

1 SEARCH FOR PRODUCTION OF A HIGGS BOSON AND A SINGLE TOP
2 QUARK IN MULTILEPTON FINAL STATES IN pp COLLISIONS AT $\sqrt{s} = 13$
3 TeV.

4 by

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21 Multivariate techniques are used to discriminate the signal from the dominant back-
22 grounds. The analysis yields a 95% confidence level (C.L.) upper limit on the com-
23 bined tH + ttH production cross section times branching ratio of 0.64 pb, with an
24 expected limit of 0.32 pb, for a scenario with $k_t = \pm 1.0$ and $k_V = 1.0$. Values of k_t
25 outside the range of ± 1.25 to ± 1.60 are excluded at 95% C.L., assuming $k_V = 1.0$.

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³³⁴ Chapter 1

³³⁵ Theoretical approach

³³⁶ 1.1 Introduction

³³⁷ The physical description of the universe is a challenge that physicists have faced by
³³⁸ making theories that refine existing principles and proposing new ones in an attempt
³³⁹ to embrace emerging facts and phenomena.

³⁴⁰ At the end of 1940s Julian Schwinger [1] and Richard P. Feynman [2], based on
³⁴¹ the work of Sin-Itiro Tomonaga [3], developed an electromagnetic theory consistent
³⁴² with special relativity and quantum mechanics that describes how matter and light
³⁴³ interact; the so-called *quantum electrodynamics* (QED) was born.

³⁴⁴ QED has become the blueprint for developing theories that describe the universe.
³⁴⁵ It was the first example of a quantum field theory (QFT), which is the theoretical
³⁴⁶ framework for building quantum mechanical models that describes particles and their
³⁴⁷ interactions. QFT is composed of a set of mathematical tools that combines classical
³⁴⁸ fields, special relativity and quantum mechanics, while keeping the quantum point
³⁴⁹ particles and locality ideas.

³⁵⁰ This chapter gives an overview of the standard model of particle physics, starting

351 with a description of the particles and their interactions, followed by a description of
 352 the electroweak interaction, the Higgs boson and the associated production of Higgs
 353 boson and a single top quark (tH). The description contained in this chapter is based
 354 on References [4–6].

355 1.2 Standard model of particle physics

356 The *standard model of particle physics (SM)* describes particle physics at the funda-
 357 mental level in terms of a collection of interacting particles and fields. The full picture
 358 of the SM is composed of three fields¹ whose excitations are interpreted as particles
 359 called mediators or force-carriers, a set of fields whose excitations are interpreted as
 360 elementary particles interacting through the exchange of those mediators, and a field
 361 that gives the mass to elementary particles. Figure 1.1 shows a scheme of the SM
 362 particles’ organization. In addition, for each of the particles in the scheme there exists
 363 an antiparticle with the same mass and opposite quantum numbers. The existence of
 364 antiparticles is a prediction of the relativistic quantum mechanics from the solution
 365 of the Dirac equation for which a negative energy solution is also possible. In some
 366 cases a particle is its own anti-particle, like photon or Higgs boson.

367 The mathematical formulation of the SM is based on group theory and the use of
 368 Noether’s theorem [8] which states that for a physical system modeled by a Lagrangian
 369 that is invariant under a group of transformations a conservation law is expected. For
 370 instance, a system described by a time-independent Lagrangian is invariant (symmet-
 371 ric) under time changes (transformations) with the total energy conservation law as
 372 the expected conservation law. In QED, the charge operator (Q) is the generator of

¹ The formal and complete treatment of the SM is out of the scope of this document, however a plenty of textbooks describing it at several levels are available in the literature. The treatment in References [5, 6] is quite comprehensive and detailed. Note that gravitational field is not included in the standard model formulation

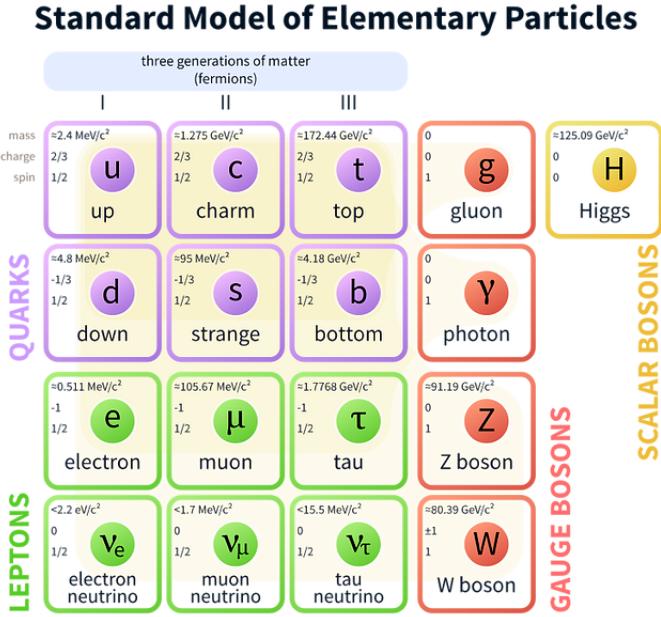


Figure 1.1: Schematic representation of the Standard Model of particle physics. The SM is a theoretical model intended to describe three of the four fundamental forces of the universe in terms of a set of particles and their interactions. [7].

373 the U(1) symmetry which according to the Noether's theorem means that there is a
374 conserved quantity; this conserved quantity is the electric charge and thus the law
375 conservation of electric charge is established.

In the SM, the symmetry group $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ describes three of the four fundamental interactions in nature (see Section 1.2.2): strong interaction (SI), weak interaction (WI) and electromagnetic interactions (EI) in terms of symmetries associated to physical quantities:

- 380 • Strong: $SU(3)_C$ associated to color charge

381 • Weak: $SU(2)_L$ associated to weak isospin and chirality

382 • Electromagnetic: $U(1)_Y$ associated to weak hypercharge and electric charge

383 It will be shown that the electromagnetic and weak interactions are combined in

384 the so-called electroweak interaction where chirality, hypercharge, weak isospin and
 385 electric charge are the central concepts.

386 **1.2.1 Fermions**

387 The basic constituents of the ordinary matter at the lowest level, which form the set
 388 of elementary particles in the SM formulation, are quarks and leptons. All of them
 389 have spin 1/2, therefore they are classified as fermions since they obey Fermi-Dirac
 390 statistics. There are six *flavors* of quarks and three of leptons organized in three
 391 generations, or families, as shown in Table 1.1.

		Generation		
		1st	2nd	3rd
Leptons	Type	Charged	Electron (e)	Moun(μ)
	Neutral	Electron neutrino (ν_e)	Muon neutrino (ν_μ)	Tau neutrino (ν_τ)
Quarks	Up-type	Up (u)	Charm (c)	Top (t)
	Down-type	Down (d)	Strange (s)	Bottom (b)

Table 1.1: Fermions of the SM. There are six flavors of quarks and three of leptons, organized in three generations, or families, composed of two pairs of closely related particles. The close relationship is motivated by the fact that each pair of particles is a member of an $SU(2)_L$ doublet that has an associated invariance under isospin transformations. WI between leptons is limited to the members of the same generation; WI between quarks is not limited but greatly favored, to same generation members.

392

393 There is a mass hierarchy between generations (see Table 1.2), where the higher
 394 generation particles decays to the lower one, which can explain why the ordinary
 395 matter is made of particles from the first generation. In the SM, neutrinos are modeled
 396 as massless particles so they are not subject to this mass hierarchy; however, today it
 397 is known that neutrinos are massive so the hierarchy could be restated. The reason
 398 behind this mass hierarchy is one of the most important open questions in particle
 399 physics, and it becomes more puzzling when noticing that the mass difference between

400 first and second generation fermions is small compared to the mass difference with
 401 respect to the third generation.

Lepton	Mass (MeV/c ²)	Quark	Mass (MeV/c ²)
e	0.51	u	2.2
μ	105.65	c	1.28×10^3
τ	1776.86	t	173.1×10^3
ν_e	Unknown	d	4.7
ν_μ	Unknown	s	96
τ_μ	Unknown	b	4.18×10^3

Table 1.2: Fermion masses [9]. Generations differ by mass in a way that has been interpreted as a mass hierarchy. Approximate values with no uncertainties are used, for comparison purpose.

402

403 Usually, the second and third generation fermions are produced in high energy
 404 processes, like the ones recreated in particle accelerators.

405 **1.2.1.1 Leptons**

406 A lepton is an elementary particle that is not subject to the SI. As seen in Table 1.1,
 407 there are two types of leptons, the charged ones (electron, muon and tau) and the
 408 neutral ones (the three neutrinos). The electric charge (Q) is the property that gives
 409 leptons the ability to participate in the EI. From the classical point of view, Q plays
 410 a central role determining, among others, the strength of the electric field through
 411 which the electromagnetic force is exerted. It is clear that neutrinos are not affected
 412 by EI because they don't carry electric charge.

413 Another feature of the leptons that is fundamental in the mathematical description
 414 of the SM is the chirality, which is closely related to spin and helicity. Helicity
 415 defines the handedness of a particle by relating its spin and momentum such that
 416 if they are parallel then the particle is right-handed; if spin and momentum are

417 antiparallel the particle is said to be left-handed. The study of parity conservation
 418 (or violation) in β -decay has shown that only left-handed electrons/neutrinos or right-
 419 handed positrons/anti-neutrinos are created [10]; the inclusion of that feature in the
 420 theory was achieved by using projection operators for helicity, however, helicity is
 421 frame dependent for massive particles which makes it not Lorentz invariant and then
 422 another related attribute has to be used: *chirality*.

423 Chirality is a purely quantum attribute which makes it not so easy to describe in
 424 graphical terms but it defines how the wave function of a particle transforms under
 425 certain rotations. As with helicity, there are two chiral states, left-handed chiral (L)
 426 and right-handed chiral (R). In the highly relativistic limit where $E \approx p \gg m$ helicity
 427 and chirality converge, becoming exactly the same for massless particles.

428 In the following, when referring to left-handed (right-handed) it will mean left-
 429 handed chiral (right-handed chiral). The fundamental fact about chirality is that
 430 while EI and SI are not sensitive to chirality, in WI left-handed and right-handed
 431 fermions are treated asymmetrically, such that only left-handed fermions and right-
 432 handed anti-fermions are allowed to couple to WI mediators, which is a violation of
 433 parity. The way to translate this statement in a formal mathematical formulation is
 434 based on the isospin symmetry group $SU(2)_L$.

435 Each generation of leptons is seen as a weak isospin doublet.² The left-handed
 436 charged lepton and its associated left-handed neutrino are arranged in doublets of
 437 weak isospin $T=1/2$ while their right-handed partners are singlets:

$$\begin{pmatrix} \nu_l \\ l \end{pmatrix}_L, l_R := \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L, e_R, \mu_R, \tau_R, \nu_{eR}, \nu_{\mu R}, \nu_{\tau R} \quad (1.1)$$

438 The isospin third component refers to the eigenvalues of the weak isospin operator

² The weak isospin is an analogy of the isospin symmetry in strong interaction where neutron and proton are affected equally by strong force but differ in their charge.

439 which for doublets is $T_3 = \pm 1/2$, while for singlets it is $T_3 = 0$. The physical meaning
 440 of this doublet-singlet arrangement falls in that the WI couples the two particles in
 441 the doublet by exchanging the interaction mediator while the singlet member is not
 442 involved in WI. The main properties of the leptons are summarized in Table 1.3.

443 Although all three flavor neutrinos have been observed, their masses remain un-
 444 known and only some estimations have been made [11]. The main reason is that
 445 the flavor eigenstates are not the same as the mass eigenstates which implies that
 446 when a neutrino is created its mass state is a linear combination of the three mass
 447 eigenstates and experiments can only probe the squared difference of the masses. The
 448 Pontecorvo-Maki-Nakagawa-Sakata (PMNS) mixing matrix encodes the relationship
 449 between flavor and mass eigenstates.

Lepton	$Q(e)$	T_3	L_e	L_μ	L_τ	Lifetime (s)
Electron (e)	-1	-1/2	1	0	0	Stable
Electron neutrino(ν_e)	0	1/2	1	0	0	Unknown
Muon (μ)	-1	-1/2	0	1	0	2.19×10^{-6}
Muon neutrino (ν_μ)	0	1/2	0	1	0	Unknown
Tau (τ)	-1	-1/2	0	0	1	290.3×10^{-15}
Tau neutrino (ν_τ)	0	1/2	0	0	1	Unknown

Table 1.3: Lepton properties [9]. Q: electric charge, T_3 : weak isospin. Only left-handed leptons and right-handed anti-leptons participate in the WI. Anti-particles with inverted T_3 , Q and lepton number complete the leptons set but are not listed. Right-handed leptons and left-handed anti-leptons, neither listed, form weak isospin singlets with $T_3 = 0$ and do not take part in the weak interaction.

450

451 1.2.1.2 Quarks

452 Quarks are the basic constituents of protons and neutrons. The way quarks join to
 453 form bound states, called *hadrons*, is through the SI. Quarks are affected by all the
 454 fundamental interactions which means that they carry all the four types of charges:
 455 color, electric charge, weak isospin and mass.

Flavor	$Q(e)$	I_3	T_3	B	C	S	T	B'	Y	Color
Up (u)	2/3	1/2	1/2	1/3	0	0	0	0	1/3	r,b,g
Charm (c)	2/3	0	1/2	1/3	1	0	0	0	4/3	r,b,g
Top(t)	2/3	0	1/2	1/3	0	0	1	0	4/3	r,b,g
Down(d)	-1/3	-1/2	-1/2	1/3	0	0	0	0	1/3	r,b,g
Strange(s)	-1/3	0	-1/2	1/3	0	-1	0	0	-2/3	r,b,g
Bottom(b)	-1/3	0	-1/2	1/3	0	0	0	-1	-2/3	r,b,g

Table 1.4: Quark properties [9]. Q: electric charge, I_3 : isospin, T_3 : weak isospin, B: baryon number, C: charmness, S: strangeness, T: topness, B' : bottomness, Y: hypercharge. Anti-quarks posses the same mass and spin as quarks but all charges (color, flavor numbers) have opposite sign.

456

457 Table 1.4 summarizes the features of quarks, among which the most remarkable
 458 is their fractional electric charge. Note that fractional charge is not a problem, given
 459 that quarks are not found isolated, but serves to explain how composed particles are
 460 formed out of two or more valence quarks³.

461 Color charge is responsible for the SI between quarks and is the symmetry ($SU(3)_C$)
 462 that defines the formalism to describe SI. There are three colors: red (r), blue (b)
 463 and green (g) and their corresponding three anti-colors; thus each quark carries one
 464 color unit while anti-quarks carries one anti-color unit. As explained in Section 1.2.2,
 465 quarks are not allowed to be isolated due to the color confinement effect, hence, their
 466 features have been studied indirectly by observing their bound states created when

- 467 • one quark with a color charge is attracted by an anti-quark with the correspond-
 468 ing anti-color charge forming a colorless particle called a *meson*.

 469 • three quarks (anti-quarks) with different color (anti-color) charges are attracted
 470 among them forming a colorless particle called a *baryon (anti-baryon)*.

³ Hadrons can contain an indefinite number of virtual quarks and gluons, known as the quark and gluon sea, but only the valence quarks determine hadrons' quantum numbers.

471 In practice, when a quark is left alone isolated a process called *hadronization* occurs
 472 where the quark emits gluons (see Section 1.2.4) which eventually will generate new
 473 quark-antiquark pairs and so on; those quarks will recombine to form hadrons that
 474 will decay into leptons. This proliferation of particles looks like a *jet* coming from
 475 the isolated quark. More details about the hadronization process and jet structure
 476 will be given in chapter3.

477 In the first version of the quark model (1964), M. Gell-Mann [12] and G. Zweig
 478 [13, 14] developed a consistent way to classify hadrons according to their properties.
 479 Only three quarks (u, d, s) were involved in a scheme in which all baryons have baryon
 480 number $B=1$ and therefore quarks have $B=1/3$; non-baryons have $B=0$. Baryon
 481 number is conserved in SI and EI which means that single quarks cannot be created
 482 but in pairs $q - \bar{q}$.

483 The scheme organizes baryons in a two-dimensional space (I_3 - Y); Y (hyper-
 484 charge) and I_3 (isospin) are quantum numbers related by the Gell-Mann-Nishijima
 485 formula [15, 16]:

$$Q = I_3 + \frac{Y}{2} \quad (1.2)$$

486 where $Y = B + S + C + T + B'$ are the quantum numbers listed in Table 1.4.

487 There are six quark flavors organized in three generations (see Table 1.1) fol-
 488 lowing a mass hierarchy which, again, implies that higher generations decay to first
 489 generation quarks.

	Quarks			T_3	Y_W	Leptons			T_3	Y_W
Doublets	$(\frac{u}{d'})_L$	$(\frac{c}{s'})_L$	$(\frac{t}{b'})_L$	$(\frac{1/2}{-1/2})$	$1/3$	$(\nu_e)_L$	$(\nu_\mu)_L$	$(\nu_\tau)_L$	$(\frac{1/2}{-1/2})$	-1
Singlets	u_R	c_R	t_R	0	$4/3$	ν_{eR}	$\nu_{\mu R}$	$\nu_{\tau R}$		
	d'_R	s'_R	b'_R	0	$-2/3$	e_R	μ_R	τ_R	0	-2

Table 1.5: Fermion weak isospin and weak hypercharge multiplets. Weak hypercharge is calculated through the Gell-Mann-Nishijima formula 1.2 but using the weak isospin and charge for quarks.

490

491 Isospin doublets of quarks are also defined (see Table 1.5), and same as for neutrinos,
 492 the WI eigenstates are not the same as the mass eigenstates which means that
 493 members of different quark generations are connected by the WI mediator; thus, up-
 494 type quarks are coupled not to down-type quarks (the mass eigenstates) directly but
 495 to a superposition of down-type quarks (q'_d ; *the weak eigenstates*) via WI according
 496 to:

497

$$q'_d = V_{CKM} q_d$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad (1.3)$$

498 where V_{CKM} is known as Cabibbo-Kobayashi-Maskawa (CKM) mixing matrix [17,18]
 499 given by

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} = \begin{pmatrix} 0.97427 \pm 0.00015 & 0.22534 \pm 0.00065 & 0.00351^{+0.00015}_{-0.00014} \\ 0.22520 \pm 0.00065 & 0.97344 \pm 0.00016 & 0.0412^{+0.0011}_{-0.0005} \\ 0.00867^{+0.00029}_{-0.00031} & 0.0404^{+0.0011}_{-0.0005} & 0.999146^{+0.000021}_{-0.000046} \end{pmatrix}. \quad (1.4)$$

500 The weak decays of quarks are represented in the diagram of Figure 1.2; again
 501 the CKM matrix plays a central role since it contains the probabilities for the differ-
 502 ent quark decay channels, in particular, note that quark decays are greatly favored
 503 between generation members.

504 CKM matrix is a 3×3 unitary matrix parametrized by three mixing angles and
 505 the *CP-mixing phase*; the latter is the parameter responsible for the Charge-Parity

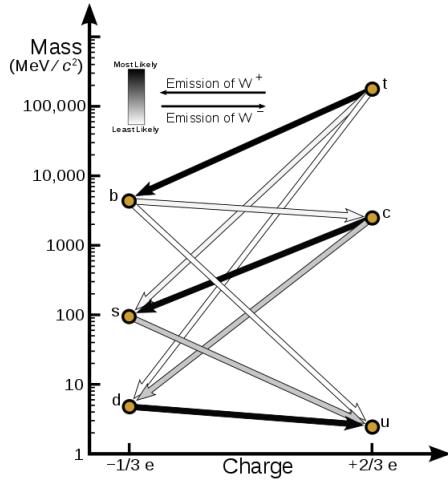


Figure 1.2: Transformations between quarks through the exchange of a WI. Higher generations quarks decay to first generation quarks by emitting a W boson. The arrow color indicates the likelihood of the transition according to the grey scale in the top left side which represent the CKM matrix parameters [19].

506 symmetry violation (CP-violation) in the SM. The fact that the top quark decays
 507 almost all the time to a bottom quark is exploited in this thesis when making the
 508 selection of the signal events by requiring the presence of a jet tagged as a jet coming
 509 from a b quark in the final state.

510 1.2.2 Fundamental interactions

511 Even though there are many manifestations of force in nature, like the ones repre-
 512 sented in Figure 1.3, we can classify all of them in four fundamental interactions:

- 513 • *Electromagnetic interaction (EI)* affects particles that are *electrically charged*,
 514 like electrons and protons. Figure 1.4a. shows a graphical representation, known
 515 as *Feynman diagram*, of electron-electron scattering.
- 516 • *Strong interaction (SI)* described by Quantum Chromodynamics (QCD). Hadrons
 517 like the proton and the neutron have internal structure given that they are com-

Fundamental interactions.

Illustration: Typoform

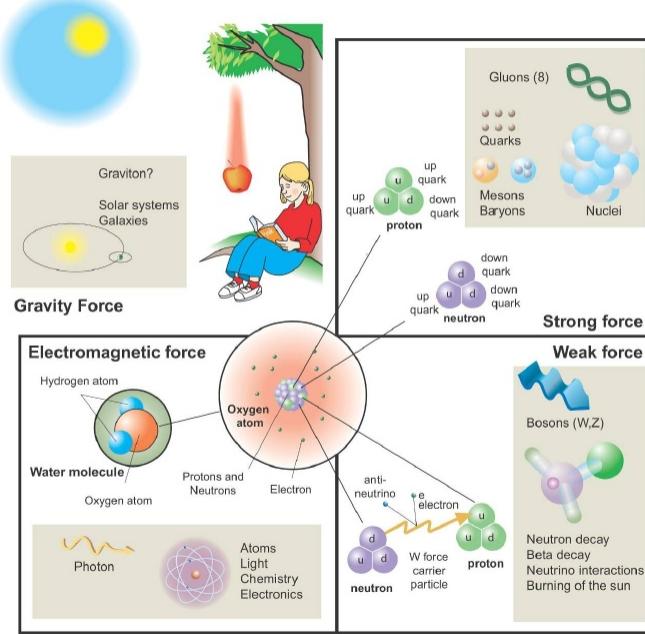


Figure 1.3: Fundamental interactions in nature. Despite the many manifestations of forces in nature, we can track all of them back to one of the fundamental interactions. The most common forces are gravity and electromagnetic given that all of us are subject and experience them in everyday life.

518 posed of two or more valence quarks⁴. Quarks have fractional electric charge
 519 which means that they are subject to electromagnetic interaction and in the case
 520 of the proton they should break apart due to electrostatic repulsion; however,
 521 quarks are held together inside the hadrons against their electrostatic repulsion
 522 by the *Strong Force* through the exchange of *gluons*. The analog to the electric
 523 charge is the *color charge*. Electrons and photons are elementary particles as
 524 quarks but they don't carry color charge, therefore they are not subject to SI. A
 525 Feynman diagram for gluon exchange between quarks is shown in Figure 1.4b.

 526 • *Weak interaction (WI)* described by the weak theory (WT), is responsible, for
 527 instance, for the radioactive decay in atoms and the deuterium production

⁴ Particles made of four and five quarks are exotic states not so common.

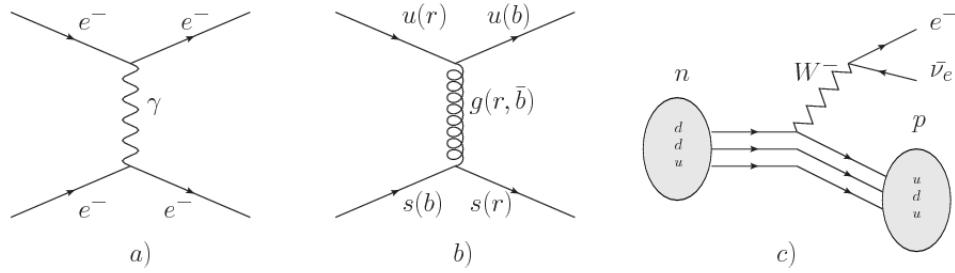


Figure 1.4: Feynman diagrams representing the interactions in SM; a) EI: e - e scattering; b) SI: gluon exchange between quarks ; c) WI: β -decay

within the sun. Quarks and leptons are the particles affected by the weak interaction; they possess a property called *flavor charge* (see 1.2.1) which can be changed by emitting or absorbing one weak force mediator. There are three mediators of the *weak force* known as Z boson in the case of electrically neutral flavor changes and W^\pm bosons in the case of electrically charged flavor changes. The *weak isospin* is the WI analog to electric charge in EI, and color charge in SI, and defines how quarks and leptons are affected by the weak force. Figure 1.4c. shows the Feynman diagram of β -decay where a neutron (n) is transformed in a proton (p) by emitting a W^- particle.

- *Gravitational interaction (GI)* described by General Theory of Relativity (GR). It is responsible for the structure of galaxies and black holes as well as the expansion of the universe. As a classical theory, in the sense that it can be formulated without even appeal to the concept of quantization, it implies that the space-time is a continuum and predictions can be made without limitation to the precision of the measurement tools. The latter represents a direct contradiction of the quantum mechanics principles. Gravity is deterministic while quantum mechanics is probabilistic; despite that, efforts to develop a quantum theory of gravity have predicted the *graviton* as mediator of the gravitational

546 force⁵.

Interaction	Acts on	Relative strength	Range (m)	Mediators
Electromagnetic (QED)	Electrically charged particles	10^{-2}	Infinite	Photon
Strong (QCD)	Quarks and gluons	1	10^{-15}	Gluon
Weak (WI)	Leptons and quarks	10^{-6}	10^{-18}	W^\pm, Z
Gravitational (GI)	Massive particles	10^{-39}	Infinite	Graviton

Table 1.6: Fundamental interactions features [20].

547

548 Table 1.6 summarizes the main features of the fundamental interactions. The
 549 strength of the interactions is represented by the coupling constants which depend
 550 on the energy scale at which the interaction is evaluated, therefore, it is the relative
 551 strength of the fundamental forces that reveals the meaning of strong and weak; in
 552 a context where the relative strength of the SI is 1, the EI is about hundred times
 553 weaker and WI is about million times weaker than the SI. A good description on how
 554 the relative strength and range of the fundamental interactions are calculated can
 555 be found in References [20, 21]. In the everyday life, only EI and GI are explicitly
 556 experienced due to the range of these interactions; i.e., at the human scale distances
 557 only EI and GI have appreciable effects, in contrast to SI which at distances greater
 558 than 10^{-15} m become negligible. Is it important to clarify that the weakness of the
 559 WI is attributed to the fact that its mediators are highly massive which affects the
 560 propagators of the interaction, as a result, the effect of the coupling constant is
 561 reduced.

⁵ Actually a wide variety of theories have been developed in an attempt to describe gravity; some famous examples are string theory and supergravity.

562 **1.2.3 Gauge invariance.**

563 QED was built successfully on the basis of the classical electrodynamics theory (CED)
 564 of Maxwell and Lorentz, following theoretical and experimental requirements imposed
 565 by

- 566 • Lorentz invariance: independence on the reference frame.
- 567 • Locality: interacting fields are evaluated at the same space-time point to avoid
 568 action at a distance.
- 569 • Renormalizability: physical predictions are finite and well defined.
- 570 • Particle spectrum, symmetries and conservation laws already known must emerge
 571 from the theory.
- 572 • Local gauge invariance.

573 The gauge invariance requirement reflects the fact that the fundamental fields
 574 cannot be directly measured but associated fields which are the observables. Electric
 575 (**E**) and magnetic (**B**) fields in CED are associated with the electric scalar potential
 576 V and the vector potential **A**. In particular, **E** can be obtained by measuring the
 577 change in the space of the scalar potential (ΔV); however, two scalar potentials
 578 differing by a constant f correspond to the same electric field. The same happens
 579 in the case of the vector potential **A**; thus, different configurations of the associated
 580 fields result in the same set of values of the observables. The freedom in choosing one
 581 particular configuration is known as *gauge freedom*; the transformation law connecting
 582 two configurations is known as *gauge transformation* and the fact that the observables
 583 are not affected by a gauge transformation is called *gauge invariance*.

584 When the gauge transformation:

$$\begin{aligned} \mathbf{A} &\rightarrow \mathbf{A} - \Delta f \\ V &\rightarrow V - \frac{\partial f}{\partial t} \end{aligned} \tag{1.5}$$

585 is applied to Maxwell equations, they are still satisfied and the fields remain invariant.
 586 Thus, CED is invariant under gauge transformations and is called a *gauge theory*.
 587 The set of all gauge transformations form the *symmetry group* of the theory, which
 588 according to the group theory, has a set of *group generators*. The number of group
 589 generators determine the number of *gauge fields* of the theory.

590 As mentioned in the first lines of Section 1.2, QED has one symmetry group ($U(1)$)
 591 with one group generator (the Q operator) and one gauge field (the electromagnetic
 592 field A^μ). In CED there is not a clear definition, beyond the historical convention,
 593 of which fields are the fundamental and which are the associated, but in QED the
 594 fundamental field is A^μ . When a gauge theory is quantized, the gauge fields are
 595 quantized and their quanta are called *gauge bosons*. The word boson characterizes
 596 particles with integer spin which obey Bose-Einstein statistics.

597 As will be detailed in Section 1.3, interactions between particles in a system can
 598 be obtained by considering first the Lagrangian density of free particles in the sys-
 599 tem, which of course is incomplete because the interaction terms have been left out,
 600 and demanding global phase transformation invariance. Global phase transforma-
 601 tion means that a gauge transformation is performed identically to every point
 602 in the space⁶ and the Lagrangian remains invariant. Then, the global transforma-
 603 tion is promoted to a local phase transformation (this time the gauge transformation
 604 depends on the position in space) and again invariance is required.

⁶ Here space corresponds to the 4-dimensional space i.e. space-time.

605 Due to the space dependence of the local transformation, the Lagrangian density is
 606 not invariant anymore. In order to reinstate the gauge invariance, the gauge covariant
 607 derivative is introduced in the Lagrangian and with it the gauge field responsible for
 608 the interaction between particles in the system. The new Lagrangian density is gauge
 609 invariant, includes the interaction terms needed to account for the interactions and
 610 provides a way to explain the interaction between particles through the exchange of
 611 the gauge boson.

612 This recipe was used to build QED and the theories that aim to explain the
 613 fundamental interactions.

614 1.2.4 Gauge bosons

615 The importance of the gauge bosons comes from the fact that they are the force
 616 mediators or force carriers. The features of the gauge bosons reflect those of the fields
 617 they represent and they are extracted from the Lagrangian density used to describe
 618 the interactions. In Section 1.3, it will be shown how the gauge bosons of the EI and
 619 WI emerge from the electroweak Lagrangian. The SI gauge bosons features are also
 620 extracted from the SI Lagrangian but it is not detailed in this document. The main
 621 features of the SM gauge bosons will be briefly presented below and summarized in
 622 Table 1.7.

623 • **Photon.** EI occurs when the photon couples to (is exchanged between) parti-
 624 cles carrying electric charge; however, The photon itself does not carry electric
 625 charge, therefore, there is no coupling between photons. Given that the photon
 626 is massless the EI is of infinite range, i.e., electrically charged particles interact
 627 even if they are located far away one from each other; this also implies that
 628 photons always move with the speed of light.

- 629 • **Gluon.** SI is mediated by gluons which just as photons are massless. They
 630 carry one unit of color charge and one unit of anticolor charge, hence, gluons
 631 can couple to other gluons. As a result, the range of the SI is not infinite
 632 but very short due to the attraction between gluons, giving rise to the *color*
 633 *confinement* which explains why color charged particles cannot be isolated but
 634 live within composite particles, like quarks inside protons.
- 635 • **W, Z.** W^\pm and Z, are massive which explains their short-range. Given that
 636 the WI is the only interaction that can change the flavor of the interacting
 637 particles, the W boson is the responsible for the nuclear transmutation where
 638 a neutron is converted into a proton or vice versa with the involvement of an
 639 electron and a neutrino (see Figure 1.4c). The Z boson is the responsible for the
 640 neutral weak processes like neutrino elastic scattering where no electric charge
 641 but momentum transference is involved. WI gauge bosons carry isospin charge
 642 which makes interaction between them possible.

Interaction	Mediator	Electric charge (e)	Color charge	Weak Isospin	mass (GeV/c ²)
Electromagnetic	Photon (γ)	0	No	0	0
Strong	Gluon (g)	0	Yes -octet	No	0
Weak	W^\pm	± 1	No	± 1	80.385 ± 0.015
	Z	0	No	0	91.188 ± 0.002

Table 1.7: SM gauge bosons main features [9].

643

644 1.3 Electroweak unification and the Higgs 645 mechanism

646 Physicists dream of building a theory that contains all the interactions in one single
 647 interaction, i.e., showing that at some scale in energy all the four fundamental inter-

actions are unified and only one interaction emerges in a *Theory of everything*. The first sign of the feasibility of such unification came from success in the construction of the CED. Einstein spent years trying to reach that full unification, which by 1920 only involved electromagnetism and gravity, with no success; however, a new partial unification was achieved in the 1960's, when S.Glashow [22], A.Salam [23] and S.Weinberg [24] independently proposed that electromagnetic and weak interactions are two manifestations of a more general interaction called *electroweak interaction* (EWI). EWI was developed by following the useful prescription provided by QED and the gauge invariance principles.

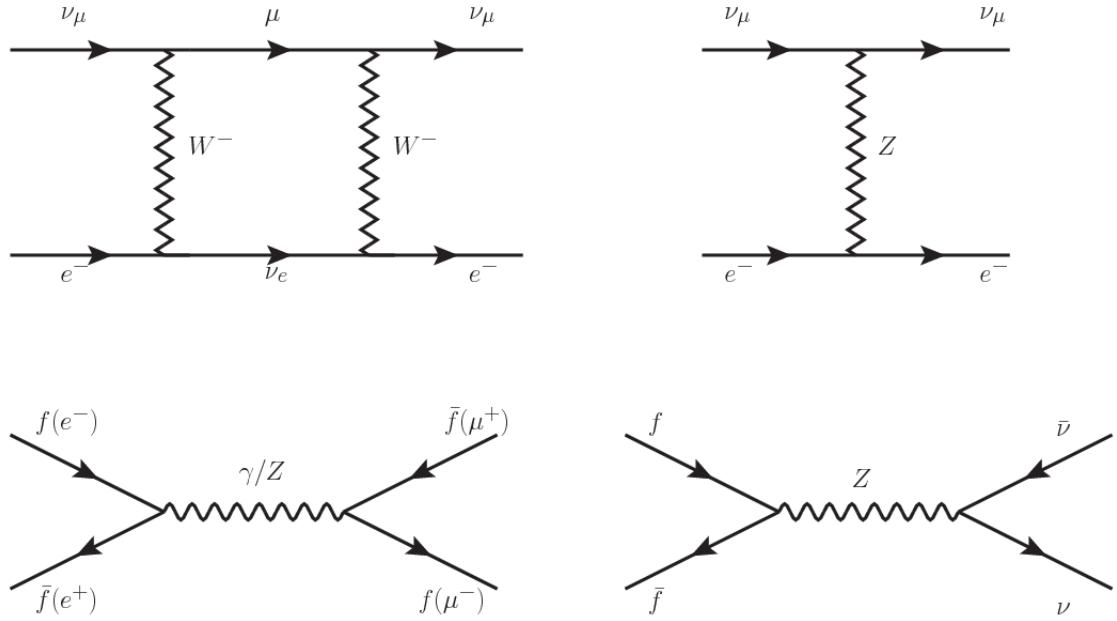


Figure 1.5: Top: $\nu_\mu - e^-$ scattering going through charged currents (left) and neutral currents (right). Bottom: neutral current processes for charged fermions (left) and involving neutrinos (right). While neutral current processes involving only charged fermions can proceed through EI or WI, those involving neutrinos can only proceed via WI.

The *classic* weak theory developed by Fermi, did not have the concept of the W boson but instead it was treated as a point interaction with the dimensionful constant G_F associated with it. It works really well at low energies very far off the W mass

660 shell. When going up in energy, the theory of weak interactions involving the W
 661 boson is capable of explaining the β -decay and in general the processes mediated by
 662 W^\pm bosons. However, there were some processes like the $\nu_\mu - e$ scattering which
 663 would require the exchange of two W bosons (see Figure 1.5 top diagrams) giving
 664 rise to divergent loop integrals and then non-finite predictions. The EWI theory, by
 665 including neutral currents involving fermions via the exchange of a neutral bosons Z,
 666 overcomes those divergences and the predictions become realistic.

667 Neutral weak interaction vertices conserve flavor in the same way as the electro-
 668 magnetic vertices do, but additionally, the Z boson can couple to neutrinos which
 669 implies that processes involving charged fermions can proceed through EI or WI but
 670 processes involving neutrinos can proceed only through WI.

671 The prescription to build a gauge theory of the WI consists of proposing a free
 672 field Lagrangian density that includes the particles involved; next, by requesting
 673 invariance under global phase transformations first and generalizing to local phase
 674 transformations invariance later, the conserved currents are identified and interactions
 675 are generated by introducing gauge fields. Given that the goal is to include the EI
 676 and WI in a single theory, the group symmetry considered should be a combination of
 677 $SU(2)_L$ and $U(1)_{em}$, however the latter cannot be used directly because the EI treats
 678 left and right-handed particles indistinctly in contrast to the former. Fortunately, the
 679 weak hypercharge, which is a combination of the weak isospin and the electric charge
 680 (Eqn. 1.2) is suitable to be used since it is conserved by the EI and WI. Thus, the
 681 symmetry group to be considered is

$$G \equiv SU(2)_L \otimes U(1)_Y \quad (1.6)$$

682 The following treatment applies to any of the fermion generations, but for sim-

683 plicity the first generation of leptons will be considered [5, 6, 25, 26].

684 Given the first generation of leptons

$$\psi_1 = \begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \quad \psi_2 = \nu_{eR}, \quad \psi_3 = e_R^- \quad (1.7)$$

685 the charged fermionic currents are given by

$$J_\mu \equiv J_\mu^+ = \bar{\nu}_{eL} \gamma_\mu e_L, \quad J_\mu^\dagger \equiv J_\mu^- = \bar{e}_L \gamma_\mu \nu_{eL} \quad (1.8)$$

686 and the free Lagrangian is given by

$$\mathcal{L}_0 = \sum_{j=1}^3 i\bar{\psi}_j(x) \gamma^\mu \partial_\mu \psi_j(x). \quad (1.9)$$

687 Mass terms are included directly in the QED free Lagrangians since they preserve
 688 the invariance under the symmetry transformations involved which treat left and right
 689 handed particles similarly, however mass terms of the form

$$m_W^2 W_\mu^\dagger(x) W^\mu(x) + \frac{1}{2} m_Z^2 Z_\mu(x) Z^\mu(x) - m_e \bar{\psi}_e(x) \psi_e(x) \quad (1.10)$$

690 which represent the mass of W^\pm , Z and electrons, are not invariant under G trans-
 691 formations, therefore the gauge fields described by the EWI are in principle massless.

692 Experiments have shown that the EWI gauge fields are not massless [27–30];
 693 however, they have to acquire mass through a mechanism compatible with the gauge
 694 invariance; that mechanism is known as the *Higgs mechanism* and will be considered
 695 later in this Section. The global transformations in the combined symmetry group G
 696 can be written as

$$\begin{aligned}
\psi_1(x) &\xrightarrow{G} \psi'_1(x) \equiv U_Y U_L \psi_1(x), \\
\psi_2(x) &\xrightarrow{G} \psi'_2(x) \equiv U_Y \psi_2(x), \\
\psi_3(x) &\xrightarrow{G} \psi'_3(x) \equiv U_Y \psi_3(x)
\end{aligned} \tag{1.11}$$

697 where U_L represent the $SU(2)_L$ transformation acting only on the weak isospin dou-
 698 blet and U_Y represent the $U(1)_Y$ transformation acting on all the weak isospin mul-
 699 tiplets. Explicitly

$$U_L \equiv \exp\left(i \frac{\sigma_i}{2} \alpha^i\right), \quad U_Y \equiv \exp(i y_i \beta) \quad (i = 1, 2, 3) \tag{1.12}$$

700 with σ_i the Pauli matrices and y_i the weak hypercharges. In order to promote the
 701 transformations from global to local while keeping the invariance, it is required that
 702 $\alpha^i = \alpha^i(x)$, $\beta = \beta(x)$ and the replacement of the ordinary derivatives by the covariant
 703 derivatives

$$\begin{aligned}
D_\mu \psi_1(x) &\equiv \left[\partial_\mu + ig\sigma_i W_\mu^i(x)/2 + ig'y_1 B_\mu(x) \right] \psi_1(x) \\
D_\mu \psi_2(x) &\equiv \left[\partial_\mu + ig'y_2 B_\mu(x) \right] \psi_2(x) \\
D_\mu \psi_3(x) &\equiv \left[\partial_\mu + ig'y_3 B_\mu(x) \right] \psi_3(x)
\end{aligned} \tag{1.13}$$

704 introducing in this way four gauge fields, $W_\mu^i(x)$ and $B_\mu(x)$, in the process. The
 705 covariant derivatives (Eqn. 1.13) are required to transform in the same way as fermion
 706 fields $\psi_i(x)$ themselves, therefore, the gauge fields transform as:

$$\begin{aligned} B_\mu(x) &\xrightarrow{G} B'_\mu(x) \equiv B_\mu(x) - \frac{1}{g'} \partial_\mu \beta(x) \\ W_\mu^i(x) &\xrightarrow{G} W_\mu^{i\prime}(x) \equiv W_\mu^i(x) - \frac{i}{g} \partial_\mu \alpha_i(x) - \varepsilon_{ijk} \alpha_i(x) W_\mu^j(x). \end{aligned} \quad (1.14)$$

707 The G invariant version of the Lagrangian density 1.9 can be written as

$$\mathcal{L}_0 = \sum_{j=1}^3 i \bar{\psi}_j(x) \gamma^\mu D_\mu \psi_j(x) \quad (1.15)$$

708 where free massless fermion and gauge fields and fermion-gauge boson interactions
 709 are included. The EWI Lagrangian density must additionally include kinetic terms
 710 for the gauge fields (\mathcal{L}_G) which are built from the field strengths, according to

$$B_{\mu\nu}(x) \equiv \partial_\mu B_\nu - \partial_\nu B_\mu \quad (1.16)$$

$$W_{\mu\nu}^i(x) \equiv \partial_\mu W_\nu^i(x) - \partial_\nu W_\mu^i(x) - g \varepsilon^{ijk} W_\mu^j W_\nu^k \quad (1.17)$$

711 the last term in Eqn. 1.17 is added in order to hold the gauge invariance; therefore,

$$\mathcal{L}_G = -\frac{1}{4} B_{\mu\nu}(x) B^{\mu\nu}(x) - \frac{1}{4} W_{\mu\nu}^i(x) W_i^{\mu\nu}(x) \quad (1.18)$$

712 which contains not only the free gauge fields contributions, but also the gauge fields
 713 self-interactions and interactions among them.

714 The three weak isospin conserved currents resulting from the $SU(2)_L$ symmetry
 715 are given by

$$J_\mu^i(x) = \frac{1}{2} \bar{\psi}_1(x) \gamma_\mu \sigma^i \psi_1(x) \quad (1.19)$$

716 while the weak hypercharge conserved current resulting from the $U(1)_Y$ symmetry is
 717 given by

$$J_\mu^Y = \sum_{j=1}^3 \bar{\psi}_j(x) \gamma_\mu y_j \psi_j(x) \quad (1.20)$$

718 In order to evaluate the electroweak interactions modeled by an isos triplet field
 719 W_μ^i that couples to isospin currents J_μ^i with strength g and additionally the singlet
 720 field B_μ which couples to the weak hypercharge current J_μ^Y with strength $g'/2$. The
 721 interaction Lagrangian density to be considered is

$$\mathcal{L}_I = -g J^{i\mu}(x) W_\mu^i(x) - \frac{g'}{2} J^{Y\mu}(x) B_\mu(x) \quad (1.21)$$

722 Note that the weak isospin currents are not the same as the charged fermionic cur-
 723 rents that were used to describe the WI (Eqn. 1.8), since the weak isospin eigenstates
 724 are not the same as the mass eigenstates, but they are closely related

$$J_\mu = \frac{1}{2}(J_\mu^1 + iJ_\mu^2), \quad J_\mu^\dagger = \frac{1}{2}(J_\mu^1 - iJ_\mu^2). \quad (1.22)$$

725 The same happens with the gauge fields W_μ^i which are related to the mass eigen-
 726 states W^\pm by

$$W_\mu^+ = \frac{1}{\sqrt{2}}(W_\mu^1 - iW_\mu^2), \quad W_\mu^- = \frac{1}{\sqrt{2}}(W_\mu^1 + iW_\mu^2). \quad (1.23)$$

727 The fact that there are three weak isospin conserved currents is an indication that
 728 in addition to the charged fermionic currents, which couple charged to neutral leptons,
 729 there should be a neutral fermionic current that does not involve electric charge
 730 exchange; therefore, it couples neutral fermions or fermions of the same electric charge.
 731 The third weak isospin current contains a term that is similar to the electromagnetic

732 current (j_μ^{em}), indicating that there is a relation between them and resembling the
 733 Gell-Mann-Nishijima formula 1.2 adapted to electroweak interactions

$$Q = T_3 + \frac{Y_W}{2}. \quad (1.24)$$

734 Just as Q generates the $U(1)_{em}$ symmetry, the weak hypercharge generates the
 735 $U(1)_Y$ symmetry as said before. It is possible to write the relationship in terms of
 736 the currents as

$$j_\mu^{em} = J_\mu^3 + \frac{1}{2} J_\mu^Y. \quad (1.25)$$

737 The neutral gauge fields W_μ^3 and B_μ cannot be directly identified with the Z
 738 and the photon fields since the photon interacts similarly with left and right-handed
 739 fermions; however, they are related through a linear combination given by

$$\begin{aligned} A_\mu &= B_\mu \cos \theta_W + W_\mu^3 \sin \theta_W \\ Z_\mu &= -B_\mu \sin \theta_W + W_\mu^3 \cos \theta_W \end{aligned} \quad (1.26)$$

where θ_W is known as the *Weinberg angle*. The interaction Lagrangian is now given by

$$\begin{aligned} \mathcal{L}_I = -\frac{g}{\sqrt{2}}(J^\mu W_\mu^+ + J^{\mu\dagger} W_\mu^-) - &\left(g \sin \theta_W J_\mu^3 + g' \cos \theta_W \frac{J_\mu^Y}{2}\right) A^\mu \\ &- \left(g \cos \theta_W J_\mu^3 - g' \sin \theta_W \frac{J_\mu^Y}{2}\right) Z^\mu \end{aligned} \quad (1.27)$$

740 the first term is the weak charged current interaction, while the second term is the

741 electromagnetic interaction under the condition

$$g \sin \theta_W = g' \cos \theta_W = e, \quad \frac{g'}{g} = \tan \theta_W \quad (1.28)$$

742 contained in the Eqn.1.25; the third term is the neutral weak current.

743

744 Note that the neutral fields transformation given by the Eqn. 1.26 can be written
 745 in terms of the coupling constants g and g' as:

$$A_\mu = \frac{g' W_\mu^3 + g B_\mu}{\sqrt{g^2 + g'^2}}, \quad Z_\mu = \frac{g W_\mu^3 - g' B_\mu}{\sqrt{g^2 + g'^2}}. \quad (1.29)$$

746 So far, the Lagrangian density describing the non-massive EWI is:

$$\mathcal{L}_{nmEWI} = \mathcal{L}_0 + \mathcal{L}_G \quad (1.30)$$

747 where fermion and gauge fields have been considered massless because their regular
 748 mass terms are manifestly non invariant under G transformations; therefore, masses
 749 have to be generated in a gauge invariant way. The mechanism by which this goal is
 750 achieved is known as the *Higgs mechanism* and is closely connected to the concept of
 751 *spontaneous symmetry breaking*.

752 1.3.1 Spontaneous symmetry breaking (SSB)

753 Figure 1.6 left shows a steel nail (top) which is subject to an external force; the form
 754 of the potential energy is also shown (bottom).

755 Before reaching the critical force value, the system has rotational symmetry with
 756 respect to the nail axis; however, after the critical force value is reached the nail buck-

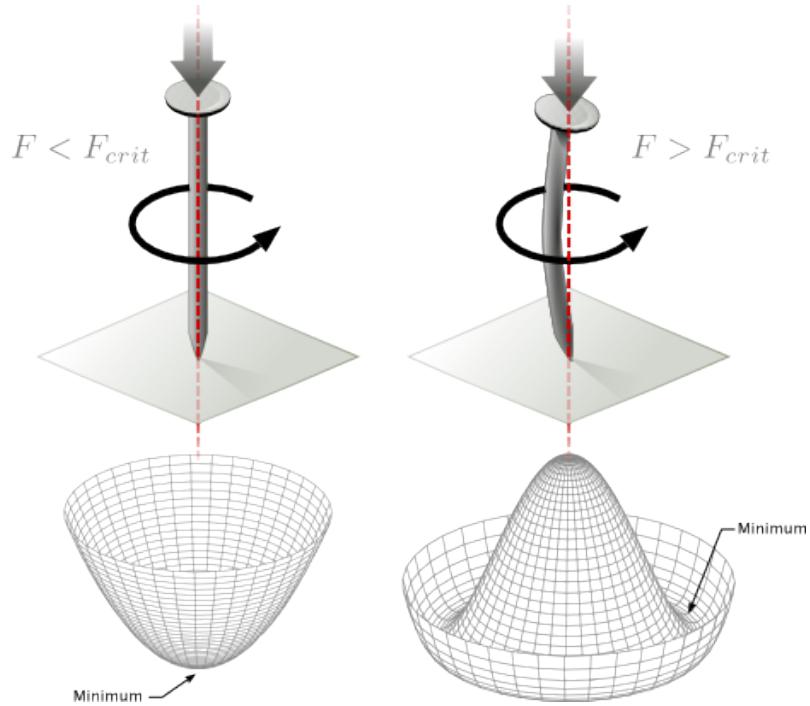


Figure 1.6: Spontaneous symmetry breaking mechanism. The steel nail, subject to an external force (top left), has rotational symmetry with respect to its axis. When the external force overcomes a critical value the nail buckles (top right) choosing a minimal energy state (ground state) and thus *breaking spontaneously the rotational symmetry*. The potential energy (bottom) changes but holds the rotational symmetry; however, an infinite number of asymmetric ground states are generated and circularly distributed in the bottom of the potential [31].

les (top right). The form of the potential energy (bottom right) changes appearing a set of infinity minima but preserving its rotational symmetry. Right before the nail buckles there is no indication of the direction the nail will bend because any of the directions are equivalent, but once the nail bends, choosing a direction, an arbitrary minimal energy state (ground state) is selected and it does not share the system's rotational symmetry. This mechanism for reaching an asymmetric ground state is known as *spontaneous symmetry breaking*.

The lesson from this analysis is that the way to introduce the SSB mechanism into a system is by adding the appropriate potential to it.

Figure 1.7 shows a plot of the potential $V(\phi)$ in the case of a scalar field ϕ

$$V(\phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 \quad (1.31)$$

If $\mu^2 > 0$ the potential has only one minimum at $\phi = 0$ and describes a scalar field with mass μ . If $\mu^2 < 0$ the potential has a local maximum at $\phi = 0$ and two minima at $\phi = \pm\sqrt{-\mu^2/\lambda}$ which enables the SSB mechanism to work.

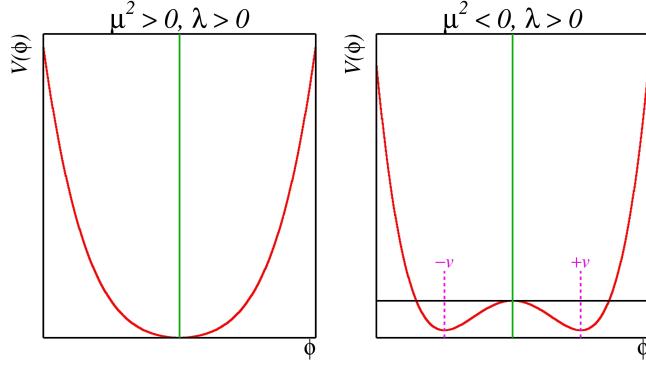


Figure 1.7: Shape of the potential $V(\phi)$ for $\lambda > 0$ and: $\mu^2 > 0$ (left) and $\mu^2 < 0$ (right). The case $\mu^2 < 0$ corresponds to the potential suitable for introducing the SSB mechanism by choosing one of the two ground states which are connected via reflection symmetry. [31].

In the case of a complex scalar field $\phi(x)$

$$\phi(x) = \frac{1}{\sqrt{2}}(\phi_1 + i\phi_2) \quad (1.32)$$

the Lagrangian (invariant under global $U(1)$ transformations) is given by

$$\mathcal{L} = (\partial_\mu \phi)^\dagger (\partial^\mu \phi) - V(\phi), \quad V(\phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 \quad (1.33)$$

where an appropriate potential has been added in order to introduce the SSB.

