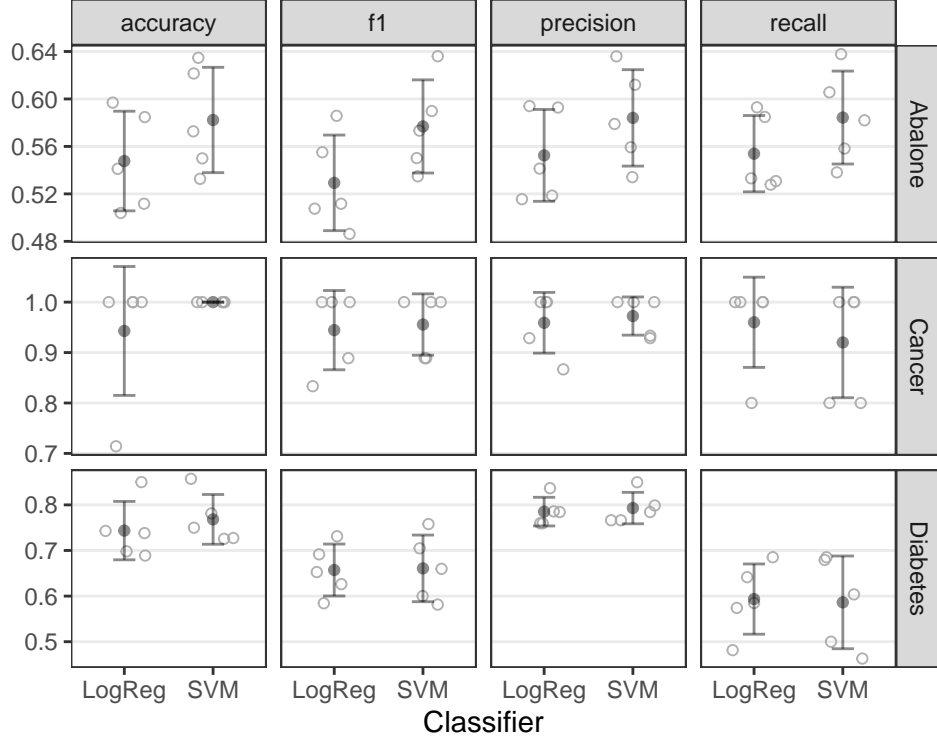


Figure 1: Performance metrics (accuracy, f1, precision, and recall) in 5-fold cross-validation of logistic regression and support vector classifiers for Abalone, Cancer, and Diabetes datasets. Means \pm sd are shown as black point and errorbars, with individual observations are shown as grey circles. Note that different scales are used for each dataset.

In evaluation by 5-fold cross-validation, I found that the support vector machine classifiers performed slightly better across datasets and metrics than the logistic regression classifier (with the exception of recall for the cancer data), however these differences only were significant at the $\alpha = 0.05$ level for the abalone dataset metrics (all four) and for precision on the diabetes data, according to paired t-tests (fig. 1, table 1). Perhaps if 10-fold cross validation were performed, the sample size would allow for lower-error estimates of performance, though the cancer dataset has only a few observations, making 10-fold cross-validation unfeasible.

Interestingly, the model hyperparameters selected through grid-search cross-validation often varied between folds of a given dataset (see end of document for list). For the abalone data, the best SVM classifiers always used the radial basis kernel, suggesting that the problem cannot be solved linearly (eg. by logistic regression). With the cancer and diabetes datasets, the best SVM classifiers always used the linear kernel with the smallest regularization penalty ($C = 1$), suggesting that these problems are more easily solved in linear space. The best logistic regression classifiers used the l1 regularization for the diabetes data but a mix of l1 and l2 tunings were selected with cancer and abalone data. The logistic regression penalty parameter varied between nearly all folds, but usually not by a large amount. As such, it is difficult to draw any clear conclusions from the optimal logistic regression tunings. Perhaps in some cases the l2 regularization performs better because of the variable selection process inherent to the method; this would make sense for the cancer data, where low importance PC's may not provide useful information.

Table 2: Estimates of performance from 5-fold cross-validation of logistic regression and SVM classifiers applied to 3 datasets. Data are expressed as ‘means (standard deviation)’

Dataset	Metric	Logistic Regression	SVM	p_value	sig
Abalone	accuracy	0.548 (0.042)	0.582 (0.044)	0.033	*
Abalone	f1	0.529 (0.04)	0.577 (0.039)	0.012	*
Abalone	precision	0.552 (0.039)	0.584 (0.041)	0.028	*
Abalone	recall	0.554 (0.032)	0.584 (0.039)	0.016	*
Cancer	accuracy	0.943 (0.128)	1 (0)	0.374	
Cancer	f1	0.944 (0.079)	0.956 (0.061)	0.374	
Cancer	precision	0.959 (0.06)	0.972 (0.038)	0.374	
Cancer	recall	0.96 (0.089)	0.92 (0.11)	0.374	
Diabetes	accuracy	0.744 (0.064)	0.768 (0.055)	0.119	
Diabetes	f1	0.657 (0.057)	0.661 (0.073)	0.707	
Diabetes	precision	0.785 (0.031)	0.793 (0.034)	0.033	*
Diabetes	recall	0.593 (0.077)	0.586 (0.102)	0.726	

Model hyperparameters selected in evaluations

Abalone test train

Logistic Regression: 'C': 0.0695, 'penalty': 'l1'
SVN: 'C': 10, 'gamma': 0.3, 'kernel': 'rbf'

Abalone 5 fold:

Logistic Regression: 'C': 4.83, 'penalty': 'l2' (x 2)
Logistic Regression: 'C': 0.021, 'penalty': 'l2'
Logistic Regression: 'C': 1.438, 'penalty': 'l1'
Logistic Regression: 'C': 0.038, 'penalty': 'l1'
SVN: 'C': 10, 'gamma': 0.3, 'kernel': 'rbf' (x 4)
SVN: 'C': 1, 'gamma': 0.1, 'kernel': 'rbf'

Cancer test train

Logistic Regression: 'C': 0.0207, 'penalty': 'l2'
SVN: 'C': 1, 'kernel': 'linear'

Cancer 5 fold:

Logistic Regression: 'C': 4.833, 'penalty': 'l2'
Logistic Regression: 'C': 0.0018, 'penalty': 'l2'
Logistic Regression: 'C': 0.0036, 'penalty': 'l2'
Logistic Regression: 'C': 100.0, 'penalty': 'l1'
Logistic Regression: 'C': 0.001, 'penalty': 'l2'
SVN: 'C': 1, 'kernel': 'linear' (all 5)

Diabetes test-train

Logistic Regression: 'C': 0.785, 'penalty': 'l1'
SVN: 'C': 1, 'kernel': 'linear'

Diabetes 5 fold:

Logistic Regression: all l1 penalty, variable C (0.2-2.63)
SVN: 'C': 1, 'kernel': 'linear' (all 5)