As seen in Figure 1.8, the potential has now an infinite number of minima circularly distributed along the ξ -direction which makes possible the occurrence of the SSB by choosing an arbitrary ground state; for instance, $\xi = 0$, i.e. $\phi_1 = v, \phi_2 = 0$

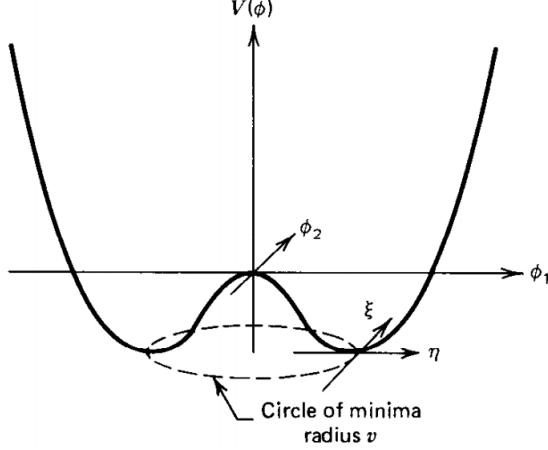


Figure 1.8: Potential for complex scalar field. There is a circle of minima of radius v along the ξ -direction [6].

$$\phi_0 = \frac{v}{\sqrt{2}} \exp(i\xi) \xrightarrow{\text{SSB}} \phi_0 = \frac{v}{\sqrt{2}} \quad (1.34)$$

776 As usual, excitations over the ground state are studied by making an expansion
 777 about it; thus, the excitations can be parametrized as:

$$\phi(x) = \frac{1}{\sqrt{2}}(v + \eta(x) + i\xi(x)) \quad (1.35)$$

778 which when substituted into Eqn. 1.33 produces a Lagrangian in terms of the new
 779 fields η and ξ

$$\mathcal{L}' = \frac{1}{2}(\partial_\mu \xi)^2 + \frac{1}{2}(\partial_\mu \eta)^2 + \mu^2 \eta^2 - V(\phi_0) - \lambda v \eta (\eta^2 + \xi^2) - \frac{\lambda}{4}(\eta^2 + \xi^2)^2 \quad (1.36)$$

780 where the last two terms represent the interactions and self-interaction between the
 781 two fields η and ξ . The particular feature of the SSB mechanism is revealed when
 782 looking to the first three terms of \mathcal{L}' . Before the SSB, only the massless ϕ field is

783 present in the system; after the SSB there are two fields of which the η -field has
 784 acquired mass $m_\eta = \sqrt{-2\mu^2}$ while the ξ -field is still massless (see Figure 1.9).

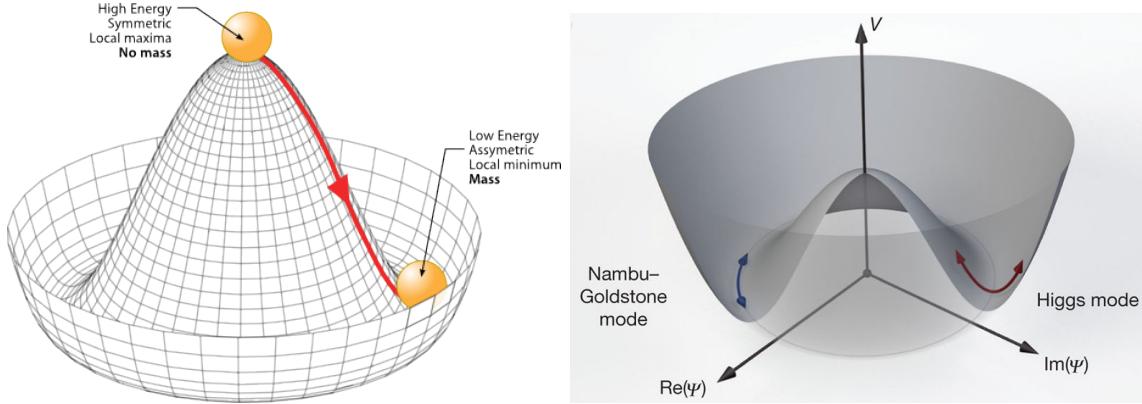


Figure 1.9: SSB mechanism for a complex scalar field [31, 32].

785 Thus, the SSB mechanism serves as a method to generate mass but as a side ef-
 786 fect a massless field is introduced in the system. This fact is known as the Goldstone
 787 theorem and states that a massless scalar field appears in the system for each con-
 788 tinuous symmetry spontaneously broken. Another version of the Goldstone theorem
 789 states that “if a Lagrangian is invariant under a continuous symmetry group G , but
 790 the vacuum is only invariant under a subgroup $H \subset G$, then there must exist as many
 791 massless spin-0 particles (Nambu-Goldstone bosons) as broken generators.” [26] The
 792 Nambu-Goldstone boson can be understood considering that the potential in the ξ -
 793 direction is flat so excitations in that direction are not energy consuming and thus
 794 represent a massless state.

795 1.3.2 Higgs mechanism

796 When the SSB mechanism is introduced in the formulation of the EWI in an attempt
 797 to generate the mass of the so far massless gauge bosons and fermions, an interesting
 798 effect is revealed. In order to keep the G symmetry group invariance and generate

799 the mass of the EW gauge bosons, a G invariant Lagrangian density (\mathcal{L}_S) has to be
 800 added to the non massive EWI Lagrangian (Eqn. 1.30)

$$\mathcal{L}_S = (D_\mu \phi)^\dagger (D^\mu \phi) - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2, \quad \lambda > 0, \mu^2 < 0 \quad (1.37)$$

$$D_\mu \phi = \left(i\partial_\mu - g \frac{\sigma_i}{2} W_\mu^i - g' \frac{Y}{2} B_\mu \right) \phi \quad (1.38)$$

801 ϕ has to be an isospin doublet of complex scalar fields so it preserves the G invariance;
 802 thus ϕ can be defined as:

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix}. \quad (1.39)$$

803 The minima of the potential are defined by

$$\phi^\dagger \phi = \frac{1}{2} (\phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2) = -\frac{\mu^2}{2\lambda}. \quad (1.40)$$

804 The choice of the ground state is critical. By choosing a ground state, invariant
 805 under $U(1)_{em}$ gauge symmetry, the photon will remain massless and the W^\pm and Z
 806 bosons masses will be generated which is exactly what is needed. In that sense, the
 807 best choice corresponds to a weak isospin doublet with $T_3 = -1/2$, $Y_W = 1$ and $Q = 0$
 808 which defines a ground state with $\phi_1 = \phi_2 = \phi_4$ and $\phi_3 = v$:

$$\phi_0 \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}, \quad v^2 \equiv -\frac{\mu^2}{\lambda}. \quad (1.41)$$

809 where the vacuum expectation value v is fixed by the Fermi coupling G_F according
 810 to $v = (\sqrt{2}G_F)^{1/2} \approx 246$ GeV.

811 The G symmetry has been broken and three Nambu-Goldstone bosons will appear.

812 The next step is to expand ϕ about the chosen ground state as:

$$\phi(x) = \frac{1}{\sqrt{2}} \exp\left(\frac{i}{v} \sigma_i \theta^i(x)\right) \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix} \approx \frac{1}{\sqrt{2}} \begin{pmatrix} \theta_1(x) + i\theta_2(x) \\ v + H(x) - i\theta_3(x) \end{pmatrix} \quad (1.42)$$

813 to describe fluctuations from the ground state ϕ_0 . The fields $\theta_i(x)$ represent the
 814 Nambu-Goldstone bosons while $H(x)$ is known as *Higgs field*. The fundamental fea-
 815 ture of the parametrization used is that the dependence on the $\theta_i(x)$ fields is factored
 816 out in a global phase that can be eliminated by taking the physical *unitary gauge*
 817 $\theta_i(x) = 0$. Therefore the expansion about the ground state is given by:

$$\phi(x) \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix} \quad (1.43)$$

818 which when substituted into \mathcal{L}_S (Eqn. 1.37) results in a Lagrangian containing the
 819 now massive three gauge bosons W^\pm, Z , one massless gauge boson (photon) and
 820 the new Higgs field (H). The three degrees of freedom corresponding to the Nambu-
 821 Goldstone bosons are now integrated into the massive gauge bosons as their lon-
 822 gitudinal polarizations which were not available when they were massless particles.
 823 The effect by which vector boson fields acquire mass after an spontaneous symmetry
 824 breaking, but without an explicit gauge invariance breaking is known as the *Higgs*
 825 *mechanism*.

826 The mechanism was proposed by three independent groups: F.Englert and R.Brout
 827 in August 1964 [33], P.Higgs in October 1964 [34] and G.Guralnik, C.Hagen and
 828 T.Kibble in November 1964 [35]; however, its importance was not realized until
 829 S.Glashow [22], A.Salam [23] and S.Weinberg [24], independently, proposed that elec-
 830 tromagnetic and weak interactions are two manifestations of a more general interac-
 831 tion called *electroweak interaction* in 1967.

832 **1.3.3 Masses of the gauge bosons**

833 The masses of the gauge bosons are extracted by evaluating the kinetic part of La-
 834 grangian \mathcal{L}_S in the ground state (known also as the vacuum expectation value), i.e.,

$$\left| \left(\partial_\mu - ig \frac{\sigma_i}{2} W_\mu^i - i \frac{g'}{2} B_\mu \right) \phi_0 \right|^2 = \left(\frac{1}{2} v g \right)^2 W_\mu^+ W^{-\mu} + \frac{1}{8} v^2 (W_\mu^3, B_\mu) \begin{pmatrix} g^2 & -gg' \\ -gg' & g'^2 \end{pmatrix} \begin{pmatrix} W^{3\mu} \\ B^\mu \end{pmatrix} \quad (1.44)$$

835 comparing with the typical mass term for a charged boson $M_W^2 W^+ W^-$

$$M_W = \frac{1}{2} v g. \quad (1.45)$$

The second term in the right side of the Eqn.1.44 comprises the masses of the neutral bosons, but it needs to be written in terms of the gauge fields Z_μ and A_μ in order to be compared to the typical mass terms for neutral bosons, therefore using Eqn. 1.29

$$\begin{aligned} \frac{1}{8} v^2 [g^2 (W_\mu^3)^2 - 2gg' W_\mu^3 B^\mu + g'^2 B_\mu^2] &= \frac{1}{8} v^2 [g W_\mu^3 - g' B_\mu]^2 + 0[g' W_\mu^3 + g B_\mu]^2 \quad (1.46) \\ &= \frac{1}{8} v^2 [\sqrt{g^2 + g'^2} Z_\mu]^2 + 0[\sqrt{g^2 + g'^2} A_\mu]^2 \end{aligned}$$

836 and then

$$M_Z = \frac{1}{2} v \sqrt{g^2 + g'^2}, \quad M_A = 0 \quad (1.47)$$

837 **1.3.4 Masses of the fermions**

838 The lepton mass terms can be generated by introducing a gauge invariant Lagrangian
 839 term describing the Yukawa coupling between the lepton field and the Higgs field

$$\mathcal{L}_{Yl} = -G_l \left[(\bar{\nu}_l, \bar{l})_L \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} l_R + \bar{l}_R (\phi^-, \bar{\phi}^0) \begin{pmatrix} \nu_l \\ l \end{pmatrix} \right], \quad l = e, \mu, \tau. \quad (1.48)$$

840 After the SSB and replacing the usual field expansion about the ground state
 841 (Eqn.1.41) into \mathcal{L}_{Yl} , the mass term arises

$$\mathcal{L}_{Yl} = -m_l (\bar{l}_L l_R + \bar{l}_R l_L) - \frac{m_l}{v} (\bar{l}_L l_R + \bar{l}_R l_L) H = -m_l \bar{l} l \left(1 + \frac{H}{v} \right) \quad (1.49)$$

842

$$m_l = \frac{G_l}{\sqrt{2}} v \quad (1.50)$$

843 where the additional term represents the lepton-Higgs interaction. The quark masses
 844 are generated in a similar way as lepton masses but for the upper member of the
 845 quark doublet a different Higgs doublet is needed:

$$\phi_c = -i\sigma_2 \phi^* = \begin{pmatrix} -\bar{\phi}^0 \\ \phi^- \end{pmatrix}. \quad (1.51)$$

846 Additionally, given that the quark isospin doublets are not constructed in terms
 847 of the mass eigenstates but in terms of the flavor eigenstates, as shown in Table 1.5,
 848 the coupling parameters will be related to the CKM matrix elements; thus, the quark
 849 Lagrangian is given by:

$$\mathcal{L}_{Yq} = -G_d^{i,j} (\bar{u}_i, \bar{d}'_i)_L \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} d_{jR} - G_u^{i,j} (\bar{u}_i, \bar{d}'_i)_L \begin{pmatrix} -\bar{\phi}^0 \\ \phi^- \end{pmatrix} u_{jR} + h.c. \quad (1.52)$$

850 with $i, j = 1, 2, 3$. After SSB and expansion about the ground state, the diagonal form

851 of \mathcal{L}_{Yq} is:

$$\mathcal{L}_{Yq} = -m_d^i \bar{d}_i d_i \left(1 + \frac{H}{v}\right) - m_u^i \bar{u}_i u_i \left(1 + \frac{H}{v}\right) \quad (1.53)$$

852 Fermion masses depend on arbitrary couplings G_l and $G_{u,d}$ and are not predicted
853 by the theory.

854 1.3.5 The Higgs field

855 After the characterization of the fermions and gauge bosons as well as their interac-
856 tions, it is necessary to characterize the Higgs field itself. The Lagrangian \mathcal{L}_S in Eqn.
857 1.37 written in terms of the gauge bosons is given by

$$\mathcal{L}_S = \frac{1}{4} \lambda v^4 + \mathcal{L}_H + \mathcal{L}_{HV} \quad (1.54)$$

858

$$\mathcal{L}_H = \frac{1}{2} \partial_\mu H \partial^\mu H - \frac{1}{2} m_H^2 H^2 - \frac{1}{2v} m_H^2 H^3 - \frac{1}{8v^2} m_H^2 H^4 \quad (1.55)$$

859

$$\mathcal{L}_{HV} = m_H^2 W_\mu^+ W^{\mu-} \left(1 + \frac{2}{v} H + \frac{2}{v^2} H^2\right) + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \left(1 + \frac{2}{v} H + \frac{2}{v^2} H^2\right) \quad (1.56)$$

860 The mass of the Higgs boson is deduced as usual from the mass term in the Lagrangian
861 resulting in:

$$m_H = \sqrt{-2\mu^2} = \sqrt{2\lambda}v \quad (1.57)$$

862 however, it is not predicted by the theory either. The experimental measurement of
863 the Higgs boson mass have been performed by the *Compact Muon Solenoid (CMS)*
864 experiment and the *A Toroidal LHC Appartus (ATLAS)* experiments at the *Large
865 Hadron Collider (LHC)*, [36–38], and is presented in Table 1.8.

Property	Value
Electric charge	0
Color charge	0
Spin	0
Weak isospin	-1/2
Weak hypercharge	1
Parity	1
Mass (GeV/c ²)	125.09±0.21 (stat.)±0.11 (syst.)

Table 1.8: Higgs boson properties. Higgs mass is not predicted by the theory and the value here corresponds to the experimental measurement.

1.3.6 Production of Higgs bosons at LHC

868 At the LHC, Higgs bosons are produced as a result of the collision of two counter-
869 rotating protons beams. A detailed description of the LHC machine will be presented
in chapter 2.

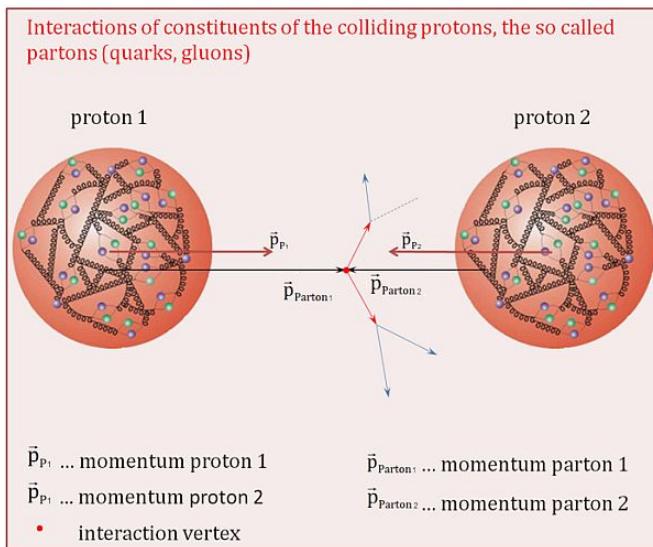


Figure 1.10: Proton-proton collision. Protons are composed of 3 valence quarks, a sea of quarks and gluons; therefore in a proton-proton collision, quarks and gluons are those who collide. [39].

870

871 Protons are composed of quarks and these quarks are bound by gluons; however,
872 what is commonly called the quark content of the proton makes reference to the
873 valence quarks. In fact, a proton is not just a rigid entity with three balls in it all
874 tied up with springs, but the gluons exchanged by the valence quarks tend to split

875 spontaneously into quark-antiquark pairs or more gluons, creating *sea of quarks and*
 876 *gluons* as represented in Figure 1.10.

877 In a proton-proton (pp) collision, the proton's constituents, quarks and gluons, are
 878 those that collide. The pp cross section depends on the momentum of the colliding
 879 particles, reason for which it is needed to know how the momentum is distributed
 880 inside the proton. Quarks and gluons are known as partons, hence, the functions
 881 that describe how the proton momentum is distributed among partons inside it are
 882 called *parton distribution functions (PDFs)*; PDFs are determined from experimental
 883 data obtained in experiments where the internal structure of hadrons is tested, and
 884 depend on the momentum transfer Q and the fraction of momentum x carried by an
 885 specific parton. Figure 1.11 shows the proton PDFs ($xf(x, Q^2)$) for two values of Q .

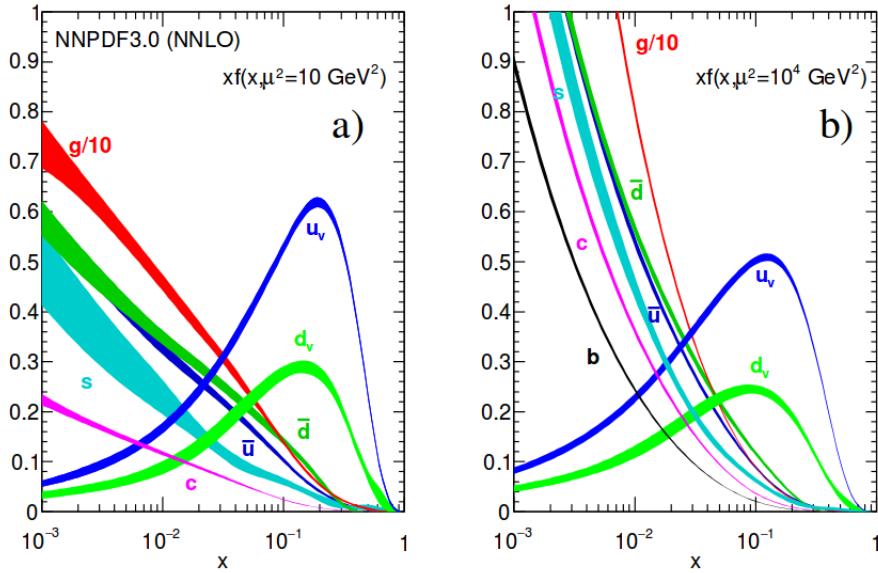


Figure 1.11: Proton PDFs for two values of Q^2 : left. $\mu^2 = Q^2 = 10 \text{ GeV}^2$, right. $\mu^2 = Q^2 = 10^4 \text{ GeV}^2$. u_v and d_v correspond to the u and d valence quarks, $s, c, b, \bar{u}, \bar{d}$ correspond to sea quarks, and g corresponds to gluons. Note that gluons carry a high fraction of the proton's momentum. [9]

886 In physics, a common approach to study complex systems consists of starting
 887 with a simpler version of them, for which a well known description is available, and

adding an additional *perturbation* which represents a small deviation from the known behavior. If the perturbation is small enough, the physical quantities associated with the perturbed system are expressed as a series of corrections to those of the simpler system. The perturbation series corresponds to an expansion in power series of a small parameter, therefore, the more terms are considered in the series (the higher order in the perturbation series), the more precise is the description of the complex system. If the perturbation does not get progressively smaller, the strategy cannot be applied and new methods have to be employed.

High energy systems, like the Higgs production at LHC explored in this thesis, usually can be treated perturbatively with the expansion made in terms of the coupling constants. The overview presented here will be oriented specifically to the Higgs boson production mechanisms in pp collisions at LHC.

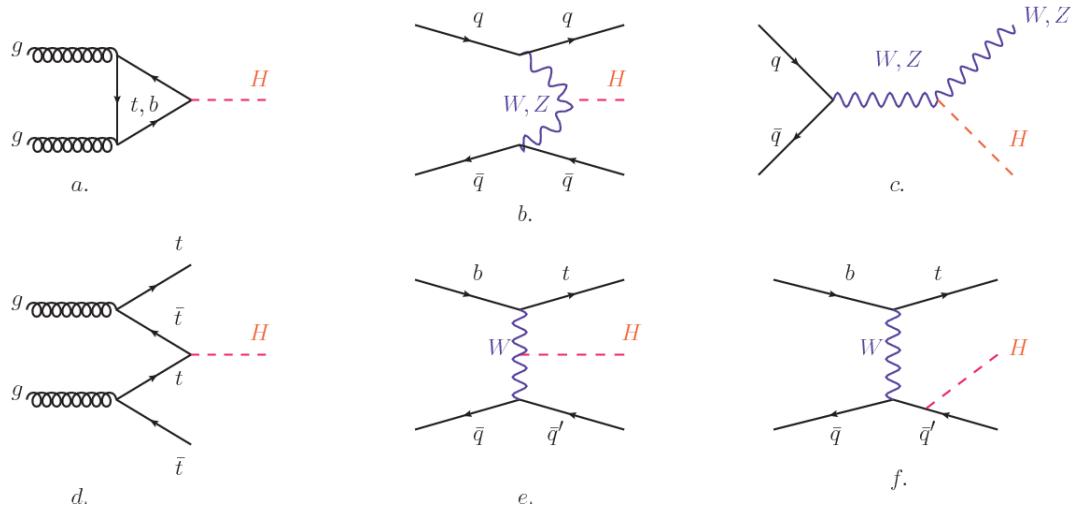


Figure 1.12: Main Higgs boson production mechanism Feynman diagrams. a. gluon-gluon fusion, b. vector boson fusion (VBF), c. Higgs-strahlung, d. Associated production with a top or bottom quark pair, e-f. associated production with a single top quark.

Figure 1.12 shows the Feynman diagrams for the leading order (first order) Higgs production processes at LHC; note that in these diagrams the incoming particles are not the protons themselves but the partons from the protons that actually participate

in the interaction, hence, theorists typically calculate the cross section for the parton interaction, and then convolute that cross section with the information from the PDFs to get a production cross section that is actually measured in experiments. The cross section for Higgs production as a function of the center of mass-energy (\sqrt{s}) for pp collisions is showed in Figure 1.13 left. The tags NLO (next to leading order), NNLO (next to next to leading order) and N3LO (next to next to next to leading order) make reference to the order at which the perturbation series have been considered while the tags QCD and EW correspond to the strong and electroweak coupling constants respectively.

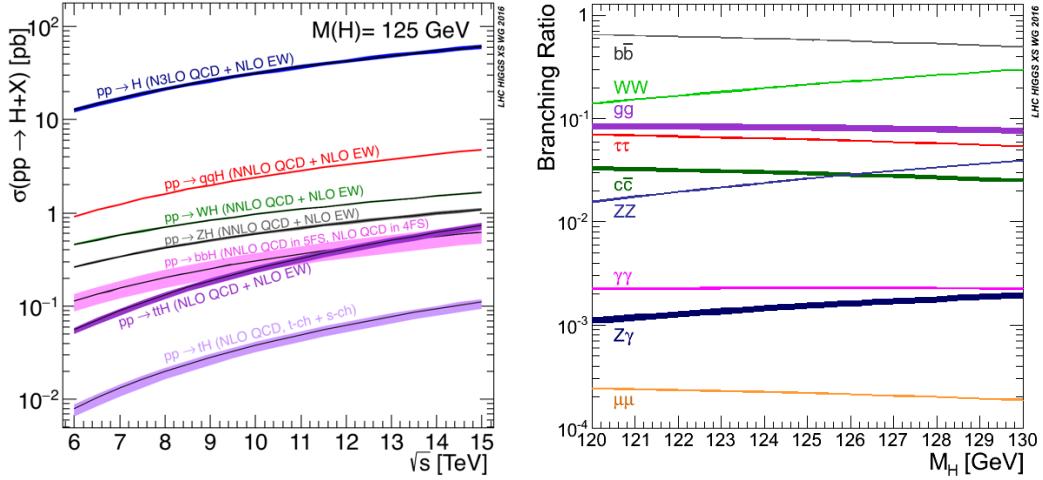


Figure 1.13: Higgs boson production cross sections (left) and decay branching ratios (right) for the main mechanisms. The VBF is indicated as qqH [40].

The main production mechanism is the gluon fusion (Figure 1.12a and $pp \rightarrow H$ in Figure 1.13) given that gluons carry the highest fraction of momentum of the protons in pp colliders (as shown in Figure ??). Since the Higgs boson does not couple to gluons, the mechanism proceeds through the exchange of a virtual top-quark loop. Note that in this process the Higgs boson is produced alone, turning out to be problematic for some Higgs decays, because such absence of anything produced in

918 association with the Higgs represent a trouble for triggering, however, this mechanism
 919 is experimentally clean when combined with the two-photon or the four-lepton decay
 920 channels (see Section 1.3.7).

921 Vector boson fusion (Figure 1.12b and $pp \rightarrow qqH$ in Figure 1.13) has the second
 922 largest production cross section. The scattering of two fermions is mediated by a weak
 923 gauge boson which later emits a Higgs boson. In the final state, the two fermions tend
 924 to be located in the central region of the detector; this kind of features are generally
 925 used as a signature when analyzing the datasets provided by the experiments⁷.

926 In the Higgs-strahlung mechanism (Figure 1.12c and $pp \rightarrow WH, pp \rightarrow ZH$ in
 927 Figure 1.13) two fermions annihilate to form a weak gauge boson. If the initial
 928 fermions have enough energy, the emergent boson might emit a Higgs boson.

929 The associated production with a top or bottom quark pair and the associated
 930 production with a single top quark (Figure 1.12d-f and $pp \rightarrow bbH, pp \rightarrow t\bar{t}H, pp \rightarrow tH$
 931 in Figure 1.13) have a smaller cross section than the main three mechanisms above,
 932 but they provide a good opportunity to test the Higgs-top coupling. The analysis
 933 reported in this thesis is developed using these production mechanisms. A detailed
 934 description of the tH mechanism will be given in Section 1.5.

935 1.3.7 Higgs boson decay channels

936 When a particle can decay through several modes, also known as channels, the prob-
 937 ability of decaying through a given channel is quantified by the *branching ratio (BR)*
 938 of the decay channel; thus, the BR is defined as the ratio of number of decays go-
 939 ing through that given channel to the total number of decays. In regard to the
 940 Higgs boson decay, the BR can be predicted with accuracy once the Higgs mass is
 941 known [41, 42]. In Figure 1.13 right, a plot of the BR as a function of the Higgs mass

⁷ More details about how to identify events of interest in this analysis will be given in chapter 6.

942 is presented; the largest predicted BR corresponds to the $b\bar{b}$ pair decay channel (see
 943 Table 1.9) given that it is the heaviest particle pair whose on-shell⁸ production is
 944 kinematically allowed in the decay.

Decay channel	Branching ratio	Rel. uncertainty
$H \rightarrow b\bar{b}$	5.84×10^{-1}	+3.2% – 3.3%
$H \rightarrow W^+W^-$	2.14×10^{-1}	+4.3% – 4.2%
$H \rightarrow \tau^+\tau^-$	6.27×10^{-2}	+5.7% – 5.7%
$H \rightarrow ZZ$	2.62×10^{-2}	+4.3% – 4.1%
$H \rightarrow \gamma\gamma$	2.27×10^{-3}	+5.0% – 4.9%
$H \rightarrow Z\gamma$	1.53×10^{-3}	+9.0% – 8.9%
$H \rightarrow \mu^+\mu^-$	2.18×10^{-4}	+6.0% – 5.9%

Table 1.9: Predicted branching ratios and the relative uncertainty for some decay channels of a SM Higgs boson with $m_H = 125\text{GeV}/c^2$ [9]; the uncertainties are driven by theoretical uncertainties for the different Higgs boson partial widths and by parametric uncertainties associated to the strong coupling and the masses of the quarks which are the input parameters. Further details on these calculations can be found in Reference [43]

945

946 Decays to other lepton and quark pairs, like electron, strange, up, and down
 947 quark pairs not listed in the table, are also possible but their likelihood is too small
 948 to measure since they are very lightweight, hence, their interaction with the Higgs
 949 boson is very weak. On other hand, the decay to top quark pairs is heavily suppressed
 950 due to the top quark mass ($\approx 173\text{ GeV}/c^2$).

951 Decays to gluons proceed indirectly through a virtual top quark loop while the
 952 decays to photons proceed through a virtual W boson loop, therefore, their branching
 953 ratio is smaller compared to direct interaction decays. Same is true for the decay to
 954 a photon and a Z boson.

⁸ In general, on-shell or real particles are those which satisfy the energy-momentum relation ($E^2 - |\vec{p}|^2 c^2 = m^2 c^4$); off-shell or virtual particles does not satisfy it which is possible under the uncertainty principle of quantum mechanics. Usually, virtual particles correspond to internal propagators in Feynman diagrams.

955 In the case of decays to pairs of W and Z bosons, the decay proceed with one of
 956 the bosons being on-shell and the other being off-shell. The likelihood of the process
 957 diminish depending on how far off-shell are the virtual particles involved, hence, the
 958 branching ratio for W boson pairs is bigger than for Z boson pairs since Z boson mass
 959 is bigger than W boson mass.

960 Note that the decay to a pair of virtual top quarks is possible, but the probability
 961 is way too small.

962 **1.4 Experimental status of the anomalous
 963 Higgs-fermion coupling**

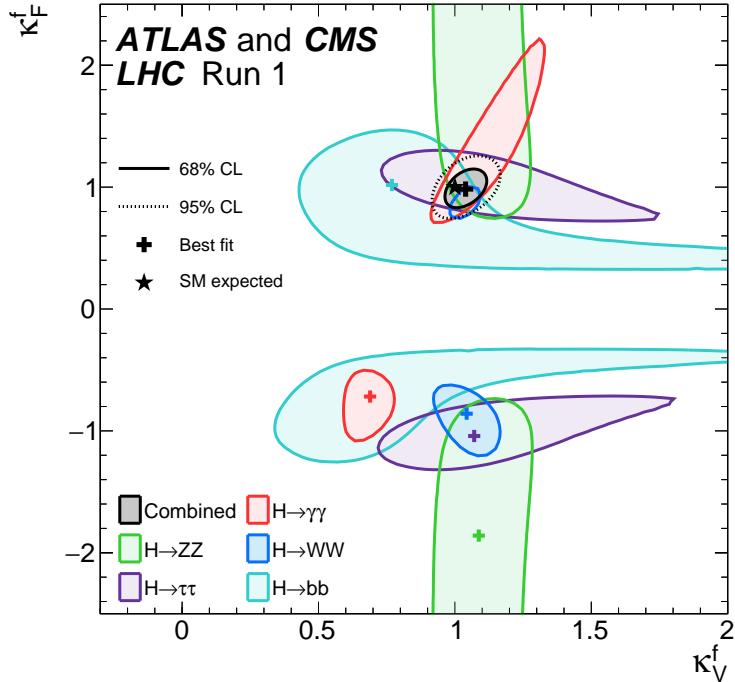


Figure 1.14: Combination of the ATLAS and CMS fits for coupling modifiers $\kappa_t - \kappa_V$; also shown the individual decay channels combination and their global combination. No assumptions have been made on the sign of the coupling modifiers [44].

964 ATLAS and CMS have performed analyses of the anomalous Higgs-fermion cou-
 965 pling by making likelihood scans for the two coupling modifiers, κ_f and κ_V , under
 966 the assumption that $\kappa_Z = \kappa_W \equiv \kappa_V$ and $\kappa_t = \kappa_\tau = \kappa_b \equiv \kappa_f$. Figure 1.14 shows the
 967 result of the combination of ATLAS and CMS fits; also the individual decay channels
 968 combination and the global combination results are shown. Note that from this plot
 969 there is limited information on the sign of the coupling since the only information
 970 available about the sign of the coupling comes from decays rather than production.

971 While all the channels are compatible for positive values of the modifiers, for
 972 negative values of κ_f there is no compatibility. The best fit for individual channels
 973 is compatible with negative values of κ_f except for the $H \rightarrow bb$ channel. The best
 974 fit for the combination yields $\kappa_f \geq 0$, in contrast to the yields from the individual
 975 channels; the reason of this yield resides in the $H \rightarrow \gamma\gamma$ coupling. $H \rightarrow \gamma\gamma$ decay
 976 proceeds through a loop of either top quarks or W bosons, hence, this channel is
 977 sensitive to κ_t thanks to the interference of these two amplitude contributions; under
 978 the assumption that no beyond SM particles take part in the loops, a flipped sign
 979 of κ_t will increase the $H \rightarrow \gamma\gamma$ branching fraction by a factor of ~ 2.4 which is not
 980 supported by measurements; thus, this large asymmetry between the positive and
 981 negative coupling ratios in the $H \rightarrow \gamma\gamma$ channel drives the yield of the global fit and
 982 would mean that the anomalous H-t coupling is excluded as stated in Reference [44],
 983 but there is a caveat, this exclusion holds only if no new particles contribute to the
 984 loop in the main diagram for that decay.

985 Although the $H \rightarrow bb$ channel is expected to be the most sensitive channel and
 986 its best fit value of κ_t is positive, and then the global fit yield is still supported,
 987 the contributions from all the other decay channels, small compared to the $H \rightarrow bb$,
 988 indicate that the anomalous H-t coupling cannot be excluded completely, motivating
 989 to look at tH processes which can help with both, the limited information on the sign

990 of the H-t coupling and the access to information from the Higgs boson production
 991 rather than from its decays.

992 It will be shown in Section 1.5 that the same interference effect enhance the
 993 tH production rate and could reveal evidence of direct production of heavy new par-
 994 ticles as predicted in composite and little Higgs models [45], or new physics related
 995 to Higgs boson mediated flavor changing neutral currents [46] as well as probes the
 996 CP-violating phase of the H-t coupling [47, 48].

997 **1.5 Associated production of a Higgs boson and a 998 single top quark**

999 The production of Higgs boson in association with a top quark has been extensively
 1000 studied [47, 49–52]. While measurements of the main Higgs production mechanisms
 1001 rates are sensitive to the strength of the Higgs coupling to W boson or top quark,
 1002 they are not sensitive to the relative sign between the two couplings. In this thesis,
 1003 the Higgs boson production mechanism explored is the associated production with a
 1004 single top quark (tH) which offers sensitivity to the relative sign of the Higgs couplings
 1005 to W boson and to top quark. The description given here is based on Reference [51]

A process where two incoming particles interact and produce a final state with two
 particles can proceed in three called channels (see, for instance, Figure 1.15 omitting
 the red line). The t-channel represents processes where an intermediate particle is
 emitted by one of the incoming particles and absorbed by the other. The s-channel
 represents processes where the two incoming particles merge into an intermediate par-
 ticle which eventually will split into the particles in the final state. The third channel,
 u-channel, is similar to the t-channel but the two outgoing particles interchange their

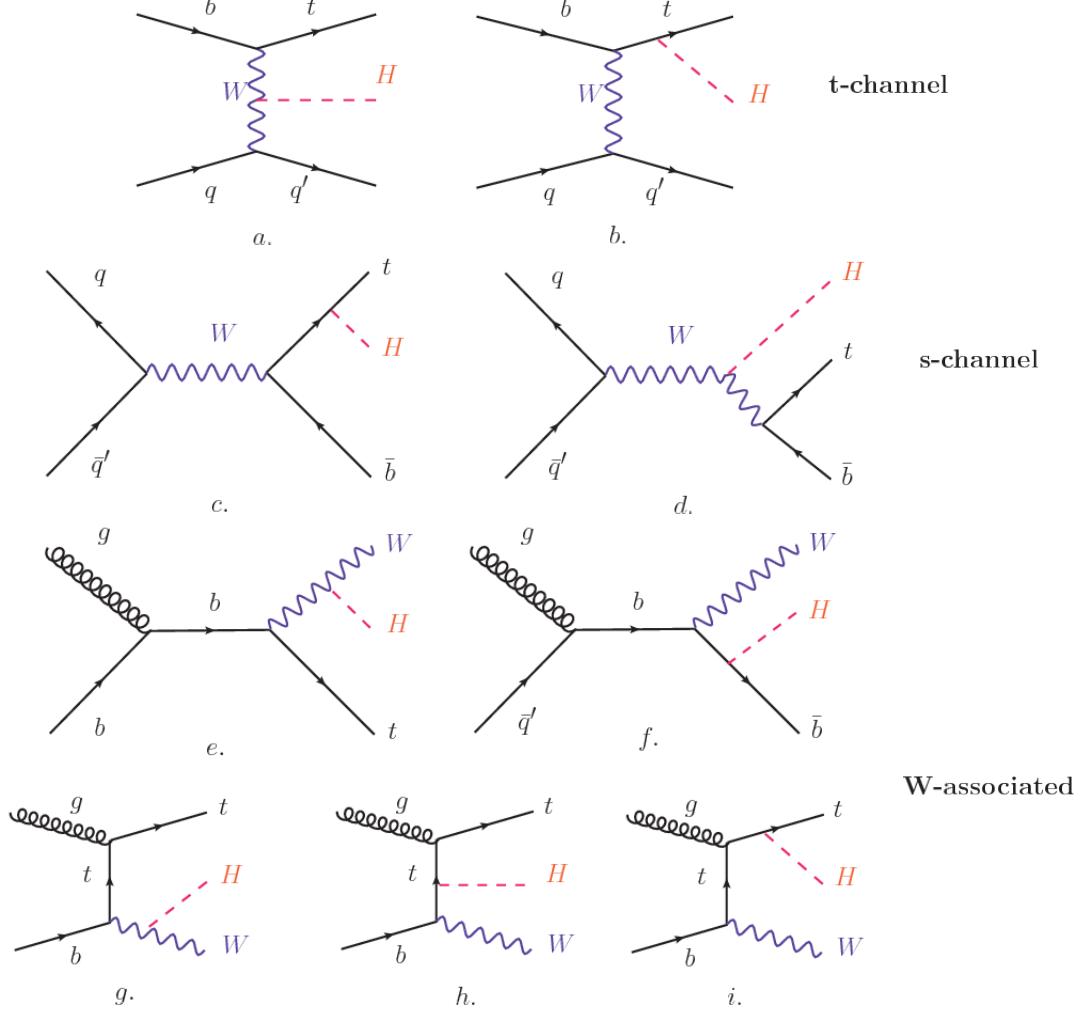


Figure 1.15: Associated Higgs boson production with a top quark mechanism Feynman diagrams. a.,b. t-channel (tHq), c.,d. s-channel (tHb), e-i. W-associated.

roles. These three channels are connected to the so-called Mandelstam variables

$$s = (p_1 + p_2)^2 = (p'_1 + p'_2)^2 \rightarrow \text{square of the center mass-energy.} \quad (1.58)$$

$$t = (p_1 - p'_1)^2 = (p'_2 - p_2)^2 \rightarrow \text{square of the four-momentum transfer.} \quad (1.59)$$

$$u = (p_1 - p'_2)^2 = (p'_1 - p_2)^2 \rightarrow \text{square of the crossed four-momentum transfer.} \quad (1.60)$$

$$s + t + u = m_1^2 + m_2^2 + m'_1^2 + m'_2^2 \quad (1.61)$$

1006 which relate the momentum, energy and the angles of the incoming and outgoing
 1007 particles in an scattering process of two particles to two particles. The importance of
 1008 the Mandelstam variables reside in that they form a minimum set of variables needed
 1009 to describe the kinematics of this scattering process; they are Lorentz invariant which
 1010 makes them very useful when doing calculations.

1011 The tH production, where Higgs boson can be radiated either from the top quark or
 1012 from the W boson, is represented by the leading order Feynman diagrams in Figure
 1013 1.15. The cross section for the tH process is calculated, as usual, summing over
 1014 the contributions from the different Feynman diagrams; therefore it depends on the
 1015 interference between the contributions. In the SM, the interference for t-channel (tHq
 1016 process) and W-associated (tHW process) production is destructive [49] resulting in
 1017 the small cross sections presented in Table 1.10.

tH production channel	Cross section (fb)
t-channel ($pp \rightarrow tHq$)	$70.79^{+2.99}_{-4.80}$
W-associated ($pp \rightarrow tHW$)	$15.61^{+0.83}_{-1.04}$
s-channel($pp \rightarrow tHb$)	$2.87^{+0.09}_{-0.08}$

Table 1.10: Predicted SM cross sections for tH production at $\sqrt{s} = 13$ TeV [53, 54].

1018

1019 The s-channel contribution can be neglected. It will be shown that a deviation
 1020 from the SM destructive interference would result in an enhancement of the tH cross
 1021 section compared to that in SM, which could be used to get information about the
 1022 sign of the Higgs-top coupling [51, 52]. In order to describe tH production processes,
 1023 Feynman diagram 1.15b will be considered; there, the W boson is radiated by a quark
 1024 in the proton and eventually it will interact with the b quark. In the high energy
 1025 regime, the effective W approximation [55] is used to describe the process as the

1026 emission of an approximately on-shell W and its hard scattering with the b quark;
 1027 i.e. $Wb \rightarrow th$. The scattering amplitude for the process is given by

$$\mathcal{A} = \frac{g}{\sqrt{2}} \left[(\kappa_t - \kappa_V) \frac{m_t \sqrt{s}}{m_W v} A \left(\frac{t}{s}, \varphi; \xi_t, \xi_b \right) + \left(\kappa_V \frac{2m_W s}{v t} + (2\kappa_t - \kappa_V) \frac{m_t^2}{m_W v} \right) B \left(\frac{t}{s}, \varphi; \xi_t, \xi_b \right) \right], \quad (1.62)$$

1028 where $\kappa_V \equiv g_{HVV}/g_{HVV}^{SM}$ and $\kappa_t \equiv g_{Ht}/g_{Ht}^{SM} = y_t/y_t^{SM}$ are scaling factors that quantify
 1029 possible deviations of the couplings from the SM values, Higgs-Vector boson (H-
 1030 W) and Higgs-top (H-t) respectively, from the SM couplings; $s = (p_W + p_b)^2$, $t =$
 1031 $(p_W - p_H)^2$, φ is the Higgs azimuthal angle around the z axis taken parallel to the
 1032 direction of motion of the incoming W; A and B are functions describing the weak
 1033 interaction in terms of the chiral states (ξ_t, ξ_b) of the quarks b and t . Terms that
 1034 vanish in the high energy limit have been neglected as well as the Higgs and b quark
 1035 masses⁹.

1036 The scattering amplitude grows with energy like \sqrt{s} for $\kappa_V \neq \kappa_t$, in contrast to
 1037 the SM ($\kappa_t = \kappa_V = 1$), where the first term in 1.62 cancels out and the amplitude
 1038 is constant for large s ; therefore, a deviation from the SM predictions represents an
 1039 enhancement in the tHq cross section. In particular, for a SM H-W coupling and a
 1040 H-t coupling of inverted sign with respect to the SM ($\kappa_V = -\kappa_t = 1$) the tHq cross
 1041 section is enhanced by a factor greater 10 as seen in the Figure 1.16 taken from
 1042 Reference [51]; Reference [56] has reported similar enhancement results.

1043 A similar analysis is valid for the W-associated channel but, in that case, the in-
 1044 terference is more complicated since there are more than two contributions and an ad-
 1045 ditional interference with the production of Higgs boson and a top pair process($t\bar{t}H$).
 1046 The calculations are made using the so-called Diagram Removal (DR) technique where

⁹ A detailed explanation of the structure and approximations used to derive \mathcal{A} can be found in Reference [51]

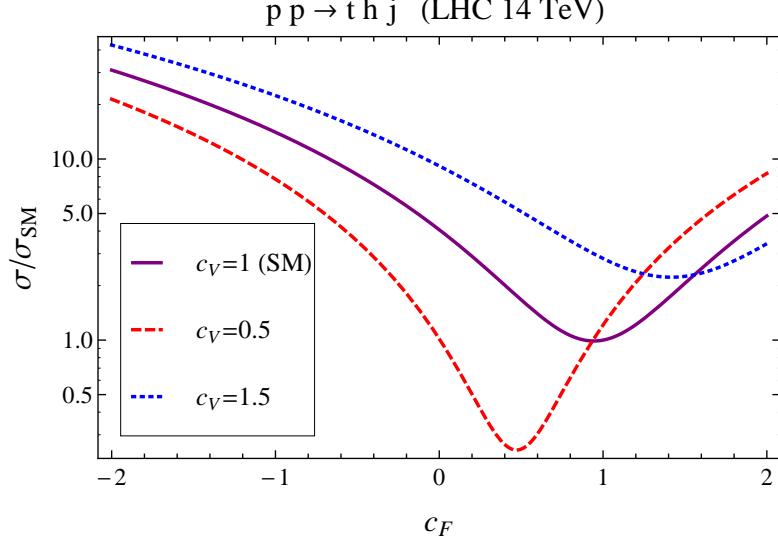


Figure 1.16: Cross section for tHq process as a function of κ_t , normalized to the SM, for three values of κ_V . In the plot c_f refers to the Higgs-fermion coupling which is dominated by the H-t coupling and represented here by κ_t . Solid, dashed and dotted lines correspond to $c_V \rightarrow \kappa_V = 1, 0.5, 1.5$ respectively. Note that for the SM ($\kappa_V = \kappa_t = 1$), the destructive effect of the interference is maximal.

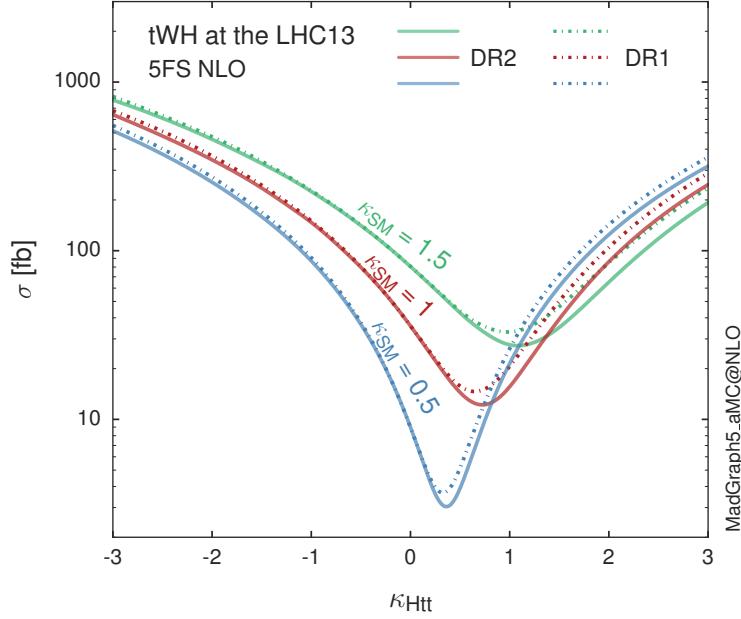


Figure 1.17: Cross section for tHW process as a function of κ_{Htt} , for three values of κ_{SM} at $\sqrt{s} = 13$ TeV. $\kappa_{Htt}^2 = \sigma_{Htt}/\sigma_{Htt}^{SM}$ is a simple re-scaling of the SM Higgs interactions.

interfering diagrams are removed (or added) from the calculations in order to evaluate the impact of the removed contributions. DR1 was defined to neglect $t\bar{t}H$ interference while DR2 was defined to take $t\bar{t}H$ interference into account [48]. As shown in Figure 1.17, the tHW cross section is enhanced from about 15 fb (SM: $\kappa_{Htt} = 1$) to about 150 fb ($\kappa_{Htt} = -1$). Differences between curves for DR1 and DR2 help to gauge the impact of the interference with $t\bar{t}H$. Results of the calculations of the tHq and tHW cross sections at $\sqrt{s} = 13$ TeV can be found in Reference [57] and a summary of the results is presented in Table 1.11.

	\sqrt{s} TeV	$\kappa_t = 1$	$\kappa_t = -1$
$\sigma^{LO}(tHq)(fb)$ [51]	8	≈ 17.4	≈ 252.7
	14	≈ 80.4	≈ 1042
$\sigma^{NLO}(tHq)(fb)$ [51]	8	$18.28^{+0.42}_{-0.38}$	$233.8^{+4.6}_{-0.0}$
	14	$88.2^{+1.7}_{-0.0}$	$982.8^{+28}_{-0.0}$
$\sigma^{LO}(tHq)(fb)$ [56]	14	≈ 71.8	≈ 893
$\sigma^{LO}(tHW)(fb)$ [56]	14	≈ 16.0	≈ 139
$\sigma^{NLO}(tHq)(fb)$ [57]	8	$18.69^{+8.62\%}_{-17.13\%}$	-
	13	$74.25^{+7.48\%}_{-15.35\%}$	$848^{+7.37\%}_{-13.70\%}$
	14	$90.10^{+7.34\%}_{-15.13\%}$	$1011^{+7.24\%}_{-13.39\%}$
$\sigma^{LO}(tHW)(fb)$ [48]	13	$15.77^{+15.91\%}_{-15.76\%}$	-
$\sigma^{NLO}DR1(tHW)(fb)$ [48]	13	$21.72^{+6.52\%}_{-5.24\%}$	≈ 150
$\sigma^{NLO}DR2(tHW)(fb)$ [48]	13	$16.28^{+7.34\%}_{-15.13\%}$	≈ 150

Table 1.11: Predicted enhancement of the tHq and tHW cross sections at LHC for $\kappa_V = 1$ and $\kappa_t = \pm 1$ at LO and NLO; the cross section enhancement of more than a factor of 10 is due to the flipping in the sign of the H-t coupling with respect to the SM one.

1055

1056 1.6 CP-mixing in tH processes

1057 In addition to the sensitivity to sign of the H-t coupling, the tHq and tHW processes
 1058 have been proposed as a tool to investigate the possibility of a H-t coupling that does

1059 not conserve CP [47, 48, 58].

1060 In this thesis, the sensitivity of tH processes to CP-mixing is also studied on the
 1061 basis of References [47, 48] using the effective field theory framework where a generic
 1062 particle (X_0) of spin-0 and a general CP violating interaction with the top quark
 1063 (Htt coupling), can couple to scalar and pseudo-scalar fermionic densities. The H-W
 1064 interaction is assumed to be SM-like. The Lagrangian modeling the H-t interaction
 1065 is given by

$$\mathcal{L}_0^t = -\bar{\psi}_t (c_\alpha \kappa_{Htt} g_{Htt} + i s_\alpha \kappa_{Att} g_{Att} \gamma_5) \psi_t X_0, \quad (1.63)$$

1066 where α is the CP-mixing phase, $c_\alpha \equiv \cos \alpha$ and $s_\alpha \equiv \sin \alpha$, κ_{Htt} and κ_{Att} are real
 1067 dimensionless re-scaling parameters¹⁰ used to parametrize the magnitude of the CP-
 1068 violating and CP-conserving parts of the amplitude. The model defines $g_{Htt} =$
 1069 $g_{Att} = m_t/v = y_t/\sqrt{2}$ with $v \sim 246$ GeV the Higgs vacuum expectation value. In
 1070 this parametrization, three special cases can be recovered

1071 • CP-even coupling $\rightarrow \alpha = 0^\circ$

1072 • CP-odd coupling $\rightarrow \alpha = 90^\circ$

1073 • SM coupling $\rightarrow \alpha = 0^\circ$ and $\kappa_{Htt} = 1$

1074 The loop induced X_0 coupling to gluons can also be described in terms of the
 1075 parametrization above, according to

$$\mathcal{L}_0^g = -\frac{1}{4} \left(c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right) X_0. \quad (1.64)$$

1076 where $g_{Hgg} = -\alpha_s/3\pi v$ and $g_{Agg} = \alpha_s/2\pi v$ and $G_{\mu\nu}$ is the gluon field strength tensors.

1077 Under the assumption that the top quark dominates the gluon-fusion process at LHC

¹⁰ analog to κ_t and κ_V

1078 energies, $\kappa_{Hgg} \rightarrow \kappa_{Htt}$ and $\kappa_{Agg} \rightarrow \kappa_{Att}$, so that the ratio between the gluon-gluon
 1079 fusion cross section for X_0 and for the SM Higgs prediction can be written as

$$\frac{\sigma_{NLO}^{gg \rightarrow X_0}}{\sigma_{NLO,SM}^{gg \rightarrow H}} = c_\alpha^2 \kappa_{Htt}^2 + s_\alpha^2 \left(\kappa_{Att} \frac{g_{Agg}}{g_{Hgg}} \right)^2. \quad (1.65)$$

1080 If the re-scaling parameters are set to

$$\kappa_{Htt} = 1, \quad \kappa_{Att} = \left| \frac{g_{Hgg}}{g_{Agg}} \right| = \frac{2}{3}. \quad (1.66)$$

1081 the gluon-fusion SM cross section is reproduced for every value of the CP-mixing
 1082 angle α ; therefore, by imposing that condition to the Lagrangian density 1.63, the
 1083 CP-mixing angle is not constrained by current data. Figure 1.18 shows the NLO cross
 1084 sections for t-channel tX_0 (blue) and $t\bar{t}X_0$ (red) associated production processes as a
 1085 function of the CP-mixing angle α . X_0 is a generic spin-0 particle with top quark
 1086 CP-violating coupling. Re-scaling factors κ_{Htt} and κ_{Att} have been set to reproduce
 1087 the SM gluon-fusion cross sections.

1088 It is interesting to notice that the tX_0 cross section is enhanced, by a factor of
 1089 about 10, when a continuous rotation in the scalar-pseudoscalar plane is applied; this
 1090 enhancement is similar to the enhancement produced when the H-t coupling is flipped
 1091 in sign with respect to the SM ($y_t = -y_{t,SM}$ in the plot), as showed in Section 1.5. In
 1092 contrast, the degeneracy in the $t\bar{t}X_0$ cross section is still present given that it depends
 1093 quadratically on the H-t coupling, but more interesting is to notice that $t\bar{t}X_0$ cross
 1094 section is exceeded by tX_0 cross section after $\alpha \sim 60^\circ$.

1095 A similar parametrization can be used to investigate the tHW process sensitivity
 1096 to CP-violating H-t coupling. As said in 1.5, the interference in the W-associated
 1097 channel is more complicated because there are more than two contributions and also
 1098 there is interference with the $t\bar{t}H$ production process.

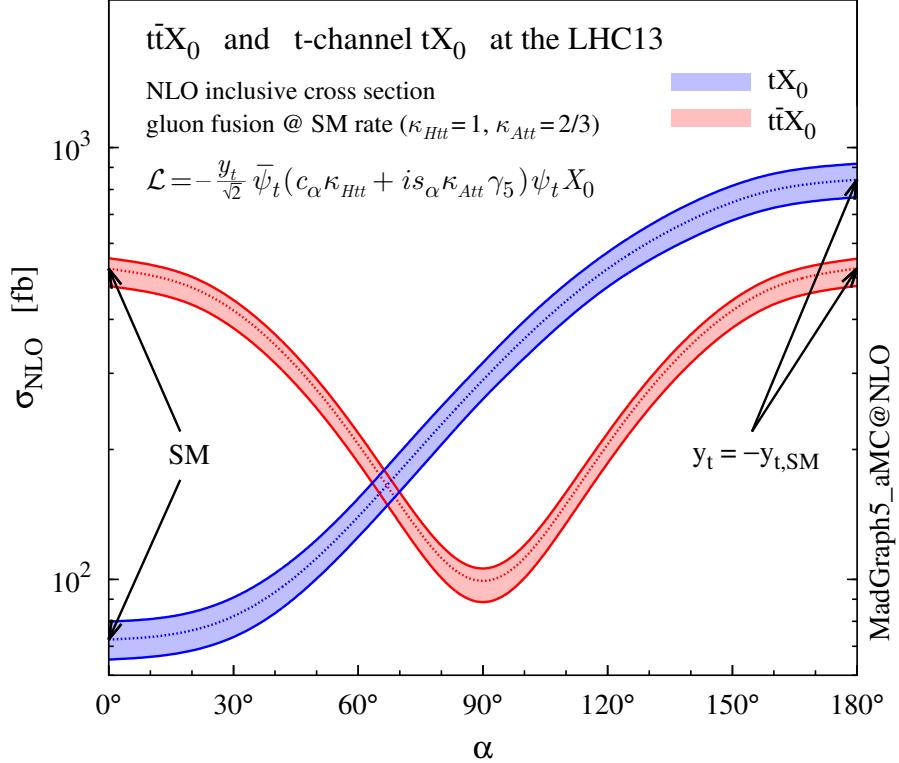


Figure 1.18: NLO cross sections for t-channel tX_0 (blue) and $t\bar{t}X_0$ (red) associated production processes as a function of the CP-mixing angle α . X_0 is a generic spin-0 particle with top quark CP-violating coupling [47].

1099 Figure 1.19 shows the NLO cross sections for t-channel tX_0 (blue), $t\bar{t}X_0$ (red)
1100 associated production and for the combined $tWX_0 + t\bar{t}X_0 + \text{interference}$ (orange) as
1101 a function of the CP-mixing angle. It is clear that the effect of the interference in the
1102 combined case is the lifting of the degeneracy present in the $t\bar{t}X_0$ production. The
1103 constructive interference enhances the cross section from about 500 fb at SM ($\alpha = 0$)
1104 to about 600 fb ($\alpha = 180^\circ \rightarrow y_t = -y_{t,SM}$).

1105 An analysis combining tHq and tHW processes will be made in this thesis taking
1106 advantage of the sensitivity improvement.

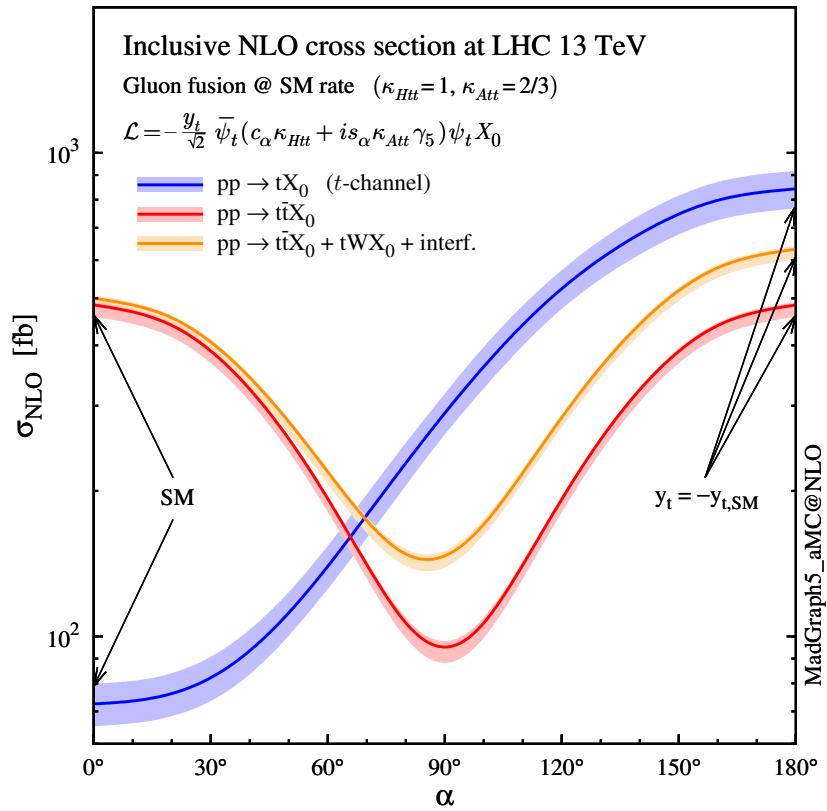


Figure 1.19: NLO cross sections for t-channel tX_0 (blue), $t\bar{t}X_0$ (red) associated production processes and combined $tWX_0 + t\bar{t}X_0$ (including interference) production as a function of the CP-mixing angle α [47].

₁₁₀₇ **Chapter 2**

₁₁₀₈ **The CMS experiment at the LHC**

₁₁₀₉ **2.1 Introduction**

₁₁₁₀ Located on the Swiss-French border, the European Council for Nuclear Research
₁₁₁₁ (CERN) is the largest scientific organization leading particle physics research. About
₁₁₁₂ 13000 people in a broad range of roles including users, students, scientists, engineers,
₁₁₁₃ among others, contribute to the data taking and analysis, with the goal of unveiling
₁₁₁₄ the secrets of nature and revealing the fundamental structure of the universe. CERN
₁₁₁₅ is also the home of the Large Hadron Collider (LHC), the largest particle accelerator
₁₁₁₆ around the world, where protons (or heavy ions) traveling close to the speed of light,
₁₁₁₇ are made to collide. These collisions open a window to investigate how particles (and
₁₁₁₈ their constituents if they are composite) interact with each other, providing clues
₁₁₁₉ about the laws of nature. This chapter presents an overview of the LHC structure
₁₁₂₀ and operation. A detailed description of the CMS detector is offered, given that the
₁₁₂₁ data used in this thesis have been taken with this detector.

1122 2.2 The LHC

1123 With 27 km of circumference, the LHC is currently the most powerful circular accelerator
 1124 in the world. It is installed in the same tunnel where the Large Electron-Positron
 1125 (LEP) collider was located, taking advantage of the existing infrastructure. The LHC
 1126 is part of the CERN's accelerator complex composed of several successive accelerat-
 1127 ing stages before the particles are injected into the LHC ring where they reach their
 1128 maximum energy (see Figure 2.1).

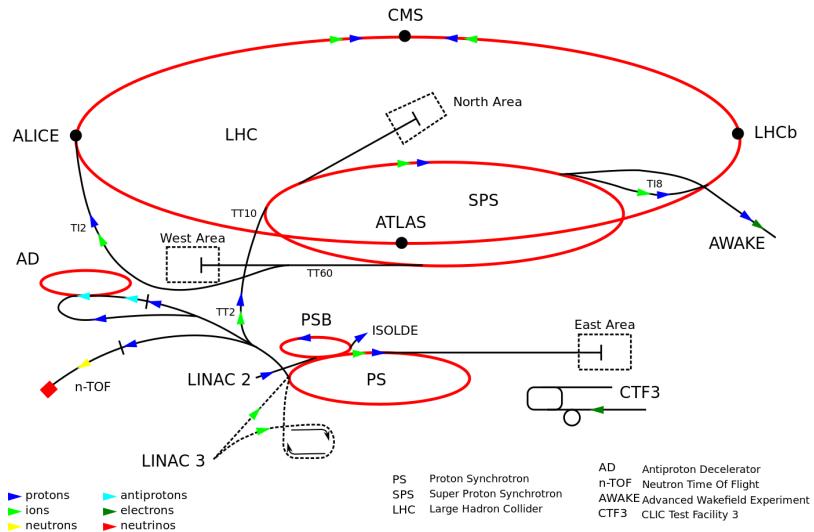


Figure 2.1: CERN accelerator complex. Blue arrows show the path followed by protons along the acceleration process [61].

1129 The LHC runs in three collision modes depending on the particles being acceler-
 1130 ated

1131 • Proton-Proton collisions (pp) for multiple physics experiments.

1132 • Lead-Lead collisions ($Pb-Pb$) for heavy ion experiments.

1133 • Proton-Lead collisions ($p-Pb$) for quark-gluon plasma experiments.

1134 In this thesis only pp collisions will be considered.

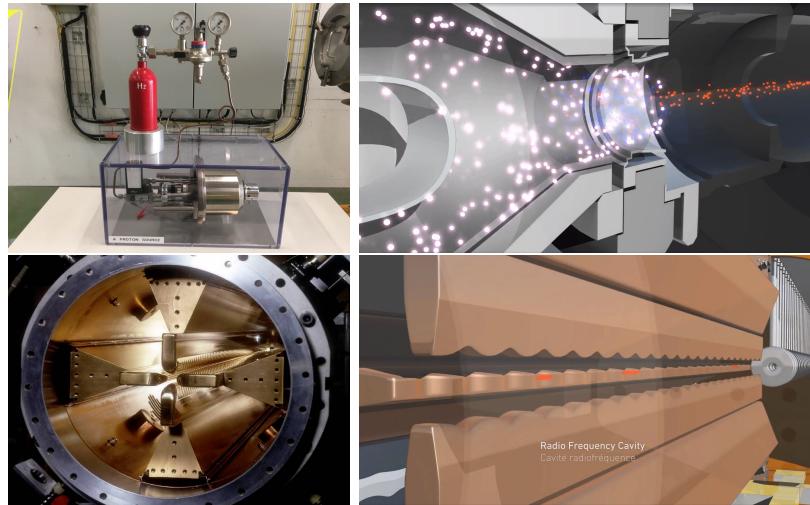


Figure 2.2: LHC protons source and the first acceleration stage. Top: the bottle contains hydrogen gas which is injected into the metal cylinder (white dots) to be broken down into electrons (blue dots) and protons (red dots); Bottom: the obtained protons are directed towards the radio frequency quadrupole which perform the first acceleration, focus the beam and create the bunches of protons. Left images are real pictures while right images are drawings [65, 66].

1135 Collection of protons starts with hydrogen atoms taken from a bottle, containing
 1136 hydrogen gas, and injecting them in a metal cylinder; hydrogen atoms are broken
 1137 down into electrons and protons by an intense electric field (see Figure 2.2 top).
 1138 The resulting protons leave the metal cylinder towards a radio frequency quadrupole
 1139 (RFQ) that focus the beam, accelerates the protons and creates the packets of protons
 1140 called bunches. In the RFQ, an electric field is generated by a RF wave at a frequency
 1141 that matches the resonance frequency of the cavity where the electrodes are contained.
 1142 The beam of protons traveling on the RFQ axis experiences an alternating electric
 1143 field gradient that generates the focusing forces.

1144 In order to accelerate the protons, a longitudinal time-varying electric field com-
 1145 ponent is added to the system; it is done by giving the electrodes a sine-like profile as
 1146 shown in Figure 2.2 bottom. By matching the speed and phase of the protons with
 1147 the longitudinal electric field the bunching is performed; protons synchronized with

1148 the RFQ (synchronous protons) do not feel an accelerating force, but those protons in
 1149 the beam that have more (or less) energy than the synchronous proton (asynchronous
 1150 protons) will feel a decelerating (accelerating) force; therefore, asynchronous protons
 1151 will oscillate around the synchronous ones forming bunches of protons [63]. From the
 1152 RFQ protons emerge with energy 750 keV in bunches of about 1.15×10^{11} protons [64].

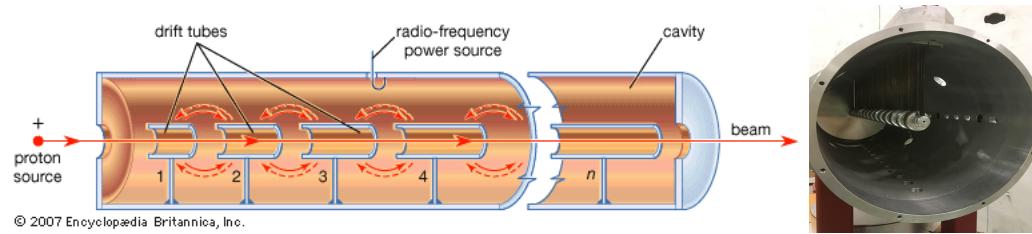


Figure 2.3: Left: drawing of the LINAC2 accelerating system at CERN. Electric fields generated by radio frequency (RF) create acceleration and deceleration zones inside the cavity; deceleration zones are blocked by drift tubes where quadrupole magnets focus the proton beam. Right: picture of a real RF cavity [67].

1153 Proton bunches coming from the RFQ go to the linear accelerator 2 (LINAC2)
 1154 where they are accelerated to reach 50 MeV energy. In the LINAC2 stage, acceleration
 1155 is performed using electric fields generated by radio frequency which create zones
 1156 of acceleration and deceleration as shown in Figure 2.3. In the deceleration zones,
 1157 the electric field is blocked using drift tubes where protons are free to drift while
 1158 quadrupole magnets focus the beam.

1159 The beam coming from LINAC2 is injected into the proton synchrotron booster
 1160 (PSB) to reach 1.4 GeV in energy. The next acceleration is provided at the proton
 1161 synchrotron (PS) up to 26 GeV, followed by the injection into the super proton
 1162 synchrotron (SPS) where protons are accelerated to 450 GeV. Finally, protons are
 1163 injected into the LHC where they are accelerated to the target energy of 6.5 TeV.

1164 PSB, PS, SPS and LHC accelerate protons using the same RF acceleration tech-
 1165 nique described before.

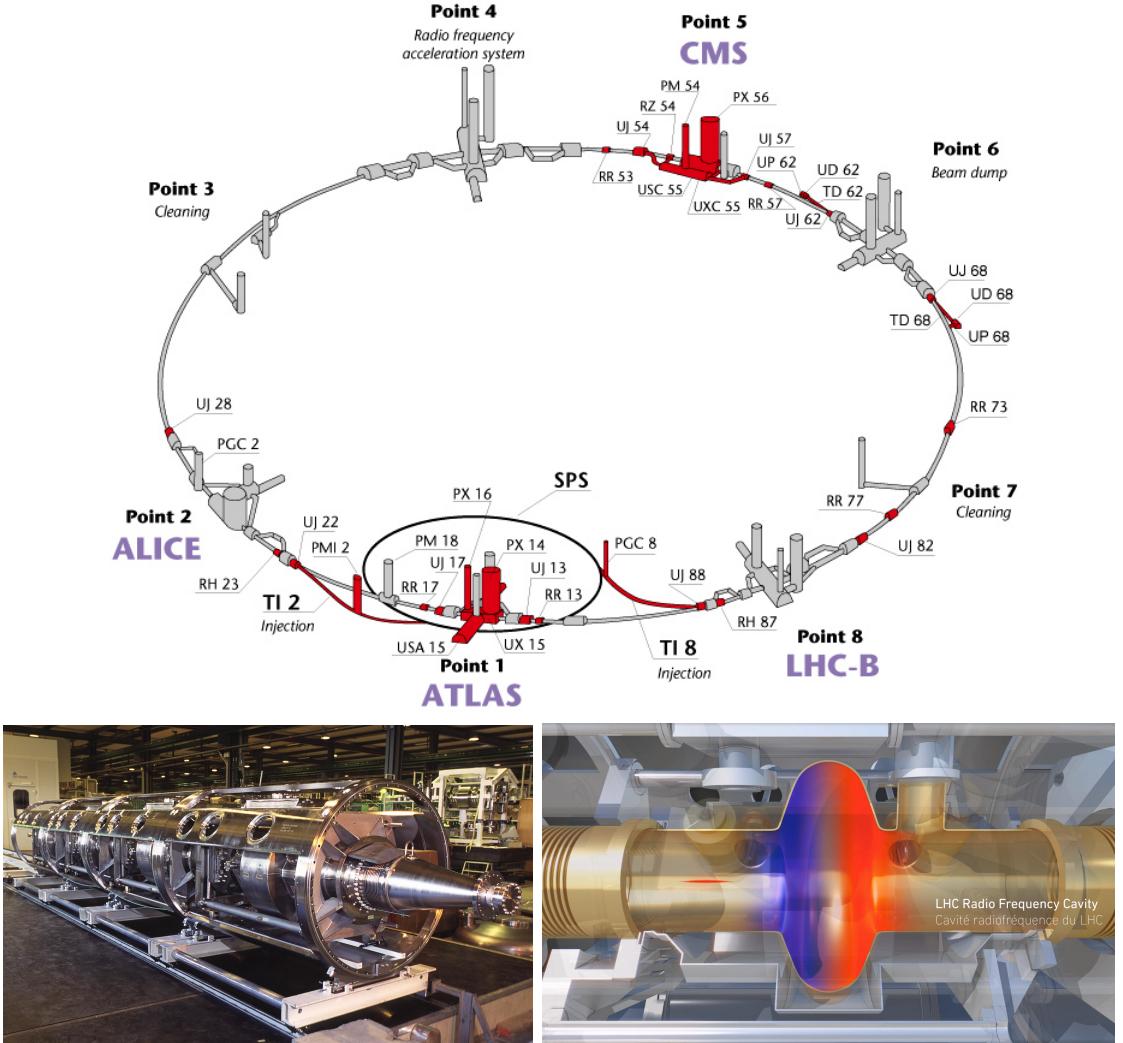


Figure 2.4: Top: LHC layout. The red zones indicate the infrastructure additions to the LEP installations, built to accommodate the ATLAS and CMS experiments which exceed the size of the former experiments located there [62]. Bottom: LHC RF cavities. A module (left picture) accommodates 4 cavities, each like the one in the right drawing, that accelerate protons and preserve the bunch structure of the beam. The color gradient pattern represents the strength of the electric field inside the cavity; red zone corresponds to the maximum of the oscillation electric field while the blue zone corresponds to the minimum. [66, 68]

1166 The LHC has a system of 16 RF cavities located in the so-called point 4, as
 1167 shown in Figure 2.4 top, tuned at a frequency of 400 MHz. The bottom side of
 1168 Figure 2.4 shows a picture of a RF module composed of 4 RF cavities working in a
 1169 superconducting state at 4.5 K; also, a representation of the accelerating electric field

that accelerates the protons in the bunch is shown. The maximum of the oscillating electric field (red region) picks the proton bunches at the entrance of the cavity and keeps accelerating them through the whole cavity. The protons are carefully timed so that in addition to the acceleration effect the bunch structure of the beam is preserved.

While protons are accelerated in one section of the LHC ring, where the RF cavities are located, in the rest of their path they have to be kept in the curved trajectory defined by the LHC ring. Technically, LHC is not a perfect circle; RF, injection, beam dumping, beam cleaning and sections before and after the experimental points where protons collide are all straight sections. In total, there are 8 arcs 2.45 km long each and 8 straight sections 545 m long each. In order to curve the proton's trajectory in the arc sections, superconducting dipole magnets are used.

Inside the LHC ring, there are two proton beams traveling in opposite directions in two separated beam pipes; the beam pipes are kept at ultra-high vacuum ($\sim 10^{-9}$ Pa) to ensure that there are no particles that interact with the proton beams. The superconducting dipole magnets used in LHC are made of a NbTi alloy, capable of transporting currents of about 12000 A when cooled at a temperature below 2K using liquid helium (see Figure 2.5).

Protons in the arc sections of LHC feel a centripetal force exerted by the dipole magnets; the magnitude of magnetic field needed to keep the protons in the LHC curved trayectomy can be found assuming that protons travel at $v \approx c$, using the standard values for proton mass and charge and the LHC radius, as

$$F_m = \frac{mv^2}{r} = qBv \rightarrow B = 8.33T \quad (2.1)$$

which is about 100000 times the Earth's magnetic field. A representation of the

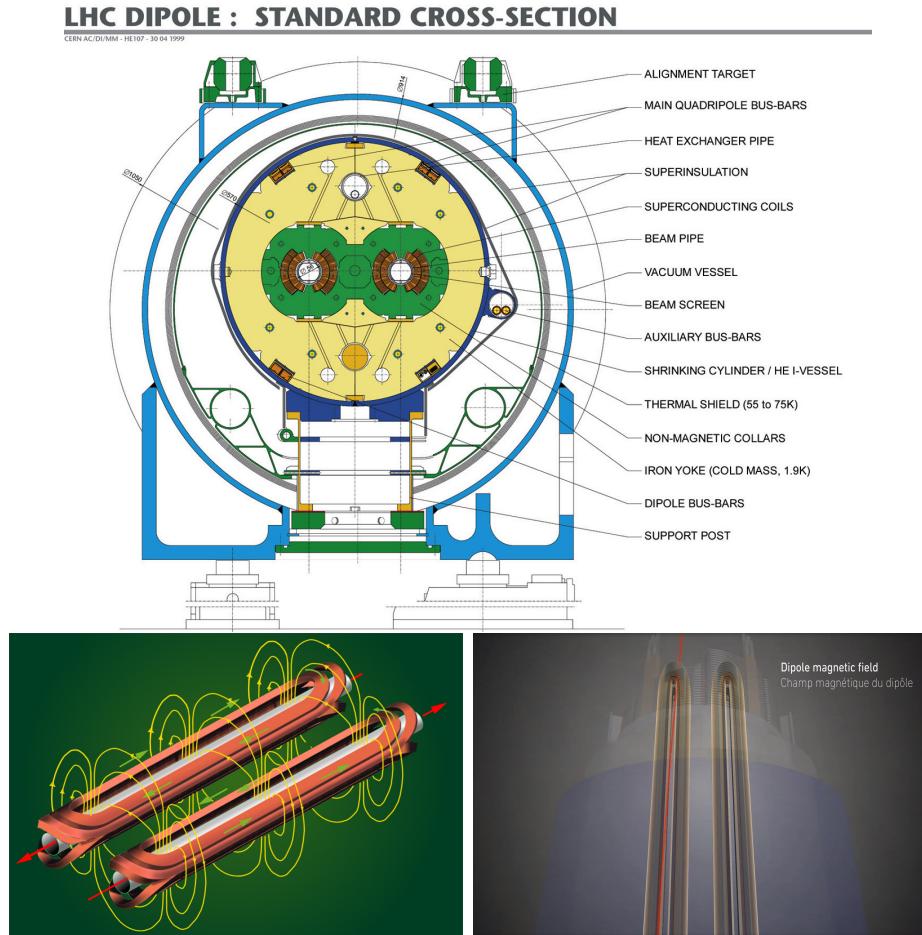


Figure 2.5: Top: LHC dipole magnet transverse view; cooling, shielding and mechanical support are indicated. Bottom left: Magnetic field generated by the dipole magnets; note that the direction of the field inside one beam pipe is opposite with respect to the other beam pipe which guarantee that both proton beams are curved in the same direction towards the center of the ring. The effect of the dipole magnetic field on the proton beam is represented on the bottom right side [66, 69, 70].

1193 magnetic field generated by the dipole magnets is shown on the bottom left side of
 1194 Figure 2.5. The bending effect of the magnetic field on the proton beam is shown on
 1195 the bottom right side of Figure 2.5. Note that the dipole magnets are not curved;
 1196 the arc section of the LHC ring is composed of straight dipole magnets of about 15
 1197 m. In total there are 1232 dipole magnets along the LHC ring.
 1198 In addition to the bending of the beam trajectory, the beam has to be focused. The

focusing is performed by quadrupole magnets installed in a different straight section; in total 858 quadrupole magnets are installed along the LHC ring. Other effects like electromagnetic interaction among bunches, interaction with electron clouds from the beam pipe, the gravitational force on the protons, differences in energy among protons in the same bunch, among others, are corrected using sextupole and other magnetic multipoles.

The two proton beams inside the LHC ring are made of bunches with a cylindrical shape of about 7.5 cm long and about 1 mm in diameter; when bunches are close to the interaction point (IP), the beam is focused up to a diameter of about 16 μm in order to maximize the probability of collisions between protons. The number of collisions per second is proportional to the cross section of the bunches with the *luminosity* (L) as the proportionality factor, thus, the luminosity can be calculated using

$$L = fn \frac{N_1 N_2}{4\pi\sigma_x\sigma_y} \quad (2.2)$$

where f is the revolution frequency, n is the number of bunches per beam, N_1 and N_2 are the numbers of protons per bunch, σ_x and σ_y are the gaussian transverse sizes of the bunches. With the expected parameters, the LHC expected luminosity is about

$$f = \frac{v}{2\pi r_{LHC}} \approx \frac{3 \times 10^8 \text{ m/s}}{27 \text{ km}} \approx 11.1 \text{ kHz},$$

$$n = 2808$$

$$N_1 = N_2 \sim 1.5 \times 10^{11}$$

$$\sigma_x = \sigma_y = 16 \mu\text{m}$$

1214

$$L = 1.28 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1} = 1.28 \times 10^{-5} \text{ fb}^{-1} \text{ s}^{-1} \quad (2.3)$$

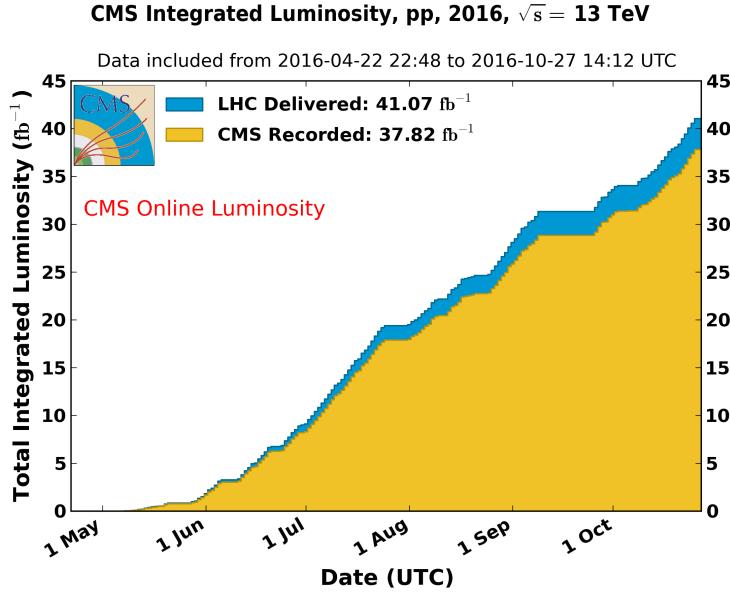


Figure 2.6: Integrated luminosity delivered by LHC and recorded by CMS during 2016. The difference between the delivered and the recorded luminosity is due to fails and issues occurred during the data taking in the CMS experiment [71].

1215 Luminosity is a fundamental aspect of LHC given that the bigger luminosity the
 1216 bigger number of collisions, which means that for processes with a very small cross
 1217 section the number of expected occurrences is increased and so the chances of being
 1218 detected. The integrated luminosity, collected by the CMS experiment during 2016
 1219 is shown in Figure 2.6; the data analyzed in this thesis corresponds to an integrated
 1220 luminosity of 35.9 fb^{-1} at a center of mass-energy $\sqrt{s} = 13 \text{ TeV}$.

1221 One way to increase L is increasing the number of bunches in the beam. Cur-
 1222 rently, the separation between two consecutive bunches in the beam is 7.5 m which
 1223 corresponds to a time separation of 25 ns. In the full LHC ring the allowed number
 1224 of bunches is $n = 27\text{km}/7.5\text{m} = 3600$; however, there are some gaps in the bunch pat-
 1225 tern intended for preparing the dumping and injection of the beam, thus, the proton
 1226 beams are composed of 2808 bunches.

1227 Once the proton beams reach the desired energy, they are brought to cross each

1228 other producing pp collisions. The bunch crossing happens in precise places where
 1229 the four LHC experiments are located, as seen in the top of Figure 2.7. In 2008 pp
 1230 collisions of $\sqrt{s} = 7$ TeV were performed; the energy was increased to 8 TeV in 2012
 1231 and to 13 TeV in 2015.

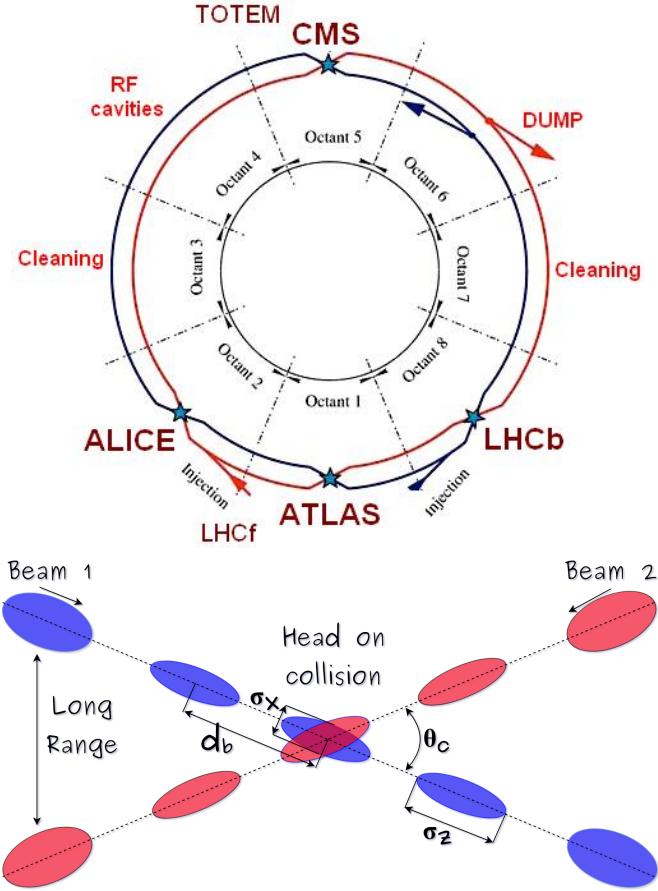


Figure 2.7: Top: LHC interaction points. Bunch crossing occurs where the LHC experiments are located [72]. Sections indicated as cleaning are dedicated to collimate the beam in order to protect the LHC ring from collisions with protons in very spreaded bunches. Bottom: bunch crossing scheme. Since the bunch crossing is not perfectly head-on, the luminosity is reduced in a factor of 17%; adapted from Reference [86].

1232 The CMS and ATLAS experiments are multi-purpose experiments, hence, they
 1233 are enabled to explore physics in any of the LHC collision modes. LHCb experiment
 1234 is optimized to explore bottom quark physics, while ALICE is optimized for heavy

1235 ion collisions searches; TOTEM and LHCf are dedicated to forward physics studies;
 1236 MoEDAL (not indicated in the Figure) is intended for monopole or massive pseudo
 1237 stable particles searches.

1238 At the IP there are two interesting details that need to be addressed. The first
 1239 one is that the bunch crossing does not occur head-on but at a small crossing angle θ_c
 1240 (280 μ rad in CMS and ATLAS) as shown in the bottom side of Figure 2.7, affecting
 1241 the overlapping between bunches; the consequence is a reduction of about 17% in
 1242 the luminosity (represented by a factor not included in eqn. 2.2). The second one
 1243 is the occurrence of multiple pp collisions in the same bunch crossing; this effect is
 1244 called *pileup* (PU). A fairly simple estimation of the PU follows from estimating the
 1245 probability of collision between two protons, one from each of the bunches in the
 1246 course of collision; it depends roughly on the ratio of proton size and the cross section
 1247 of the bunch in the IP, i.e.,

$$P(pp\text{-}collision) \sim \frac{d_{proton}^2}{\sigma_x \sigma_y} = \frac{(1\text{fm})^2}{(16\mu\text{m})^2} \sim 4 \times 10^{-21} \quad (2.4)$$

1248 however, there are $N = 1.15 \times 10^{11}$ protons in a bunch, thus the estimated number of
 1249 collisions in a bunch crossing is

$$PU = N^2 * P(pp\text{-}collision) \sim 50pp \text{ collision per bunch crossing}, \quad (2.5)$$

1250 about 20 of which are inelastic. A multiple pp collision event in a bunch crossing at
 1251 CMS is shown in Figure 2.8.

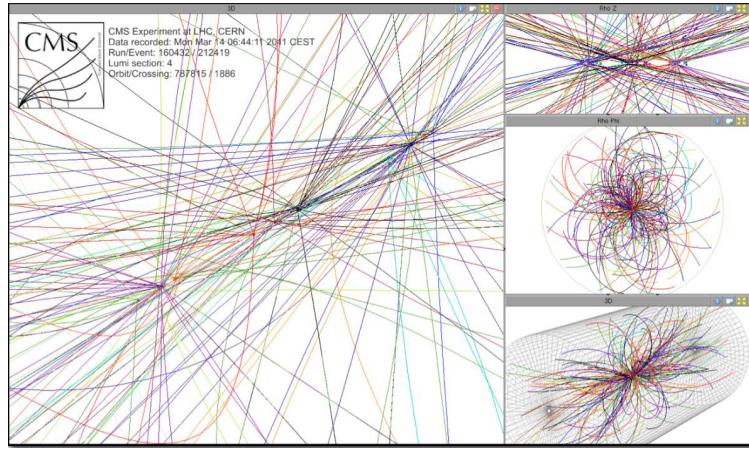


Figure 2.8: Multiple pp collision bunch crossing at CMS. [73].

1252 2.3 The CMS experiment

1253 CMS is a general-purpose detector designed to conduct research in a wide range
 1254 of physics from the standard model to new physics like extra dimensions and dark
 1255 matter. Located at Point 5 in the LHC layout as shown in Figure 2.4, CMS is
 1256 composed of several detection systems distributed in a cylindrical structure; in total,
 1257 CMS weights about 12500 tons in a very compact 21.6 m long and 14.6 m diameter
 1258 cylinder. It was built in 15 separate sections at the ground level and lowered to the
 1259 cavern individually to be assembled. A complete and detailed description of the CMS
 1260 detector and its components is given in Reference [74] on which this section is based.
 1261 Figure 2.9 shows the layout of the CMS detector. The detection system is composed
 1262 of (from the innermost to the outermost)

- 1263 • Pixel detector.
- 1264 • Silicon strip tracker.
- 1265 • Preshower detector.
- 1266 • Electromagnetic calorimeter.

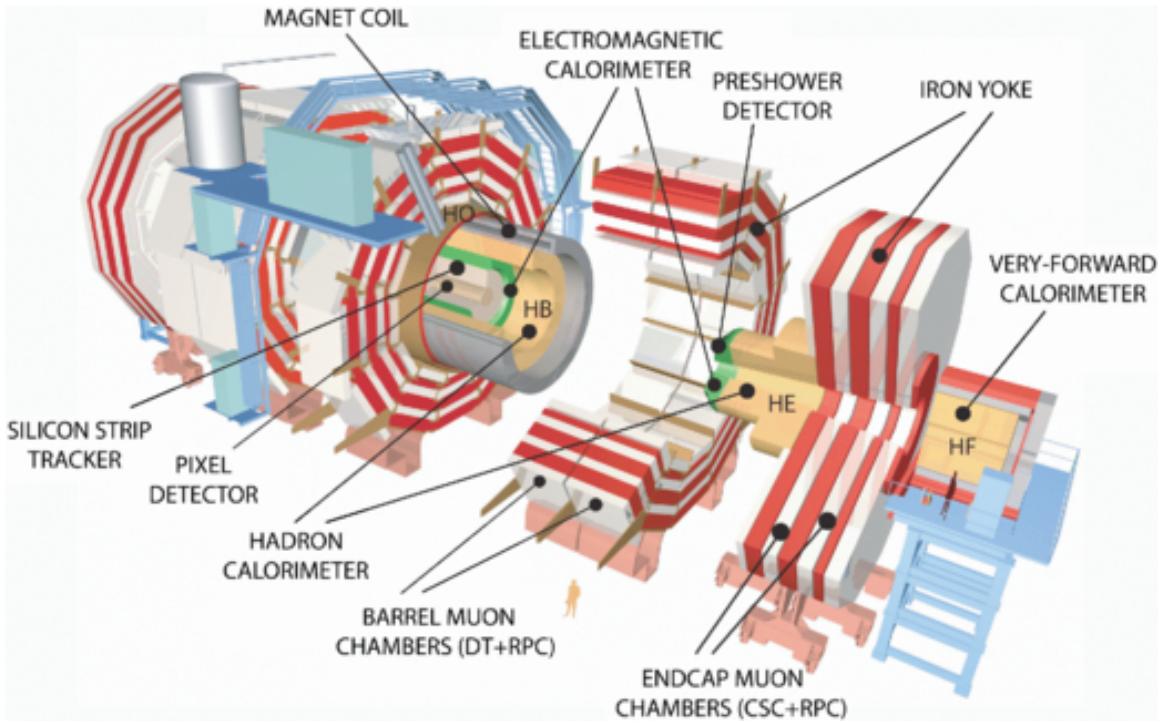


Figure 2.9: Layout of the CMS detector. The several subdetectors are indicated. The central region of the detector is referred as the barrel section while the endcaps are referred as the forward sections. [75].

1267 • Hadronic calorimeter.

1268 • Muon chambers (barrel and endcap)

1269 The central region of the detector is commonly referred as the barrel section while
1270 the endcaps are referred as the forward sections of the detector; thus, each subdetector
1271 is composed of a barrel section and a forward section.

1272 When a pp collision happens inside the CMS detector, many different particles are
1273 produced, but only some of them live long enough to be detected; they are electrons,
1274 photons, pions, kaons, protons, neutrons and muons; neutrinos are not detected by
1275 the CMS detector. Thus, the CMS detector was designed to detect those particles and
1276 measure their properties. Figure 2.10 shows a transverse slice of the CMS detector.
1277 The silicon tracker (pixel detector + strip tracker) is capable to register the track of

the charged particles traversing it, while calorimeters (electromagnetic and hadronic) measure the energy of the particles that are absorbed by their materials. Considering the detectable particles, mentioned above, emerging from the IP, a basic description of the detection process is as follows.

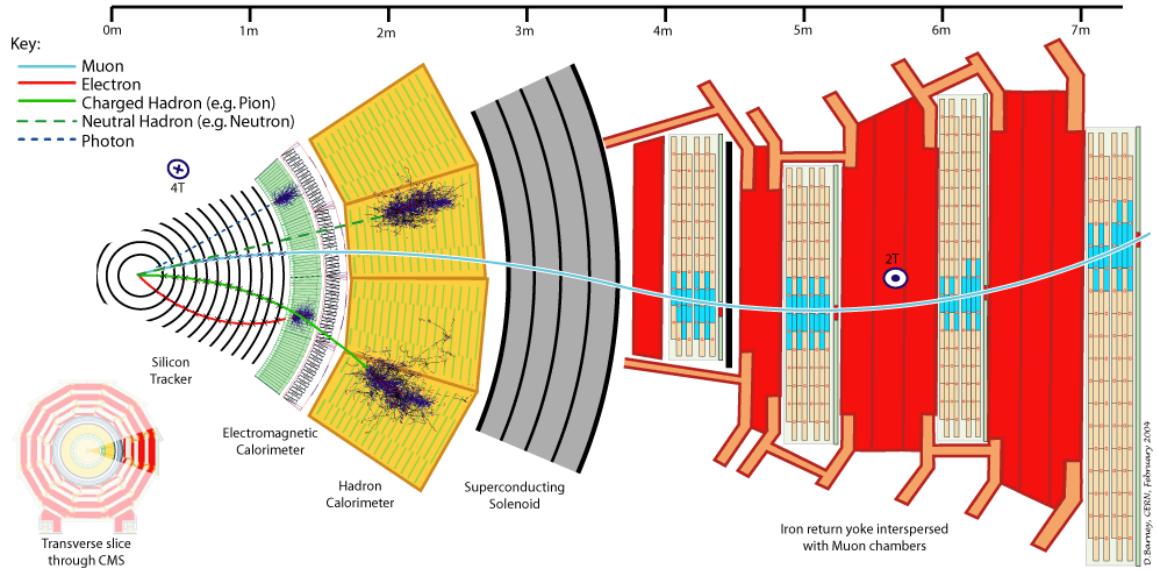


Figure 2.10: CMS detector transverse slice [76].

A muon emerging from the IP, will create a track on the silicon tracker and on the muon chambers. The design of the CMS detector is driven by the requirements on the identification, momentum resolution and unambiguous charge determination of the muons; therefore, a large bending power is provided by the solenoid magnet made of superconducting cable capable of generating a 3.8 T magnetic field. The muon track is bent twice since the magnetic field inside the solenoid is directed along the z -direction but outside its direction is reversed. Muons interact very weakly with the calorimeters, therefore, it is not absorbed but escape away from the detector.

An electron emerging from the IP will create a track along the tracker which will be bent due to the presence of the magnetic field, later, it will be absorbed in the electromagnetic calorimeter where its energy is measured.

1293 A photon will not leave a track because it is neutral, but it will be absorbed in
 1294 the electromagnetic calorimeter.

1295 A neutral hadron, like the neutron, will not leave a track either but it will lose a
 1296 small amount of its energy during its passage through the electromagnetic calorimeter
 1297 and then it will be absorbed in the hadron calorimeter depositing the rest of its energy.

1298 A charged hadron, like the proton or π^\pm , will leave a curved track on the silicon
 1299 tracker, some of its energy in the electromagnetic calorimeter and finally will be
 1300 absorbed in the hadronic calorimeter.

1301 A more detailed description of each detection system will be presented in the
 1302 following sections.

1303 2.3.1 CMS coordinate system

1304 The coordinate system used by CMS is centered on the geometrical center of the
 1305 detector which is the nominal IP as shown in Figure 2.11¹. The z -axis is parallel
 1306 to the beam direction, while the Y -axis pointing vertically upward, and the X -axis
 1307 pointing radially inward toward the center of the LHC.

1308 In addition to the common cartesian and cylindrical coordinate systems, two co-
 1309 ordinates are of particular utility in particle physics: rapidity (y) and pseudorapidity
 1310 (η), defined in connection to the polar angle θ , energy and longitudinal momentum
 1311 component (momentum along the z -axis) according to

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z} \quad \eta = -\ln \left(\tan \frac{\theta}{2} \right) \quad (2.6)$$

1312 Rapidity is related to the angle between the XY -plane and the direction in which
 1313 the products of a collision are emitted; it has the nice property that the difference

¹ Not all the pp interaction occur at the nominal IP because of the bunch lenght, therefore, each pp collision has its own IP location

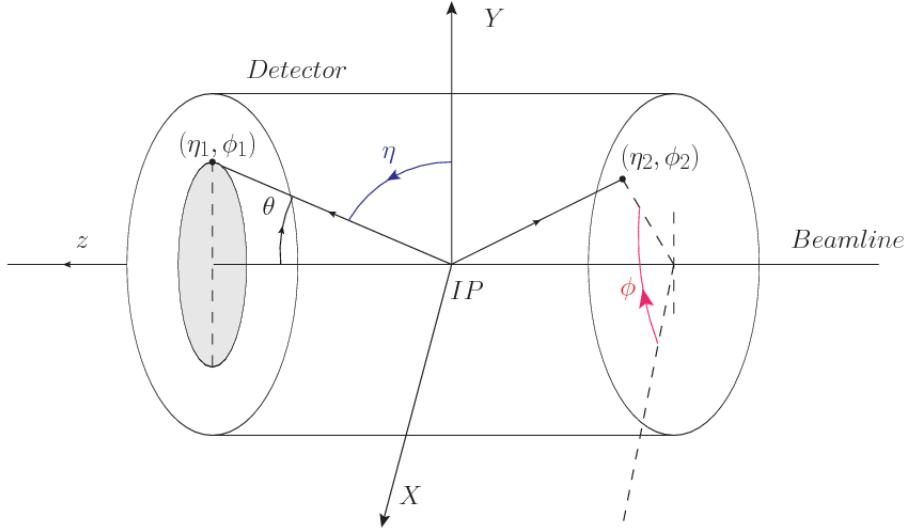


Figure 2.11: CMS detector coordinate system.

1314 between the rapidities of two particles is invariant with respect to Lorentz boosts
 1315 along the z -axis, hence, data analysis becomes more simple when based on rapid-
 1316 ity; however, it is not simple to measure the rapidity of highly relativistic particles,
 1317 as those produced after pp collisions. Under the highly relativistic motion approxi-
 1318 mation, y can be rewritten in terms of the polar angle, concluding that rapidity is
 1319 approximately equal to the pseudorapidity defined above, i.e., $y \approx \eta$. Note that η
 1320 is easier to measure than y given the direct relationship between the former and the
 1321 polar angle.

1322 The angular distance between two objects in the detector (ΔR) is commonly used
 1323 to judge the isolation of those object; it is defined in terms of their coordinates (η_1, ϕ_1) ,
 1324 (η_2, ϕ_2) as

$$\Delta R = \sqrt{(\Delta\eta)^2 - (\Delta\phi)^2} \quad (2.7)$$

1325 2.3.2 Tracking system

1326 The CMS tracking system is designed to provide a precise measurement of the trajectories (*track*) followed by the charged particles created after the pp collisions; also, the
 1327 precise reconstruction of the primary and secondary origins of the tracks (*vertices*) is
 1328 expected in an environment where, each 25 ns, the bunch crossing produces about 20
 1329 inelastic collisions and about 1000 particles.
 1330

1331 Physics requirements guiding the tracking system performance include the precise
 1332 characterization of events involving gauge bosons, W and Z, and their leptonic
 1333 decays for which an efficient isolated lepton and photon reconstruction is of capital
 1334 importance, given that isolation is required to suppress background events to a level
 1335 that allows observations of interesting processes like Higgs boson decays or beyond
 1336 SM events.

1337 The ability to identify and reconstruct b -jets and B-hadrons within these jets is also
 1338 a fundamental requirement, achieved through the ability to reconstruct accurately
 1339 displaced vertices, given that b -jets are part of the signature of top quark physics, like
 1340 the one treated in this thesis.

1341 An schematic view of the CMS tracking system is shown in Figure 2.12

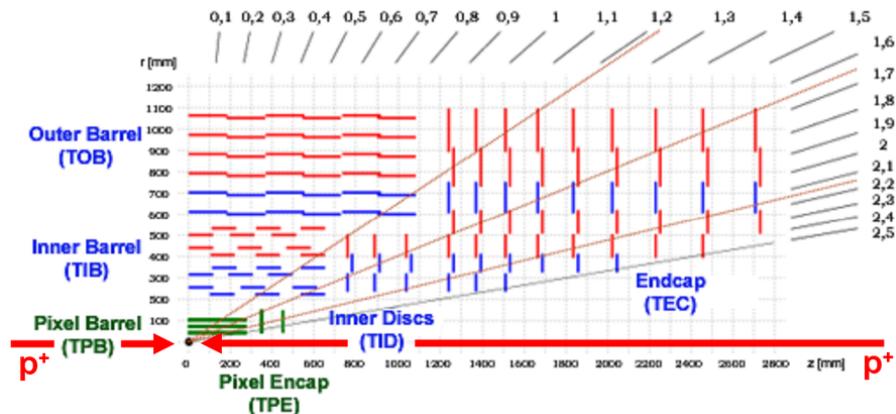


Figure 2.12: CMS tracking system schematic view [78].

1342 In order to satisfy these performance requirements, the tracking system uses two
 1343 different detector subsystems arranged in concentric cylindrical volumes, the pixel
 1344 detector and the silicon strip tracker; the pixel detector is located in the high particle
 1345 density region ($r < 20\text{cm}$) while the silicon strip tracker is located in the medium and
 1346 lower particle density regions $20\text{cm} < r < 116\text{cm}$.

1347 **Pixel detector**

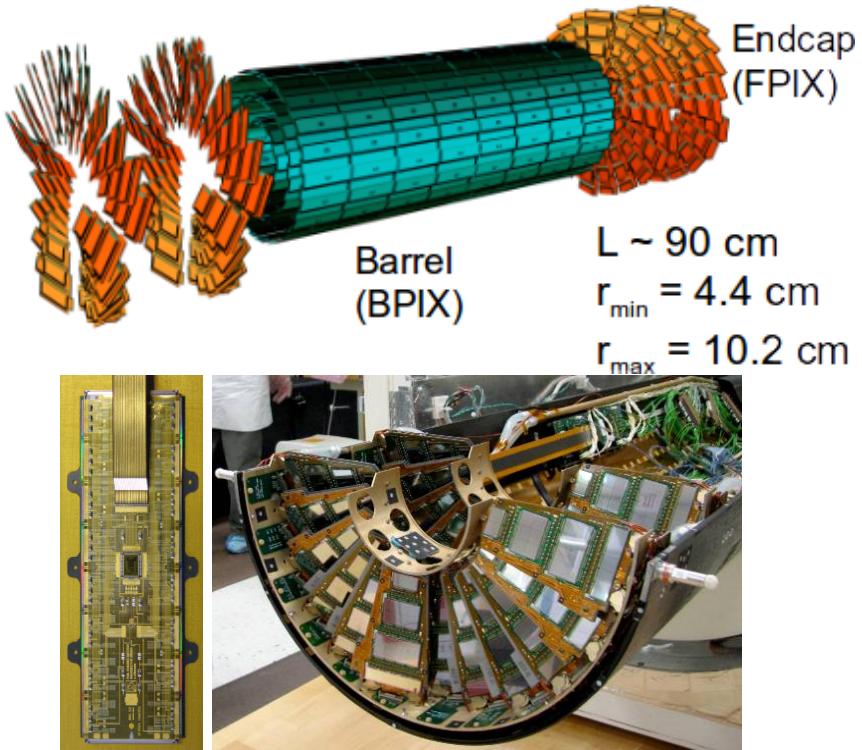


Figure 2.13: CMS pixel detector. Top: schematic view; Bottom: pictures of a barrel(BPIX) module(left) and forward modules(right) [74].

1348 The pixel detector was replaced during the 2016-2017 extended year-end technical
 1349 stop, due to the increasingly challenging operating conditions like the higher particle
 1350 flux and more radiation harsh environment, among others. The new one is responding
 1351 as expected, reinforcing its crucial role in the successful way to fulfill the new LHC

physics objectives after the discovery of the Higgs boson. Since the data sets used in this thesis were produced using the previous version of the pixel detector, it will be the subject of the description in this section. The last chapter of this thesis is dedicated to describe my contribution to the *Forward Pixel Phase 1 upgrade*.

The pixel detector was composed of 1440 silicon pixel detector modules organized in three-barrel layers in the central region (BPix) and two disks in the forward region (FPix) as shown in the top side of Figure 2.13; it was designed to record efficiently and with high precision, up to $20\mu\text{m}$ in the XY -plane and $20\mu\text{m}$ in the z -direction, the first three space-points (*hits*) nearest to the IP region in the range $|\eta| \leq 2.5$. The first barrel layer was located at a radius of 44 mm from the beamline, while the third layer was located at a radius of 102 mm, closer to the strip tracker inner barrel layer (see Section 2.3.3) in order to reduce the rate of fake tracks. The high granularity of the detector is represented in its about 66 Mpixels, each of size $100 \times 150\mu\text{m}^2$. The transverse momentum resolution of tracks can be measured with a resolution of 1-2% for muons of $p_T = 100$ GeV.

A charged particle passing through the pixel sensors produce ionization in them, giving energy for electrons to be removed from the silicon atoms, hence, creating electron-hole pairs. The collection of charges in the pixels generates an electrical signal that is read out by an electronic readout chip (ROC); each pixel has its own electronics which amplifies the signal. Combining the signal from the pixels activated by a traversing particle in the several layers of the detector allows one to reconstruct the particle's trajectory in 3D.

Commonly, the charge produced by traversing of a particle is collected by and shared among several pixels; by interpolating between pixels, the spatial resolution is improved. In the barrel section the charge sharing in the $r\phi$ -plane is due to the Lorentz effect. In the forward pixels the charge sharing is enhanced by arranging the

1378 blades in the turbine-like layout as shown in Figure 2.13 bottom left.

1379 2.3.3 Silicon strip tracker

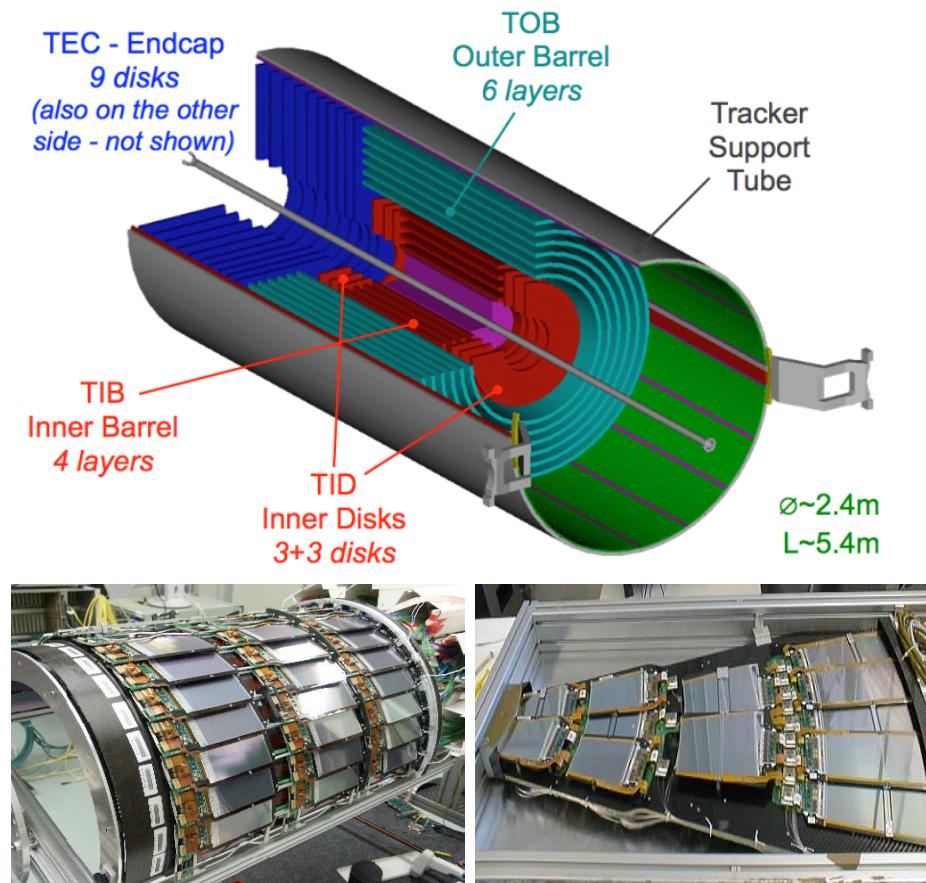


Figure 2.14: Top: CMS Silicon Strip Tracker (SST) schematic view. The SST is composed of the tracker inner barrel (TIB), the tracker inner disks (TID), the tracker outer barrel (TOB) and the tracker endcaps (TEC). Each part is made of silicon strip modules; the modules in blue represent two modules mounted back-to-back and rotated in the plane of the module by a stereo angle of 120 mrad in order to provide a 3-D reconstruction of the hit positions. Bottom: pictures of the TIB (left) and TEC (right) modules [80–82].

1380 The silicon strip tracker (SST) is the second stage in the CMS tracking system.

1381 The top side of Figure 2.14 shows a schematic of the SST. The inner tracker region is

1382 composed of the tracker inner barrel (TIB) and the tracker inner disks (TID) covering

1383 the region $r < 55$ cm and $|z| < 118$ cm. The TIB is composed of 4 layers while the TID

1384 is composed of 3 disks at each end. The silicon sensors in the inner tracker are 320
 1385 μm thick, providing a resolution of about 13-38 μm in the $r\phi$ position measurement.

1386 The modules indicated in blue in the schematic view of Figure 2.14 are two mod-
 1387 ules mounted back-to-back and rotated in the plane of the module by a *stereo* angle
 1388 of 100 mrad; the hits from these two modules, known as *stereo hits*, are combined to
 1389 provide a measurement of the second coordinate (z in the barrel and r on the disks)
 1390 allowing the reconstruction of hit positions in 3-D.

1391 The outer tracker region is composed of the tracker outer barrel (TOB) and the
 1392 tracker endcaps (TEC). The six layers of the TOB offer coverage in the region $r > 55$
 1393 cm and $|z| < 118$ cm, while the 9 disks of the TEC cover the region $124 < |z| < 282$
 1394 cm. The resolution offered by the outer tracker is about 13-38 μm in the $r\phi$ position
 1395 measurement. The inner four TEC disks use silicon sensors 320 μm thick; those in
 1396 the TOB and the outer three TEC disks use silicon sensors of 500 μm thickness. The
 1397 silicon strips run parallel to the z -axis and the distance between strips varies from 80
 1398 μm in the inner TIB layers to 183 μm in the inner TOB layers; in the endcaps the
 1399 wedge-shaped sensors with radial strips, whose pitch range between 81 μm at small
 1400 radii and 205 μm at large radii.

1401 The whole SST has 15148 silicon modules, 9.3 million silicon strips and cover a
 1402 total active area of about 198 m^2 .

1403 2.3.4 Electromagnetic calorimeter

1404 The CMS electromagnetic calorimeter (ECAL) is designed to measure the energy of
 1405 electrons and photons. It is composed of 75848 lead tungstate crystals which have a
 1406 short radiation length (0.89 cm) and fast response, since 80% of the light is emitted
 1407 within 25 ns; however, they are combined with Avalanche photodiodes (APDs) as

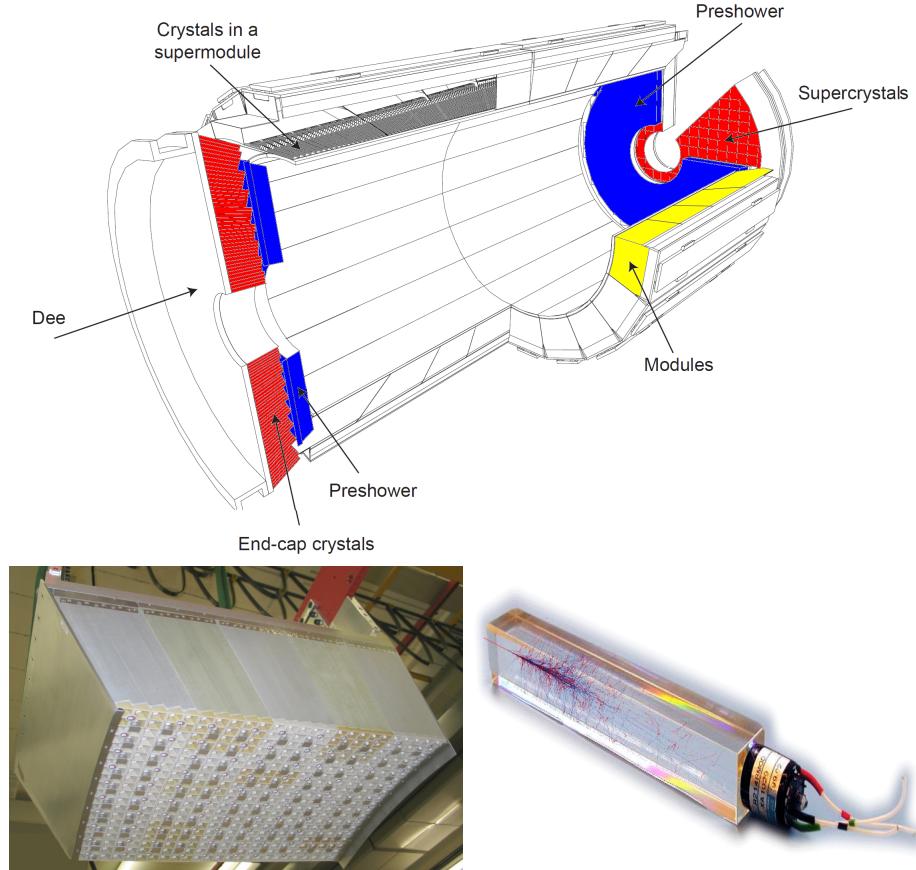


Figure 2.15: Top: CMS ECAL schematic view. Bottom: Module equipped with the crystals (left); ECAL crystal(right) with an artistic representation of an electromagnetic shower [74].

1408 photodetectors given that crystals themselves have a low light yield ($30\gamma/\text{MeV}$). A
 1409 schematic view of the ECAL is shown in Figure 2.15.

1410 Energy is measured when electrons and photons are absorbed by the crystals
 1411 which generates an electromagnetic *shower*, as seen in bottom right picture of the
 1412 Figure 2.15; the shower is seen as a *cluster* of energy which depending on the amount
 1413 of energy deposited can involve several crystals. The ECAL barrel (EB) covers the
 1414 region $|\eta| < 1.479$, using crystals of depth of 23 cm and $2.2 \times 2.2 \text{ cm}^2$ transverse
 1415 section; the ECAL endcap (EE) covers the region $1.479 < |\eta| < 3.0$ using crystals of
 1416 depth 22 cm and transverse section of $2.86 \times 2.86 \text{ cm}^2$; the photodetectors used are

vacuum phototriodes (VPTs). Each EE is divided in two structures called *Dees*.

The preshower detector (ES) is installed in front of the EE and covers the region $1.653 < |\eta| < 2.6$. The ES provides a precise measurement of the position of electromagnetic showers, which allows to distinguish electrons and photon signals from π^0 decay signals. The ES is composed of a layer of lead radiators followed by a layer of silicon strip sensors. The lead radiators initiate electromagnetic showers when reached by photons and electrons, then, the strip sensors measure the deposited energy and the transverse shower profiles. The full ES thickness is 20 cm.

2.3.5 Hadronic calorimeter

Hadrons are not absorbed by the ECAL² but by the hadron calorimeter (HCAL), which is made of a combination of alternating brass absorber layers and silicon photomultiplier(SiPM) layers; therefore, particles passing through the scintillator material produce showers, as in the ECAL, as a result of the inelastic scattering of the hadrons with the detector material. Since the particles are not absorbed in the scintillator, their energy is sampled; therefore the total energy is not measured but estimated from the energy clusters, which reduces the resolution of the detector. Brass was chosen as the absorber material due to its short interaction length ($\lambda_I = 16.42\text{cm}$) and its non-magnetivity. Figure 2.16 shows a schematic view of the CMS HCAL.

The HCAL is divided into four sections; the Hadron Barrel (HB), the Hadron Outer (HO), the Hadron Endcap (HE) and the Hadron Forward (HF) sections. The HB covers the region $0 < |\eta| < 1.4$, while the HE covers the region $1.3 < |\eta| < 3.0$. The HF, made of quartz fiber scintillator and steel as absorption material, covers the forward region $3.0 < |\eta| < 5.2$. Both the HB and HF are located inside the solenoid. The HO is placed outside the magnet as an additional layer of scintillators with the

² Most hadrons are not absorbed, but few low-energy ones might be.

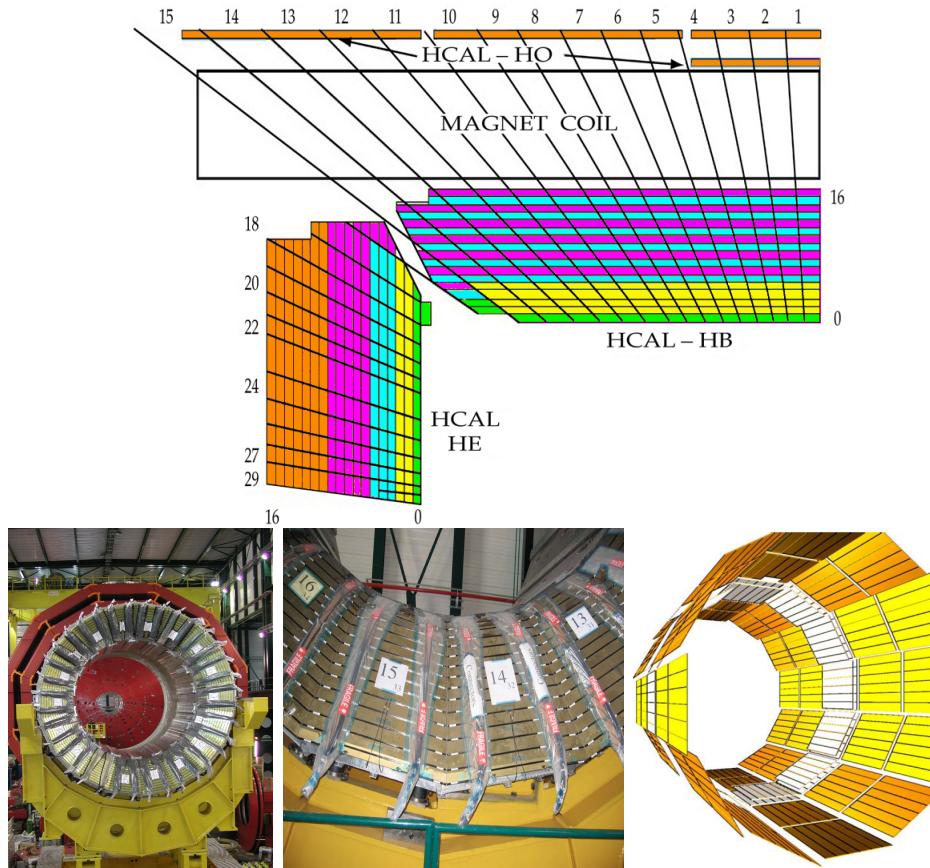


Figure 2.16: Top: CMS HCAL schematic view, the colors indicate the layers that are grouped into the same readout channels. Bottom: picture of a section of the HB; the absorber material is the golden region and scintillators are placed in between the absorber material (left and center). Schematic view of the HO (right). [83,84]

1441 purpose of measure the energy tails of particles passing through the HB and the
 1442 magnet (see Figure 2.16 top and bottom right).

1443 **2.3.6 Superconducting solenoid magnet**

1444 The superconducting magnet installed in the CMS detector is designed to provide
 1445 an intense and highly uniform magnetic field in the central part of the detector.
 1446 In fact, the tracking system takes advantage of the bending power of the magnetic
 1447 field to measure with precision the momentum of the particles that traverse it; the

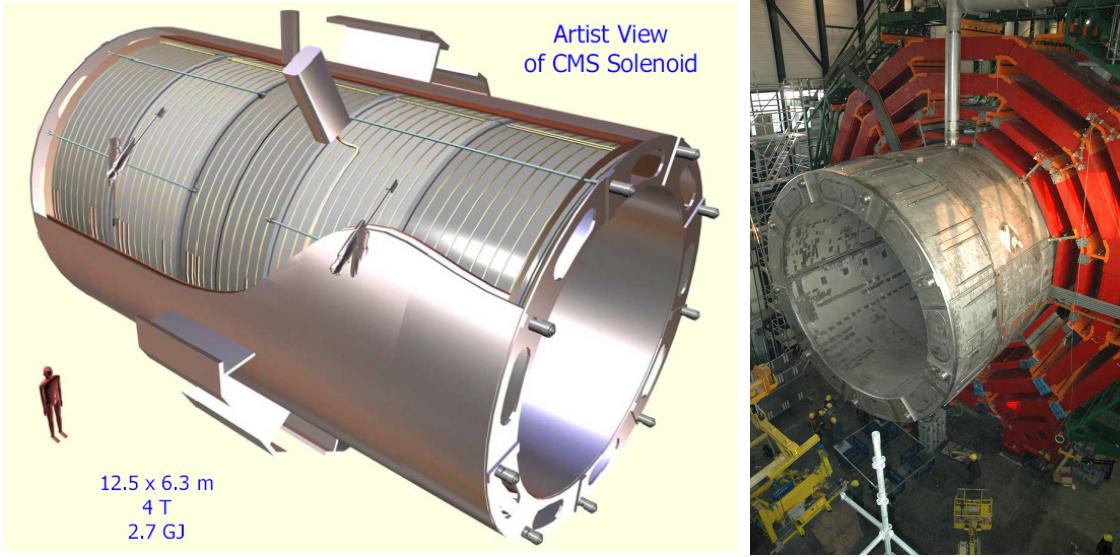


Figure 2.17: Artistic representation of the CMS solenoid magnet(left). The magnet is supported on an iron yoke (right) which also serves as the house of the muon detector and as mechanical support for the whole CMS detector [77].

1448 unambiguous determination of the sign for high momentum muons was a driving
 1449 principle during the design of the magnet. The magnet has a diameter of 6.3 m, a
 1450 length of 12.5 m and a cold mass of 220 t; the generated magnetic field reaches a
 1451 strength of 3.8T. Since it is made of Ni-Tb superconducting cable it has to operate at
 1452 a temperature of 4.7 K by using a helium cryogenic system; the current circulating in
 1453 the cables reaches 18800 A under normal running conditions. The left side of Figure
 1454 2.17 shows an artistic view of the CMS magnet, while the right side shows a transverse
 1455 view of the cold mass where the winding structure is visible.

1456 The yoke (see Figure 2.17), composed of 5 barrel wheels and 6 endcap disks made
 1457 of iron, serves not only as the media for magnetic flux return but also provides housing
 1458 for the muon detector system and structural stability to the full detector.

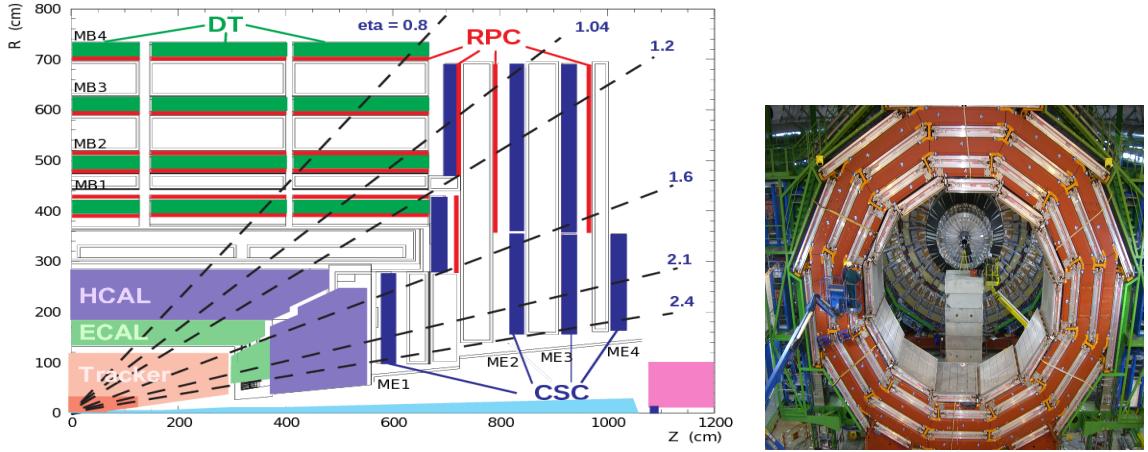


Figure 2.18: Left: CMS muon system schematic view; Right: one of the yoke rings with the muon DTs and RPCs installed; in the back it is possible to see the muon endcap [85].

1459 2.3.7 Muon system

1460 Muons are the only charged particles able to pass through all the CMS detector due
 1461 to their low ionization energy loss; thus, muons can be separated easily from the
 1462 high amount of particles produced in a pp collision. Also, muons are expected to be
 1463 produced in the decay of several new particles; therefore, good detection of muons
 1464 was one of the leading principles when designing the CMS detector.

1465 The CMS muon detection system (muon spectrometer) is embedded in the return
 1466 yoke as seen in Figure 2.18. It is composed of three different detector types, the drift
 1467 tube chambers (DT), cathode strip chambers (CSC), and resistive plate chambers
 1468 (RPC); DT are located in the central region $\eta < 1.2$ arranged in four layers of drift
 1469 chambers filled with an Ar/CO₂ gas mixture.

1470 The muon endcaps are made of CSCs covering the region $\eta < 2.4$ and filled with
 1471 a mixture of Ar/CO₂/CF₄. The reason behind using a different detector type lies on
 1472 the different conditions in the forward region like the higher muon rate and higher
 1473 residual magnetic field compared to the central region.

1474 The third type of detector used in the muon system is a set of four disks of RPCs

1475 working in avalanche mode. The RPCs provide good spatial and time resolutions. The
 1476 track of high- p_T muon candidates is built combining information from the tracking
 1477 system and the signal from up to six RPCs and four DT chambers.

1478 The muon tracks are reconstructed from the hits in the several layers of the muon
 1479 system.

1480 2.3.8 CMS trigger system

1481 CMS expects pp collisions every 25 ns, i.e., an interaction rate of 40 MHz for which
 1482 it is not possible to store the recorded data in full. In order to handle this high event
 1483 rate data, an online event selection, known as triggering, is performed; triggering
 1484 reduces the event rate to 100 Hz for storage and further offline analysis.

1485 The trigger system starts with a reduction of the event rate to 100 kHz in the
 1486 so-called *the level 1 trigger* (L1). L1 is based on dedicated programmable hardware
 1487 like Field Programmable Gate Arrays (FPGAs) and Application Specific Integrated
 1488 Circuits (ASICs), partly located in the detector itself; another portion is located in
 1489 the CMS underground cavern. Hit pattern information from the muon chambers
 1490 and the energy deposits in the calorimeter are used to decide if an event is accepted
 1491 or rejected, according to selection requirements previously defined, which reflect the
 1492 interesting physics processes. Figure 2.19 shows the L1 trigger architecture.

1493 The second stage in the trigger system is called *the high-level trigger* (HLT); events
 1494 accepted by L1 are passed to HLT in order to make an initial reconstruction of them.
 1495 HLT is software based and runs on a dedicated server farm, using selection algorithms
 1496 and high-level object definitions; the event rate at HLT is reduced to 100 Hz. The
 1497 first HLT stage takes information from the muon detectors and the calorimeters to
 1498 make the initial object reconstruction; in the next HLT stage, information from the

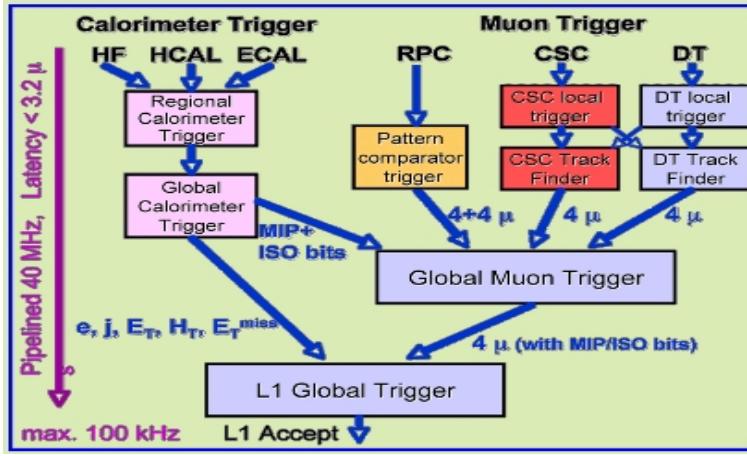


Figure 2.19: CMS Level-1 trigger architecture [86].

pixel and strip detectors is used to do first fast tracking and then full tracking online.
 This initial object reconstruction is used in further steps of the trigger system.

Events and preliminary reconstructed physics objects from HLT are sent to be fully reconstructed at the CERN computing center known also as Tier-0 facility. Again, the pixel detector information provides high-quality seeds for the track reconstruction algorithm offline, primary vertex reconstruction, electron and photon identification, muon reconstruction, τ identification, and b-tagging. After full reconstruction, data sets are made available for offline analyses.

2.3.9 CMS computing

Data coming from the experiment have to be stored and made available for further analysis; in order to cope with all the tasks implied in the offline data processing, like transfer, simulation, reconstruction and reprocessing, among others, a large computing power is required. The CMS computing system is based on the distributed architecture concept, where users of the system and physical computer centers are distributed worldwide and interconnected by high-speed networks.

The worldwide LHC computing grid (WLCG) is the mechanism used to provide

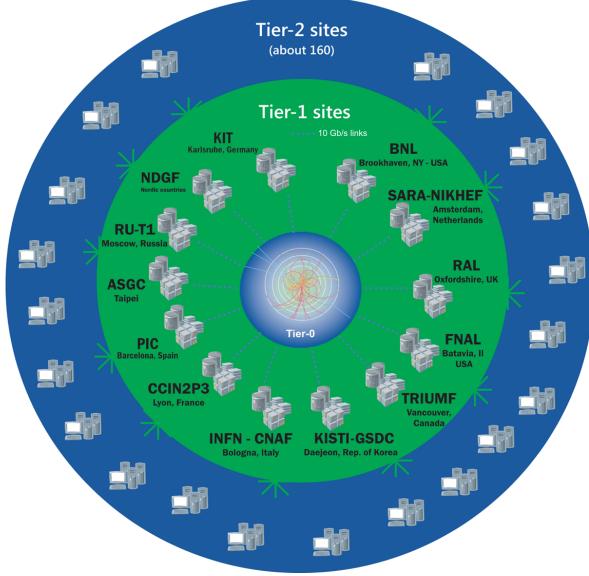


Figure 2.20: WLCG structure. The primary computer centers (Tier-0) are located at CERN (data center) and at the Wigner datacenter in Budapest. Tier-1 is composed of 13 centers and Tier-2 is composed of about 160 centers. [87].

1515 that distributed environment. WLCG is a tiered structure connecting computing
 1516 centers around the world, which provides the necessary storage and computing facil-
 1517 ities. The primary computing centers of the WLCG are located at the CERN and
 1518 the Wigner datacenter in Budapest and are known as Tier-0 as shown in Figure 2.20.
 1519 The main responsibilities for each tier level are [87]

- 1520 • **Tier-0:** initial reconstruction of recorded events and storage of the resulting
 1521 datasets, the distribution of raw data to the Tier-1 centers.
- 1522 • **Tier-1:** provide storage capacity, support for the Grid, safe-keeping of a pro-
 1523 portional share of raw and reconstructed data, large-scale reprocessing and safe-
 1524 keeping of corresponding output, generation of simulated events, distribution
 1525 of data to Tier 2s, safe-keeping of a share of simulated data produced at these
 1526 Tier 2s.
- 1527 • **Tier-2:** store sufficient data and provide adequate computing power for spe-

1528 cific analysis tasks and proportional share of simulated event production and
1529 reconstruction.

1530 Aside from the general computing strategy to manage the huge amount of data
1531 produced by experiments, CMS uses a software framework to perform a variety of
1532 processing, selection and analysis tasks. The central concept of the CMS data model
1533 referred to as *event data model* (EDM) is the *Event*; therefore, an event is the unit
1534 that contains the information from a single bunch crossing, any data derived from
1535 that information like the reconstructed objects, and the details of the derivation.

1536 Events are passed as the input to the *physics modules* that obtain information
1537 from them and create new information; for instance, *event data producers* add new
1538 data into the events, *analyzers* produce an information summary from an event set,
1539 *filters* perform selection and triggering.

1540 CMS uses several event formats with different levels of detail and precision

1541 • **Raw format:** events in this format contain the full recorded information from
1542 the detector as well as trigger decision and other metadata. An extended version
1543 of raw data is used to store information from the CMS Monte Carlo simulation
1544 tools (see Chapter 3). Raw data are stored permanently, occupying about
1545 2MB/event

1546 • **RECO format:** events in this format correspond to raw data that have been
1547 submitted to reconstruction algorithms like primary and secondary vertex re-
1548 construction, particle ID, and track finding. RECO events contain physics ob-
1549 jects and all the information used to reconstruct them; average size is about 0.5
1550 MB/event.

- 1551 • **AOD format:** Analysis Object Data (AOD) is the data format used in the
 1552 physics analyses given that it contains the parameters describing the high-level
 1553 physics objects in addition to enough information to allow a kinematic refitting if
 1554 needed. AOD events are filtered versions of the RECO events to which skimming
 1555 or other filtering have been applied, hence AOD events are subsets of RECO
 1556 events. Requires about 100 kB/event.
- 1557 • **Non-event data** are data needed to interpret and reconstruct events. Some
 1558 of the non-event data used by CMS contains information about the detector
 1559 contraction and condition data like calibrations, alignment, and detector status.

1560 Figure 2.21 shows the data flow scheme between CMS detector and tiers.

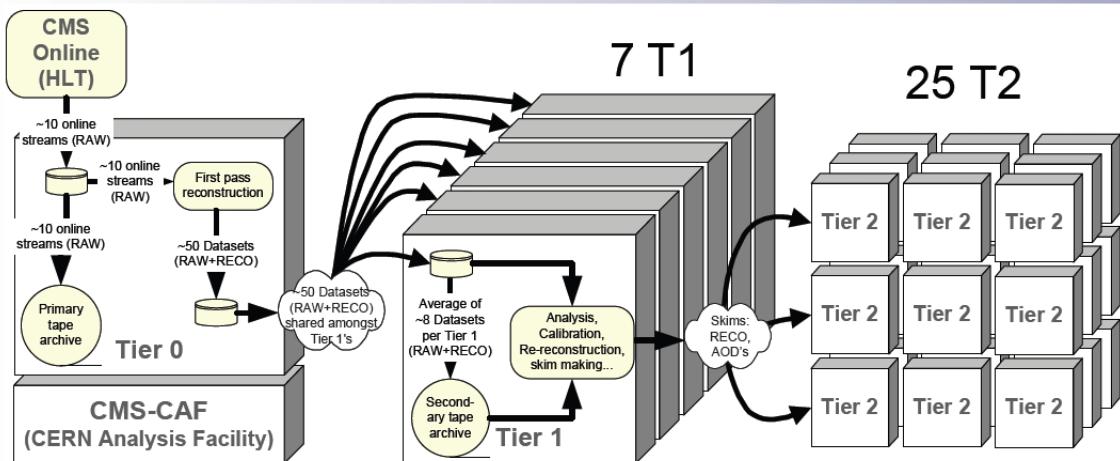


Figure 2.21: Data flow from CMS detector through tiers.

1561 The whole collection of software built as a framework is referred to as *CMSSW*. This
 1562 framework provides the services needed by the simulation, calibration and alignment,
 1563 and reconstruction modules that process event data, so that physicists can perform
 1564 analysis. The CMSSW event processing model is composed of one executable, called
 1565 cmsRun, and several plug-in modules which contains all the tools (calibration, recon-

1566 struction algorithms) needed to process an event. The same executable is used for
1567 both detector data and Monte Carlo simulations [88].

1568 **Chapter 3**

1569 **Event generation, simulation and
1570 reconstruction**

1571 The process of analyzing data recorded by the CMS experiment involves several stages
1572 where the data are processed in order to interpret the information provided by all
1573 the detection systems; in those stages, the particles produced after the pp collision
1574 are identified by reconstructing their trajectories and measuring their features. In
1575 addition, the SM provides a set of predictions that have to be compared with the
1576 experimental results; however, in most of the cases, theoretical predictions are not
1577 directly comparable to experimental results due to the diverse source of uncertainties
1578 introduced by the experimental setup and theoretical approximations, among others.

1579 The strategy to face these conditions consists in using statistical methods imple-
1580 mented in computational algorithms to produce numerical results that can be con-
1581 trasted with the experimental results. These computational algorithms are commonly
1582 known as Monte Carlo (MC) methods and, in the case of particle physics, they are
1583 designed to apply the SM rules and produce predictions about the physical observ-
1584 ables measured in the experiments. Since particle physics is governed by quantum

mechanics principles, predictions are not allowed from single events; therefore, a high number of events are *generated* and predictions are produced in the form of statistical distributions for the observables. Effects of the detector presence are included in the predictions by introducing simulations of the detector itself.

This chapter presents a description of the event generation strategy and the tools used to perform the detector simulation and physics objects reconstruction. A comprehensive review of event generators for LHC physics can be found in Reference [89] on which this chapter is based.

3.1 Event generation

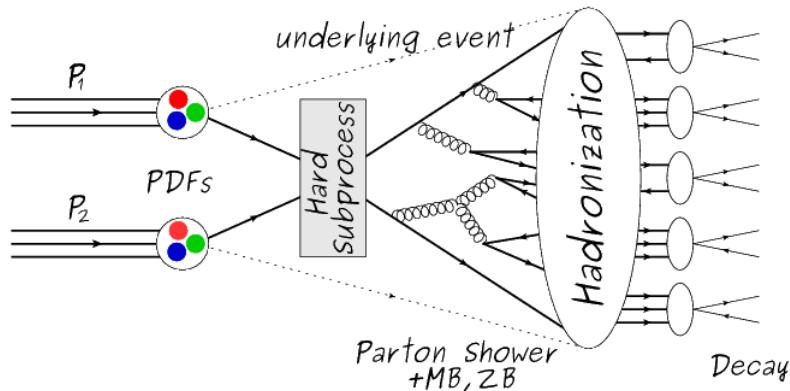


Figure 3.1: Event generation process. The actual interaction is generated in the hard subprocess. The parton shower describes the evolution of the partons from the hard subprocess. Modified from Reference [90].

The event generation is intended to create events that mimic the behavior of actual events produced in collisions; they obey a sequence of steps from the particles collision hard process to the decay process into the final state. Figure 3.1 shows a schematic view of the event generation process; the fact that the full process can be treated as several independent steps is motivated by the QCD factorization theorem.

1599 Generation starts by taking into account the PDFs of the incoming particles.
 1600 Event generators offer the option to chose from several PDF sets depending on the
 1601 particular process under simulation¹; in the following, pp collisions will be consid-
 1602 ered. The *hard subprocess* describes the actual interaction between partons from the
 1603 incoming protons; it is represented by the matrix element connecting the initial and
 1604 final states of the interaction. Normally, the matrix element can be written as a
 1605 sum over Feynman diagrams and consider interferences between terms in the sum-
 1606 mation. During the generation of the hard subprocess, the production cross section
 1607 is calculated.

1608 The order to which the cross section is calculated depends on the order of the Feyn-
 1609 man diagrams involved in the calculation; therefore, radiative corrections are included
 1610 by considering a higher order Feynman diagrams where QCD radiation dominates.
 1611 Currently, cross sections calculated to LO do not offer a satisfactory description of the
 1612 processes, i.e., the results are only reliable for the shape of distributions; therefore,
 1613 NLO calculations have to be performed with the implication that the computing time
 1614 needed is highly increased.

1615 The final parton content of the hard subprocess is subjected to the *parton shower*
 1616 which generates the gluon radiation. Parton shower evolves the partons, i.e., glouns
 1617 split into quark-antiquark pairs and quarks with enough energy radiate gluons giv-
 1618 ing rise to further parton multiplication, following the DGLAP (Dokshitzer-Gribov-
 1619 Lipatov-Altarelli-Parisi) equations. Showering continues until the energy scale is low
 1620 enough to reach the non-perturbative limit.

1621 In the simulation of LHC processes that involve b quarks, like the single top quark
 1622 or Higgs associated production, it is needed to consider that the b quark is heavier
 1623 than the proton; hence, the QCD interaction description is made in two different

¹ Tool in Reference [91] allows to plot different PDF sets under customizable conditions.

1624 schemes [95]

- 1625 • four-flavor (4F) scheme. b quarks appear only in the final state because they
 1626 are heavier than the proton and therefore they can be produced only from the
 1627 splitting of a gluon into pairs or singly in association with a t quark in high
 1628 energy-scale interactions; furthermore, during the simulation, the b -PDFs are set
 1629 to zero. Calculations in this scheme are more complicated due to the presence
 1630 of the second b quark but the full kinematics is considered already at LO and
 1631 therefore the accuracy of the description is better.

- 1632 • five-flavor (5F) scheme. b quarks are considered massless, therefore they can
 1633 appear in both initial and final states since they can now be part of the proton;
 1634 thus, during the simulation b -PDFs are not set to zero. In this scheme, calcu-
 1635 lations are simpler than in the 4F scheme and possible logarithmic divergences
 1636 are absorbed by the PDFs through the DGLAP evolution.

1637 In this thesis, the tHq events are generated using the 4F scheme in order to reduce
 1638 uncertainties, while the tHW events are generated using the 5F scheme to eliminate
 1639 LO interference with $t\bar{t}H$ process [48].

1640 Partons involved in the pp collision are the focus of the simulation, however, the
 1641 rest of the partons inside the incoming protons are also affected because the remnants
 1642 are colored objects; also, multiple parton interactions can occur. The hadronization
 1643 of the remnants and multiple parton interactions are known as *underlying event* and
 1644 it has to be included in the simulation. In addition, multiple pp collisions in the same
 1645 bunch crossing (pile-up mentioned in 2.2) occurs, actually in two forms

- 1646 • *in-time PU* which refers to multiple pp collision in the bunch crossing but that
 1647 are not considered as primary vertices.

1648 • *Out-of-time PU* which refers to overlapping pp collisions from consecutive bunch
 1649 crossings; this can occur due to the time-delays in the detection systems where
 1650 information from one bunch crossing is assigned to the next or previous one.

1651 While the underlying event effects are included in generation using generator-
 1652 specific tools, PU effects are added to the generation by overlaying Minimum-bias (MB)
 1653 and Zero-bias (ZB) events to the generated events. MB events are inelastic events
 1654 selected by using a loose trigger with as little bias as possible, therefore accepting a
 1655 large fraction of the overall inelastic event; ZB events correspond to random events
 1656 recorded by the detector when collisions are likely. MB models in-time PU and ZB
 1657 models out-of-time PU.

1658 The next step in the generation process is called *hadronization*. Since particles
 1659 with a net color charge are not allowed to exits isolated, they have to recombine
 1660 to form bound states. This is precisely the process by which the partons resulting
 1661 from the parton shower arrange themselves as color singlets to form hadrons. At
 1662 this step, the energy-scale is low and the strong coupling constant is large, therefore
 1663 hadronization process is non-perturbative and the evolution of the partons is described
 1664 using phenomenological models. Most of the baryons and mesons produced in the
 1665 hadronization are unstable and hence they will decay in the detector.

1666 The last step in the generation process corresponds to the decay of the unstable
 1667 particles generated during hadronization; it is also simulated in the hadronization
 1668 step, based on the known branching ratios.

1669 **3.2 Monte Carlo Event Generators.**

1670 The event generation described in the previous section has been implemented in
 1671 several software packages for which a brief description is given.

- 1672 • **PYTHIA 8.** It is a program designed to perform the generation of high energy
 1673 physics events which describes the collisions between particles such as electrons
 1674 and protons. Several theories and models are implemented in it, in order to
 1675 describe physical aspects like hard and soft interaction, parton distributions,
 1676 initial and final-state parton showers, multiple parton interactions, beam rem-
 1677 nants, hadronization² and particle decay. Thanks to extensive testing, several
 1678 optimized parametrizations, known as *tunings*, have been defined in order to
 1679 improve the description of actual collisions to a high degree of precision; for
 1680 analysis at $\sqrt{s} = 13$ TeV, the underline event CUETP8M1 tune is employed [97].
 1681 The calculation of the matrix element is performed at LO which is not enough
 1682 for the current required level of precision; therefore, pythia is often used for
 1683 parton shower, hadronization and decays, while other event generators are used
 1684 to generate the matrix element at NLO.
- 1685 • **MadGraph5_aMC@NLO.** MadGraph is a matrix element generator which
 1686 calculates the amplitudes for all contributing Feynman diagrams of a given
 1687 process but does not provide a parton shower while MC@NLO incorporates
 1688 NLO QCD matrix elements consistently into a parton shower framework; thus,
 1689 MadGraph5_aMC@NLO, as a merger of the two event generators MadGraph5
 1690 and aMC@NLO, is an event generator capable to calculate tree-level and NLO
 1691 cross sections and perform the matching of those with the parton shower. It is
 1692 one of the most frequently used matrix element generators; however, it has the
 1693 particular feature of the presence of negative event weights which reduce the
 1694 number of events used to reproduce the properties of the objects generated [98].
- 1695 • **POWHEG.** It is an NLO matrix element generator where the hardest emis-

² based in the Lund string model [96]

1696 sion of color charged particles is generated in such a way that the negative event
 1697 weights issue of MadGraph5_aMC@NLO is overcome; however, the method re-
 1698 quires an interface with p_T -ordered parton shower or a parton shower generator
 1699 where this highest emission can be vetoed in order to avoid double counting of
 1700 this highest-energetic emission. PYTHIA is a commonly matched to POWHEG
 1701 event generator [100].
 1702 Events resulting from the whole generation process are known as MC events.

1703 **3.3 CMS detector simulation.**

1704 After generation, MC events contain the physics of the collisions but they are not
 1705 ready to be compared to the events recorded by the experiment since these recorded
 1706 events correspond to the response of the detection systems to the interaction with
 1707 the particles traversing them. The simulation of the CMS detector has to be applied
 1708 on top of the event generation; it is simulated with a MC toolkit for the simulation
 1709 of particles passing through matter called Geant4 which is also able to simulate the
 1710 electronic signals that would be measured by all detectors inside CMS.

1711 The simulation takes the generated particles contained in the MC events as input,
 1712 makes them pass through the simulated geometry, and models physics processes that
 1713 particles experience during their passage through matter. The full set of results from
 1714 particle-matter interactions corresponds to the simulated hit which contains informa-
 1715 tion about the energy loss, momentum and position. Particles of the input event are
 1716 called *primary*, while the particles originating from GEANT4-modeled interactions of
 1717 a primary particle with matter are called a *secondary*. Simulated hits are the input
 1718 of subsequent modules that emulate the response of the detector readout system and

1719 triggers. The output from the emulated detection systems and triggers is known as
 1720 digitization [101, 102].

1721 The modeling of the CMS detector corresponds to the accurate modeling of the
 1722 interaction among particles, the detector material, and the magnetic field. This
 1723 simulation procedure includes the following standard steps

1724 • Modeling of the Interaction Region.

1725 • Modeling of the particle passage through the hierarchy of volumes that compose
 1726 CMS detector and of the accompanying physics processes.

1727 • Modeling of the effect of multiple interactions per beam crossing and/or the
 1728 effect of events overlay (Pile-Up simulation).

1729 • Modeling of the detector's electronics response, signal shape, noise, calibration
 1730 constants (digitization).

1731 In addition to the full simulation, i.e., a detailed detector simulation, a faster
 1732 simulation (FastSim) have been developed, that may be used where much larger
 1733 statistics are required. In FastSim, detector material effects are parametrized and
 1734 included in the hits; those hits are used as input of the same higher-level algorithms³
 1735 used to analyze the recorded events. In this way, comparisons between fast and full
 1736 simulations can be performed [104].

1737 After the full detector simulation, the output events can be directly compared
 1738 to events actually recorded in the CMS detector. The collection of MC events that
 1739 reproduces the expected physics for a given process is known as MC sample.

³ track fitting, calorimeter clustering, b tagging, electron identification, jet reconstruction and calibration, trigger algorithms which will be considered in the next sections

1740 **3.4 Event reconstruction.**

1741 The CMS experiment use the *particle-flow event reconstruction algorithm (PF)* to do
1742 the reconstruction of particles produced in pp collisions. Next sections will present
1743 a basic description of the *Elements* used by PF (tracker tracks, energy clusters, and
1744 muon tracks), based in the References [105, 106] where more detailed descriptions can
1745 be found.

1746 **3.4.1 Particle-Flow Algorithm.**

1747 Each of the several sub detection systems of the CMS detector is dedicated to identify
1748 an specific type of particles, i.e., photons and electrons are absorbed by the ECAL
1749 and their reconstruction is based on ECAL information; hadrons are reconstructed
1750 from clusters in the HCAL while muons are reconstructed from hits in the muon
1751 chambers. PF is designed to correlate signals from all the detector layers (tracks and
1752 energy clusters) in order to reconstruct and identify each final state particle and its
1753 properties as sketched in Figure 3.2.

1754 For instance, a charged hadron is identified by a geometrical connection, known
1755 as *link*, between one or more calorimeter clusters and a track in the tracker, provided
1756 there are no hits in the muon system; combining several measurements allows a better
1757 determination of the energy and charge sign of the charged hadron.

1758 **Charged-particle track reconstruction.**

1759 The strategy used by PF in order to reconstruct tracks is called *Iterative Tracking*
1760 which occurs in four steps

- 1761 • Seed generation where initial track candidates are found by looking for a combi-
1762 nation of hits in the pixel detector, strip tracker, and muon chambers. In total

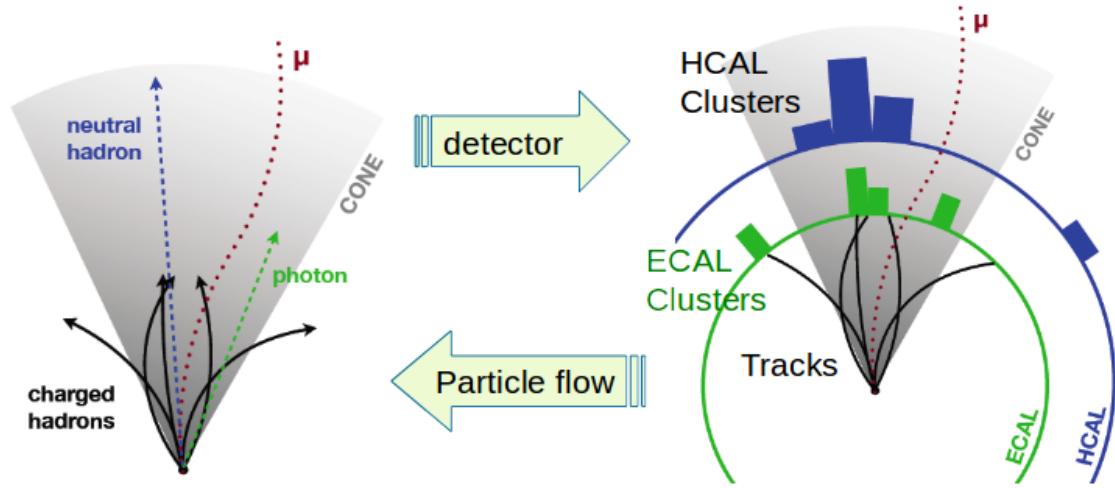


Figure 3.2: Particle flow algorithm. Information from the several CMS detection systems is provided as input to the algorithm which then combines it to identify and reconstruct all the particles in the final state and their properties. Reconstruction of simulated events is also performed by providing information from MC samples, detector and trigger simulation [107].

1763 ten iterations are performed, each one with a different seeding requirement.
 1764 Seeds are used to estimate the trajectory parameters and uncertainties at the
 1765 time of the full track reconstruction. Seeds are also considered track candidates.

- 1766 • Track finding using a tracking software known as Combinatorial Track Finder
 (CTF) [108]. The seed trajectories are extrapolated along the expected flight
 path of a charged particle, in agreement to the trajectory parameters obtained
 in the first step, in an attempt to find additional hits that can be assigned to
 the track candidates.
- 1771 • Track-fitting where the found tracks are passed as input to a module which
 provides the best estimate of the parameters of each trajectory.
- 1773 • Track selection where track candidates are submitted to a selection which dis-
 cards those that fail a set of defined quality criteria.

1775 Iterations differ in the seeding configuration and the final track selection as elab-

1776 orated in References [105, 106]. In the first iteration, high p_T tracks and tracks pro-
 1777 duced near to the interaction region are identified and those hits are masked thereby
 1778 reducing the combinatorial complexity. Next, iterations search for more complicated
 1779 tracks, like low p_T tracks and tracks from b hadron decays, which tend to be displaced
 1780 from the interaction region.

1781 **Vertex reconstruction.**

1782 During the track reconstruction, an extrapolation toward to the calorimeters is per-
 1783 formed in order to match energy deposits; that extrapolation is performed also toward
 1784 the beamline in order to find the origin of the track known as *vertex*. The vertex re-
 1785 construction is performed by selecting from the available reconstructed tracks, those
 1786 that are consistent with being originated in the interaction region where pp collisions
 1787 are produced. The selection involves a requirement on the number of tracker (pixel
 1788 and strip) hits and the goodness of the track fit.

1789 Selected tracks are clustered using a *deterministic annealing algorithm* (DA)⁴. A
 1790 set of candidate vertices and their associated tracks, resulting from the DA, are then
 1791 fitted with an *adaptive vertex fitter* (AVF) to produce the best estimate of the vertices
 1792 locations.

1793 The p_T of the tracks associated to a reconstructed vertex is added, squared and
 1794 used to organize the vertices; the vertex with the highest squared sum is designated
 1795 as the *primary vertex* (*PV*) while the rest are designated as PU vertices.

1796 **Calorimeter clustering.**

1797 After traversing the CMS tracker system, electrons, photons and hadrons deposit their
 1798 energy in the ECAL and HCAL cells. The PF clustering algorithm aims to provide

⁴ DA algorithm and AVF are described in detail in References [110, 111]

1799 a high detection efficiency even for low-energy particles and an efficient distinction
 1800 between close energy deposits. The clustering runs independently in the ECAL barrel
 1801 and endcaps, HCAL barrel and endcaps, and the two preshower layers, following two
 1802 steps

- 1803 • cells with an energy larger than a given seed threshold and larger than the energy
 1804 of the neighboring cells are identified as cluster seeds. The neighbor cells are
 1805 those that either share a side with the cluster seed candidate, or the eight closest
 1806 cells including cells that only share a corner with the seed candidate.
- 1807 • cells with at least a corner in common with a cell already in the cluster seed
 1808 and with an energy above a cell threshold are grouped into topological clusters.

1809 Clusters formed in this way are known as *particle-flow clusters*. With this cluster-
 1810 ing strategy, it is possible to detect and measure the energy and direction of photons
 1811 and neutral hadrons as well as differentiate these neutral particles from the charged
 1812 hadron energy deposits. In cases involving charged hadrons for which the track pa-
 1813 rameters are not determined accurately, for instance, low-quality and high- p_T tracks,
 1814 clustering helps in the energy measurements.

1815 Electron track reconstruction.

1816 Although the charged-particle track reconstruction described above works for elec-
 1817 trons, they lose a significant fraction of their energy via bremsstrahlung photon radi-
 1818 ation before reaching the ECAL; thus, the reconstruction performance depends on the
 1819 ability to measure also the radiated energy. The reconstruction strategy, in this case,
 1820 requires information from the tracking system and from the ECAL. Bremsstrahlung
 1821 photons are emitted at similar η values to that of the electron but at different values
 1822 of ϕ ; therefore, the radiated energy can be recovered by grouping ECAL clusters in a

1823 η window over a range of ϕ around the electron direction. The group is called ECAL
 1824 supercluster.

1825 Electron candidates from the track-seeding and ECAL super clustering are merged
 1826 into a single collection which is submitted to a full electron tracking fit with a
 1827 Gaussian-sum filter (GSF) [109]. The electron track and its associated ECAL su-
 1828 percluster form a *particle-flow electron*.

1829 **Muon track reconstruction.**

1830 Given that the CMS detector is equipped with a muon spectrometer capable to iden-
 1831 tify and measure the momentum of the muons traversing it, the muon reconstruction
 1832 is not specific to PF; therefore, three different muon types are defined

- 1833 • *Standalone muon.* A clustering on the DTs or CSCs hits is performed to form
 1834 track segments; those segments are used as seeds for the reconstruction in the
 1835 muon spectrometer. All DTs, CSCs, and RPCs hits along the muon trajectory
 1836 are combined and fitted to form the full track. The fitting output is called a
 1837 *standalone-muon track*.
- 1838 • *Tracker muon.* Each track in the inner tracker with p_T larger than 0.5 GeV and
 1839 a total momentum p larger than 2.5 GeV is extrapolated to the muon system.
 1840 A *tracker muon track* corresponds to a extrapolated track that matches at least
 1841 one muon segment.
- 1842 • *Global muon.* When tracks in the inner tracker (inner tracks) and standalone-
 1843 muon tracks are matched and turn out being compatibles, their hits are com-
 1844 bined and fitted to form a *global-muon track*.

1845 Global muons sharing the same inner track with tracker muons are merged into
 1846 a single candidate. PF muon identification uses the muon energy deposits in ECAL,
 1847 HCAL, and HO associated with the muon track to improve the muon identification.

1848 **Particle identification and reconstruction.**

1849 PF elements are connected by a linker algorithm that tests the connection between any
 1850 pair of elements; if they are found to be linked, a geometrical distance that quantifies
 1851 the quality of the link is assigned. Two elements may be linked indirectly through
 1852 common elements. Linked elements form *PF blocks* and each PF block may contain
 1853 elements originating in one or more particles. Links can be established between
 1854 tracks, between calorimeter clusters, and between tracks and calorimeter clusters.
 1855 The identification and reconstruction start with a PF block and proceed as follows

- 1856 • Muons. An *isolated global muon* is identified by evaluating the presence of
 inner track and energy deposits close to the global muon track in the (η, ϕ)
 plane, i.e., in a particular point of the global muon track, inner tracks and
 energy deposits are sought within a radius of $\Delta R = 0.3$ (see eqn. 2.7) from the
 muon track; if they exist and the p_T of the found track added to the E_T of the
 found energy deposit does not exceed 10% of the muon p_T then the global muon
 is an isolated global muon. This isolation condition is stringent enough to reject
 hadrons misidentified as muons.

1864 *Non-isolated global muons* are identified using additional selection requirements
 1865 on the number of track segments in the muon system and energy deposits along
 1866 the muon track. Muons inside jets are identified with more stringent criteria
 1867 in isolation and momentum as described in Reference [112]. The PF elements
 1868 associated with an identified muon are masked from the PF block.

- 1869 ● Electrons are identified and reconstructed as described above plus some addi-
 1870 tional requirements on fourteen variables like the amount of energy radiated,
 1871 the distance between the extrapolated track position at the ECAL and the po-
 1872 sition of the associated ECAL supercluster, among others, which are combined
 1873 in an specialized multivariate analysis strategy that improves the electron iden-
 1874 tification. Tracks and clusters used to identify and reconstruct electrons are
 1875 masked in the PF block.
- 1876 ● Isolated photons are identified from ECAL superclusters with E_T larger than 10
 1877 GeV, for which the energy deposited at a distance of 0.15, from the supercluster
 1878 position on the (η, ϕ) plane, does not exceed 10% of the supercluster energy;
 1879 note that this is an isolation requirement. In addition, there must not be links
 1880 to tracks. Clusters involved in the identification and reconstruction are masked
 1881 in the PF block.
- 1882 ● Bremsstrahlung photons and prompt photons tend to convert to electron-positron
 1883 pairs inside the tracker, therefore, a dedicated finder algorithm is used to link
 1884 tracks that seem to originate from a photon conversion; in case those two tracks
 1885 are compatible with the direction of a bremsstrahlung photon, they are also
 1886 linked to the original electron track. Photon conversion tracks are also masked
 1887 in the PF block.
- 1888 ● The remaining elements in the PF block are used to identify hadrons. In the
 1889 region $|\eta| \leq 2.5$, neutral hadrons are identified with HCAL clusters not linked
 1890 to any track while photons from neutral pion decays are identified with ECAL
 1891 clusters without links to tracks. In the region $|\eta| > 2.5$ ECAL clusters linked to
 1892 HCAL clusters are identified with a charged or neutral hadron shower; ECAL
 1893 clusters with no links are identified with photons. HCAL clusters not used yet,

1894 are linked to one or more unlinked tracks and to an unlinked ECAL in order to
 1895 reconstruct charged-hadrons or a combination of photons and neutral hadrons
 1896 according to certain conditions on the calibrated calorimetric energy.

- 1897 • Charged-particle tracks may be liked together when they converge to a *sec-*
 1898 *ondary vertex (SV)* displaced from the IP where the PV and PU vertices are
 1899 reconstructed; at least three tracks are needed in that case, of which at most
 1900 one has to be an incoming track with hits in tracker region between a PV and
 1901 the SV.

1902 The linker algorithm, as well as the whole PF algorithm, has been validated and
 1903 commissioned; results from that validation are presented in the Reference [105].

1904 **Jet reconstruction.**

1905 Quarks and gluons may be produced in the pp collisions, therefore, their hadronization
 1906 will be seen in the detector as a shower of hadrons and their decay products in the
 1907 form of a *jet*. Two classes of clustering algorithms have been developed based in
 1908 their jet definition [113]:

- 1909 • Iterative cone algorithms (IC). Jets are defined in terms of circles of fixed radius
 1910 R in the $\eta\text{-}\phi$ plane, known as *stable cones*, for which the sum of the momenta
 1911 of all the particles within the cone points in the same direction as the center
 1912 of the circle. The seed of the iteration is the hardest non-isolated particle in
 1913 the event, then, the resulting momentum direction is assigned as the new cone
 1914 direction and a new iteration starts; iteration process stops when the cone if
 1915 found to be stable.

1916 • Sequential recombination algorithms. The distance between non-isolated par-
 1917 ticles is calculated; if that distance is below a threshold, these particles are
 1918 recombined into a new object. The sequence is repeated until the separation
 1919 between the recombined object and any other particle is above certain thresh-
 1920 old; the recombined object is called a jet and the algorithm starts again with
 1921 the remaining particles.

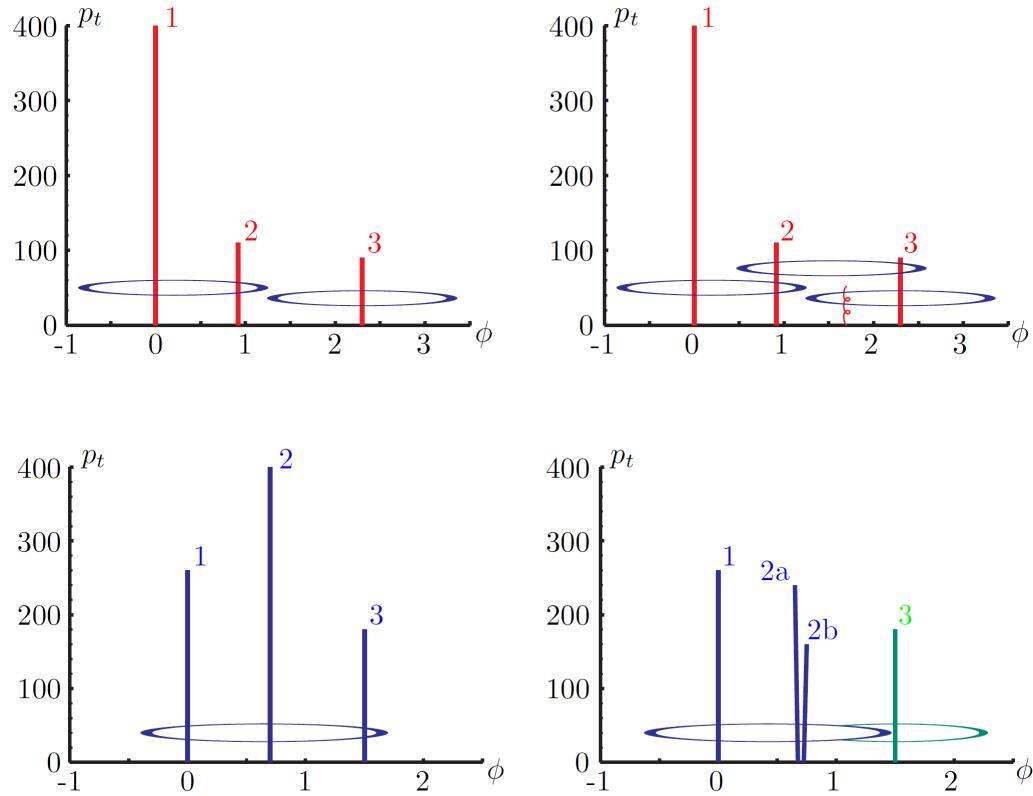


Figure 3.3: Stable cones identification using IC algorithms [113].

1922 Two conditions are of particular importance for the clustering algorithms, *infrared*
 1923 and *collinear (IRC) safety*. In order to explain the concept of infrared (IR) safety,
 1924 consider an event with three hard particles as shown in the top left side of Figure 3.3,
 1925 two stable cones are found and then two jets are identified; if a soft gluon is added, as
 1926 shown in the top right side of Figure 3.3, three stable cones are found and the three

1927 hard particles are now clustered into a single jet. If the addition of soft particles
 1928 change the outcome of the clustering, then it is said that the algorithm is IR unsafe.
 1929 Soft radiation is highly likely in perturbative QCD, which dominates the physics of
 1930 the jets, and then IR unsafe effect leads to divergences [113].

1931 The concept of collinear safety can also be explained considering a three hard
 1932 particles event, as shown in the bottom left side of Figure 3.3, where one stable cone
 1933 containing all three particles is found and one jet is identified; if the hardest particle
 1934 is split into two collinear particles (2a and 2b) in the bottom right side of Figure 3.3,
 1935 then the clustering results in a different jet identification and the algorithm is said
 1936 to be collinear unsafe. The collinear unsafe effect leads to divergences in jet cross
 1937 section calculations [114].

1938 It has been determined that IC algorithms are IRC unsafe, and therefore, they
 1939 have to be replaced by algorithms that not only provide the finite perturbative results
 1940 from theoretical computations, but also that are not highly dependent on underlying
 1941 event and pileup effects which leads to significant corrections [113].

1942 The sequential recombination algorithms arise as the IRC safe alternative used by
 1943 the CMS experiment; in particular the anti- k_t algorithm which is a generalization of
 1944 the previously existing k_t [115] and Cambridge/Aachen [116] jet clustering algorithms.

1945 The anti- k_t algorithm is used to perform the jet reconstruction by clustering those
 1946 PF particles within a cone (see Figure 3.4); previously, isolated electrons, isolated
 1947 muons, and charged particles associated with other interaction vertices are excluded
 1948 from the clustering.

1949 The anti- k_t algorithm proceeds in a sequential recombination of PF particles; the
 1950 distance between particles i and j (d_{ij}) and the distance between particles and the
 1951 beam are defined as

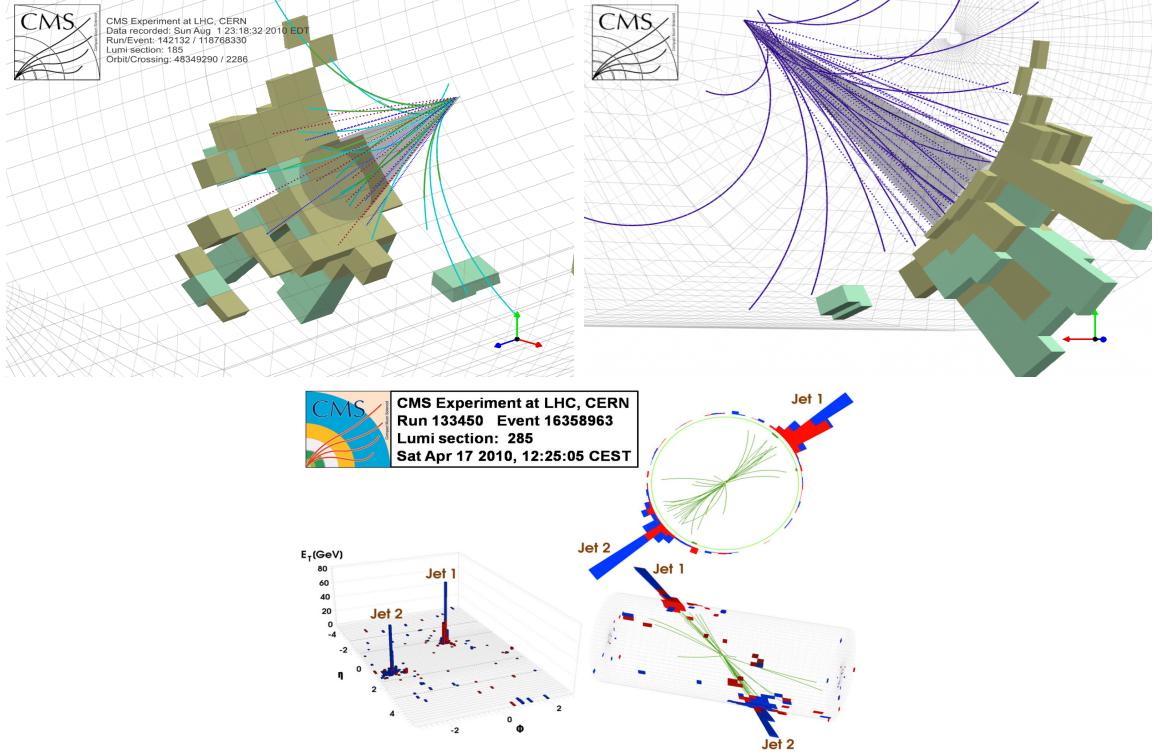


Figure 3.4: Jet reconstruction performed by the anti- k_t algorithm. Top: Two different views of a CMS recorded event are presented. Continuous lines correspond to tracks left by charged particles in the tracker while dotted lines are the imaginary paths followed by neutral particles. The green cubes represent the ECAL cells while the blue ones represent the HCAL cells; in both cases, the height of the cube represent the amount of energy deposited in the cells [117]. Bottom: Reconstruction of a recorded event with two jets [118].

$$d_{ij} = \min\left(\frac{1}{k_{ti}^2}, \frac{1}{k_{tj}^2}\right) \frac{\Delta_{ij}^2}{R^2}$$

$$d_{iB} = \frac{1}{k_{ti}^2} \quad (3.1)$$

1952 where $\Delta_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$, k_{ti} , y_i and ϕ_i are the transverse momentum, 1953 rapidity and azimuth of particle i respectively and R is the called jet radius. For all 1954 the remaining PF particles, after removing the isolated ones, d_{ij} and d_{iB} are calcu-

1955 lated⁵ and the smallest is identified; if it is a d_{ij} , particles i and j are replaced with
 1956 a new object whose momentum is the vectorial sum of the combined particles. If the
 1957 smallest distance is a d_{iB} the clustering process ends, the object i (which at this stage
 1958 should be a combination of several PF particles) is declared as a *Particle-flow-jet* (PF
 1959 jet) and all the associated PF particles are removed from the detector. The clustering
 1960 process is repeated until no PF particles remain. R is a free parameter that can be
 1961 adjusted according to the specific analysis conditions; usually, two values are used,
 1962 $R=0.4$ and $R=0.5$, giving the name to the so-called AK4-jet and AK5-jet respectively.

1963 An advantage of the anti- k_t algorithm over other clustering algorithms is the reg-
 1964 ularity of the boundaries of the resulting jets. For all known IRC safe algorithms,
 1965 soft radiation can introduce irregularities in the boundaries of the final jets; however,
 1966 anti- k_t algorithm is soft-resilient, meaning that jets shape is not affected by soft radi-
 1967 ation, which is a valuable property considering that knowing the typical shape of jets
 1968 makes experimental calibration of jets more simple. In addition, that soft-resilience
 1969 is expected to simplify certain theoretical calculations and reduce the momentum-
 1970 resolution loss caused by underlying-event (UE) and pileup contamination [114].

1971 The effect of the UE and pileup contamination over a jet identification, can be
 1972 seen as if soft events are added to the jet; for instance, if a soft event representing UE
 1973 or pileup is added to an event for which a set of jets J have been identified, and the
 1974 clustering is rerun on that new extended event, the outcome will be different in two
 1975 aspects: jets will contain some additional soft energy and the distribution of particles
 1976 in jets may have change; that effect is called *back-reaction*. The back-reaction effect in
 1977 the anti- k_t algorithm is suppressed not by the amount of momentum added to the jet
 1978 but by the jet transverse momentum $p_{T,J}$, which means that this strong suppression
 1979 leads to a smaller correction due to EU and pileup effect [114].

⁵ Notice that this is a combinatorial calculation.

1980 Jet energy Corrections

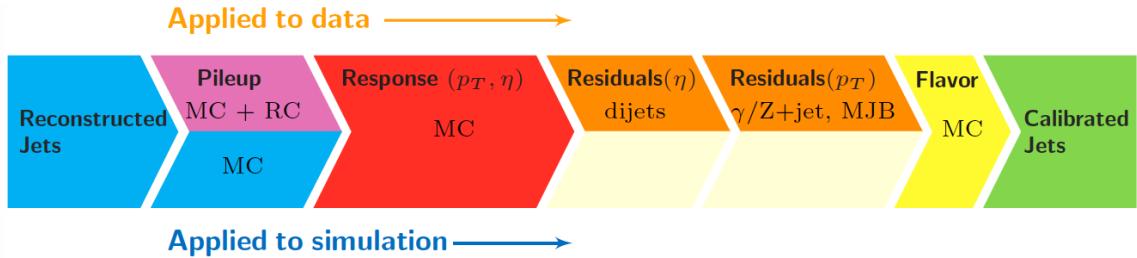


Figure 3.5: Jet energy correction diagram. Correction levels are applied sequentially in the indicated fixed order [120].

Even though jets can be reconstructed efficiently, there are some effects that are not included in the reconstruction and that lead to discrepancies between the reconstructed results and the predicted results; in order to overcome these discrepancies, a factorized model has been designed in the form of jet energy corrections (JEC) [119, 120] applied sequentially as shown in the diagram of Figure 3.5.

At each level, the jet four-momentum is multiplied by a scaling factor based on jet properties, i.e., η , flavor, etc.

- Level 1 correction removes the energy coming from pile-up. The scale factor is determined using a MC sample of QCD dijet (2 jets) events with and without pileup overlay; it is parametrized in terms of the offset energy density ρ , jet area A, jet η and jet p_T . Different corrections are applied to data and MC due to the detector simulation.
 - MC-truth correction accounts for differences between the reconstructed jet energy and the MC particle-level energy. The correction is determined on a QCD dijet MC sample and is parametrized in terms of the jet p_T and η .
 - Residuals correct remaining small differences within jet response in data and MC. The Residuals η -dependent correction compares jets of similar p_T in the

1998 barrel reference region. The Residuals p_T -dependent correct the jet absolute
 1999 scale (JES vs p_T).

- 2000 • Jet-flavor corrections are derived in the same way as MC-truth corrections but
 2001 using QCD pure flavor samples.

2002 ***b*-tagging of jets.**

2003 A particular feature of the hadrons containing bottom quarks (*b*-hadrons) is that
 2004 their lifetime is long enough to travel some distance before decaying, but it is not as
 2005 long as those of light quark hadrons; therefore, when looking at the hadrons produced
 2006 in pp collisions, *b*-hadrons decay typically inside the tracker rather than reaching the
 2007 calorimeters as some light-hadrons do. As a result, a *b*-hadron decay gives rise to a
 2008 displaced vertex (secondary vertex) with respect to the primary vertex as shown in
 2009 Figure 3.6; the SV displacement is in the order of a few millimeters. A jet resulting
 2010 from the decay of a *b*-hadron is called *b* jet; other jets are called light jets.

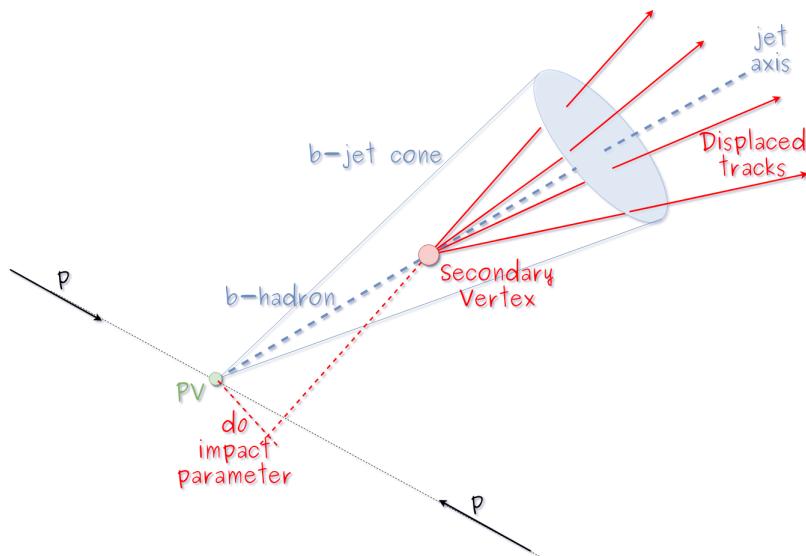


Figure 3.6: Secondary vertex in a *b*-hadron decay.

2011 Several methods to identify *b*-jets (*b*-tagging) have been developed; the method

2012 used in this thesis is known as *Combined Secondary Vertex* algorithm in its second
 2013 version (CSVv2) [121]. By using information of the impact parameter, the recon-
 2014 structed secondary vertices, and the jet kinematics as input in a multivariate analysis
 2015 that combines the discrimination power of each variable in one global discrimina-
 2016 tor variable, three working points (references): loose, medium and tight, are defined
 2017 which quantify the probabilities of mistag jets from light quarks as jets from b quarks;
 2018 10, 1 and 0.1 % respectively. Although the mistagging probability decreases with the
 2019 working point strength, the efficiency to correctly tag b -jets also decreases as 83, 69
 2020 and 49 % for the respective working point; therefore, a balance needs to be achieved
 2021 according to the specific requirements of the analysis.

2022 **Missing transverse energy.**

2023 The fact that proton bunches carry momentum along the z -axis implies that for
 2024 each event it is expected that the momentum in the transverse plane is balanced.
 2025 Imbalances are quantified by the missing transverse energy (MET) and are attributed
 2026 to several sources including particles escaping undetected through the beam pipe,
 2027 neutrinos produced in weak interactions processes which do not interact with the
 2028 detector and thus escaping without leaving a sign, or even undiscovered particles
 2029 predicted by models beyond the SM.

2030 The PF algorithm assigns the negative sum of the momenta of all reconstructed
 2031 PF particles to the *particle-flow MET* according to

$$\vec{E}_T = - \sum_i \vec{p}_{T,i} \quad (3.2)$$

2032 JEC are propagated to the calculation of the \vec{E}_T as described in the Reference [122].

2033 **3.4.2 Event reconstruction examples**

2034 Figures 3.7-3.9 show the results of the reconstruction performed on 3 recorded events.

2035 Descriptions are taken directly from the source.

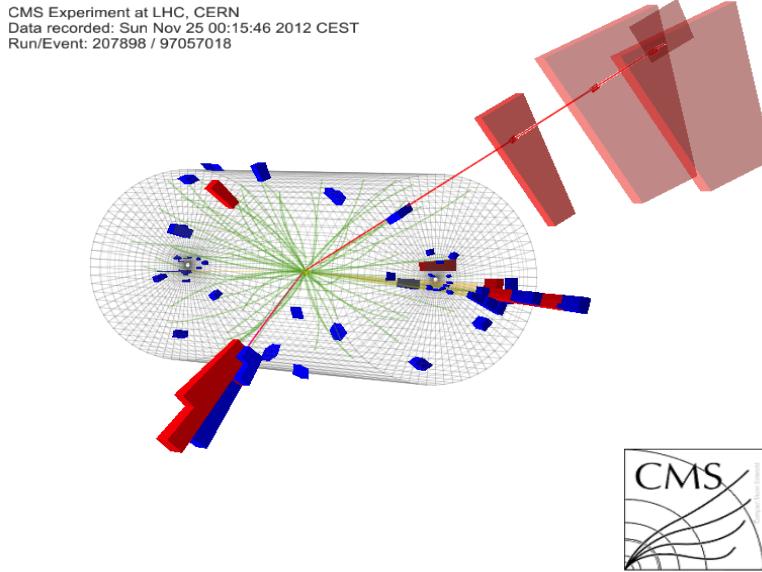


Figure 3.7: HIG-13-004 Event 1 reconstruction results; “HIG-13-004 Event 1: Event recorded with the CMS detector in 2012 at a proton-proton center-of-mass energy of 8 TeV. The event shows characteristics expected from the decay of the SM Higgs boson to a pair of τ leptons. Such an event is characterized by the production of two forward-going jets, seen here in opposite endcaps. One of the τ decays to a muon (red lines on the right) and neutrinos, while the other τ decays into a charged hadron and a neutrino.” [123].

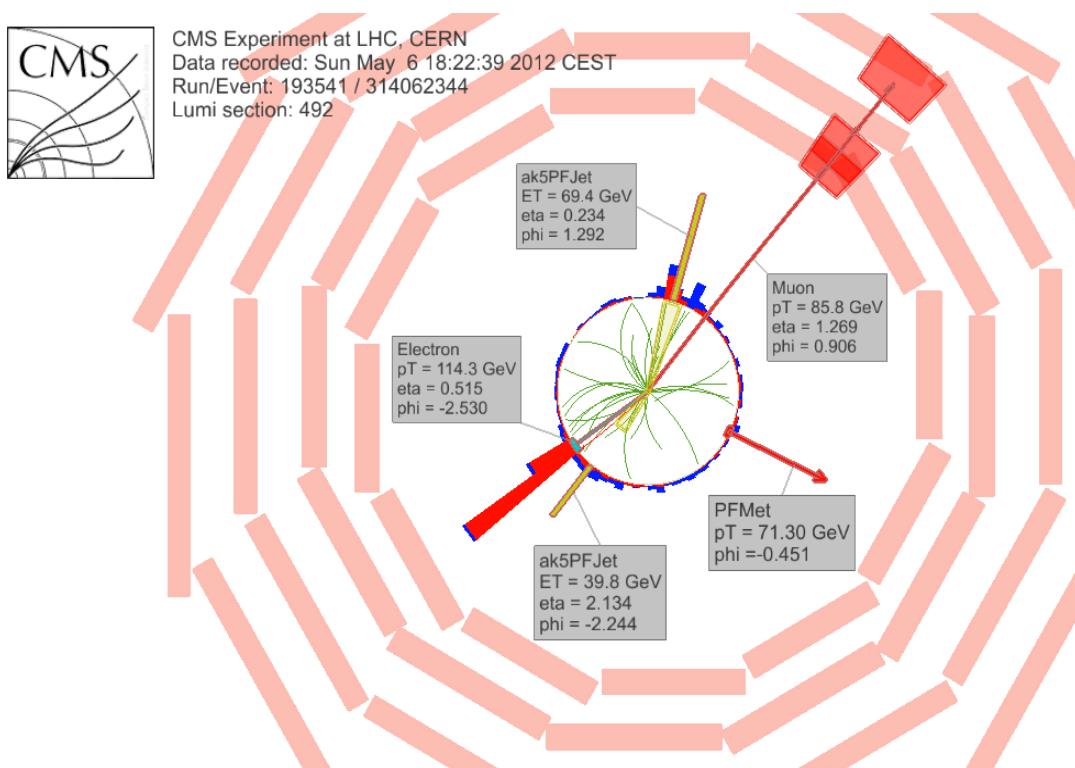


Figure 3.8: $e\mu$ event reconstruction results; “An $e\mu$ event candidate selected in 8 TeV data, as seen from the direction of the proton beams. The kinematics of the main objects used in the event selection are highlighted: two isolated leptons and two particle-flow jets. The reconstructed missing transverse energy is also displayed for reference” [124].

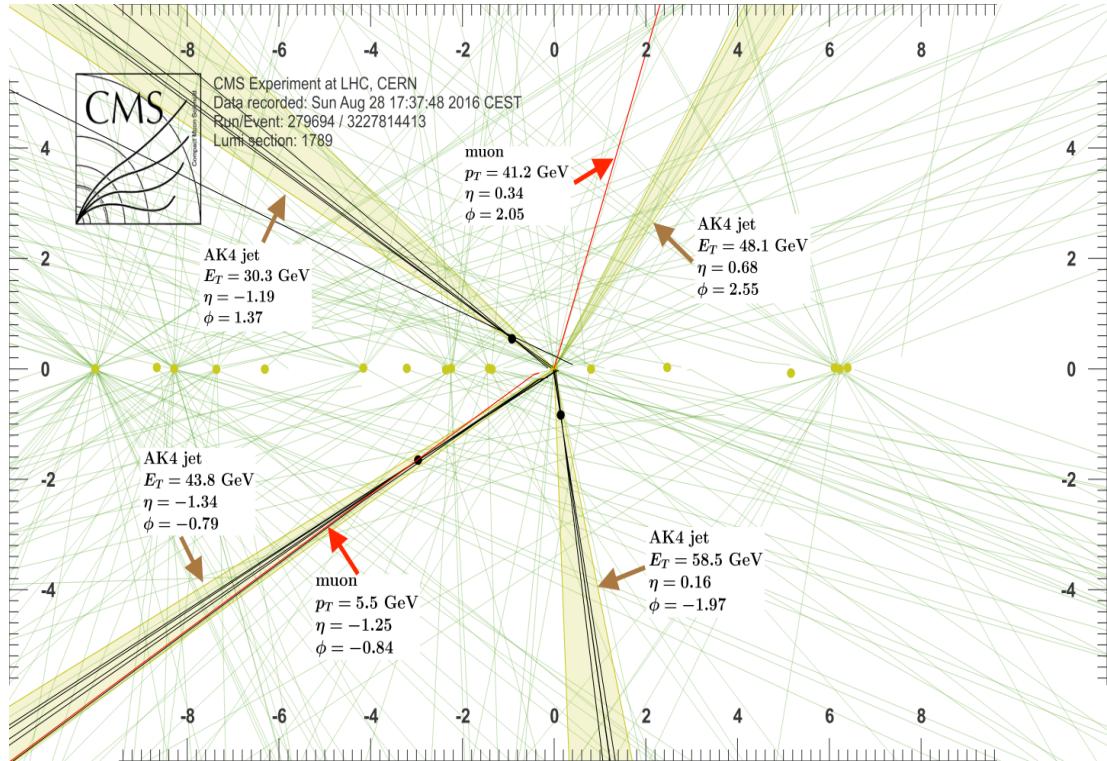


Figure 3.9: Recorded event reconstruction results; “Recorded event (ρ - z projection) with three jets with $p_T > 30$ GeV with one displaced muon track in 2016 data collected at 13 TeV. Each of the three jets has a displaced reconstructed vertex. The jet with $p_T(j) = 43.8$ GeV, $\eta(j) = -1.34$, $\phi(j) = -0.79$ contains muon with $p_T(\mu) = 5.5$ GeV, $\eta(\mu) = -1.25$, $\phi(\mu) = -0.84$. Event contains reconstructed isolated muon with $p_T(\mu) = 41.2$ GeV, $\eta(\mu) = 0.34$, $\phi(\mu) = 2.05$ and MET with $p_T = 72.5$ GeV, $\phi = -0.32$. Jet candidates for a b -jet from top quark leptonic and hadronic decays are tagged by CSVv2T algorithm. One of the other two jets is tagged by CharmT algorithm. Tracks with $p_T > 0.5$ GeV are shown. The number of reconstructed primary vertices is 18. Reconstructed $m_T(W)$ is 101.8 GeV. Beam spot position correction is applied. Reconstructed primary vertices are shown in yellow color, while reconstructed displaced vertices and associated tracks are presented in black color. Dimensions are given in cm” [125].

2036 **Chapter 5**

2037 **Statistical methods**

2038 In the course of analyzing the data sets provided by the CMS experiment and used in
2039 this thesis, several statistical tools have been employed; in this chapter, a description
2040 of these tools will be presented, starting with the general statement of the multivariate
2041 analysis methods, followed by the particularities of the Boosted Decision Trees (BDT)
2042 method and its application to the classification problem. Statistical inference methods
2043 used will also be presented. This chapter is based mainly on References [126–128].

2044 **5.1 Multivariate analysis**

2045 Multivariate data analysis (MVA) makes use of the statistical techniques developed to
2046 analyze more than one variable at once, taking into account all the correlations among
2047 variables. MVA is employed in a variety of fields like consumer and market research,
2048 quality control and process optimization. Using MVA it is possible to identify the
2049 dominant patterns in a data sample, like groups, outliers and trends, and determine
2050 to which group a set of values belong; in the particle physics context, MVA methods
2051 are used to perform the selection of certain type of events from a large data set.

2052 Processes with small cross section, such as the tHq process ($\sigma_{SM}(\sqrt{s} = 13\text{TeV}) =$
 2053 70.96 fb), are hard to detect in the presence of the processes with larger cross sections,
 2054 $\sigma_{SM}^{t\bar{t}}(\sqrt{s} = 13\text{TeV}) = 823.44 \text{ fb}$ for instance; therefore, only a small fraction of the data
 2055 contains events of interest (signal), the major part is signal-like events, which mimic
 2056 signal characteristics but belong to different processes, so they are a background to
 2057 the process of interest. This implies that it is not possible to say with certainty
 2058 that a given event is a signal or a background and statistical methods should be
 2059 involved. In that sense, the challenge can be formulated as one where a set of events
 2060 have to be classified according to certain special features; these features correspond
 2061 to the measurements of several parameters like energy or momentum, organized in a
 2062 set of *input variables*. The measurements for each event can be written in a vector
 2063 $\mathbf{x} = (x_1, \dots, x_n)$ for which

- 2064 • $f(\mathbf{x}|s)$ is the probability density (*likelihood function*) that \mathbf{x} is the set of mea-
 2065 sured values given that the event is a signal event (signal hypothesis).
- 2066 • $f(\mathbf{x}|b)$ is the probability density (*likelihood function*) that \mathbf{x} is the set of mea-
 2067 sured values given that the event is a background event (background hypothe-
 2068 sis).

2069 Figure 5.1 shows three ways to perform a classification of events for which mea-
 2070 surements of two properties, i.e., two input variables x_1 and x_2 , have been performed;
 2071 blue circles represent signal events while red triangles represent background events.
 2072 The classification on the left is *cut-based* requiring $x_1 < c_1$ and $x_2 < c_2$; usually the
 2073 cut values (c_1 and c_2) are chosen according to some knowledge about the event pro-
 2074 cess. In the middle plot, the classification is performed using a linear function of
 2075 the input variables, hence the boundary is a straight line, while in the right plot the

2076 the relationship between input variables is not linear thus the boundary is not linear
 2077 either.

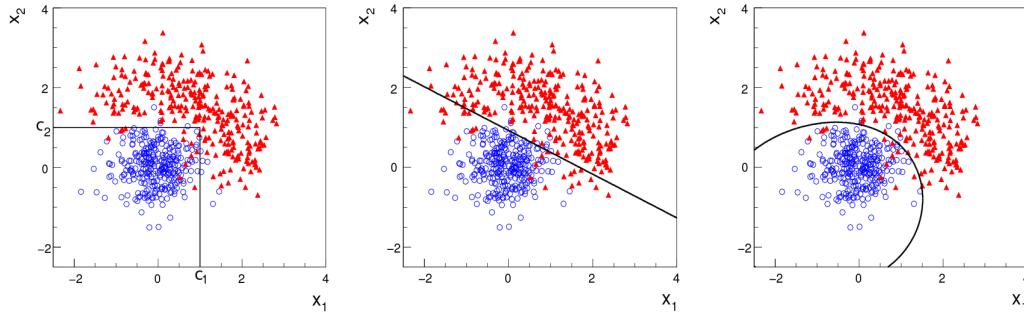


Figure 5.1: Scatter plots-MVA event classification. Distribution of two input variables x_1 and x_2 measured for a set of events; blue circles represent signal events and red triangles represent background events. The classification is based on cuts (left), linear boundary (center), and nonlinear boundary (right) [126]

2078 In general, the boundary can be parametrized in terms of the input variables such
 2079 that the cut is set on the parametrization instead of on the variables, i.e., $y(\mathbf{x}) = y_{cut}$
 2080 with y_{cut} being a constant; thus, the acceptance or rejection of an event is based on
 2081 which side of the boundary the event is located. If $y(\mathbf{x})$, usually called *test statistic*,
 2082 has functional form, it can be used to determine the probability distribution functions
 2083 $p(y|s)$ and $p(y|b)$ and then perform a test statistic with a single cut on the scalar
 2084 variable y .

2085 Figure 5.2 shows an example of what would be the probability distribution func-
 2086 tions under the signal and background hypotheses for a scalar test statistic with a cut
 2087 on the classifier y . Note that the tails of the distributions indicate that some signal
 2088 events fall in the rejection region and some background events fall on the acceptance
 2089 region; therefore, it is convenient to define the *efficiency* with which events of a given
 2090 type are accepted. The signal and background efficiencies are given by

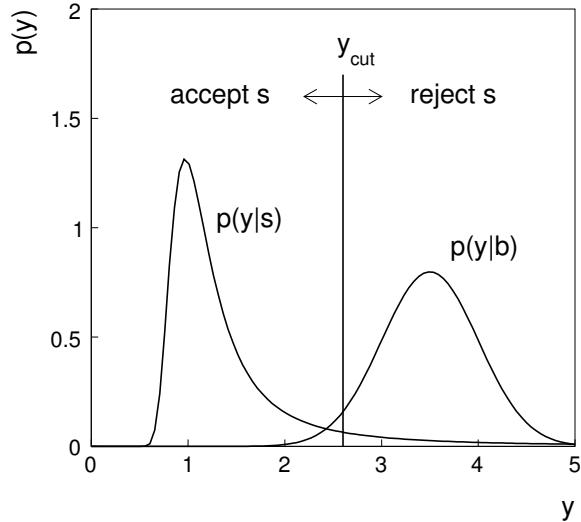


Figure 5.2: Distributions of the scalar test statistic $y(\mathbf{x})$ under the signal and background hypotheses. [126]

$$\varepsilon_s = P(\text{accept event}|s) = \int_A f(\mathbf{x}|s) d\mathbf{x} = \int_{-\infty}^{y_{cut}} p(y|s) dy , \quad (5.1)$$

$$\varepsilon_b = P(\text{accept event}|b) = \int_A f(\mathbf{x}|b) d\mathbf{x} = \int_{-\infty}^{y_{cut}} p(y|b) dy , \quad (5.2)$$

where A is the acceptance region. If the background hypothesis is the *null hypothesis* (H_0), the signal hypothesis would be *alternative hypothesis* (H_1); in this context, the background efficiency corresponds to the significance level of the test (α) and describes the misidentification probability, while the signal efficiency corresponds to the power of the test ($1-\beta$)¹ and describes the probability of rejecting the background hypothesis if the signal hypothesis is true. What is sought in an analysis is to maximize the power of the test relative to the significance level, i.e., set a selection with the largest possible selection efficiency and the smallest possible misidentification probability.

¹ β is the fraction of signal events that fall out of the acceptance region

2099 **5.1.1 Decision trees**

2100 For this thesis, the implementation of the MVA strategy, described above, is per-
 2101 formed through decision trees by using the TMVA software package [127] included
 2102 in the ROOT analysis framework [129]. In a simple picture, a decision tree classifies
 2103 events according to their input variables values by setting a cut on each input variable
 2104 and checking which events are on which side of the cut, just as proposed in the MVA
 2105 strategy, but in addition, as a machine learning algorithm, decision trees offer the
 2106 possibility to be trained and then perform the classification efficiently.

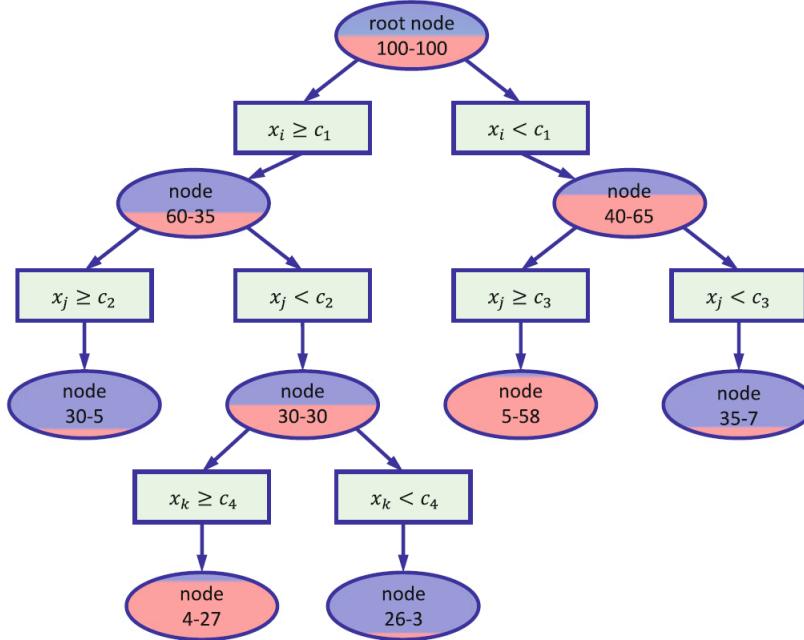


Figure 5.3: Example of a decision tree. Each node is fed with a MC sample mixing signal and background events (left-right numbers); nodes colors represent the relative number of signal/background events [128].

2107 The training or growing of a decision tree is the process where the rules for clas-
 2108 sifying events are defined; this process is represented in Figure 5.3 and consists of
 2109 several steps:

- 2110 • take MC samples of signal and background events and split them into two parts

2111 each; the first parts will be used in the decision tree training, while the second
 2112 parts will be used for testing the final classifier obtained from the training.
 2113 Each event has associated a set of input variables $\mathbf{x} = (x_1, \dots, x_n)$ which serve
 2114 to distinguish between signal and background events. The training sample is
 2115 taken in at the *root node*.

- 2116 • Pick one variable, say x_i .
- 2117 • Pick one value of x_i , each event has its own value of x_i , and split the training
 sample into two subsamples B_1 and B_2 ; B_1 contains events for which $x_i < c_1$
 while B_2 contains the rest of the training events;
- 2120 • scan all possible values of x_i and find the splitting value that provides the *best*
 classification², i.e., B_1 is mostly made of signal events while B_2 is mostly made
 of background events.
- 2123 • It is possible that variables other than the picked one produce a better classi-
 fication, hence, all the variables have to be evaluated. Pick the next variable,
 say x_j , and repeat the scan over its possible values.
- 2126 • At the end, all the variables and their values will have been scanned, the *best*
 variable and splitting value will have been identified, say x_1, c_1 , and there will
 be two nodes fed with the subsamples B_1 and B_2 .

2129 Nodes are further split by repeating the decision process until a given number of
 2130 final nodes is obtained, nodes are largely dominated by either signal or background
 2131 events, or nodes have too few events to continue. Final nodes are called *leaves* and
 2132 they are classified as signal or background leaves according to the class of the majority
 2133 of events in them. Each *branch* in the tree corresponds to a sequence of cuts.

² Quality of the classification will be treated in the next paragraph.

2134 The quality of the classification at each node is evaluated through a separation
 2135 criteria; there are several of them but the *Gini Index* (G) is the one used in the
 2136 decision trees trained for the analysis in this thesis. G is written in terms of the
 2137 purity (P), i.e., the fraction of signal events in the samples after the separation is
 2138 made; it is given by

$$G = P(1 - P) \quad (5.3)$$

2139 note that $P=0.5$ at the root node while $G=0$ for pure leaves. For a node A split into
 2140 two nodes B_1 and B_2 the G gain is

$$\Delta G = G(A) - G(B_1) - G(B_2). \quad (5.4)$$

2141 The *best* classification corresponds to that for which the gain of G is maximized;
 2142 hence, the scanning over all the variables in an event and their values is of great
 2143 importance.

2144 In order to provide a numerical output for the classification, events in a sig-
 2145 nal(background) leaf are assigned an score of 1(-1) each, defining in this way the
 2146 decision tree *classifier/weak learner* as

$$f(\mathbf{x}) = \begin{cases} 1 & \mathbf{x} \text{ in signal region,} \\ -1 & \mathbf{x} \text{ in background region.} \end{cases}$$

2147 Figure 5.4 shows an example of the classification of a sample of events, containing
 2148 two variables, performed by a decision tree.

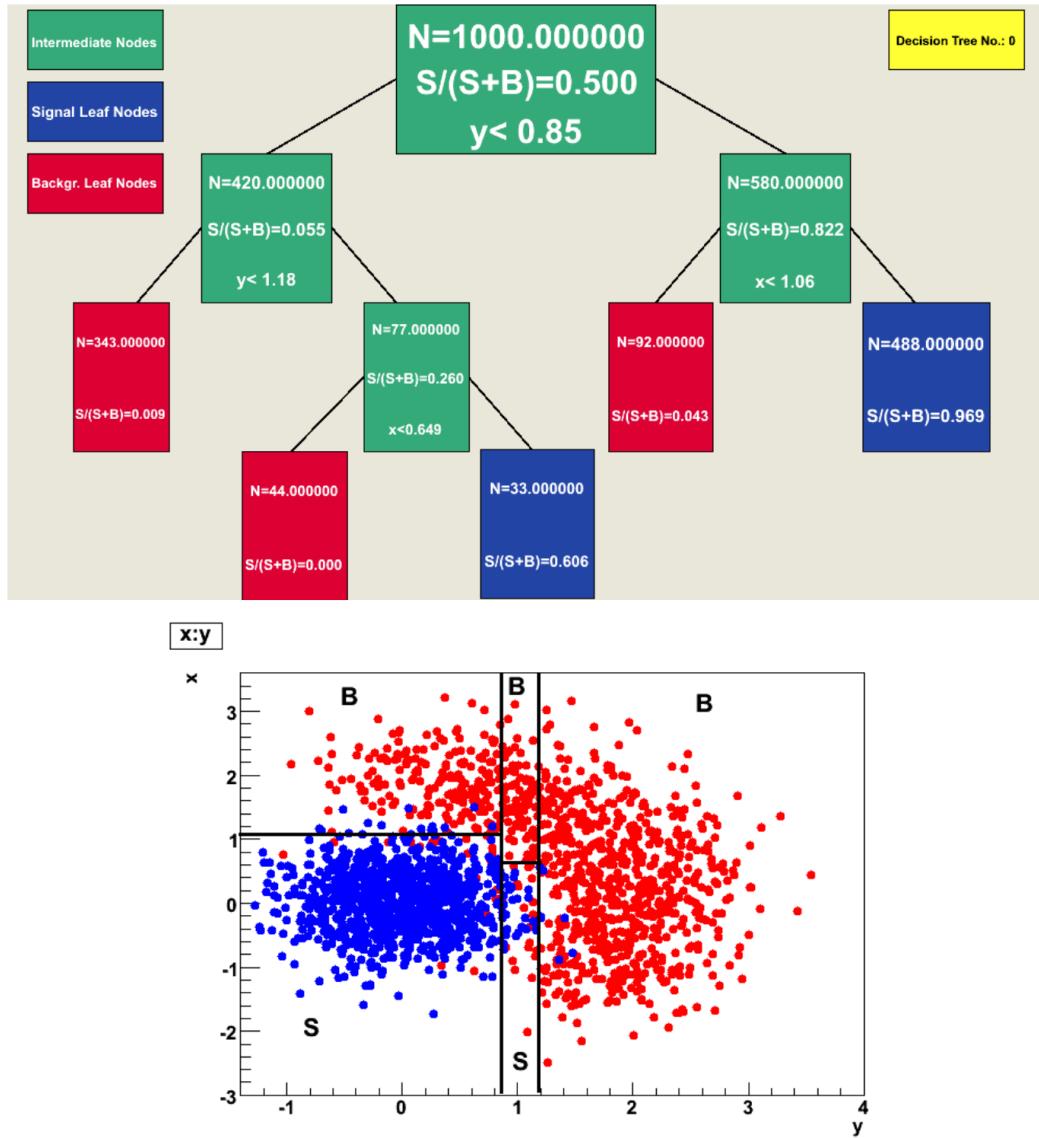


Figure 5.4: Example of a decision tree output. Each leaf, blue for signal events and red for background events, is represented by a region in the variables phase space [130].

2149 5.1.2 Boosted decision trees (BDT).

2150 Event misclassification occurs when a training event ends up in the wrong leaf, i.e., a
 2151 signal event ends up in a background leaf or a background event ends up in a signal
 2152 leaf. A way to correct it is to assign a weight to the misclassified events and train
 2153 a second tree using the reweighted events; the event reweighting is performed by a

2154 boosting algorithm in such a way that when used in the training of a new decision
 2155 tree the *boosted events* get correctly classified. The process is repeated iteratively
 2156 adding a new tree to the forest and creating a set of classifiers, which are combined
 2157 to create the next classifier; the final classifier offers more stability³ and has a smaller
 2158 misclassification rate than any individual ones. The resulting tree collection is known
 2159 as a *boosted decision tree (BDT)*.

2160 Thus, purity of the sample is generalized to

$$P = \frac{\sum_s w_s}{\sum_s w_s + \sum_b w_b} \quad (5.5)$$

2161 where w_s and w_b are the weights of the signal and background events respectively;
 2162 the Gini index is also generalized

$$G = \left(\sum_i^n w_i \right) P(1 - P) \quad (5.6)$$

2163 with n the number of events in the node. The final score of an event, after pass-
 2164 ing through the forest, is calculated as the renormalized sum of all the individual
 2165 (possibly weighted) scores; thus, high(low) score implies that the event is most likely
 2166 signal(background).

2167 The boosting procedure, implemented in the *Gradient boosting* algorithm used in
 2168 this thesis, produces a classifier $F(\mathbf{x})$ which is the weighted sum of the individual
 2169 classifiers obtained after each iteration, i.e.,

$$F(\mathbf{x}) = \sum_{m=1}^M \beta_m f(\mathbf{x}; a_m) \quad (5.7)$$

2170 where M is the number of trees in the forest. The *loss function* $L(F, y)$ represents the

³ Decision trees suffer from sensitivity to statistical fluctuations in the training sample which may lead to very different results with a small change in the training samples.

2171 deviation between the classifier $F(\mathbf{x})$ response and the true value y obtained from the
 2172 training sample (1 for signal events and -1 for background event), according to

$$L(F, y) = \ln(1 + e^{-2F(\mathbf{x})y}) \quad (5.8)$$

2173 thus, the reweighting is employed to ensure the minimization of the loss function; a
 2174 more detailed description of the minimization procedure can be found in Reference
 2175 [131]. The final classifier output is later used as a final discrimination variable, labeled
 2176 as *BDT output/response*.

2177 5.1.3 Overtraining

2178 Decision trees offer the possibility to have as many nodes as desired in order to
 2179 reduce the misclassification to zero (in theory); however, when a classifier is too much
 2180 adjusted to a particular training sample, the classifier's response to a slightly different
 2181 sample may leads to a completely different classification results; this effect is known
 2182 as *overtraining*.

2183 An alternative to reduce the overtraining in BDTs consists in pruning the tree
 2184 by removing statistically insignificant nodes after the tree growing is completed but
 2185 this option is not available for BDTs with gradient boosting in the TMVA-toolkit,
 2186 therefore, the overtraining has to be reduced by tuning the algorithm, number of
 2187 nodes, minimum number of events in the leaves, etc. The overtraining can be evaluated
 2188 by comparing the responses of the classifier when running over the training and
 2189 test samples.

2190 5.1.4 Variable ranking

2191 BDTs have a couple of particular advantages related to the input variables; they are
 2192 relatively insensitive to the number of input variables used in the vector \mathbf{x} . The
 2193 ranking of the BDT input variables is determined by counting the number of times a
 2194 variable is used to split decision tree nodes; in addition, the separation gain-squared
 2195 achieved in the splitting and the number of events in the node are accounted by
 2196 applying a weighting to that number. Thus, those variables with small or no power
 2197 to separate signal and background events are rarely chosen to split the nodes, i.e., are
 2198 effectively ignored.

2199 In addition, variables correlations play an important role for some MVA methods
 2200 like the Fisher discriminant algorithm in which the first step consist of performing a
 2201 linear transformation to a phase space where the correlations between variables are
 2202 removed; in the case of BDT algorithm, correlations do not affect the performance.

2203 5.1.5 BDT output example

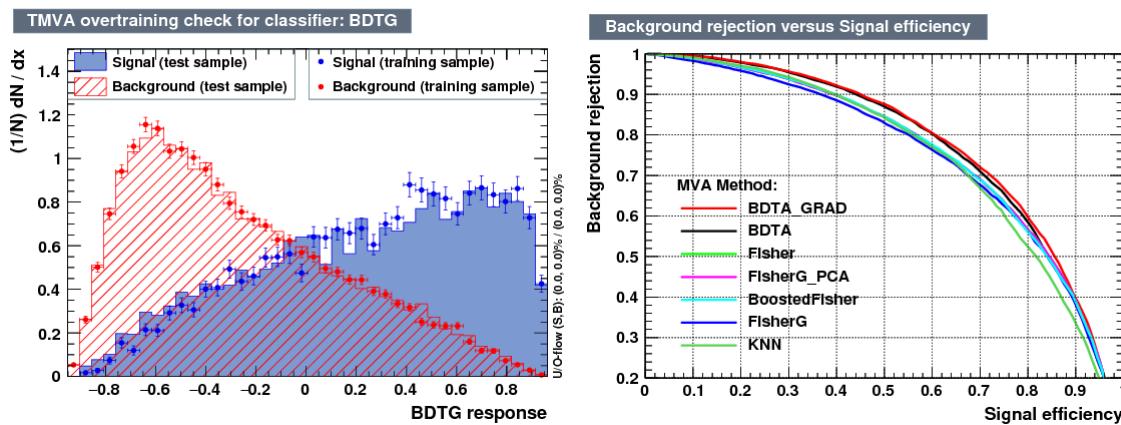


Figure 5.5: Left: Output distributions for the gradient boosted decision tree (BDTG) classifier using a sample of signal ($pp \rightarrow tHq$) and background ($pp \rightarrow tt$) events. Right: Background rejection vs signal efficiency (ROC curves) for various MVA classifiers running over the same sample used to produce the plot on the left.

2204 The left side of figure 5.5 shows the BDT output distributions for signal ($pp \rightarrow$
 2205 tHq) and background ($pp \rightarrow t\bar{t}$) events; this plot is the equivalent to the one showed
 2206 in Figure 5.2. A forest with 800 trees, maximum depth per tree = 3, and gradient
 2207 boosting have been used as training parameters. The BDTG classifier offers a good
 2208 separation power. There is a small overtraining in the signal distribution, while the
 2209 background distribution is very well predicted which might indicate that the sample
 2210 is composed of more background than signal events.

2211 The right side of figure 5.5 shows the background rejection vs signal efficiency
 2212 curves for several combinations of MVA classifiers-boosting algorithms running over
 2213 the same MC sample; these curves are known as ROC curves and give an indication
 2214 of the performance of the classifier. In this particular example, the best performance
 2215 is achieved with the BDTG classifier (BDTA_GRAD), which motivate its use in this
 2216 thesis.

2217 **5.2 Statistical inference**

2218 Once events are classified, the next step consists of finding the parameters that define
 2219 the likelihood functions $f(\mathbf{x}|s)$, $f(\mathbf{x}|b)$ for signal and background events respectively.
 2220 In general, likelihood functions depend not only on the measurements but also on
 2221 parameters (θ_m) that define their shapes; the process of estimating these *unknown*
 2222 *parameters* and their uncertainties from the experimental data is called *inference*.

2223 The statistical inference tools used in this analysis are implemented in the RooFit
 2224 toolkit [132] and COMBINE package [133] included in the CMSSW software frame-
 2225 work.

2226 **5.2.1 Nuisance parameters**

2227 The unknown parameter vector θ is made of two types of parameters: those pa-
 2228 rameters that provide information about the physical observables of interest for the
 2229 experiment or *parameters of interest*, and the *nuisance parameters* that are not of
 2230 direct interest for the experiment but that need to be included in the analysis in
 2231 order to achieve a satisfactory description of the data; they represent effects of the
 2232 detector response like the finite resolutions of the detection systems, miscalibrations,
 2233 and in general any source of uncertainty introduced in the analysis.

2234 Nuisance parameters can be estimated from experimental data; for instance, data
 2235 samples from a test beam are usually employed for calibration purposes. In cases
 2236 where experimental samples are not availables, the estimation of nuisance parameters
 2237 makes use of dedicated simulation programs to provide the required samples.

2238 The estimation of the unknown parameters involves certain deviations from their
 2239 true values, hence, the measurement of the nuisance parameter is written in terms
 2240 of an estimated value, also called central value, $\hat{\theta}$ and its uncertainty $\delta\theta$ using the
 2241 notation

$$\theta = \hat{\theta} \pm \delta\theta \quad (5.9)$$

2242 where the interval $[\hat{\theta} - \delta\theta, \hat{\theta} + \delta\theta]$ is called *confidence interval*; it is usually interpreted,
 2243 in the limit of infinite number of experiments, as the interval where the true value
 2244 of the unknown parameter θ is contained with a probability of 0.6827 (if no other
 2245 convention is stated); this interval represents the area under a Gaussian distribution
 2246 in the interval $\pm 1\sigma$.

2247 The uncertainties associated with nuisance parameters produce *systematic uncer-*
 2248 *tainties* in the final measurement, while the uncertainties related only to fluctuations

2249 in data and that affect the determination of parameters of interest produce *statistical*
 2250 *uncertainties*.

2251 **5.2.2 Maximum likelihood estimation method**

2252 The estimation of the unknown parameters that are in best agreement with the ob-
 2253 served data is performed through a function of the data sample that returns the
 2254 estimate of those parameters; that function is called an *estimator*. Estimators are
 2255 usually constructed using mathematical expressions encoded in algorithms.

2256 In this thesis, the estimator used is the likelihood function $f(\mathbf{x}|\boldsymbol{\theta})$ ⁴ which depends
 2257 on a set of measured variables \mathbf{x} and a set of unknown parameters $\boldsymbol{\theta}$. The likelihood
 2258 function for N events in a sample is the combination of all the individual likelihood
 2259 functions, i.e.,

$$L(\boldsymbol{\theta}) = \prod_{i=1}^N f(\mathbf{x}^i|\boldsymbol{\theta}) = \prod_{i=1}^N f(x_1^i, \dots, x_n^i; \theta_1, \dots, \theta_m) \quad (5.10)$$

2260 and the estimation method used is the *Maximum Likelihood Estimation* method
 2261 (MLE); it is based on the combined likelihood function defined by eqn. 5.10 and
 2262 the procedure seeks for the parameter set that corresponds to the maximum value of
 2263 the combined likelihood function, i.e., the *maximum likelihood estimator* of the un-
 2264 known parameter vector $\boldsymbol{\theta}$ is the function that produces the vector of *best estimators*
 2265 $\hat{\boldsymbol{\theta}}$ for which the likelihood function $L(\boldsymbol{\theta})$ evaluated at the measured \mathbf{x} is maximum.

2266 Usually, the logarithm of the likelihood function is used in numerical algorithm
 2267 implementations in order to avoid underflow the numerical precision of the computers
 2268 due to the product of low likelihoods. In addition, it is common to minimize the
 2269 negative logarithm of the likelihood function, therefore, the negative log-likelihood

⁴ analogue to the likelihood functions described in previous sections

2270 function is

$$F(\boldsymbol{\theta}) = -\ln L(\boldsymbol{\theta}) = -\sum_{i=1}^N f(\mathbf{x}^i | \boldsymbol{\theta}). \quad (5.11)$$

2271 The minimization process is performed by the software MINUIT [134] implemented in the ROOT analysis framework. In case of data samples with large number 2272 of measurements, the computational resources necessary to calculate the likelihood 2273 function are too big; therefore, the parameter estimation is performed using binned 2274 distributions of the variables of interest for which the *binned likelihood function* is 2275 given by

$$L(\mathbf{x}|r, \boldsymbol{\theta}) = \prod_{i=1} \frac{(r \cdot s_i(\boldsymbol{\theta}) + b_i(\boldsymbol{\theta}))^{n_i}}{n_i!} e^{-r \cdot s_i(\boldsymbol{\theta}) - b_i(\boldsymbol{\theta})} \prod_{j=1} \frac{1}{\sqrt{2\pi}\sigma_{\theta_j}^2} e^{-(\theta_j - \theta_{0,j})^2/2\sigma_{\theta_j}^2}, \quad (5.12)$$

2277 with s_i and b_i the expected number of signal and background yields for the bin i , n_i 2278 is the observed number of events in the bin i and $r = \sigma/\sigma_{SM}$ is the signal strength. 2279 Note that the number of entries per bin follows a Poisson distribution. The effect 2280 of the nuisance parameters have been included in the likelihood function through 2281 the multiplication by a Gaussian distribution that models the nuisance. The three 2282 parameters, r , s_i and b_i are jointly fitted to estimate the value of r .

2283 5.3 Upper limits

2284 In this analysis, two hypotheses are considered; the background only hypothesis 2285 ($H_0(b)$) and the signal plus background hypothesis ($H_1(s+b)$), i.e., the sample of 2286 events is composed of background only events ($r=0$) or it is a mixture of signal plus 2287 background events ($r=1$). The exclusion of one hypothesis against the other means 2288 that the observed data sample better agrees with H_0 or rather with H_1 . In order 2289 to discriminate these hypotheses, a test statistic is constructed on the basis of the

2290 likelihood function evaluated for each of the hypothesis.

2291 The *Neyman-Pearson* lemma [135] states that the test statistic that provides the
 2292 maximum power for H_1 for a given significance level (background misidentification
 2293 probability α), is given by the ratio of the likelihood functions $L(\mathbf{x}|H_1)$ and $L(\mathbf{x}|H_0)$;
 2294 however, in order to use that definition it is necessary to know the true likelihood
 2295 functions, which in practice is not always possible. Approximate functions obtained
 2296 by numerical methods, like the BDT method described above, have to be used, so
 2297 that the *profile likelihood* test statistic is defined by

$$\lambda(\mathbf{r}) = \frac{L(\mathbf{x}|r, \hat{\boldsymbol{\theta}}(r))}{L(\mathbf{x}|\hat{r}, \hat{\boldsymbol{\theta}})}, \quad (5.13)$$

2298 where, \hat{r} and $\hat{\boldsymbol{\theta}}$ maximize the likelihood function, and $\hat{\boldsymbol{\theta}}$ maximizes the likelihood
 2299 function for a given value of the signal strength modifier r . In practice, the test
 2300 statistic t_r

$$t_r = -2\ln\lambda(r) \quad (5.14)$$

2301 is used to evaluate the presence of signal in the sample, since the minimum of t_r at
 2302 $r = \hat{r}$ suggests the presence of signal with signal strength \hat{r} . The uncertainty interval
 2303 for r is determined by the values of r for which $t_r = +1$.

2304 The expected probability density function (p.d.f) $f(t_r|r, \boldsymbol{\theta})$ of the test statistic t_r
 2305 can be obtained numerically by generating MC samples where one hypothesis, $H_0(b)$
 2306 or $H_1(s+b)$, is assumed; thus, MC samples contain the possible values of t_r obtained
 2307 from *pseudo-experiments* as shown in Figure 5.6. The probability that t_r takes a value
 2308 equal or greater than the observed value ($t_{r,obs}$) when a signal with a signal modifier
 2309 r is present in the data sample, is called the *p-value* of the observation; it can be
 2310 calculated using

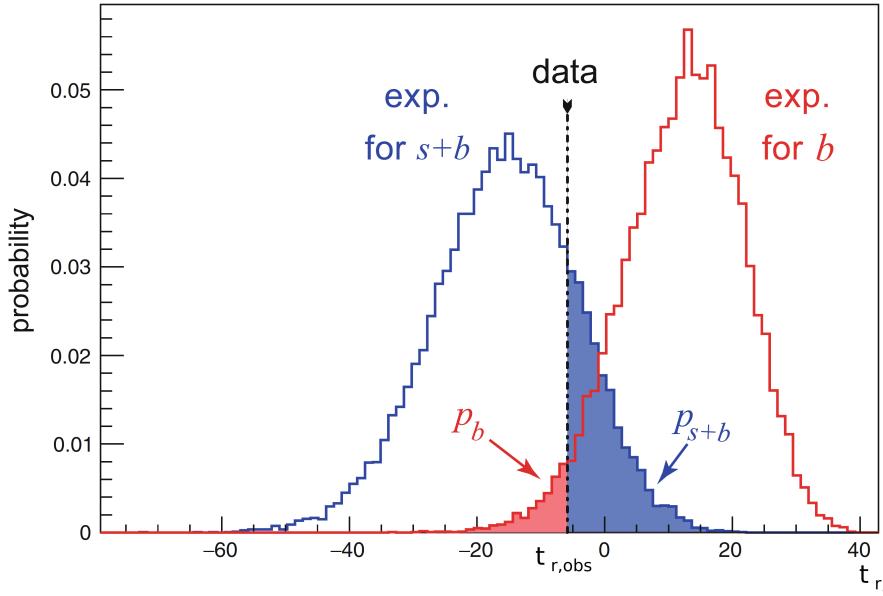


Figure 5.6: t_r p.d.f. from MC pseudo experiments assuming H_0 (red) and H_1 (blue). The black dashed line shows the value of the test statistic as measured from data. Adapted from Reference [128].

$$p_r = \int_{t_{r,obs}}^{\infty} f(t'_r | r, \boldsymbol{\theta}) dt'_r, \quad (5.15)$$

thus, $p_r < 0.05$ means that, for that particular value of r , H_1 could be excluded at 95% Confidence Level (CL). The corresponding background-only p-value is given by

$$1 - p_b = \int_{t_{r,obs}}^{\infty} f(t'_r | 0, \boldsymbol{\theta}) dt'_r, \quad (5.16)$$

If the t_r p.d.f.s for both hypotheses are well separated, as shown in the top side of Figure 5.7, the experiment is sensitive to the presence of signal in the sample. If the signal presence is small, both p.d.f.s will be largely overlapped (bottom of Figure ??) and either the signal hypothesis could be rejected with not enough justification because the experiment is not sensitive to the signal or a fluctuation of the background could be misinterpreted as presence of signal with the corresponding rejection of the

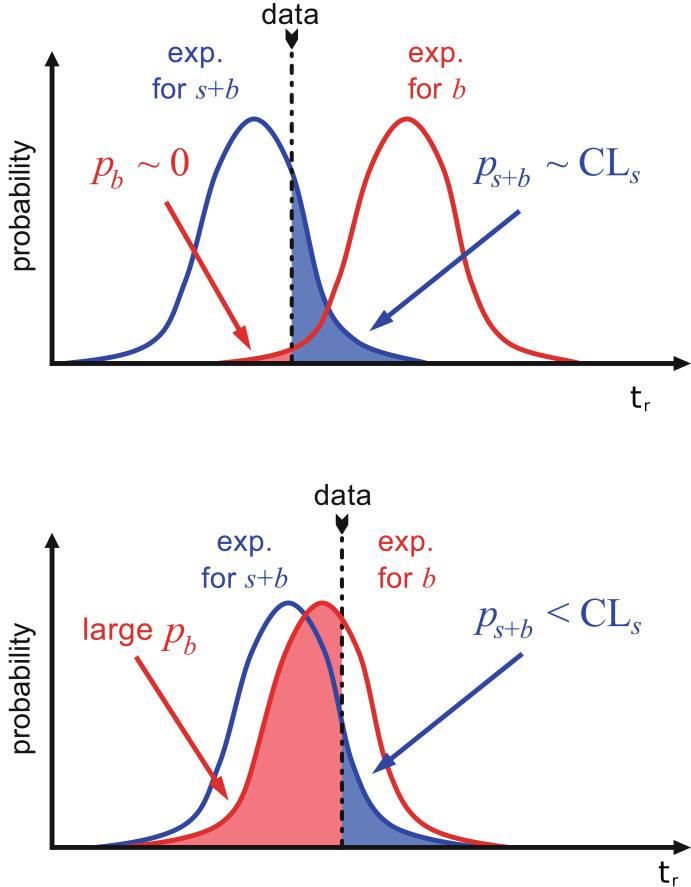


Figure 5.7: CL_s limit illustration. When the test statistic p.d.f. for the two hypotheses H_0 and H_1 are well separated (top) and when they are largely overlapped (bottom). Adapted from Reference [128].

2319 background-only hypothesis. These issues are corrected by using the modified p-
2320 value [136]

$$p'_r = \frac{p_r}{1 - p_b} \equiv CL_s. \quad (5.17)$$

2321 If H_1 is true, then p_b is small, $CL_s \simeq p_r$ and H_0 is rejected; if there is large
2322 overlap and an statistical fluctuation cause that p_b is large, then both numerator and
2323 denominator in Eqn. 5.17 become small but CL_s would allow the rejection of H_1
2324 even if there is poor sensitivity to signal.

The upper limit of the parameter of interest r^{up} is determined by excluding the range of values of r for which $CL_s(r, \theta)$ is lower than the confidence level desired, normally 90% or 95%, e.g, scanning over r and finding the value for which $p_r'^{up} = 0.05$. The expected upper limit can be calculated using pseudo-experiments based on the background-only hypothesis and obtaining a distribution for r_{ps}^{up} ; the median of that distribution corresponds to the expected upper limit, while the $\pm 1\sigma$ and $\pm 2\sigma$ deviations correspond to the values of the distribution that defines the 68% and 95% of the area under the distribution centered in the median. It is usual to present all the information about the expected and observed limits in the so-called *Brazilian-flag plot* as the one showed in Figure 5.8. The solid line represent the observed CL_s

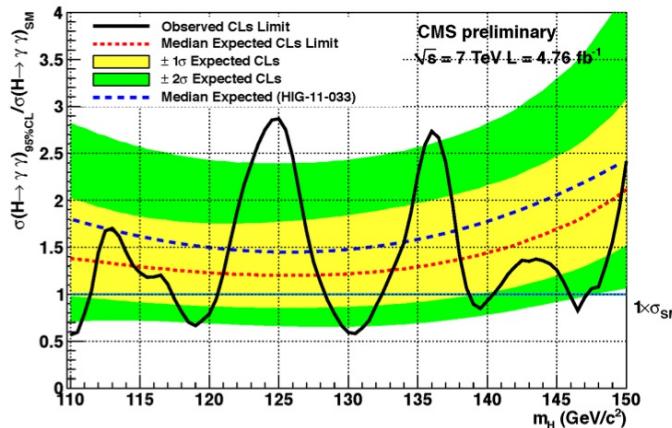


Figure 5.8: Brazilian flag plot of CMS experiment limits for Higgs boson decaying to photons [137].

2335 5.4 Asymptotic limits

As said before, the complexity of the likelihood functions, the construction of test statistics, and the calculation of the limits and their uncertainties is not always manageable and requires extensive computational resources; in order to overcome those issues, asymptotic approximations for likelihood-based test statistics, like the ones

2340 described in previous sections, have been developed [138, 139] using Wilks' theorem.
2341 Asymptotic approximations replace the construction of the test statistics p.d.f.s using
2342 MC pseudo-experiments, with the approximate calculation of the test statistics p.d.f.s
2343 by employing the so-called *Asimov dataset*.

2344 The Asimov dataset is defined as the dataset that produce the true values of the
2345 nuisance parameters when it is used to evaluate the estimators for all the parameters;
2346 it is obtained by setting the values of the variables in the dataset to their expected
2347 values [139].

2348 Limits calculated by using the asymptotic approximation and the Asimov dataset
2349 are know as *asymptotic limits*.

2350 **Chapter 6**

2351 **Search for production of a Higgs
2352 boson and a single top quark in
2353 multilepton final states in pp
2354 collisions at $\sqrt{s} = 13$ TeV**

2355 **6.1 Introduction**

2356 The Higgs boson discovery, supported on experimental observations and theoretical
2357 predictions made about the SM, gives the clue of the way in that elementary particles
2358 acquire mass through the Higgs mechanism; therefore, knowing the Higgs mass, the
2359 Higgs-vector boson and Higgs-fermion couplings can be determined. In order to test
2360 the Higgs-top coupling, several measurements have been performed, as stated in the
2361 chapter 1, but they are limited in sensitivity to measure the square of the coupling.
2362 The production of a Higgs boson in association with a single top quark (tH) not
2363 only offers access to the sign of the coupling, but also, to the CP phase of the Higgs

2364 couplings.

2365 This chapter presents the search for the associated production of a Higgs boson
 2366 and a single top quark (tHq) events, focusing on leptonic signatures provided by the
 2367 Higgs decay modes to WW , ZZ , and $\tau\tau$; the 13 TeV dataset produced in 2016, which
 2368 corresponds to an integrated luminosity of 35.9fb^{-1} , is used.

2369 As shown in Section 1.5, the SM cross section of tHq process is driven by a
 2370 destructive interference between two contributions (see Figure 1.15), where the Higgs
 2371 couples to either the W boson or the top quark; however, if the sign of the Higgs-
 2372 top coupling is flipped with respect to the SM prediction, a large enhancement of
 2373 the cross section occurs, making this analysis sensitive to such deviation. A second
 2374 process, where the Higgs boson and top quark are accompanied by a W boson (tHW)
 2375 has similar behavior, albeit with a weaker interference pattern and lower contribution
 2376 to the cross section, therefore, a combination of both processes would increase the
 2377 sensitivity to the sign of the coupling; in this analysis both contributions are combined
 2378 and referred as tH channel. A third contribution comes from $t\bar{t}H$ process. The purpose
 2379 of this analysis is to investigate the exclusion of the presence of the $tH + t\bar{t}H$ processes
 2380 under the assumption of the anomalous Higgs-top coupling modifier ($\kappa_t = -1$). The
 2381 analysis exploits signatures with two leptons of the same sign ($2lss$) channel and three
 2382 leptons ($3l$) channel in the final state.

2383 Constraints on the sign of the Higgs-top coupling (y_t) have been derived from the
 2384 decay rate of Higgs boson to photon pairs [50] and from the cross section for associated
 2385 production of Higgs and Z bosons via gluon fusion [141], with recent results disfavoring
 2386 negative signs of the coupling [44, 59, 142], although the negative sign coupling have
 2387 not been completely excluded.

2388 The analysis presented here, expands previous analyses performed at 8 TeV [143,
 2389 144] and searches for associated production of $t\bar{t}$ pair and a Higgs boson in the multi-

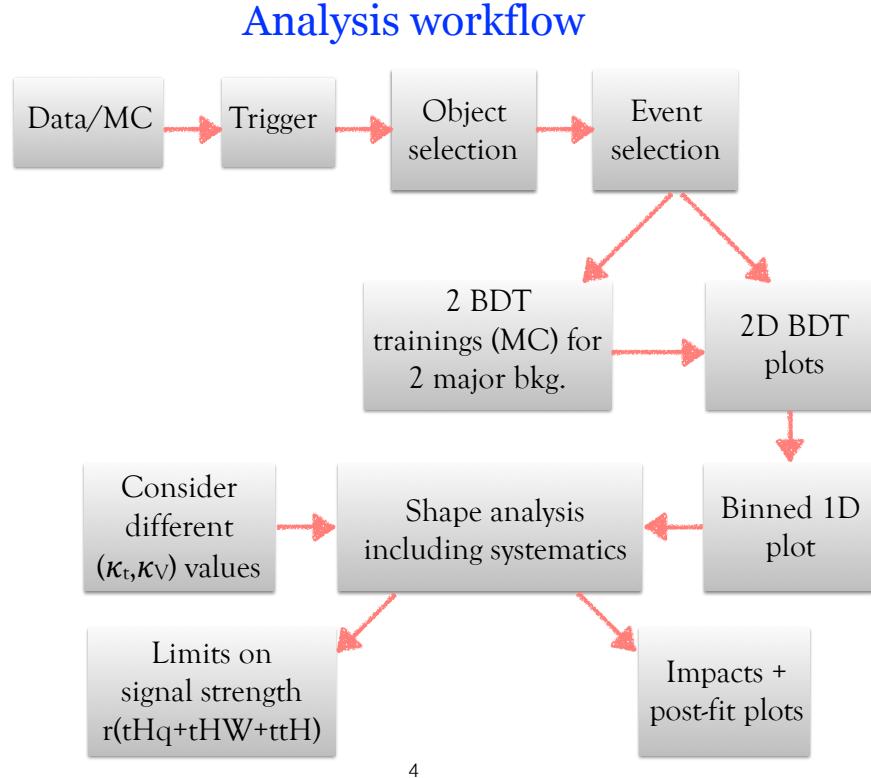
2390 lepton final state channel [145]; it also complements searches in other decay channels
 2391 targeting $H \rightarrow b\bar{b}$ [146].

2392 The first sections present the characteristic tHq signature as well as the expected
 2393 backgrounds. The MC samples, data sets, and the physics object definitions are
 2394 then defined. Following, the background predictions, the signal extraction, and the
 2395 statistical treatment of the selected events as well as the systematic uncertainties are
 2396 described. The final section present the results for the exclusion limits as a function
 2397 of the ratio of κ_t and the dimensionless modifier of the Higgs-vector boson coupling
 2398 κ_V .

2399 The analysis is designed to efficiently identify and select prompt leptons from on-
 2400 shell W and Z boson decays and to reject non-prompt leptons from b quark decays
 2401 and spurious lepton signatures from hadronic jets. Events are then selected in the
 2402 $2lss$ and $3l$ channels, and are required to contain hadronic jets, some of which must
 2403 be consistent with b quark hadronization. Finally, the signal yield is extracted by
 2404 simultaneously fitting the output of two dedicated multivariate discriminants, trained
 2405 to separate the tHq signal from the two dominant backgrounds, in all categories. The
 2406 fit result is then used to set an upper limit on the combined $t\bar{t}H + tH$ production
 2407 cross section, as a function of the relative coupling strengths of Higgs-top quark and
 2408 Higgs-Vector boson. Figure 6.1 shows an schematic overview of the analysis strategy
 2409 workflow.

2410 With respect to the 8 TeV analysis, the object selections have been adjusted for
 2411 the updated LHC running conditions at 13 TeV, the lepton identification has been
 2412 improved, and more powerful multivariate analysis techniques are used for the signal
 2413 extraction.

2414 The analysis has been made public by CMS as a Physics Analysis Summary [147]
 2415 combining the result for the three lepton and two lepton same-sign channels; the



4

Figure 6.1: A schematic overview of the analysis workflow. Based on sets of optimized physics object definitions and selection criteria, signal and background events in a data sample are discriminated. The discrimination is performed by a BDT, previously trained using MC samples of the dominant backgrounds, using discriminant variables based on the b -jet multiplicity, the activity in the forward region of the detector, and the kinematic properties of leptons. The CL_s limits on the combined $t\bar{t}H + tH$ production cross section, as a function of the relative coupling strengths are calculated.

2416 content present in this chapter is based on that document and on References [145,149]
 2417 unless other Reference is stated. Currently, an effort to turn the analysis into a paper
 2418 combining the multilepton and $H \rightarrow b\bar{b}$ is ongoing.

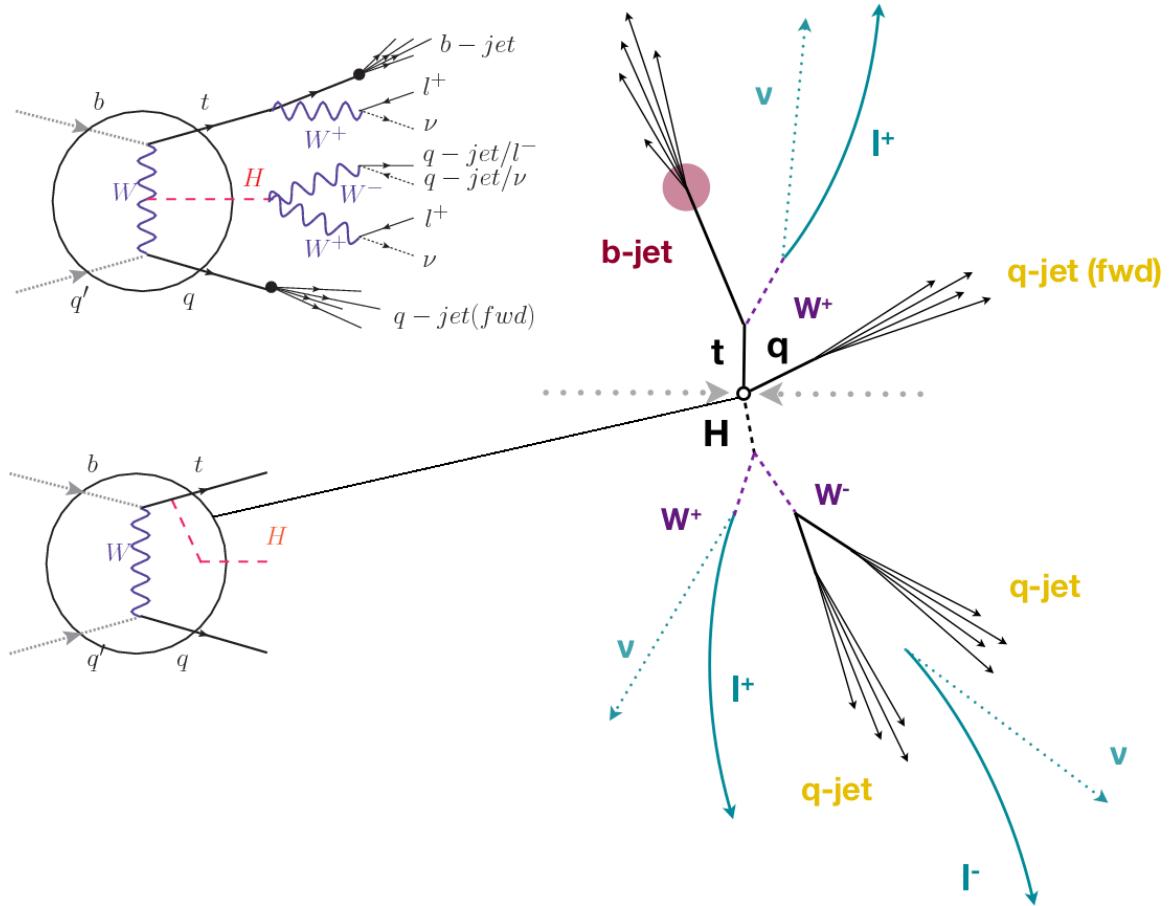


Figure 6.2: tHq event signature. Left: Feynman diagram including the whole evolution up to the final state for the case of the Higgs boson emitted by the W boson (top); Feynman diagram for the case where the Higgs boson is emitted by the top quark. Right: Schematic view as it would be seen in the detector; the circle in the Feynman diagrams on the left corresponds to the circle in the center of the schematic view as indicated by the line connecting them. In the $2lss$ channel, one of the W bosons from the Higgs boson decays to two light-quark jets while in the $3l$ channel both W bosons decay to leptons.

2419 6.2 tHq signature

2420 In order to select events of tHq process, its features are translated into a set of
 2421 selection rules; Figure 6.2 shows the Feynman diagram and an schematic view of the
 2422 tHq process from the pp collision to the final state configuration. A single top quark
 2423 is produced accompanied by a light quark, denoted as q ; this light quark is produced

2424 predominantly in the forward region of the detector. The Higgs boson can be either
 2425 emitted by the exchanged W boson or directly by the singly produced top quark.

2426 Due to their high masses/short lifetimes, top quark and Higgs boson decay after
 2427 their production within the detector. The Higgs boson is required to decay into a W
 2428 boson pair¹. The top quark almost always decays into a bottom quark and a W boson,
 2429 as encoded in the CMK matrix. The W bosons are required to decay leptonically
 2430 either all the three in the $3l$ channel or the pair with equal electrical charge in the
 2431 $2lss$ channel case; τ leptons are not reconstructed separately and only their leptonic
 2432 decays into either electrons or muons are considered in this analysis.

2433 In summary, the signal process is characterized by a the final state with

2434 • one light-flavored forward jet,

2435 • one central b-jet,

2436 • $2lss$ channel → two leptons of the same sign, two neutrinos and two light (often
 2437 soft) jets,

2438 • $3l$ channel → three leptons, three neutrinos and no central light-flavored jets,

2439 The presence of neutrinos is inferred from the presence of MET.

2440 6.3 Background processes

2441 The background processes are those that can mimic the signal signature or at least
 2442 can be reconstructed as that as a result of certain circumstances. The backgrounds
 2443 can be classified as

¹ ZZ and $\tau\tau$ decays are also include in the analysis but they are not separately reconstructed

- 2444 • irreducible backgrounds: where genuine prompt leptons are produced in on-
 2445 shell W and Z boson decays; they can be reliably estimated directly from MC
 2446 simulated events, using higher-order cross sections or data control regions for
 2447 the overall normalization.
- 2448 • reducible backgrounds: where at least one of the leptons is *non-prompt*, i.e.,
 2449 produced within a hadronic jet; genuine leptons from heavy flavor decays and
 2450 misreconstructed jets, also known as *mis-ID leptons* or *fake leptons*, are consid-
 2451 ered non-prompt leptons. These non-prompt leptons leave tracks and hits in
 2452 the detection systems as would a prompt lepton, but correlating those hits with
 2453 nearby jets could be a way of removing them. The misassignment of electron
 2454 charge in processes like $t\bar{t}$ or Drell-Yan, represent an additional source of back-
 2455 ground, but it is relevant only for the $2lss$ channel. Reducible backgrounds are
 2456 not well predicted by simulation, hence, they are estimated using data-driven
 2457 methods.

2458 The main sources of background events for tHq process are $t\bar{t}$ process and $t\bar{t} +$
 2459 $X(X = W, Z, \gamma)$ processes, the latter regarded together as $t\bar{t}V$ process. Figure 6.3
 2460 shows the signature for $t\bar{t}$ and $t\bar{t}W$ processes.

2461 The largest contribution to irreducible backgrounds comes from $t\bar{t}W$ and $t\bar{t}Z$ processes
 2462 for which the number of ($b-$)jets (($b-$)jet multiplicity) is higher than that of the sig-
 2463 nal events, while for other contributing background events, WZ , ZZ , and rare SM
 2464 processes like $W^\pm W^\pm qq$, $t\bar{t}t\bar{t}$, tZq , tZW , WWW , WWZ , WZZ , ZZZ , the ($b-$)jet
 2465 multiplicity is lower compared to that of the signal events. None of the irreducible
 2466 backgrounds present activity in the forward region of the detector.

2467 On the side of the reducible backgrounds, the largest contribution comes from the
 2468 $t\bar{t}$ events which have a very similar signature to the signal events but does no present

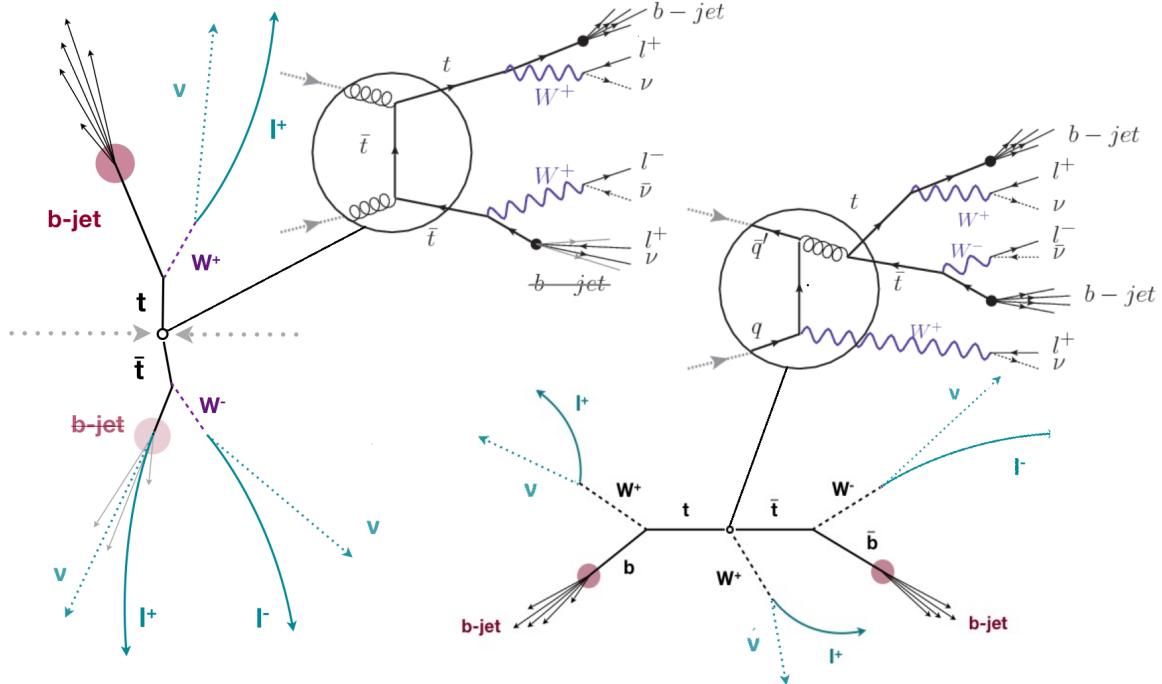


Figure 6.3: $t\bar{t}$ (left) and $t\bar{t}W$ (right) events signature as they would be seen in the detector; the Feynman diagrams including the whole evolution up to the final state are also showed. The $t\bar{t}$ process signature is very similar to that of the signal process with one fake lepton and no forward activity. The $t\bar{t}W$ process present a higher b-jet multiplicity compared to the signal process, a prompt lepton and no forward activity.

2469 activity in the forward region of the detector either; A particular feature of the $t\bar{t}$
 2470 events is their charge-symmetry, which is also a difference with respect to the signal
 2471 events.

2472 6.4 Data and MC Samples

2473 6.4.1 Full 2016 data set

2474 The data set used in this analysis was collected by the CMS experiment during 2016
 2475 at while running at $\sqrt{s} = 13\text{TeV}$ and corresponds to a total integrated luminosity
 2476 of 35.9fb^{-1} . Only periods when the CMS magnet was on were considered when

2477 selecting the data samples; that corresponds to the 23Sep2016 (Run B to G) and
 2478 PromptReco (Run H) versions of the datasets.

2479 Multilepton final states with either two same-sign leptons or three leptons tar-
 2480 get the case where the Higgs boson decays to a pair of W bosons, τ leptons, or Z
 2481 bosons, and where the top quark decays leptonically, hence, the SingleElectron,
 2482 SingleMuon, DoubleEG, MuonEG, DoubleMuon dataset (see Table A.1) compose the
 2483 full dataset. The certified luminosity sections are selected using the golden JSON file
 2484 defined by the CMS experiment [148].

2485 6.4.2 Triggers

2486 The events considered are those online-reconstructed events triggered by one, two, or
 2487 three leptons. Single-lepton triggers are included in order to boost the acceptance
 2488 of events where the p_T of the sub-leading lepton falls below the threshold of the
 2489 double-lepton triggers. The trigger efficiency is increased by including double-lepton
 2490 triggers in the $3l$ category, and single-lepton triggers in all categories; it is possible
 2491 given the logical “or” of the trigger decisions of all the individual triggers in a given
 2492 category. Table A.2 shows the lowest-threshold non-prescaled triggers present in the
 2493 High-Level Trigger (HLT) menus for both Monte-Carlo and data in 2016.

2494 Trigger efficiency scale factors

2495 Trigger efficiency describes the ability of events to pass the trigger requirements. It
 2496 is measured in simulated events using generator information given that there is no
 2497 trigger bias with the MC sample. Measuring the trigger efficiency in data requires a
 2498 more elaborated procedure; first, select a set of events collected by a trigger that is
 2499 uncorrelated with the lepton triggers such that the selected events form an unbiased

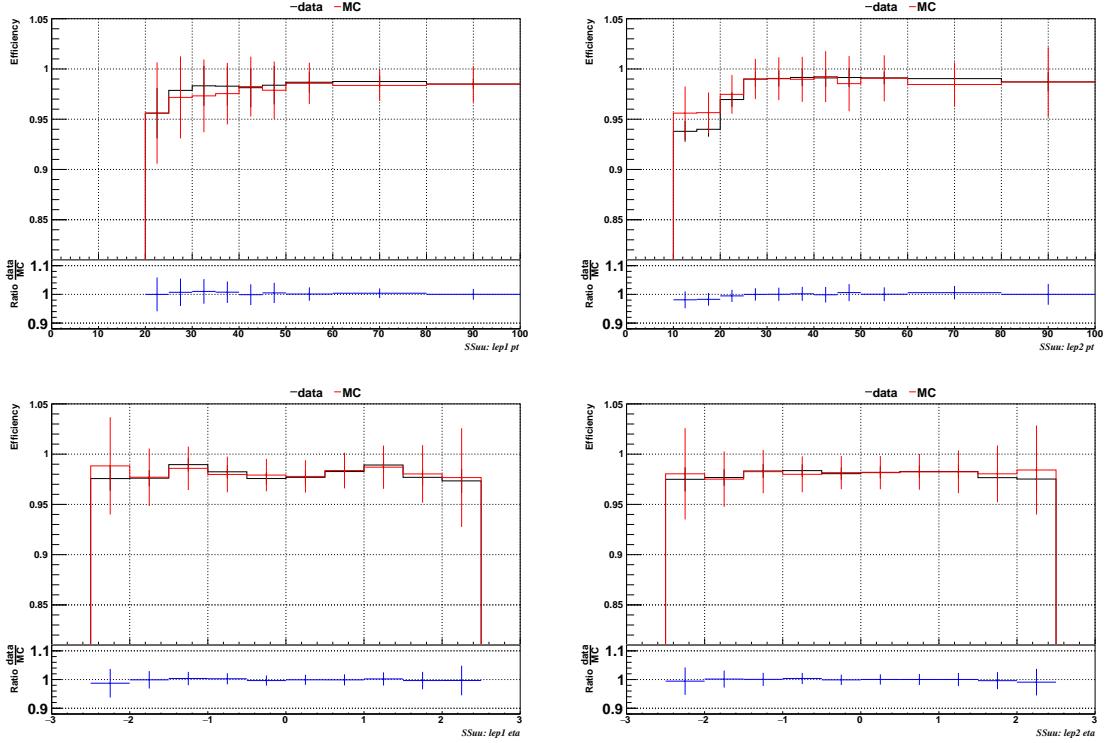


Figure 6.4: Comparison between data and MC trigger efficiencies in the same-sign $\mu\mu$ category, as a function of the p_T and η of the leading lepton (left) and the sub-leading lepton (right) [149].

sample. In this analysis, that uncorrelated trigger is a MET trigger. Second step is looking for candidate events with exactly two good leptons (exactly three good leptons for the $3l$ channel). Finally, measure the efficiency for the candidate events to pass the logical “or” of triggers being considered in a given event category as defined in Table A.2.

Comparisons between the data and MC efficiencies for each category, showed in Figures 6.4, 6.5, and 6.6, reveal that they are in good agreement; the difference is corrected by applying scale factors derived from the ratio between both efficiencies.

Applied flat scale factors in each category are shown in Table 6.1; they have been inherited from Reference [149].

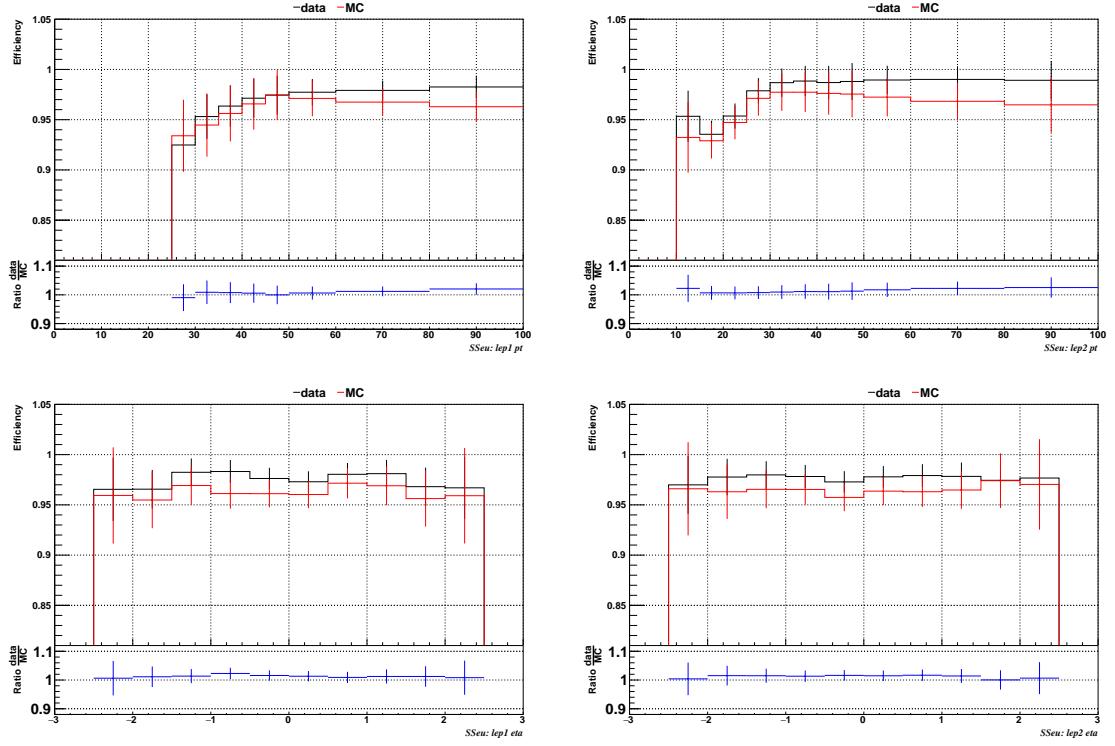


Figure 6.5: Comparison between data and MC trigger efficiencies in the same-sign $e\mu$ category as a function of the p_T and η of the leading lepton (left) and the sub-leading lepton (right) [149].

Category	Scale Factor
ee	1.01 ± 0.02
$e\mu$	1.01 ± 0.01
$\mu\mu$	1.00 ± 0.01
3l	1.00 ± 0.03

Table 6.1: Trigger efficiency scale factors and associated uncertainties, shown here rounded to the nearest percent.

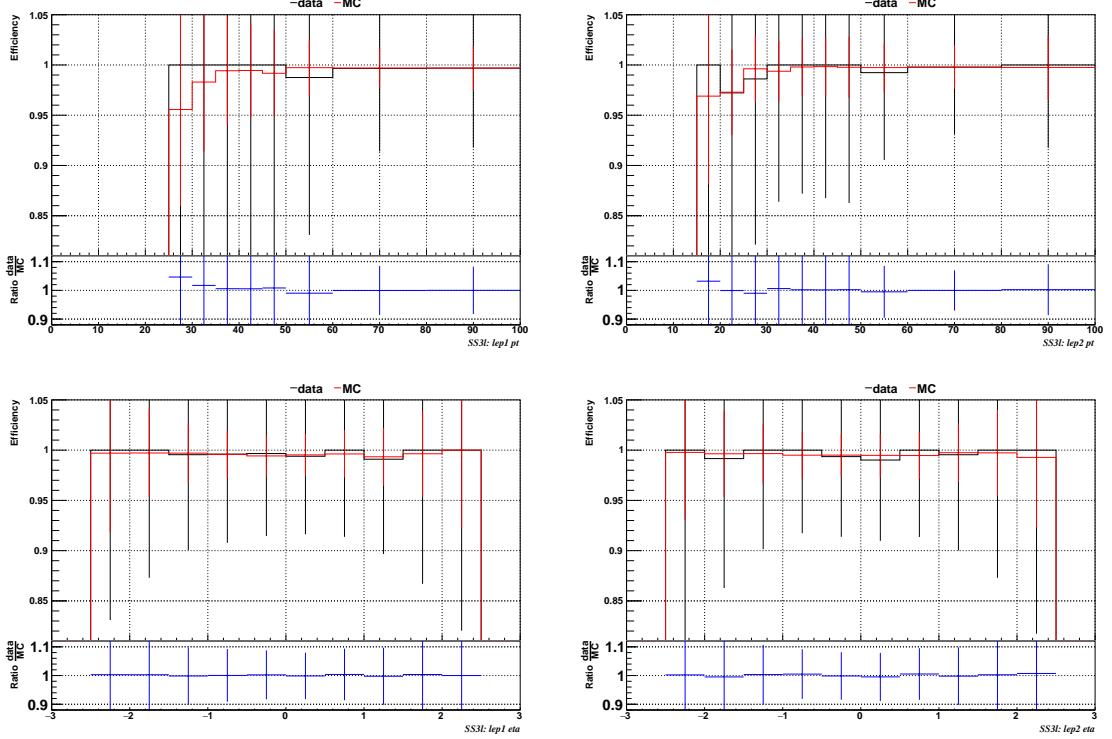


Figure 6.6: Comparison between data and MC trigger efficiencies in the $3l$ category, as a function of the p_T and η of the leading lepton (left) and the sub-leading lepton (right) [149].

2510 6.4.3 MC samples

2511 Current event generators allow for adjusting the kinematics of the generated events,
 2512 based on an event-wise reweighting; in this way, several generation parameters phase
 2513 spaces can be explored according to the experimental interests. The signal samples
 2514 used in this analysis were generated in such a way that not only the case $\kappa_t = -1$, but
 2515 an extended range of κ_t and κ_V values may be investigated.

2516 tHq and tHW cross section in the κ_t - κ_V phase space are shown in Figure 6.7. As
 2517 said in section 3.1, the tHq sample was generated using the 4F scheme which provides
 2518 a better description of the additional b quark from the initial gluon splitting, while the
 2519 tHW sample was generated using the 5F scheme in order to remove its interference
 2520 with $t\bar{t}H$ at LO.

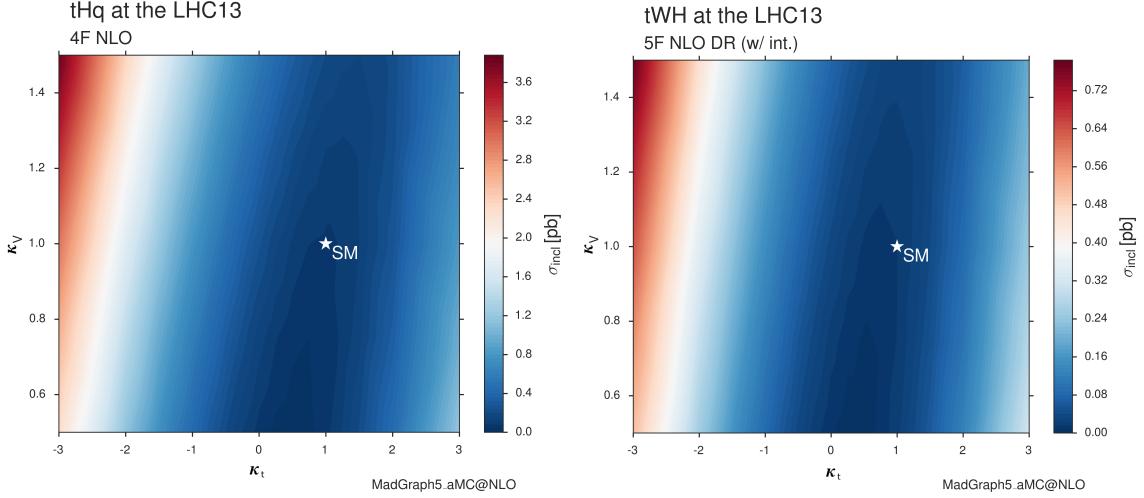


Figure 6.7: tHq and tHW cross section in the κ_t - κ_V phase space [150].

2521 MC signal samples

2522 The two signal samples, tHq and tHW , correspond to the `RunIISummer16MiniAODv2`
 2523 campaign produced with `CMSSW_80X`; they were produced with `MG5_aMC@NLO`
 2524 (version 5.2.2.3), in LO order mode at $\sqrt{s} = 13$ TeV, and are normalized to NLO cross
 2525 sections (see Table 6.2). The Higgs boson is assumed to be SM-like except for the
 2526 values of its couplings to the top quark and W boson. Each sample was generated
 2527 with a set of event weights corresponding to 51 different values of (κ_t, κ_V) couplings,
 2528 accessible in terms of LHE event weights as shown in Table A.3; however, the main
 2529 interest is the $(\kappa_t = -1, \kappa_V = 1)$ case.

Sample	σ [pb]	BF
<code>/THQ_Hincl_13TeV-madgraph-pythia8_TuneCUETP8M1/</code>	0.7927	0.324
<code>/THW_Hincl_13TeV-madgraph-pythia8_TuneCUETP8M1/</code>	0.1472	1.0
<code>/tthJetToNonbb_M125_13TeV_amcatnloFXFX_madspin_pythia8_mWCutfix/</code>	0.2151	1.0

Table 6.2: MC signal samples used in this analysis; cross section and branching fraction are also listed [150].

2530 The $t\bar{t}H$ sample was produced using `AMC@NLO` interfaced to `PYTHIA 8` for
 2531 the parton shower, and is scaled to NLO cross sections. The $t\bar{t}H$ cross section depends

2532 quadratically on κ_t ; however, in contrast to the tHq and tHW samples, the scaling
 2533 is not performed during the sample generation process but in the analysis code since
 2534 it was decided to include the $t\bar{t}H$ process as part of the signal in the course of the
 2535 analysis.

2536 **MC background samples**

2537 Several MC generators were used to generate the samples of the background processes.
 2538 The dominant background sources ($t\bar{t}$, $t\bar{t}W$, $t\bar{t}Z$) were produced using AMC@NLO
 2539 interfaced to PYTHIA8, and are scaled to NLO cross sections. Other minor back-
 2540 ground processes are simulated using POWHEG interfaced to PYTHIA, or bare
 2541 PYTHIA as stated in the sample names in Table A.4. Pileup interactions are in-
 2542 cluded in the simulation in order to reflect the observed multiplicity in data; the
 2543 simulated events are weighted according to the actual pileup in data, estimated from
 2544 the measured bunch-to-bunch instantaneous luminosity and the total inelastic cross
 2545 section, 69.2 mb. All events are finally passed through a full simulation of the CMS
 2546 detector based on GEANT4, and reconstructed using the same algorithms as used for
 2547 the data.

2548 **6.5 Object Identification**

2549 In this section, the specific definitions of the physical objects in terms of the numerical
 2550 values assigned to the reconstruction parameters are presented; thus, the provided
 2551 details summarize and complement the descriptions presented in previous chapters.
 2552 The object reconstruction and selection strategy used in this thesis is inherited from
 2553 the analyses in References [145, 149], thus, the information in this section is extracted
 2554 from those documents unless other References are stated.

2555 **6.5.1 Lepton reconstruction and identification**

2556 Two types of leptons are defined in this analysis: *signal leptons* are those coming from
 2557 W, Z and τ decays which usually are isolated from other particles; *background leptons*
 2558 are defined as leptons produced in b -jet hadron decays, light-jets misidentification,
 2559 and photon conversions.

2560 The process of reconstruction and identification of electron and muon candidates
 2561 was described in chapter3, hence, the identification variables used in order to retain
 2562 the highest possible efficiency for signal leptons while maximizing the rejection of
 2563 background leptons are listed and described in the following sections ².

2564 The identification variables include not only observables related directly to the re-
 2565 constructed leptons themselves, but also to the clustered energy deposits and charged
 2566 particles in a cone around the lepton direction (jet-related variables); an initial loose
 2567 preselection of leptons candidates is performed and then an MVA discriminator, re-
 2568 ferred to as *lepton MVA* discriminator, is used to distinguish signal leptons from
 2569 background leptons.

2570 **Muons**

2571 The Physics Objects Groups (POG) at CMS, are in charge of studying and defining
 2572 the set of selection criteria applied on the course of reconstruction and identification
 2573 of particles. These selection criteria are implemented in the CMS framework in the
 2574 form of several object identification working points according to the strength of the
 2575 requirements.

2576 The muon candidates are reconstructed by combining information from the tracker
 2577 system and the muon detection system of CMS detector and the POG defined three

² the studies performed to optimize the identification are far from the scope of this thesis, therefore, only general descriptions are provided

2578 working points for muon identification *MuonID* [153];

- 2579 • *POG Loose Muon ID* is a particle identified as a muon by the PF event re-
 2580 construction and also reconstructed either as a global-muon or as an arbitrated
 2581 tracker-muon. This identification criteria is designed to be highly efficient for
 2582 prompt muons and for muons from heavy and light quark decays; it can be com-
 2583 plemented by applying impact parameter cuts in analyses with prompt muon
 2584 signals.
- 2585 • *POG Medium Muon ID* is a Loose muon with additional track-quality and
 2586 muon-quality (spatial matching between the individual measurements in the
 2587 tracker and the muon system) requirements. This identification criteria is de-
 2588 signed to be highly efficient in the separation of the muons coming from decay
 2589 in flight of heavy quarks and muons coming from B meson decays as well as
 2590 prompt muons. An additional category *MVA Prompt ID* is defined in this iden-
 2591 tification criteria directed to discriminated muons from B mesons and prompt
 2592 muons (from W,Z and τ decays). The Medium ID provides the same fake rate as
 2593 the Tight Muon ID but a higher efficiency on prompt and B-decays muons. [154]
- 2594 • *POG Tight Muon ID* is a global muon with additional muon-quality require-
 2595 ments Tight Muon ID selects a subset of the PF muons.

2596 Only muons within the muon system acceptance $|\eta| < 2.4$ and minimum p_T of 5
 2597 GeV are considered.

2598 **Electrons**

2599 Electrons are reconstructed using information from the tracker and from the electro-
 2600 magnetic calorimeter and identified by an MVA algorithm (*MVA eID* discriminant)

2601 using the shape of the calorimetric shower variables like the shape in η and ϕ , the clus-
 2602 ter circularity, widths along η and ϕ ; track-cluster matching variables like E_{tot}/p_{in} ,
 2603 E_{Ele}/p_{out} , $\Delta\eta_{in}$, $\Delta\eta_{out}$, $\Delta\phi_{in}$, $1/E - 1/p$; and track quality variables like χ^2 of the
 2604 GSF tracks, the number of hits used by the GSF filter [155].

2605 A loose selection based on η -dependent cuts on this discriminant is used to prese-
 2606 lect electron candidates, the full shape of the discriminant is used in the lepton MVA
 2607 selection to separate signal leptons from background leptons (described in Section
 2608 6.5.1).

2609 In order to reject electrons from photon conversions, electron candidates with
 2610 missing hits in the pixel tracker layers or matched to a conversion secondary vertex
 2611 are discarded. Electrons are selected for the analysis if they have $p_T > 7$ GeV and
 2612 are located within the tracker system acceptance region ($|\eta| < 2.5$).

2613 Lepton vertexing and pile-up rejection

2614 The impact parameter in the transverse plane d_0 , impact parameter along the z -
 2615 axis d_z , and the impact parameter significance in the detector space SIP_{3D} , are
 2616 considered to perform the identification and rejection of pile-up, misreconstructed
 2617 tracks, and background leptons from b-hadron decays; pile-up and misreconstructed
 2618 track mitigation is achieved by imposing loose cuts on the impact parameter variables.
 2619 The full shape of the those variables is used in a lepton MVA classifier to achieve the
 2620 best separation between the signal and the background leptons.

2621 Lepton isolation

2622 PF is able to recognize leptons from two different sources: on one side, leptons from
 2623 the decays of heavy particles, such as W and Z bosons, which are normally isolated
 2624 in space from the hadronic activity in the event; on the other side, leptons from the

2625 decays of hadrons and jets misidentified as leptons, which are not isolated as the
 2626 former. For highly boosted systems, like the lepton and the b -jet generated in the
 2627 semileptonic decay of a boosted top, the decay products tend to be more closer and
 2628 sometimes they even overlap; thus, the PF standard definition of isolation in terms of
 2629 the separation between the lepton candidates and other PF objects in the η - ϕ plane,

$$\Delta R = \sqrt{(\eta^l - \eta^i)^2 + (\phi^l - \phi^i)^2} < 0.3 \quad (6.1)$$

2630 which considers all the neutral, charged hadrons and photons in a cone around the
 2631 leptons, is refocused to the local isolation of the leptons through the mini-isolation
 2632 I_{mini} [156] defined as the sum of particle flow candidates p_T within a cone around
 2633 the lepton, corrected for the effects of pileup and divided by the lepton p_T

$$I_{mini} = \frac{\sum_R p_T(h^\pm) - \max\left(0, \sum_R p_T(h^0) + p_T(\gamma) - \rho \mathcal{A}\left(\frac{R}{0.3}\right)^2\right)}{p_T(l)} \quad (6.2)$$

2634 where ρ is the pileup energy density, h^\pm, h^0, γ, l , represent the charged hadron, neutral
 2635 hadrons, photons, and the lepton, respectively. The radius R of the cone depends on
 2636 the p_T of the lepton according to

$$R = \frac{10\text{GeV}}{\min(\max(p_T(l), 50\text{GeV}), 200\text{GeV})}, \quad (6.3)$$

2637 The p_T dependence of the cone size allows for greater signal efficiency. Setting a
 2638 cut on I_{mini} below a given threshold ensures that the lepton is locally isolated, even
 2639 in boosted systems. The effect of pileup is mitigated using the so-called effective area
 2640 correction \mathcal{A} listed in Table 6.3.

2641 A loose cut on I_{mini} is applied to pre-select the muon and electron candidates;

$ \eta $ range	$\mathcal{A}(e)$ neutral/charged	$A(\mu)$ neutral/charged
0.0 - 0.8	0.1607 / 0.0188	0.1322 / 0.0191
0.8 - 1.3	0.1579 / 0.0188	0.1137 / 0.0170
1.3 - 2.0	0.1120 / 0.0135	0.0883 / 0.0146
2.0 - 2.2	0.1228 / 0.0135	0.0865 / 0.0111
2.2 - 2.5	0.2156 / 0.0105	0.1214 / 0.0091

Table 6.3: Effective areas, for electrons and muons used to mitigate the effect of pileup by using the so-called effective area correction.

however, the full shape is used in the lepton MVA discriminator when performing the signal lepton selection.

Jet-related variables

In order to reject misidentified leptons from b -jets, mostly coming from $t\bar{t}$ +jets, Drell-Yan+jets, and W +jets events, the vertexing and isolation described in previous sections are complemented with additional variables related to the closest reconstructed jet to the lepton, i.e., the PF jets reconstructed³ around the leptons with $\Delta R = \sqrt{(\eta^l - \eta^{jet})^2 + (\phi^l - \phi^{jet})^2} < 0.5$. The identification variables used in the MVA discriminator are the ratio p_T^l/p_T^{jet} , the CSV b-tagging discriminator value of the jet, the number of charged tracks of the jet, and the relative p_T given by

$$p_T^{rel} = \frac{(\vec{p}_{jet} - \vec{p}_l) \cdot \vec{p}_l}{||\vec{p}_{jet} - \vec{p}_l||}. \quad (6.4)$$

LeptonMVA discriminator

Electrons and muons passing the basic selection process described above are referred to as *loose leptons*. Additional discrimination between signal leptons and background leptons is crucial considering that the rate of $t\bar{t}$ production is much larger than the signal, hence, an overwhelming background from $t\bar{t}$ production. To maximally ex-

³ charged hadrons from PU vertices are not removed prior to the jet clustering.

2657 ploit the available information in each event to that end, the dedicated lepton MVA
 2658 discriminator, based on a boosted decision tree (BDT) algorithm, has been built so
 2659 that all the identification variables can be used together.

2660 The lepton MVA discriminator training is performed using simulated signal Loose
 2661 leptons from the $t\bar{t}H$ MC sample and fake leptons from the $t\bar{t}$ +jets MC sample,
 2662 separately for muons and electrons. The input variables used include vertexing, iso-
 2663 lation and jet-related variables, the p_T and η of the lepton, the electron MVA eID
 2664 discriminator and the muon segment-compatibility variables. An additional require-
 2665 ment known as *tight-charge* requirement, is imposed by comparing two independent
 2666 measurement of the charge, one from the ECAL supercluster and the other from the
 2667 tracker; thus, the consistency in the measurements of the electron charge is ensured
 2668 so that events with a wrong electron charge assignment are rejected; this variable is
 2669 particularly used in the $2lss$ channel to suppress opposite-sign events for which the
 2670 charge of one of the leptons has been mismeasured. The tight-charge requirement for
 2671 muons is represented by the requirement of a consistently well measured track trans-
 2672 verse momentum given by $\Delta p_T/p_T < 0.2$. Leptons are selected for the final analysis
 2673 if they pass a given threshold of the BDT output, and are referred to as *tight leptons*
 2674 in the following.

2675 The validation of the lepton MVA algorithm and the lepton identification variables
 2676 is performed using data in various control regions; the details about that validation
 2677 are not discussed here but can be found in Reference [149].

2678 Selection definitions

2679 Electron and muon object identification is defined in three different sets of selections
 2680 criteria; the *Loose*, *Fakeable Object*, and *Tight* selection. These three levels of selection
 2681 are designed to serve for event level vetoes, the fake rate estimation application region

2682 (see Section 6.7.2), and the final signal selection, respectively. The p_T of fakeable
 2683 objects is defined as $0.85 \times p_T(\text{jet})$, where the jet is the one associated to the lepton
 2684 object. This mitigates the dependence of the fake rate on the momentum of the
 2685 fakeable object and thereby improves the precision of the method.

2686 Tables 6.4 and 6.5 list the full criteria for the different selections of muons and
 2687 electrons.

Cut	Loose	Fakeable object	Tight
$ \eta < 2.4$	✓	✓	✓
p_T	$> 5\text{GeV}$	$> 15\text{GeV}$	$> 15\text{GeV}$
$ d_{xy} < 0.05$ (cm)	✓	✓	✓
$ d_z < 0.1$ (cm)	✓	✓	✓
$\text{SIP}_{3D} < 8$	✓	✓	✓
$I_{\text{mini}} < 0.4$	✓	✓	✓
is Loose Muon	✓	✓	✓
jet CSV	–	< 0.8484	< 0.8484
is Medium Muon	–	–	✓
tight-charge	–	–	✓
lepMVA > 0.90	–	–	✓

Table 6.4: Requirements on each of the three muon selections. In the cases where the cut values change between the selections, those values are listed in the table. Otherwise, whether the cut is applied is indicated.

2688 In addition to the previously defined requirements for jets, they are required to
 2689 be separated from any lepton candidates passing the fakeable object selections by
 2690 $\Delta R > 0.4$.

2691 6.5.2 Lepton selection efficiency

2692 Efficiencies of reconstruction and selecting loose leptons are measured both for muons
 2693 and electrons using a tag and probe method on both data and MC, using $Z \rightarrow \ell^+ \ell^-$
 2694 [157]. The scale factors are derived from the ratio of efficiencies $\varepsilon_i(p_T, \eta)$ measured

Cut	Loose	Fakeable Object	Tight
$ \eta < 2.5$	✓	✓	✓
p_T	$> 7\text{GeV}$	$> 15\text{GeV}$	$> 15\text{GeV}$
$ d_{xy} < 0.05 \text{ (cm)}$	✓	✓	✓
$ d_z < 0.1 \text{ (cm)}$	✓	✓	✓
$\text{SIP}_{3D} < 8$	✓	✓	✓
$I_{\text{mini}} < 0.4$	✓	✓	✓
MVA eID $> (0.0, 0.0, 0.7)$	✓	✓	✓
$\sigma_{in\eta} < (0.011, 0.011, 0.030)$	—	✓	✓
$\text{H/E} < (0.10, 0.10, 0.07)$	—	✓	✓
$\Delta\eta_{in} < (0.01, 0.01, 0.008)$	—	✓	✓
$\Delta\phi_{in} < (0.04, 0.04, 0.07)$	—	✓	✓
$-0.05 < 1/E - 1/p < (0.010, 0.010, 0.005)$	—	✓	✓
p_T^{ratio}	—	$> 0.5^\dagger / -$	—
jet CSV	—	$< 0.3^\dagger / < 0.8484$	< 0.8484
tight-charge	—	—	✓
conversion rejection	—	—	✓
Number of missing hits	< 2	$== 0$	$== 0$
lepton MVA > 0.90	—	—	✓

Table 6.5: Criteria for each of the three electron selections. In cases where the cut values change between selections, those values are listed in the table. Otherwise, whether the cut is applied is indicated. In some cases, the cut values change for different η ranges. These ranges are $0 < |\eta| < 0.8$, $0.8 < |\eta| < 1.479$, and $1.479 < |\eta| < 2.5$ and the respective cut values are given in the form (value₁, value₂, value₃). For the two p_T^{ratio} and CSV rows, the cuts marked with a \dagger are applied to leptons that fail the lepton MVA cut, while the loose cut value is applied to those that pass the lepton MVA cut.

2695 for a given lepton in data/MC, according to

$$\rho(p_T, \eta) = \frac{\varepsilon_{\text{data}}(p_T, \eta)}{\varepsilon_{\text{MC}}(p_T, \eta)}. \quad (6.5)$$

2696 The scale factor for each event is used to correct the weight of the event in the
 2697 full sample; therefore, the full simulation correction is given by the product of all
 2698 the individual scale factors. The scale factors used in this thesis are inherited from
 2699 Reference [149] which in turns inherited them from leptonic SUSY analyses using
 2700 equivalent lepton selections.

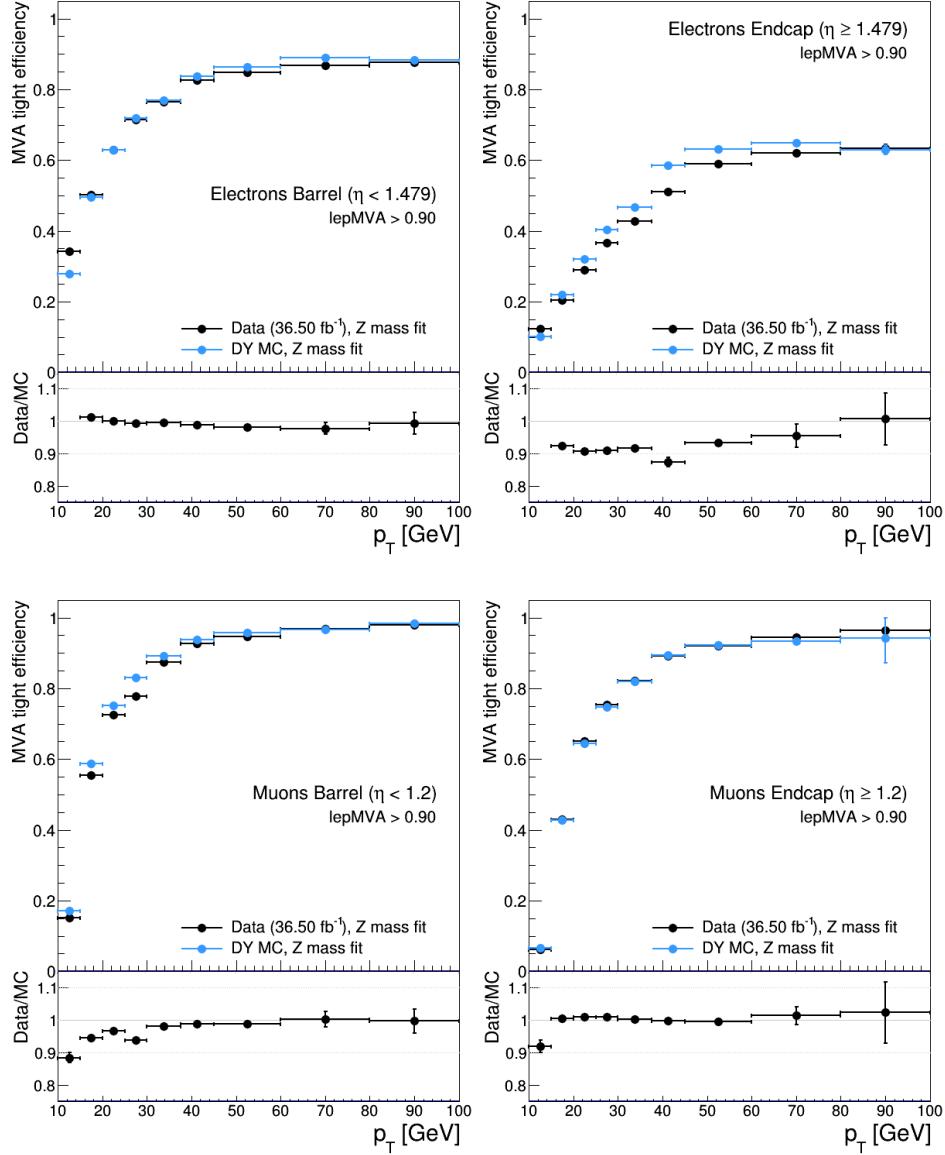


Figure 6.8: Tight vs loose selection efficiencies for electrons (top), and muons (bottom), for the $2lss$ definition, i.e., including the tight-charge requirement.

2701 The efficiency of applying the tight selection as defined in Tables 6.4 and 6.5, on the
 2702 loose leptons are determined by using a tag and probe method on a sample of Drell-
 2703 Yan enriched events. Figures 6.8 and 6.9 show the efficiencies for the $2lss$ channel and
 2704 $3l$ channel respectively. Efficiencies in the $2lss$ channel have been produced including
 2705 the tight-charge requirement, while for the $3l$ channel it is not included. Number

of passed and failed probes are determined from a fit to the invariant mass of the dilepton system. Simulation is corrected using these scale factors; note that they depends on η and p_T .

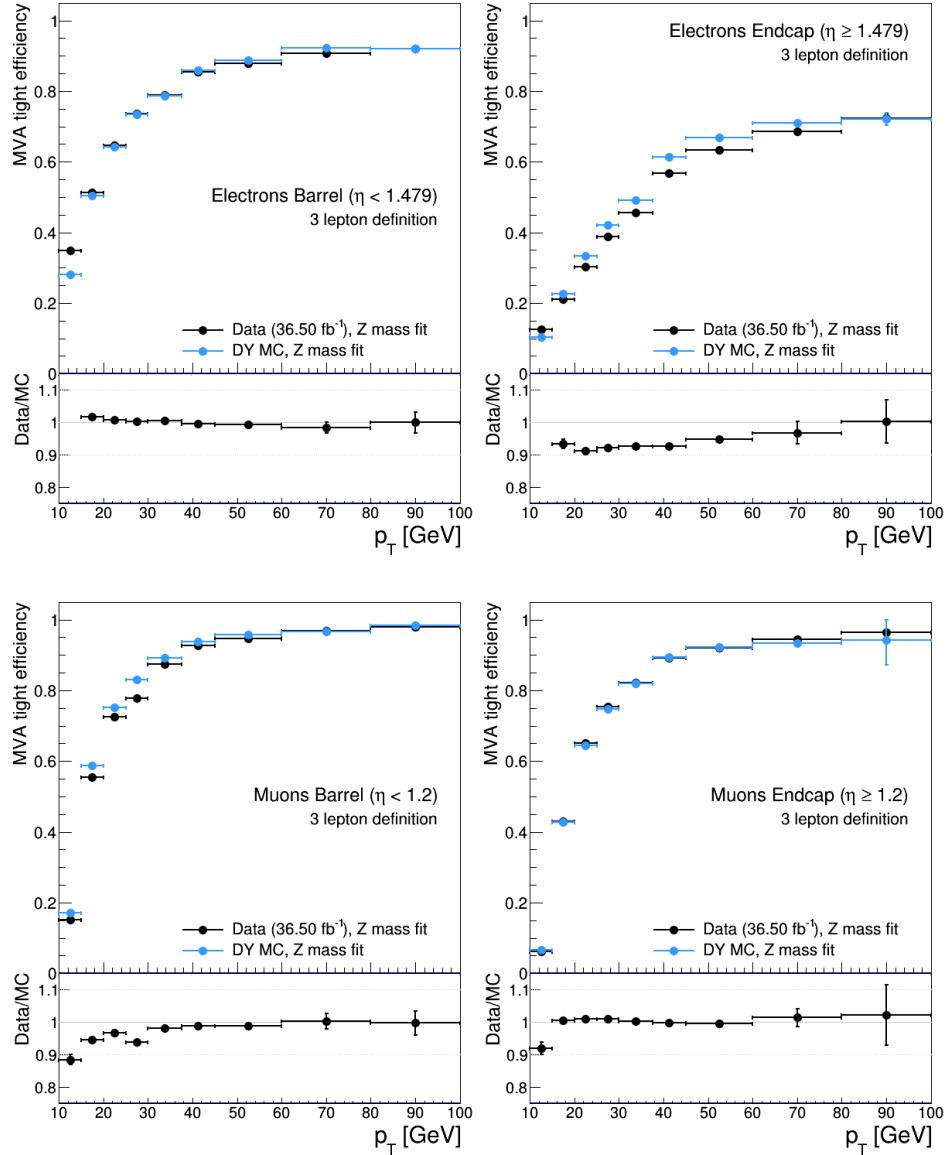


Figure 6.9: Tight vs loose selection efficiencies for electrons (top), and muons (bottom), for the $3l$ channel not including the tight-charge requirement.

2709 **6.5.3 Jets and b -jet tagging**

2710 In this analysis, jets are reconstructed by clustering PF candidates using the anti- k_t
 2711 algorithm with parameter distance $\Delta R = 0.4$; those charged hadrons that are not
 2712 consistent with the selected primary vertex are discarded from the clustering. The
 2713 jet energy is then corrected for the varying response of the detector as a function
 2714 of transverse momentum p_T and pseudorapidity η . Jets are selected for use in the
 2715 analysis only if they have $p_T > 25$ GeV and are separated from any selected leptons
 2716 by $\Delta R > 0.4$.

2717 Jets coming from the primary vertex and jets coming from pile-up vertices are
 2718 distinguished using a MVA discriminator based on the differences in the jet shapes,
 2719 in the relative multiplicity of charged and neutral components, and in the different
 2720 fraction of transverse momentum which is carried by the hardest components. Jet
 2721 tracks are also required to be compatible with the primary vertex.

2722 Jets originated from the hadronization of a b quark are selected using a MVA
 2723 likelihood discriminant which uses track-based lifetime information and reconstructed
 2724 secondary vertices (CSV algorithm). Only jets within the CMS tracker acceptance
 2725 ($\eta < 2.4$) are identified with this tool. Data samples are used to measure the efficiency
 2726 of the b -jet tagging and the probability to misidentify jets from light quarks or gluons;
 2727 in both cases the measurements are parametrized as a function of the jet p_T and η
 2728 and later used to correct differences between the data and MC simulation in the b
 2729 tagging performance, by applying per-jet weights to the simulation, dependent on
 2730 the jet p_T , η , b tagging discriminator, and flavor (from simulation truth) [151]. The
 2731 per-event weight is taken as the product of the per-jet weights, including those of the
 2732 jets associated to the leptons. The weights are derived on $t\bar{t}$ and Z+jets events.

2733 Two working points are defined, based on the CSV algorithm output: ‘*loose*’ work-

ing point ($\text{CSV} > 0.46$) with a b signal tagging efficiency of about 83% and a mistagging rate of about 8%; and *medium* working point ($\text{CSV} > 0.80$) with b -tagging efficiency of about 69% and mistagging rate of order 1% [152]. Tagging of jets from charm quarks have efficiencies of about 40% and 18% for loose and medium working points respectively. Separate scale factors are applied to jets originating from bottom/charm quarks and from light quarks in simulated events to match the tagging efficiencies measured in the data.

6.5.4 Missing Energy MET

As stated in Section 3.4.1, the MET vector is calculated as the negative of the vector sum of transverse momenta of all PF candidates in the event and its magnitude is referred to as E_T^{miss} . Due to pile-up interactions, the performance in determining MET is degraded; in order to correct for that, the energy from the selected jets and leptons that compose the event is assigned to the variable H_T^{miss} . It is calculated in the same way as E_T^{miss} and although it has worse resolution than E_T^{miss} , it is more robust in the sense that it does not rely on the soft part of the event. The event selection uses a linear discriminator based on the two variables given by

$$E_T^{\text{miss}}_{LD} = 0.00397 * E_T^{\text{miss}} + 0.00265 * H_T^{\text{miss}} \quad (6.6)$$

taking advantage of the fact that the correlation between E_T^{miss} and H_T^{miss} is less for events with instrumental missing energy than for events with real missing energy. The working point $E_T^{\text{miss}}_{LD} > 0.2$ was chosen to ensure a good signal efficiency while keeping a good background rejection.

2754 6.6 Event selection

2755 Events are selected considering the features of the signal process and the decay sig-
 2756 nature as described in Section 6.2. At the trigger level, events are selected to contain
 2757 either one, two, or three leptons with minimal p_T thresholds:

- 2758 • single-lepton trigger → 24 GeV for muons and at 27 GeV for electrons
- 2759 • double-lepton triggers → leading and sub-leading leptons: 17 and 8 GeV for
 2760 muons and 23 and 12 GeV for electrons.
- 2761 • three-lepton triggers → threshold on the third hardest lepton in the event: 5
 2762 and 9 GeV for muons and electrons, respectively.

2763 The offline event selection level targets the specific topology of the tHq signal
 2764 with $H \rightarrow WW$ and $t \rightarrow Wb \rightarrow l\nu b$; therefore, the resulting state is composed of three
 2765 W bosons, one b quark, and a light spectator quark at high rapidity. The selection
 2766 criteria for the two channels exploited in this analysis are summarized in Table 6.6.
 2767 This selection includes contributions from $H \rightarrow \tau\tau$ and $H \rightarrow ZZ$ as well.

Same-sign $\ell\ell$ channel	$\ell\ell\ell$ channel
have fired one of the corresponding trigger paths	
No loose leptons with $m_{\ell\ell} < 12\text{GeV}$	
One or more b tagged jets (CSV medium) $ \eta < 2.4$	
One or more non-tagged jets: central → $p_T > 25\text{ GeV}$, $\eta < 2.4$ forward → $p_T > 40\text{ GeV}$, $\eta > 2.4$	
	$E_{T,LD}^{\text{miss}} > 0.2$
Exactly two tight same-sign leptons	Exactly three tight leptons
Lepton $p_T > 25/15\text{GeV}$	Lepton $p_T > 25/15/15\text{GeV}$
Electrons are triple-charge consistent.	No OSSF lepton pair with $ m_{\ell\ell} - m_Z < 15\text{GeV}$
Muon p_T resolution: $\Delta p_T/p_T < 0.2$.	
No ee pair with $ m_{ee} - m_Z < 10\text{GeV}$	

Table 6.6: Summary of event pre-selection.

2768 In the $2lss$ channel, events with additional tight leptons are vetoed as well as those
 2769 for which a loose lepton pair has an invariant mass below 12 GeV. A threshold in p_T of
 2770 the leading and sub-leading leptons is also required. Events where the two electrons
 2771 have invariant mass within 10 GeV of the Z boson mass (Z -*veto*) are discarded in
 2772 order to reject events from DY+jets production with charge misidentified electrons.
 2773 In addition, contribution from the associated production of two W bosons of equal
 2774 charge and two light jets $W^\pm W^\pm qq$ and from same-sign W boson pairs can also be
 2775 produced in double parton scattering (DPS) processes, where each of the colliding
 2776 protons gives two partons, resulting in two hard interactions.

2777 In the $3l$ lepton channel, leptons are required to have respectively $p_T > 25\text{GeV}$, $>$
 2778 15 GeV, and > 15 GeV. Events with an opposite-sign same-flavor lepton combination
 2779 (OSSF) with invariant mass within 15 GeV of the Z boson mass are discarded in order
 2780 to reject events from $WZ + \text{jets}$ production.

2781 6.7 Background modeling and predictions

2782 The dominant background contribution is expected to arise from top quark produc-
 2783 tion processes, either $t\bar{t}$ pair production or in $t\bar{t}$ associated production with a W/Z.
 2784 Processes with production of single top quarks also contribute, mainly in the associ-
 2785 ated production with a Z boson (tZq) or when produced with both a W and a Z boson
 2786 (tZW). Background contamination from diboson processes is strongly suppressed by
 2787 imposing the Z-veto, vetoing additional leptons and requiring b -jets in the event.

2788 The selection criteria in Table 6.6 represent a relatively loose selection that allows
 2789 to maintain a large signal efficiency while suppressing the main backgrounds; thus
 2790 that selection is called *pre-selection*. The events obtained from the pre-selection are
 2791 then used to extract the signal contribution in a second analysis step, using BDT dis-

2792 discriminators against the main backgrounds of $t\bar{t}W/t\bar{t}Z$ and non-prompt leptons from
 2793 $t\bar{t}$. The shape of the discriminator variables is then fit to the observed data distribu-
 2794 tion to estimate the signal and background yields, simultaneously for all channels.

2795 Irreducible backgrounds are reliably estimated from MC simulated events; there-
 2796 fore, in this analysis all backgrounds involving prompt leptons are estimated in this
 2797 way. Reducible backgrounds, like non-prompt lepton backgrounds, are not well pre-
 2798 dicted by simulation, hence, they are estimated using data-driven methods.

2799 **6.7.1 $t\bar{t}V$ and diboson backgrounds**

2800 Backgrounds from $t\bar{t}W$ and $t\bar{t}Z$ processes are estimated using simulated events, cor-
 2801 rected for data/MC differences and inefficiencies (trigger and lepton selection) in the
 2802 same way as signal events. Their production cross sections are calculated at NLO
 2803 order of QCD and EWK, considering theoretical uncertainties from unknown higher
 2804 orders of 12% for $t\bar{t}W$ and 10% for $t\bar{t}Z$. Additional uncertainties arise from the knowl-
 2805 edge of PDFs and α_s of about 4% each for $t\bar{t}W$ and $t\bar{t}Z$.

2806 The diboson contribution is also estimated from simulated events; however, the
 2807 overall normalization of this process is obtained from a dedicated control region.
 2808 The motivation behind that strategy is that even though the measured inclusive
 2809 cross section for diboson processes (WZ, ZZ) is in good agreement with the NLO
 2810 calculations [149], that agreement is perturbed when leptonic Z decays and hadronic
 2811 jets in the final state are required; those requirements are precisely the ones that
 2812 make the diboson production a background for the tHq signal. Thus, by using a
 2813 dedicated control region dominated by WZ production⁴, the overall normalization is
 2814 constrained.

⁴ ZZ background is strongly reduced by the cut on MET.

2815 The control region is defined by the presence of at least three leptons, of which
 2816 one opposite-sign pair must be compatible with a Z boson decay, i.e., invert the Z-
 2817 veto which makes the control region orthogonal to signal region; the b-jet tagging
 2818 requirements is also inverted with respect to the signal region, i.e., require two not
 2819 b -jets. A scale factor is extracted from the predicted distribution of WZ events in the
 2820 control region, and the observed data, while keeping other processes fixed; this factor
 2821 is used to scale the diboson prediction in the signal selection region. More details
 2822 about the procedure used can be found in Reference [149] from where the scale factor
 2823 is taken.

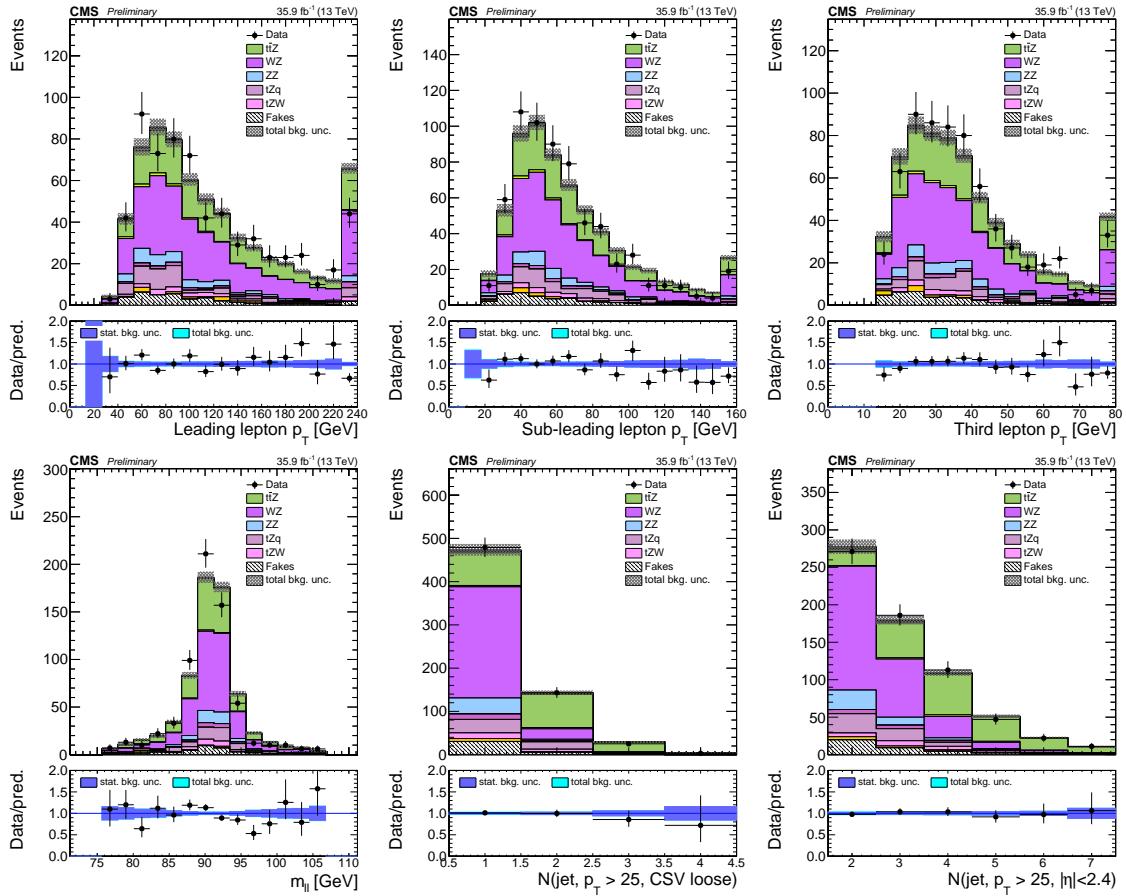


Figure 6.10: Kinematic distributions in the diboson control region.

2824 In order to test the usability of the diboson background scale factor in this analysis,

2825 a Z-enriched control region⁵ was defined by inverting the Z-veto and requiring exactly
 2826 three tight leptons with $p_T > 25/15/15$ GeV, one or more jets passing the CSVv2 loose
 2827 working point and less than four central jets. Figure 6.10 shows the distribution of
 2828 three variables in the diboson control region; the good agreement between MC and
 2829 data motivates the adoption of the diboson background scale factor.

2830 Most of the diboson events passing the signal selection contain jets from light
 2831 quarks and gluons that are incorrectly tagged as b -jets; it makes the estimate mainly
 2832 sensitive to the experimental uncertainty in the mis-tag rate rather than the theore-
 2833 tical uncertainty in the jet flavor composition. The overall uncertainty assigned to
 2834 the diboson prediction is estimated from the statistical uncertainty due to the limited
 2835 sample size in the control region (30%), the residual background in the control region
 2836 (20%), the uncertainties on the b -tagging rate (10-40%), and from the knowledge of
 2837 PDFs and the theoretical uncertainties of the extrapolation (up to 10%).

2838 **6.7.2 Non-prompt and charge mis-ID backgrounds**

2839 The non-prompt lepton background contribution to the final selection is estimated
 2840 using the fake factor method. The main idea of the method is to define a control
 2841 region of events enriched in the background to estimate and determine a factor that
 2842 relates (extrapolates) these events to those in the signal region. The method is data-
 2843 driven in the sense that the control sample is selected from data, and the extrapolation
 2844 factor is measured from data.

2845 In the signal region of this analysis, non-prompt leptons are predominantly pro-
 2846 duced in $t\bar{t}$ events, with a much smaller contribution, from Drell-Yan production;
 2847 therefore, the control region also known as *application region*, is defined by modifying
 2848 the event selection criteria in such a way that most of the events after selection are

⁵ This control region is different to the one used to find the scale factor.

2849 $t\bar{t}$ events and thus the misidentification rate is increased. The application regions
 2850 for electrons and muons are defined by the fakeable object definitions in Tables 6.4
 2851 and 6.5. Since the fakeable definition is a loosened version of the tight definition, in
 2852 the context of fake rates the fakeable definition becomes the loose selection.

2853 The ratio between the number of events that pass both, the loose and tight se-
 2854 lections, and the number of events that pass the loose selection but fail the tight
 2855 one, corresponds to the *loose-to-tight ratio or fake factor/rate (f)*. The measurement
 2856 of the fake factor is made using two background dominated data samples, collected
 2857 with dedicated triggers, as a function of p_T and $|\eta|$ and separately for muons and
 2858 electrons:

- 2859 • A sample dominated by QCD multijet events, collected using single lepton trig-
 2860 gers at relatively high p_T thresholds. It is used to extract ratios for lepton
 2861 candidates with p_T above 30 GeV.
- 2862 • A sample dominated by $Z + \text{jets}$ events, where the two high p_T leptons resulting
 2863 from the Z decay are used to trigger the events without biasing the p_T spectrum
 2864 of a third lepton at low transverse momentum. It is used to determine the ratios
 2865 for low p_T leptons.

2866 Processes like $W + \text{jets}$, $Z + \text{jets}$, WZ and ZZ produce prompt leptons that
 2867 contaminate the samples; thus, they are suppressed by vetoing additional leptons in
 2868 the selection, and the residual contamination is then subtracted using the transverse
 2869 mass as a discriminating variable.

2870 The extrapolation from the application region to the signal region is performed
 2871 by weighting the events in the application region using the fake factor according to
 2872 the following rules:

- 2873 • events with one lepton failing the tight criteria are weighted with the factor
 2874 $\frac{f}{(1-f)}$ for the estimate to the signal region.
- 2875 • events with two leptons (i,j) failing the tight criteria are weighted with the factor
 2876 $-\frac{f_i f_j}{(1-f_i)(1-f_j)}$ for the estimate to the signal region.
- 2877 • events with three leptons (i,j,k) failing the tight criteria are weighted with the
 2878 factor $\frac{f_i f_j f_k}{(1-f_i)(1-f_j)(1-f_k)}$ for the estimate to the signal region.

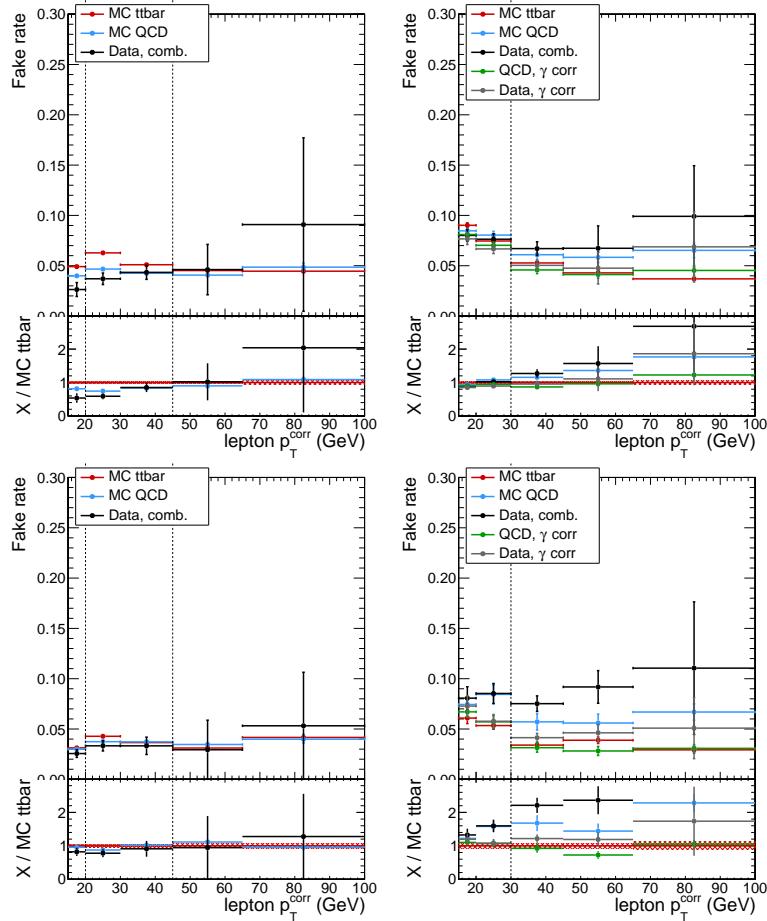


Figure 6.11: Fake rate measurement in events in data for muons (left column) and electrons (right column). Predictions from simulated events in the measurement region (blue) and from non-prompt leptons in $t\bar{t}$ (red) are included for comparison. Top row is for $|\eta| < 2.5$ and bottom row for $|\eta| > 2.5$.

2879 Figure 6.11 shows the fake rates for electrons and muons used in this analysis
 2880 which were taken from the studies in Reference [149].

2881 The resulting prediction of the event yield in the signal selection carries an uncer-
 2882 tainty of 30-50% which is composed of the statistical uncertainty in the measurement
 2883 of the fake rates due to prescaling of lepton triggers, the uncertainty in the subtraction
 2884 of residual prompt leptons from the control region, and from testing the closure of the
 2885 method in simulated background events; hence, it is one of the dominant limitations
 2886 on the performance of multilepton analyses in general and this analysis in particular.

2887 Finally, an additional source of background arises in the $2lss$ channel from events
 2888 with an originally opposite-sign lepton pair for which the charge of one of the leptons
 2889 is misidentified (*charge mis-ID*); usually this happens because of the conversion of
 2890 hard bremsstrahlung photons emitted from the initial lepton, hence, it is more likely
 2891 to happen for electrons than for muons.

2892 The charge mis-ID background is estimated from the yield of opposite-sign event
 2893 in the signal region by measuring the charge mis-ID probability in same-sign and
 2894 opposite-sign events compatible with a Z boson decay, in several bins of p_T and η ,
 2895 and weighting events with opposite-sign leptons in the signal selection.

Data	$10 \leq p_T < 25$ GeV	$25 \leq p_T < 50$ GeV	$50 \text{ GeV} \leq p_T$
$0 \leq \eta < 1.48$	0.0442 ± 0.0011	0.0179 ± 0.0004	0.0262 ± 0.0020
$1.48 \leq \eta < 2.5$	0.1329 ± 0.0066	0.1898 ± 0.0014	0.3067 ± 0.0113
<hr/>			
MC			
$0 \leq \eta < 1.48$	0.0378 ± 0.0016	0.0222 ± 0.0003	0.0233 ± 0.0015
$1.48 \leq \eta < 2.5$	0.0956 ± 0.0044	0.2108 ± 0.0027	0.3157 ± 0.0018

Table 6.7: Electron charge mis-ID probabilities (in percent), determined in data (top) and Drell-Yan MC (bottom) [149].

2896 The charge mis-ID probability is found to be negligible for this analysis for muons,
 2897 whereas for electrons it ranges from about 0.02% in the barrel section ($|\eta| < 1.48$)

2898 up to about 0.35% in the detector endcaps ($1.48 < |\eta| < 2.5$). as shown in Table 6.7
 2899 and Figure 6.12.

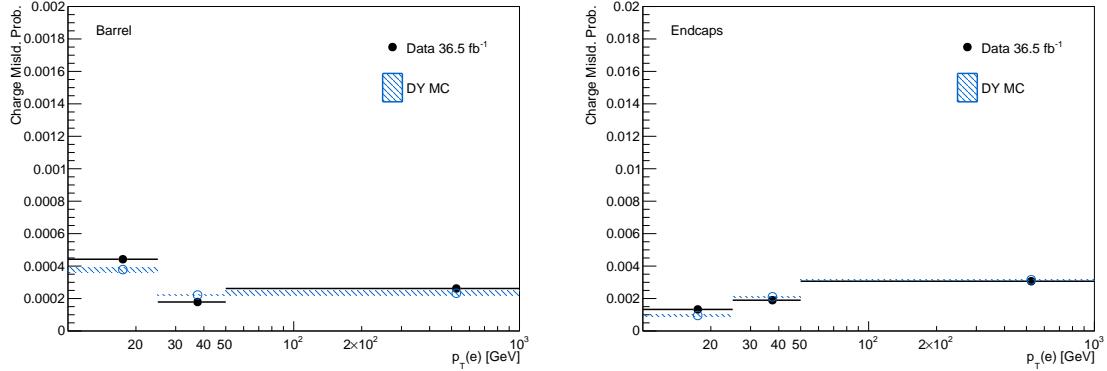


Figure 6.12: Electron charge mis-ID probabilities as a function of p_T for $|\eta| < 2.5$ (left) and $|\eta| < 2.5$ (right) [149].

2900 The contribution from charge mis-ID electrons in signal selection of this analysis
 2901 comes mainly from $t\bar{t}$ and Drell-Yan events. The systematic uncertainty of the nor-
 2902 malization of the charge mis-id. estimate is evaluated at about 30%, arising from a
 2903 slight disagreement of the mis-ID. probability between data and simulation. Given
 2904 that it only affects the $e\mu$ channel, its impact on the final sensitivity is very limited.

2905 6.8 Pre-selection yields

2906 The expected and observed event yields of the pre-selection are shown in Table 6.8;
 2907 Figure 6.13 shows the distributions of some relevant kinematic variables, normalized
 2908 to the cross section of the respective processes and to the integrated luminosity. The
 2909 remaining variables distributions are shown in Appendix B.1.

2910 For the tH and $t\bar{t}H$ processes, the largest contribution comes from Higgs decays
 2911 to WW (about 75%), followed by $\tau\tau$ (about 20%) and ZZ (about 5%). Other Higgs

	3ℓ	$\mu^\pm\mu^\pm$	$e^\pm\mu^\pm$
$t\bar{t}W$	22.50 ± 0.35	68.03 ± 0.61	97.00 ± 0.71
$t\bar{t}Z/\gamma^*$	32.80 ± 1.79	25.89 ± 1.12	64.82 ± 2.42
WZ	8.22 ± 0.86	15.07 ± 1.19	26.25 ± 1.57
ZZ	1.62 ± 0.33	1.16 ± 0.29	2.86 ± 0.45
$W^\pm W^\pm qq$	–	3.96 ± 0.52	6.99 ± 0.69
$W^\pm W^\pm(\text{DPS})$	–	2.48 ± 0.42	4.17 ± 0.54
VVV	0.42 ± 0.16	2.99 ± 0.34	4.85 ± 0.43
ttt	1.84 ± 0.44	2.32 ± 0.45	4.06 ± 0.57
tZq	3.92 ± 1.48	5.77 ± 2.24	10.73 ± 3.03
tZW	1.70 ± 0.12	2.13 ± 0.13	3.91 ± 0.18
γ conversions	7.43 ± 1.94	–	23.81 ± 6.04
Non-prompt	25.61 ± 1.26	80.94 ± 2.02	135.34 ± 2.83
Charge mis-ID	–	–	58.50 ± 0.31
All backgrounds	106.05 ± 3.45	210.74 ± 3.61	443.30 ± 8.01
tHq ($\kappa_t = -1.0$)	7.48 ± 0.14	18.48 ± 0.22	27.41 ± 0.27
tHW ($\kappa_V = -1.0$)	7.38 ± 0.16	7.72 ± 0.17	11.23 ± 0.20
$t\bar{t}H$	18.29 ± 0.41	24.18 ± 0.48	35.21 ± 0.58
Data ($35.9 fb^{-1}$)	127	280	525

Table 6.8: Expected and observed yields for $35.9 fb^{-1}$ after the pre-selection in all final states. Uncertainties are statistical only.

2912 production modes contribute negligible event yields (< 5% of the $tH+t\bar{t}H$ yield) as
 2913 shown in Table 6.9.

2914 A significant fraction of selected data events (about 50% in the dilepton channels,
 2915 and about 80% in the trilepton channel) also passes the selection used in the dedicated
 2916 search for tH in multilepton channels [149]. This is particularly important when
 2917 considering a possible combination of the measurements from both studies. More
 2918 details about the overlap between this both analyses are presented in Appendix E.

2919 6.9 Signal discrimination

2920 The production cross section for the signal processes tHq , tHW , and $t\bar{t}H$ is only
 2921 about 600 fb (the enhancement provided by inverted couplings, $\kappa_t = -1$ almost double

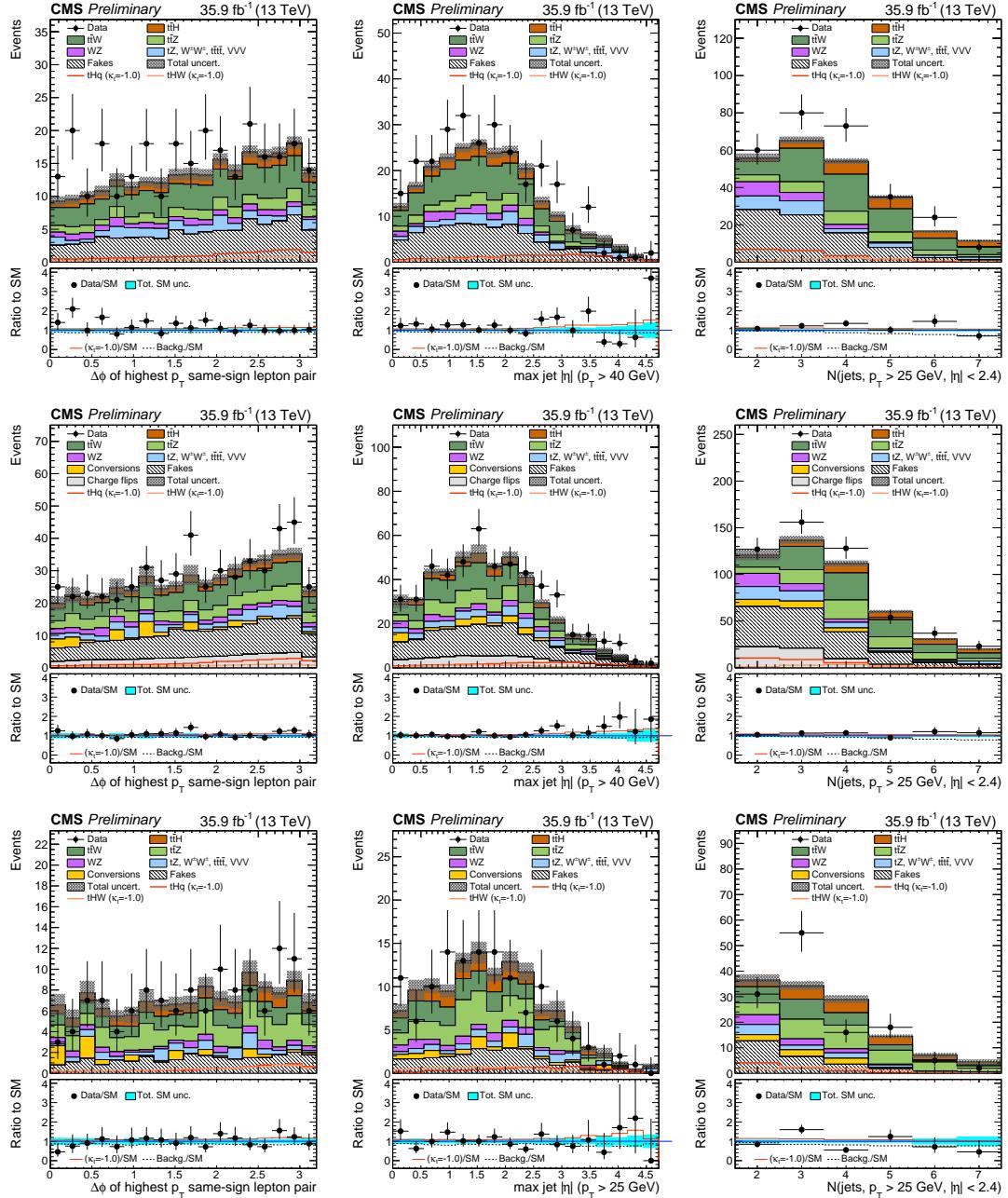


Figure 6.13: Distributions of discriminating variables for the event pre-selection for the same-sign $\mu^\pm\mu^\pm$ channel (top row), the same-sign $e^\pm\mu^\pm$ channel (middle row) and three lepton channel (bottom row), normalized to 35.9 fb^{-1} , before fitting the signal discriminant to the observed data. Uncertainties are statistical and unconstrained (pre-fit) normalization systematics. The shape of the two tH signals for $\kappa_t = -1.0$ is shown, normalized to their respective cross sections for $\kappa_t = -1.0, \kappa_V = 1.0$.

	3ℓ	$\mu^\pm\mu^\pm$		
tHq (Inclusive)	6.57	100.0%	17.38	100.0%
$tHq(H \rightarrow WW)$	4.84	73.9%	13.33	76.9%
$tHq(H \rightarrow \tau\tau)$	1.04	15.9%	3.62	20.6%
$tHq(H \rightarrow ZZ)$	0.48	7.2%	0.37	2.2%
$tHq(H \rightarrow \mu\mu)$	0.21	3.0%	0.04	0.2%
$tHq(H \rightarrow \gamma\gamma)$	< 0.01	0.1%	0.02	0.1%
$tHq(H \rightarrow bb)$	< 0.01	< 0.1%	0.01	< 0.1%
tHW (Inclusive)	7.32	100.0%	7.62	100.0%
$tHW(H \rightarrow WW)$	5.50	76.9%	5.60	74.1%
$tHW(H \rightarrow \tau\tau)$	1.40	20.6%	1.81	23.1%
$tHW(H \rightarrow ZZ)$	0.31	2.2%	0.21	2.7%
$tHW(H \rightarrow \mu\mu)$	0.12	0.2%	0.01	0.1%
$tHW(H \rightarrow \gamma\gamma)$	< 0.01	< 0.1%	< 0.01	< 0.1%
$tHW(H \rightarrow bb)$	< 0.01	< 0.1%	< 0.01	< 0.1%

Table 6.9: Signal yields split by decay channels of the Higgs boson. Forward jet p_T cut at 25 GeV.

it), resulting in a small signal to background ratio even for a tight selection. A multivariate method is hence employed to train discriminators to separate tH signal events from the dominant background events.

6.9.1 MVA classifiers evaluation

Several MVA classifier algorithms were evaluated in order to determine the most appropriate method for this analysis⁶. The comparison is based on the performance of the classifiers, encoded in the plot of the background rejection as a function of the signal efficiency (ROC curve). The top row of Figure 6.14 shows the ROC curves for the several methods evaluated; two separated training were performed in the $3l$ channel: against $t\bar{t}$ (right) and $t\bar{t}V$ (left) processes.

⁶ The choice of the tested algorithms was based on the recommendations provided by the official TMVA user guide, the experience from previous analyses and considering the expertise of the members of the tHq and $t\bar{t}H$ analyses groups. Only the BDT classifier is described in this thesis and a detailed description of all available methods can be found in Reference [127]

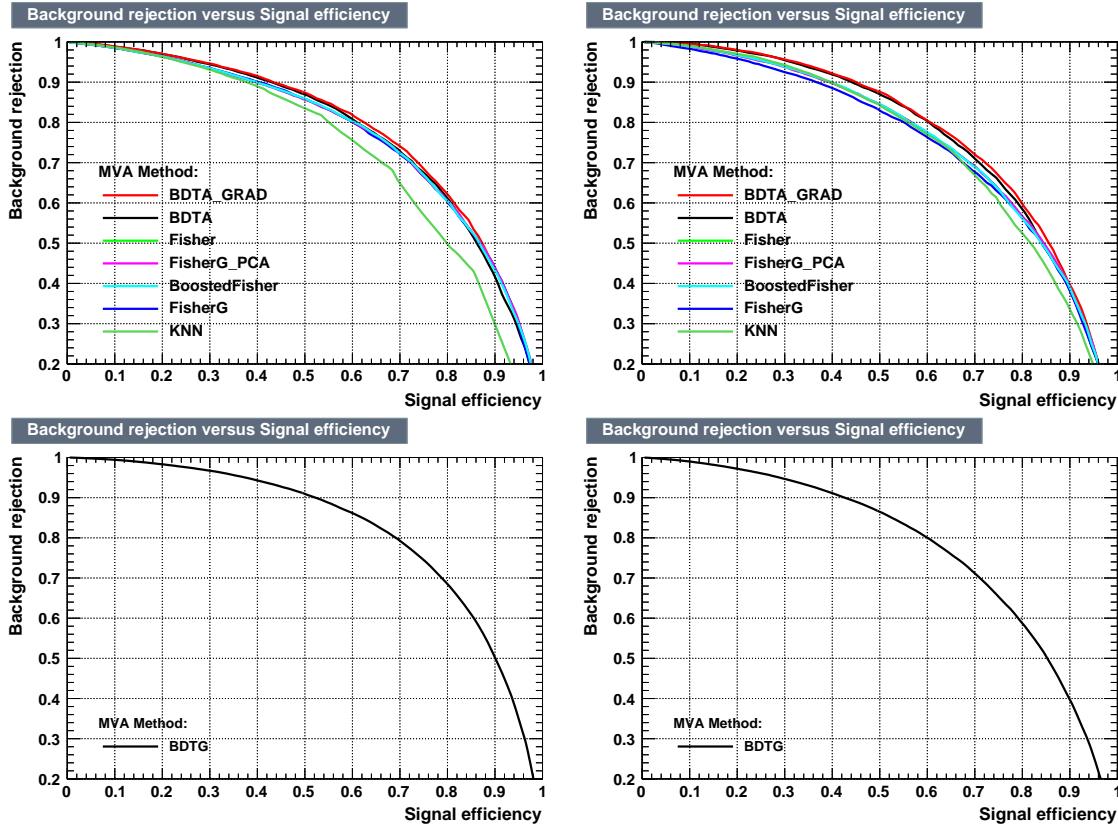


Figure 6.14: Top: Background rejection vs signal efficiency (ROC curves) for various MVA classifiers in the $3l$ channel for training against $t\bar{V}$ (left) and $t\bar{t}$ (right). Bottom: background rejection vs signal efficiency (ROC curve) in the $2lss$ channel for a single discriminator: BDTG, against $t\bar{V}$ (left) and $t\bar{t}$ (right).

2932 In both cases, the gradient boosted decision tree $BDTG$ ($BDTA_GRAD$ in the
 2933 plot) classifier offers the best results, followed by the adaptive BDT classifier ($BDTA$);
 2934 the several Fisher classifiers tested, which differ in their parameters and/or boosting
 2935 method, they offer similar performance among them, while the k-Nearest Neighbour
 2936 (kNN) classifier performance is below the rest of the classifiers. The corresponding
 2937 ROC curves and in the $2lss$ channel for trainings against $t\bar{V}$ (left) and $t\bar{t}$ (right)
 2938 processes are shown in the bottom row of Figure 6.14; the BDTG performance is
 2939 similar to that in the $3l$ channel.

2940 **6.9.2 Discriminating variables**

2941 The classifier chosen to separate the tHq signal from the main backgrounds is the
 2942 BDTG classifier, trained on simulated signal and background events. The samples
 2943 used in the training are the tHq sample in Table 6.2, the samples in the third section
 2944 of table A.4 and the samples marked with an * in the same table.

2945 As explained in Section 5.1.1, a set of discriminating variables are given as input to
 2946 the BDTG which combines the individual discrimination power of each input variable
 2947 to produce a discriminator with the maximum discrimination power. Table 6.10 lists
 2948 the input variables used in the BDTG trainings for this analysis. The same set of
 2949 input variables was used to produce the plots for MVA classifiers evaluation.

Variable name	Description
nJet25	Number of jets with $p_T > 25$ GeV, $ \eta < 2.4$
nJetEta1	Number of jets with $ \eta > 1.0$, non-CSV-loose
MaxEtaJet25	Max. $ \eta $ of any (non-CSV-loose) jet with $p_T > 25$ GeV
detaFwdJetClosestLep	$\Delta\eta$ forward light jet and closest lepton
detaFwdJetBJet	$\Delta\eta$ forward light jet and hardest CSV loose jet
detaFwdJet2BJet	$\Delta\eta$ forward light jet and second hardest CSV loose jet
Lep3Pt/Lep2Pt	p_T of the 3 rd lepton (2 nd for ss2l)
totCharge	Sum of lepton charges
minDRll	Min ΔR any two leptons
dphiHighestPtSSPair	$\Delta\phi$ of highest p_T same-sign lepton pair

Table 6.10: BDTG input variables. First section lists variables related to jet multiplicities; second section lists variables related to forward jet activity, and third section lists variables related to lepton kinematics.

2950 Plots in Figure 6.15 shows the BDTG input variables distributions for the signal
 2951 and background samples, in the 3 l channels.

2952 All the input variables have some discrimination power, however, that power is
 2953 bigger for some of them; for instance, the third lepton p_T plot (top left in Figure 6.15)
 2954 shows some discrimination power against WZ and VVV backgrounds for which there
 2955 is a peak around 30 GeV while tHq peak around 18 GeV; although the discrimination

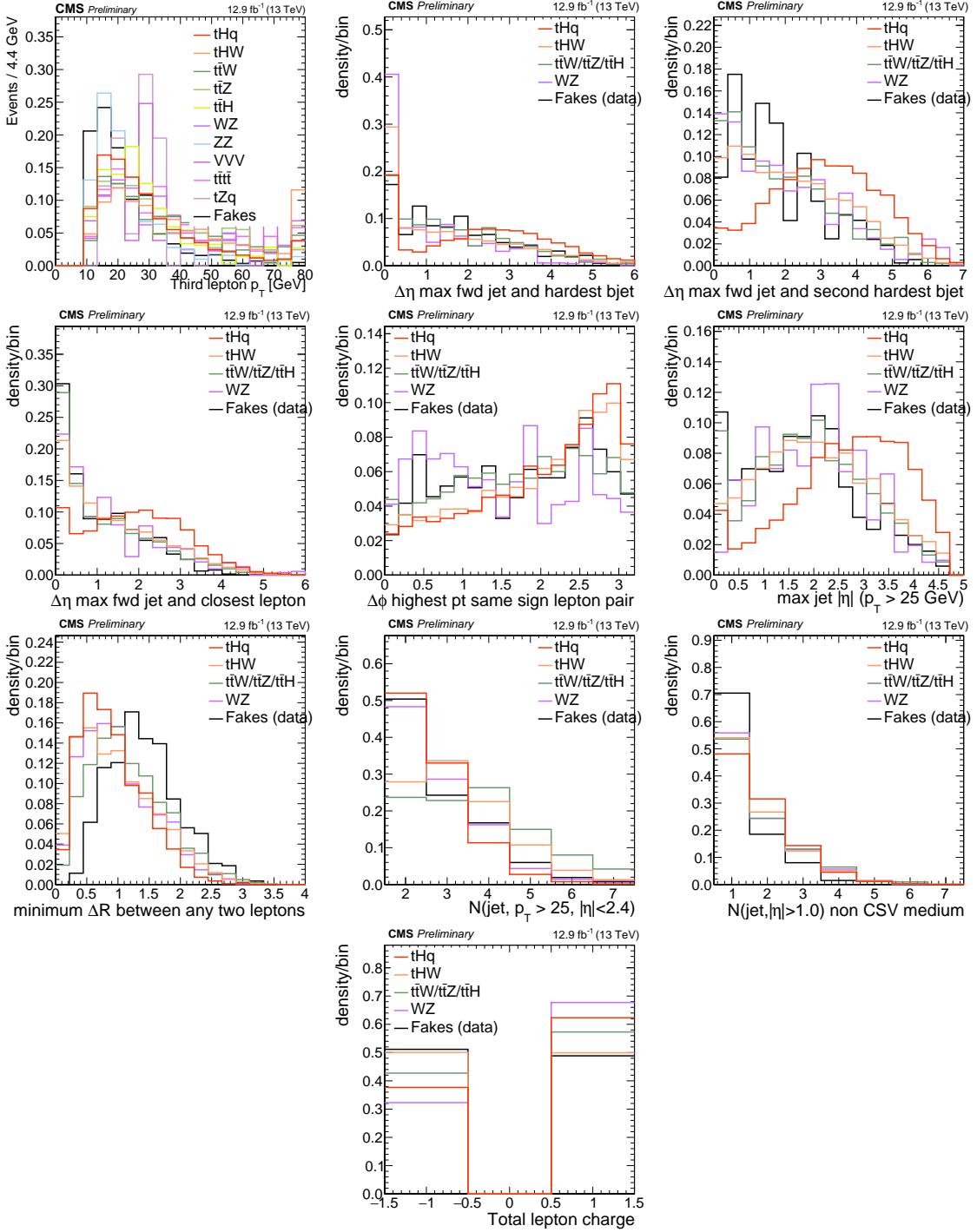


Figure 6.15: Distributions of the BDTG classifier input variables (not normalized) for signal discrimination in the $3l$ channel.

power does not cover all the backgrounds, it counts for the final discriminator. A similar situation can be seen in the plot for the number of jets (row three, column two); $t\bar{t}W$, $t\bar{t}Z$ and $t\bar{t}H$ processes tend to have more jets compared to the tHq process. The discrimination power is more evident in other plots like in the plot of the maximum $|\eta|$ of the jets in the event (row two, column three). The same or equivalent input variables are found to be performing well for both $3l$ and $2lss$ channels. Figure B.4 shows the corresponding input variables distribution plots for the $2lss$ channel.

Discrimination power from BDTG classifier

The Discrimination power of the input variables can also be evaluated from the BDTG training, exclusively for the training samples, i.e., dominant backgrounds ($t\bar{t}$ and $t\bar{t}V$); the training samples are submitted to the selection cuts on Table 6.6.

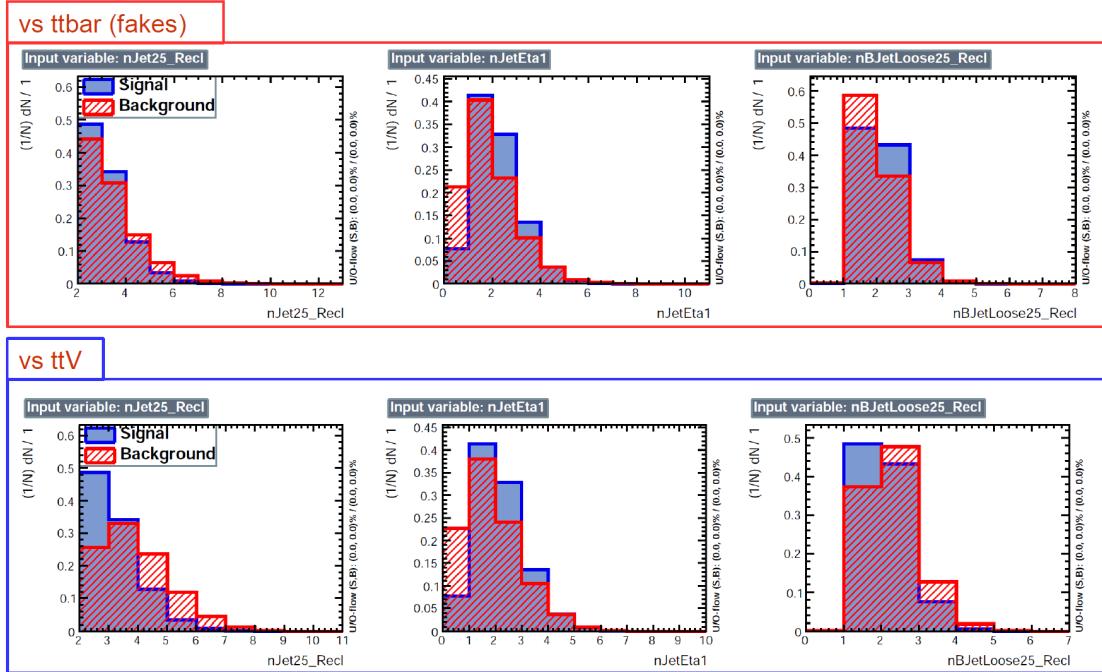


Figure 6.16: BDT input variables as seen by BDTG classifier for the $3l$ channel, tHq signal(blue) discriminated against $t\bar{t}V$ background (red).

Figure 6.16 shows the comparison between input variables for the two trainings in the $3l$ channel; it reveals that some variables show opposite behavior for the two background sources, which results in potentially screening the discrimination power if they were to be used in a single discriminant, i.e., if the training would join $t\bar{t}$ and $t\bar{t}V$. For some other variables the distributions are similar in both background cases. In contrast to the distributions in Figure 6.15 only the dominant backgrounds are included; however, the discrimination power agrees among plots.

Figures in the Appendix B.5, B.6, B.7, and B.8 show the input variables distributions for the $2lss$ and $3l$ channel as seen by the BDTG classifier.

2976 Input variables correlations

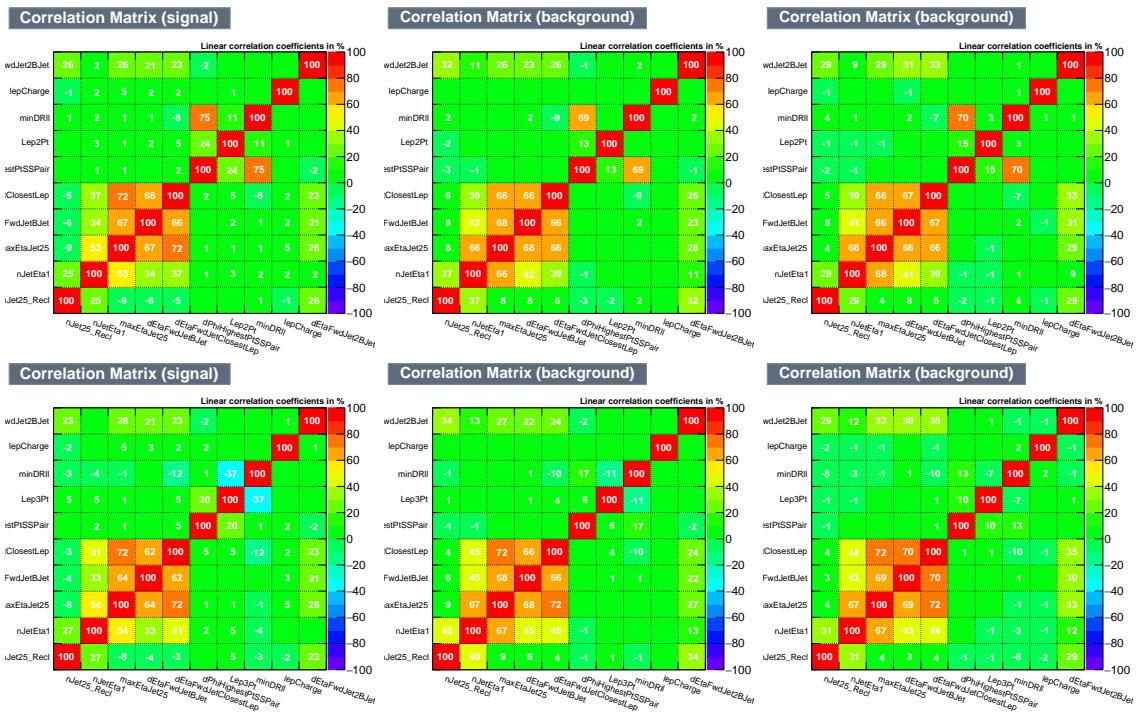


Figure 6.17: Signal (left), $t\bar{t}$ background (middle), and $t\bar{t}V$ background (right.) correlation matrices for the input variables in the BDTG classifier for the $2lss$ (top) and $3l$ (bottom) channels.

2977 From Table 6.10, it is clear that the input variables are correlated to some extend.

2978 These correlations play an important role for some MVA methods like the Fisher
 2979 discriminant method in which the first step consist of performing a linear transfor-
 2980 mation to an phase space where the correlations between variables are removed. In
 2981 the case of BDT, correlations do not affect the performance. Figure 6.17 shows the
 2982 linear correlation coefficients for signal and background for the two training cases (the
 2983 signal values are identical by construction). As expected, strong correlations appears
 2984 for variables related to the forward jet activity.

2985 6.9.3 BDTG classifiers response

2986 After the training stage, the BDTG classifier is tested to ensure its ability to discrim-
 2987 inate between simulated signal and background events. The BDTG classifier output
 2988 distributions for signal and backgrounds in the $3l$ channel are shown in Figure 6.18.
 2989 As expected, a good discrimination power is obtained using default discriminator
 2990 parameter values; some overtraining is also visible.

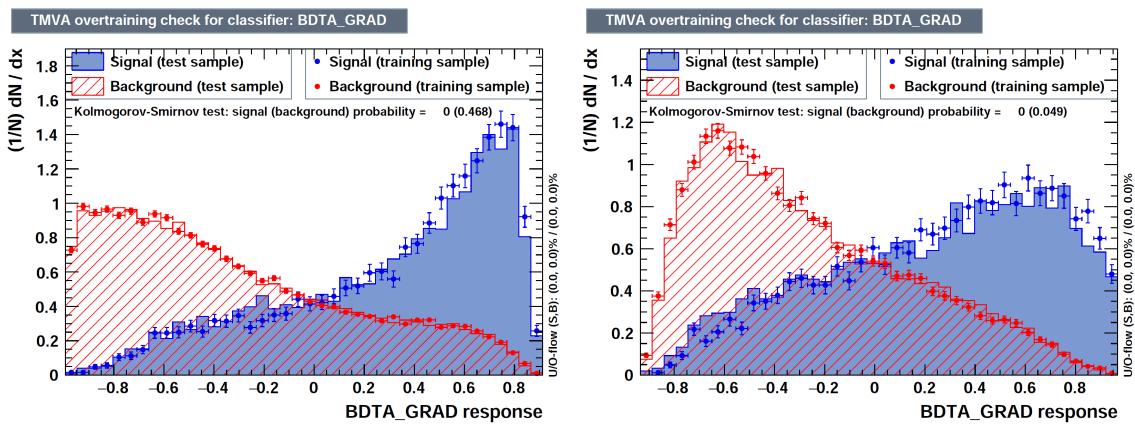


Figure 6.18: BDTG classifier output for trainings against $t\bar{t}V$ (left) and $t\bar{t}$ (right). Default BDTG parameters have been used.

2991 In order to explore further optimization in the BDTG performance, several changes
 2992 from the default BDTG parameters were tested; Table 6.11 list the set of parameters
 2993 found to be most discriminant with minimal overtraining as shown in Figure 6.19.

TMVA.Types.kBDT		
Option	Default	Used
NTrees	200	800
BoostType	AdaBoost	Grad
Shrinkage	1	0.1
nCuts	20	50
MaxDepth	3	

Table 6.11: Configuration used in the final BDTG training. Parameters not listed were not tested.

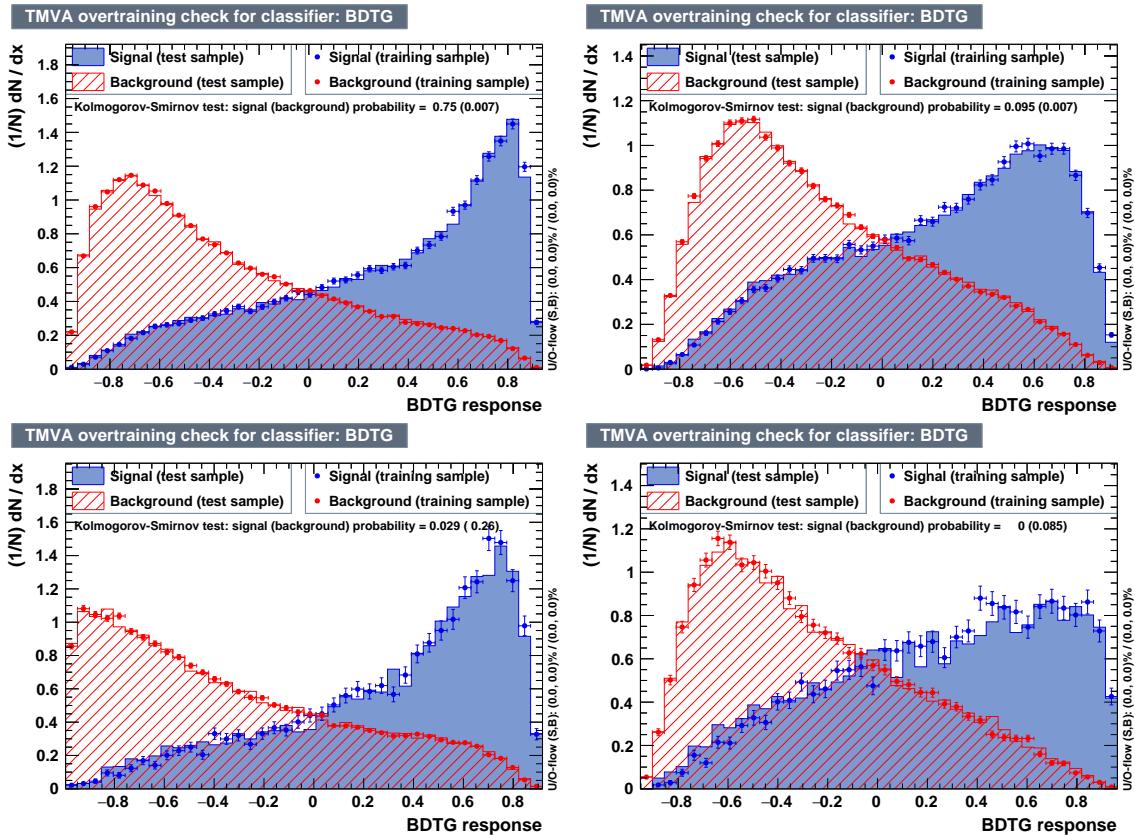


Figure 6.19: BDTG classifiers output for training against $t\bar{t}V$ (left) and $t\bar{t}$ (right) for $2lss$ channel(top) and $3l$ channel (bottom) .

2994 The ranking of the input variables by their importance in the classification process
 2995 is shown in Table 6.12; for both trainings the rankings show almost the same 5
 2996 variables in the first places.

$t\bar{t}$ training		
Rank	Variable	
1	minDRll	dEtaFwdJetBJet
2	dEtaFwdJetClosestLep	Lep3Pt
3	dEtaFwdJetBJet	maxEtaJet25
4	dPhiHighestPtSSPair	dEtaFwdJet2BJet
5	Lep3Pt	dEtaFwdJetClosestLep
6	maxEtaJet25	minDRll
7	dEtaFwdJet2BJet	dPhiHighestPtSSPair
8	nJetEta1	nJet25_Recl
9	nJet25_Recl	nJetEta1
10	lepCharge	lepCharge
$t\bar{t}V$ training		
Rank	Variable	
1	dEtaFwdJetClosestLep	maxEtaJet25
2	minDRll	dEtaFwdJet2BJet
3	maxEtaJet25	dEtaFwdJetBJet
4	dPhiHighestPtSSPair	Lep2Pt
5	Lep2Pt	dEtaFwdJetClosestLep
6	dEtaFwdJetBJet	minDRll
7	dEtaFwdJet2BJet	nJet25_Recl
8	nJetEta1	dPhiHighestPtSSPair
9	nJet25	nJetEta1
10	lepCharge	lepCharge

Table 6.12: Input variables ranking for BDTG classifiers for the trainings in the $2lss$ channel (first section) and $3l$ channel (second section). For both trainings the rankings show almost the same 5 variables in the first places.

2997 6.9.4 Additional discriminating variables

2998 Given that the forward jet in background processes could be originated from pileup,
 2999 two additional discriminating variables accounting for that were tested. These addi-
 3000 tional variables describe the forward jet momentum (fwdJetPt25) and the forward jet
 3001 identification(fwdJetPUID); their distributions in the $3l$ channel are shown in Fig-
 3002 ure 6.20. The forward jet identification distribution show that for both, signal and
 3003 background, jets are mostly originated in the primary vertex.

3004 The testing was performed by including in the BDTG input one variable at a time,
 3005 so the discrimination power of each variable can be evaluated individually, and then
 3006 both simultaneously. fwdJetPUID was ranked in the last place in importance (11) in
 3007 both training ($t\bar{t}V$ and $t\bar{t}$) while fwdJetPt25 was ranked 3 in the $t\bar{t}V$ training and 7 in

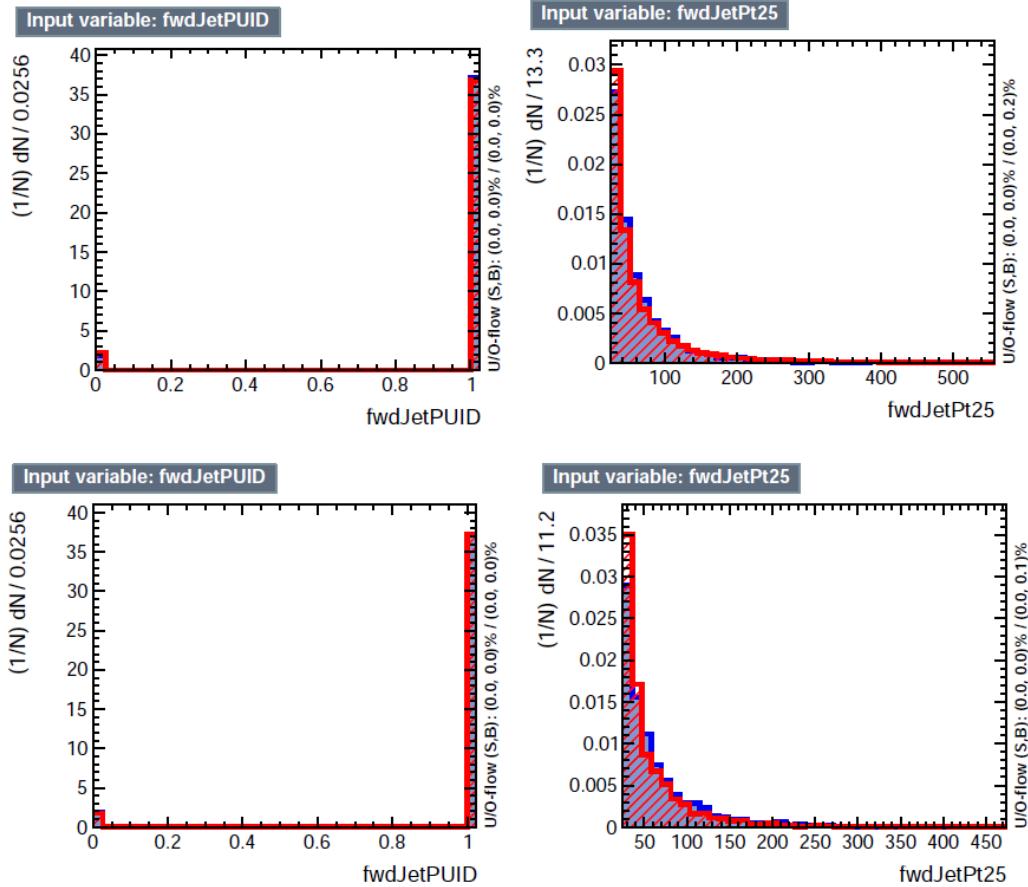


Figure 6.20: Additional discriminating variables distributions for $t\bar{t}V$ training (top row) and $t\bar{t}$ training (bottom row) in the $3l$ channel. The origin of the jets in the forward jet identification distribution is tagged as 0 for *pileup jets* while *primary vertex jets* are tagged as 1.

3008 the $t\bar{t}$ training. When training using 12 variables, fwdJetPt25 was ranked 5 and 7 in
 3009 the $t\bar{t}V$ and $t\bar{t}$ trainings respectively, while fwdJetPUID was ranked 12 in both cases.
 3010 The improvement in the discrimination performance provided by the additional
 3011 variables is about 1%, so it was decided not to include them in the procedure. Table
 3012 6.13 show the ROC-integral for all the testing cases performed.

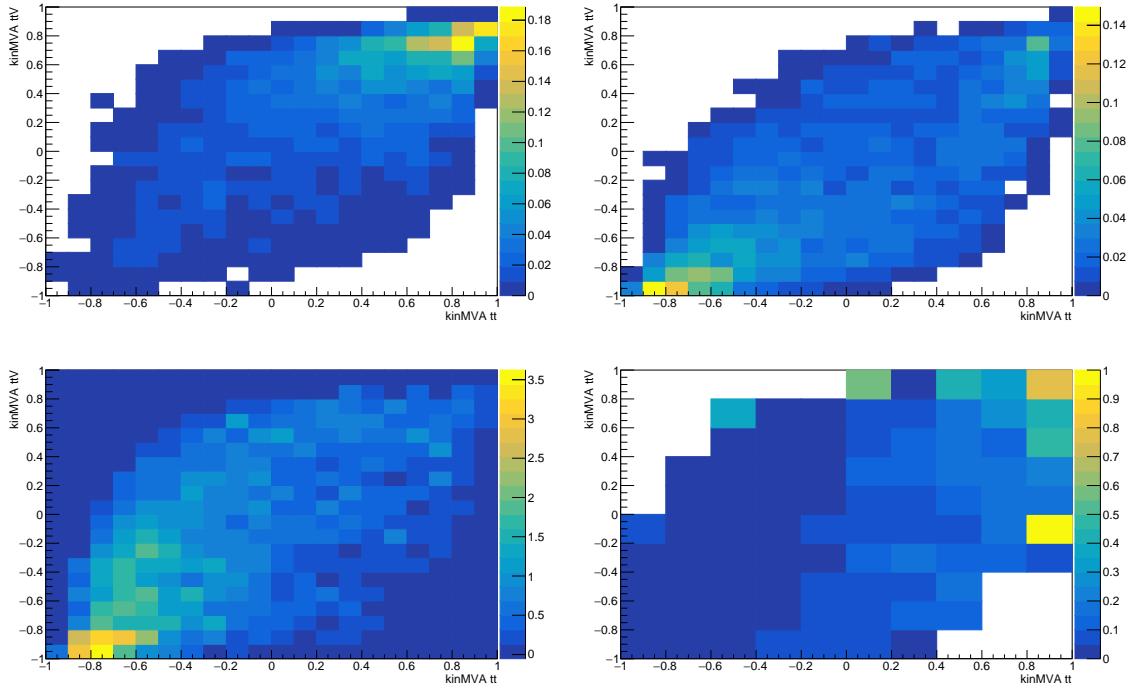


Figure 6.21: BDT classifier output planes (training vs $t\bar{t}$ on x-axis and vs $t\bar{t}V$ on y-axis) for the tHq and tHW signals (top row), and for the combined backgrounds (bottom left). Bottom right: S/B ratio (combining tHq and tHW) in the same plane. Plots are for $3l$ channel.

3013 6.9.5 Signal extraction procedure

3014 Once the two BDTG classifiers, introduced in the previous section, are trained against
 3015 the dominant backgrounds in each channel, they are used to classify the events in the
 3016 samples; their outputs are then used to evaluate the signal cross section limits in a

	ROC-integral	
	$t\bar{t}V$	$t\bar{t}$
base 10 var	0.848	0.777
+ fwdJetPUID	0.849	0.777
+ fwdJetPt25	0.856	0.787
12 var	0.856	0.787

Table 6.13: ROC-integral for all the testing cases performed in the evaluation of the additional variables discriminating power. The improvement in the discrimination performance provided by the additional variables is about 1% .

3017 fit to the classifier shape. Figure 6.21 shows the expected output distributions in a
 3018 2D plane of one training vs. the other, i.e., $t\bar{t}V$ vs. $t\bar{t}$. Top row shows the 2D planes
 3019 for tHq and tHW signals, while the bottom left plot shows the corresponding 2D
 3020 plane for the combined backgrounds, which are evaluated as in the final background
 3021 prediction, i.e., these are not the samples used in the BDTG training and this includes
 3022 data-driven backgrounds. The signal (combining of tHq and tHW) to background
 3023 ratio (S/B) is showed in the bottom right plot of Figure 6.21.

3024 Each event is now classified into one of ten 2D-bins according to its position in the
 3025 plane, as shown in Figure 6.22. The number of bins is chosen such that no bins are
 3026 entirely empty for any process. The bin boundary positions and number of bins have
 3027 been studied and optimized with respect to the expected limit on the signal strength
 3028 (see Sec. 6.9.6).

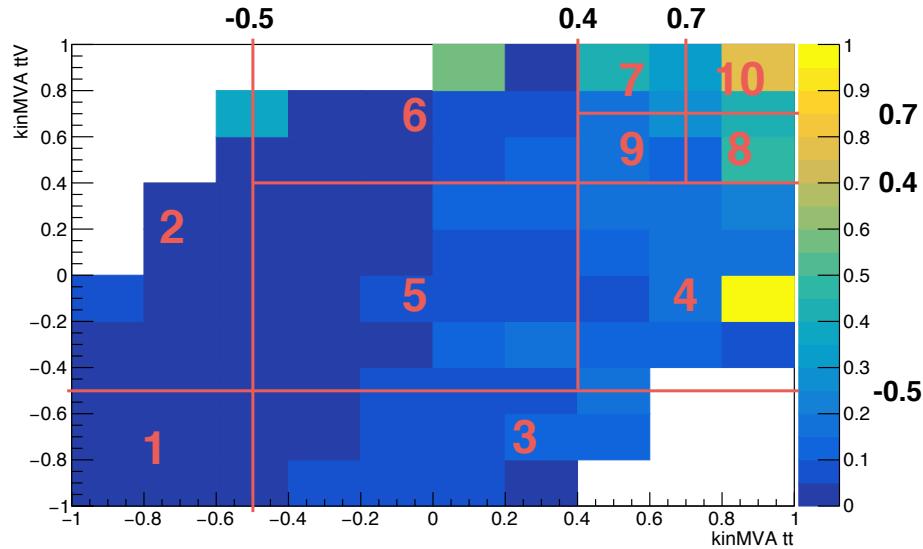


Figure 6.22: Binning overlaid on the S/B ratio map on the plane of classifier outputs.

3029 From this event categorization, a 1D histogram of expected distribution is pro-
 3030 duced for each signal and background process, and fit to the observed data (or the
 3031 Asimov dataset for expected limits).

3032 6.9.6 Binning and selection optimization

3033 The effect of the choice of pre-selection cuts and the number of bins of the 1D his-
 3034 togram on the cross section limit is evaluated by varying the most important cuts and
 3035 re-calculating the limit in each case. In this analysis, the optimization was performed
 3036 in the $3l$ channel, by evaluating the upper limits on the $tHq + tHW$ expected signal
 3037 strength only (without $t\bar{t}H$ component), always evaluated at $\kappa_t = -1.0$, $\kappa_V = 1.0$.

3038 Table 6.14 shows the several variations explored, compared with a baseline; the
 3039 baseline is similar to the selection reported in Table 6.6 but only a loose CSV jet and
 3040 a Z veto of ± 10 GeV are required.

Selection	Variation	Expected limit
Baseline		< 2.93
Loose CSV tags	$\geq 1 \rightarrow \geq 2$	< 3.81
Medium CSV tags	$\geq 0 \rightarrow \geq 1$	< 2.76
Light forward jet η	$\geq 0 \rightarrow \geq 1$	< 2.94
Light forward jet η	$\geq 0 \rightarrow \geq 1.5$	< 3.00
MET > 30 GeV		< 2.91
Z veto ($ m_{\ell\ell} - m_Z $)	$> 10\text{GeV} \rightarrow > 15\text{ GeV}$	< 2.79
One medium CSV + 15 GeV Z veto	combined	< 2.62

Table 6.14: Signal strength limit variation as a function of tighter cuts. The baseline selection corresponds to a looser selection compared to the one reported in Tab. 6.6 where only a CSV-loose b -jet is required, and the Z veto is loosened to ± 10 GeV. The optimal selection determined here corresponds to the baseline plus the two variations in the last row.

3041 The optimal limit is found when requiring a slightly tighter selection with respect
 3042 to the baseline. The optimal selection is reported in Table 6.6.

3043 The signal strength limit also depends on the chosen binning in the 2D plane as
 3044 the S/B ratio varies across the plane, hence, several sizes and binning combinations
 3045 were tested in order to improve the limit. Figure 6.23 shows some of the binning
 3046 combinations tested; in the default combination all the bins have the same size, while

3047 the best limit was found for a set of 10 bins. The bin borders and the resulting limits
 3048 are shown in Table 6.15.

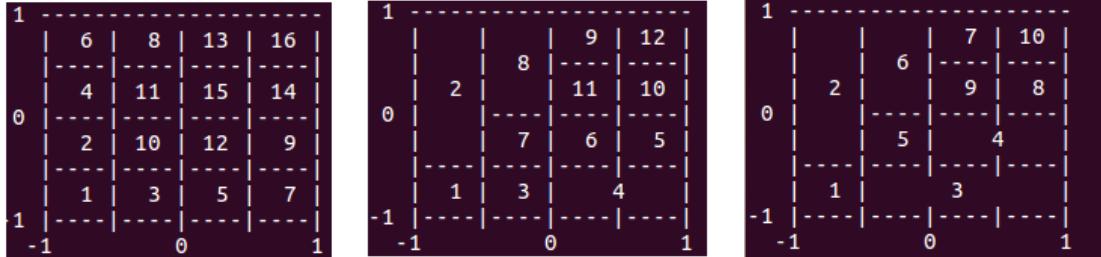


Figure 6.23: Binning combination scheme.

Number of bins	Bin borders						Expected limit
	x_1	x_2	x_3	y_1	y_2	y_3	
16 (default)	-0.5	0.0	0.5	-0.5	0.0	0.5	< 2.91
16	-0.5	0.3	0.7	-0.5	0.3	0.7	< 2.83
10	-0.5	0.0	0.5	-0.5	0.0	0.5	< 2.93
10	-0.5	0.0	0.7	-0.5	0.0	0.7	< 2.86
10	-0.5	0.0	0.7	-0.5	0.0	0.5	< 2.84
10	-0.5	0.0	0.5	-0.5	0.0	0.7	< 2.87
10	-0.5	0.4	0.7	-0.5	0.4	0.7	< 2.81

Table 6.15: Limit variation as a function of bin size. The final bin borders used in the $3l$ channel are indicated in bold.

3049 Combining the optimization of binning and using the tighter pre-selection cuts,

3050 the expected limit in the $3l$ channel alone reaches **r<2.59**.

3051 A similar binning optimization was made for $2lss$ channel, including other binning
 3052 combinations. First, the $3l$ channel binning was used to estimate the expected limit,
 3053 then, bin borders were varied to obtain the best possible expected limit. The bin
 3054 borders and the resulting signal strength limits for the same-sign dimuon channel are
 3055 shown in Table 6.16:

3056 The expected limit was found to be **r<1.69** for optimized bin borders in 10 bins

3057 and optimized pre-selection cuts.

Number of bins	Bin borders						Expected limit
	x_1	x_2	x_3	y_1	y_2	y_3	
16	-0.5	0.4	0.7	-0.5	0.4	0.7	< 1.72
12	-0.5	0.4	0.7	-0.5	0.4	0.7	< 1.72
12	-0.3	0.4	0.7	-0.5	0.4	0.7	< 1.71
12	-0.3	0.3	0.7	-0.5	0.4	0.7	< 1.71
12	-0.3	0.3	0.7	-0.4	0.4	0.7	< 1.70
12	-0.3	0.3	0.7	-0.3	0.4	0.7	< 1.70
12	-0.3	0.3	0.7	-0.3	0.2	0.7	< 1.68
12	-0.3	0.3	0.7	-0.3	0.1	0.7	< 1.70
12	-0.3	0.3	0.7	-0.3	0.2	0.6	< 1.70
10	-0.5	0.4	0.7	-0.5	0.4	0.7	< 1.75
10	-0.3	0.3	0.7	-0.3	0.2	0.6	< 1.69

Table 6.16: Limit variation as a function of bin size in the same-sign dimuon channel. (In bold: the final bin borders used in the $2lss$ channel.)

3058 Two additional binning strategies were tested, however, the obtained limits are
 3059 degraded; they are documented in Appendix C.

3060 6.10 Forward jet mismodeling

3061 As said in previous section, among the features of the tHq signature with that serves
 3062 as a powerful discriminating variable is the presence of a forward jet; unfortunately,
 3063 its η distribution is poorly modeled in simulation. To estimate the effect of a mis-
 3064 modeled forward jet distribution, a reweighting of the events in simulation based on
 3065 the normalized data/MC ratio in a control region is performed; as a result, an al-
 3066 ternative shape of the BDT output distributions that reflects a hypothetical perfect
 3067 data/MC agreement is derived.

3068 Using a sample of dileptonic $t\bar{t}$ events, the control region is defined by requiring
 3069 two opposite-sign tight leptons in the $e\mu$ channel, with at least two jets and at least
 3070 one medium CSV tagged jet. (Otherwise the selection is identical to the same-sign
 3071 $e^\pm\mu^\pm$ channel selection). Some distributions related to the forward jet for MC and

3072 data are shown in Figure 6.24.

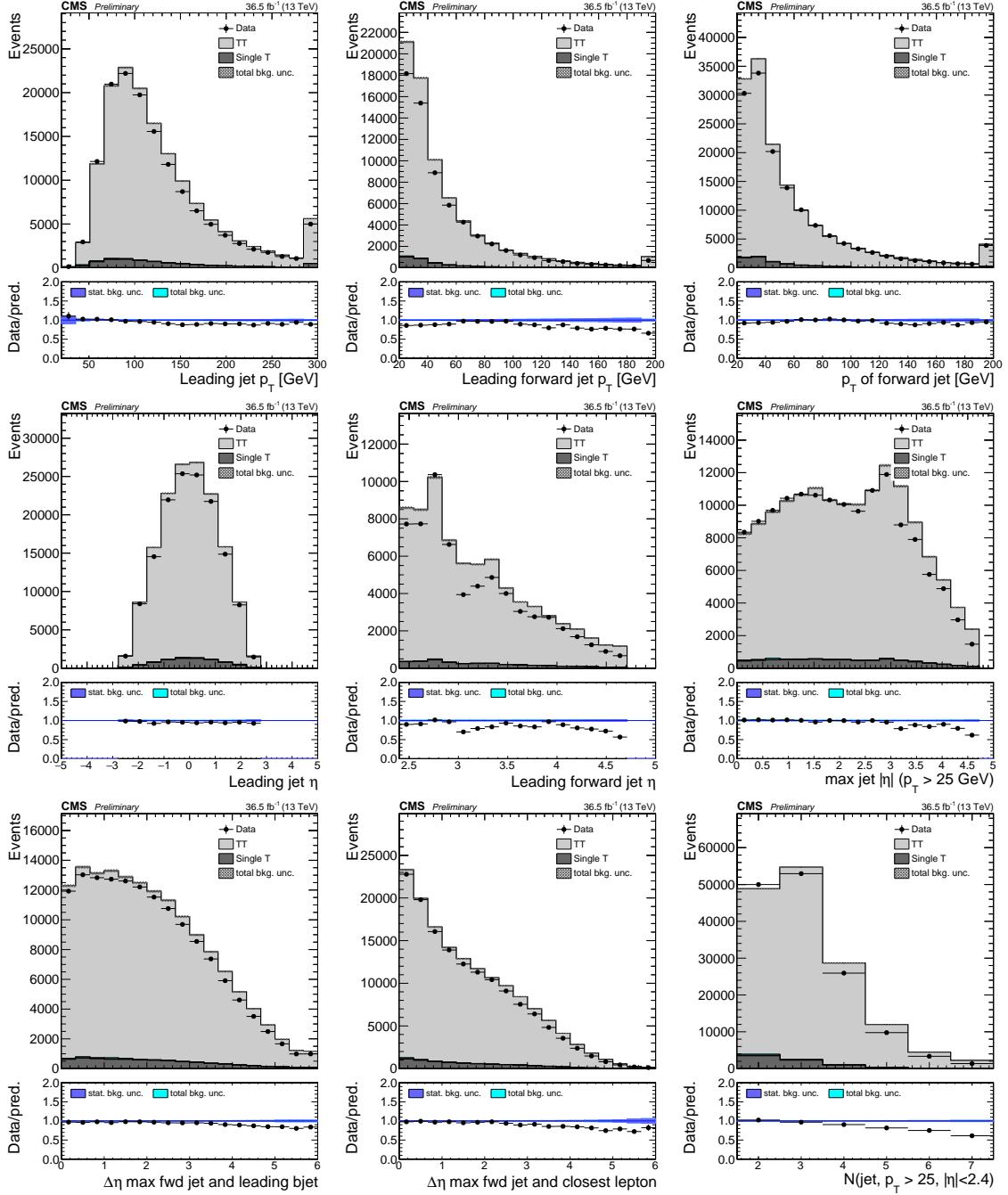


Figure 6.24: Kinematic distributions in the $t\bar{t}$ -enriched opposite-sign $e\mu$ selection. Top row, left to right: leading central ($\eta < 2.4$) jet p_T , leading forward ($\eta > 2.4$) jet p_T , p_T of non-CSV-loose jet with highest η (“light forward jet”). Middle row: η distribution of those same jets. Bottom row: $\Delta\eta$ between light forward jet and leading CSV-loose tagged jet; $\Delta\eta$ between light forward jet and closest lepton; number of central jets.

3073 The disagreement of the η distribution of forward jets for a p_T cut of 25 GeV is
 3074 well visible especially at higher values of $|\eta|$. The multiplicity for central jets is poorly
 3075 described by the MadgraphMLM sample used here; consistent with other observations
 3076 of the same sample. The $t\bar{t}$ background in this analysis is modeled with a data-driven
 3077 method and these disagreements do not directly affect the $t\bar{t}$ contribution in the
 3078 analysis. They do however reflect the expected agreement in these distributions for
 3079 the irreducible backgrounds and the signal.

3080 The effect of higher p_T cuts on the forward jet has been studied for three values:
 3081 25, 30 and 40 GeV. In order to take into account the data/MC disagreement in the
 3082 high η regions, the events are weighted accordingly to the data/MC ratio of the unity
 3083 normalized control plots shown in Figure 6.25. The data/MC agreement in the
 3084 forward jet η distribution improves significantly at higher jet p_T s.

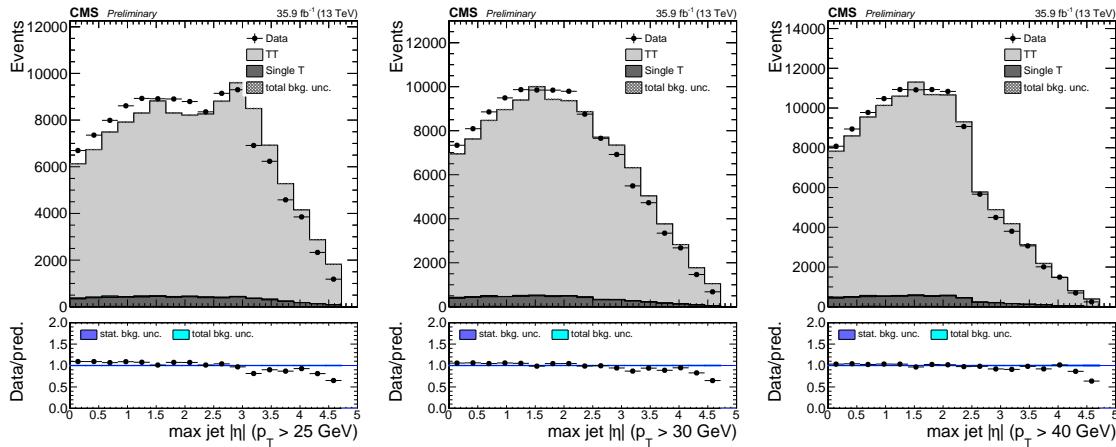


Figure 6.25: Pseudorapidity distributions of the most forward, non-CSV-loose tagged jet in the $t\bar{t}$ -enriched opposite-sign $e\mu$ selection for the three p_T values studied.

3085 Table 6.17 shows the scale factors obtained for the three p_T values. The expected
 3086 limit on cross section in the $3l$ was used to determine the most appropriate forward
 3087 jet p_T cut; higher p_T cut improves from 1.54 at 25 GeV to 1.51 at 30 GeV and 1.50
 3088 at 40 GeV. The impact of the data/MC disagreement for forward jet η is observed

η range	$p_T > 25$ GeV	$p_T > 30$ GeV	$p_T > 40$ GeV
0 – 0.278	1.0925	1.0566	1.0326
0.278 – 0.556	1.0920	1.0617	1.0407
0.556 – 0.833	1.0675	1.0459	1.0244
0.833 – 1.111	1.0888	1.0593	1.0340
1.111 – 1.389	1.0759	1.0508	1.0322
1.389 – 1.667	1.0109	0.9847	0.9661
1.667 – 1.944	1.0727	1.0448	1.0239
1.944 – 2.222	1.0715	1.0457	1.0169
2.222 – 2.500	1.0112	0.9871	0.9746
2.500 – 2.778	1.0387	0.9942	0.9816
2.778 – 3.056	0.9687	0.9427	0.9200
3.056 – 3.333	0.8137	0.8695	0.9092
3.333 – 3.611	0.9010	0.9387	0.9807
3.611 – 3.889	0.8685	0.8887	0.9213
3.889 – 4.167	0.9277	0.9466	1.0135
4.167 – 4.444	0.8111	0.8278	0.8637
4.444 – 4.722	0.6497	0.6485	0.6367
4.722 – 5.000	1.0000	1.0000	1.0000
Exp. limit ($\ell\ell\ell$)	$r < 1.54$	$r < 1.51$	$r < 1.50$

Table 6.17: Data/MC scale factors for η distribution of most forward, non-tagged jet with three different p_T cuts, see Figure 6.25.

3089 to reduce with higher p_T cuts. Figures F.1, F.2 and F.3 show this reduction in the
 3090 impact of the forward jet η nuisance in the fit.

3091 6.11 Signal model

3092 It is worth to remind that the main goal of this analysis is to test the compatibility
 3093 of points in the parameter space of Higgs-to-vector boson and Higgs-to-top quark
 3094 couplings. This is achieved by using simulated tHq , tHW , and $t\bar{t}H$ signal events
 3095 which are weighted to reflect the impact of the couplings on kinematic distributions,
 3096 and together with different predictions of the respective production cross sections and
 3097 branching ratios, to produce limits on the cross section for different values of κ_V and

3098 κ_t . See Section 6.4.3 and Table A.3 for the set of κ_t and κ_V values generated. The
 3099 slight shape-dependence of the BDTG classifier outputs as a function of the couplings
 3100 is showed in Appendix D.

3101 In addition to the (κ_t, κ_V) dependence of the tHq and tHW production cross
 3102 sections, due to interferences, the cross section of $t\bar{t}H$ depends quadratically on κ_t
 3103 according to []:

$$\sigma(tHq) = (2.633\kappa_t^2 + 3.578\kappa_V^2 - 5.211\kappa_t\kappa_V) * \sigma_{SM}(tHq), \quad (6.7)$$

$$\sigma(tHW) = (2.909\kappa_t^2 + 2.310\kappa_V^2 - 4.220\kappa_t\kappa_V) * \sigma_{SM}(tHW), \quad (6.8)$$

$$\sigma(t\bar{t}H) = \kappa_t^2 * \sigma_{SM}(t\bar{t}H). \quad (6.9)$$

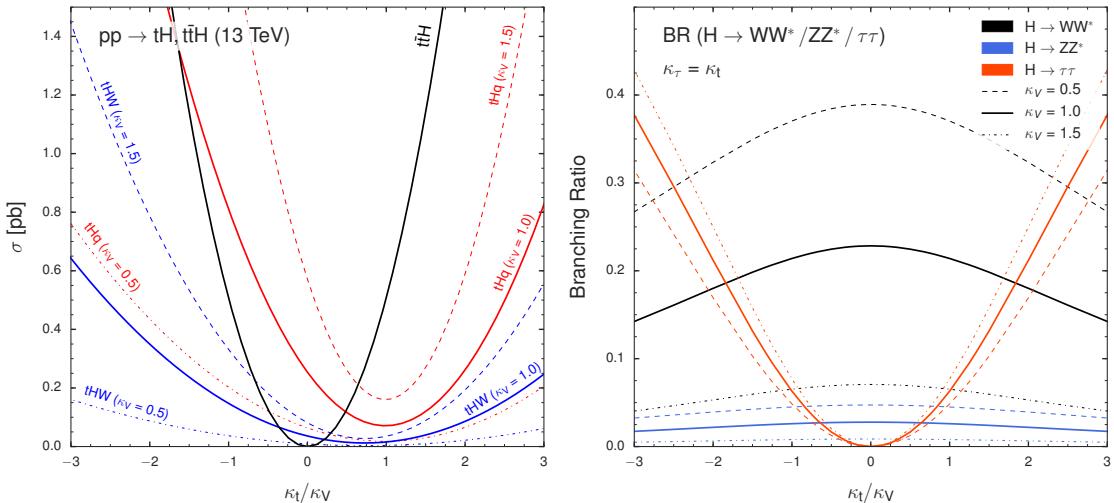


Figure 6.26: Scaling of the tHq , tHW , and $t\bar{t}H$ production cross sections (left) and of the $H \rightarrow WW^*$, $H \rightarrow \tau\tau$, and $H \rightarrow ZZ^*$ branching ratios (right), as a function of κ_t/κ_V , for three different values of κ_V .

3104 The Higgs branching fractions to vector bosons depend on κ_V , and the overall
 3105 Higgs decay width depend both on κ_t and κ_V when considering resolved top-quark

loops in the $H \rightarrow \gamma\gamma$, $H \rightarrow Z\gamma$, and $H \rightarrow gg$ decays. The relative contributions from $H \rightarrow WW$, $H \rightarrow ZZ$, and $H \rightarrow \tau\tau$ also changes with changing κ_V .

If the Higgs-to-tau coupling modifier (κ_τ) is assumed to be equal to κ_t , the relative fractions of WW , ZZ , and $\tau\tau$ in the event selection will only depend on the ratio of κ_t/κ_V ; thus, any limit set at any given value of κ_t/κ_V is valid for all values of κ_t and κ_V with that ratio, and could then be compared with theoretical predictions of cross sections at different values of either modifier. Figure 6.26 shows the tHq , tHW and $t\bar{t}H$ cross sections(left) and the Higgs boson branching ratios $H \rightarrow WW$, $H \rightarrow ZZ$, and $H \rightarrow \tau\tau$ (right) as a function of the κ_t/κ_V ratio.

Thus, this analysis sets an upper limit on the combined cross section times branching ratio of tHq , tHW , and $t\bar{t}H$ as a function of the ratio κ_t/κ_V .

Similar interpretation can be made if instead of reporting the limits as a function of the κ_t/κ_V ratio, they are reported as a function of the relative strength of Higgs-top and Higgs-vector-boson couplings, multiplied by the relative sign

$$f_t = \text{sign}\left(\frac{\kappa_t}{\kappa_V}\right) \times \frac{\kappa_t^2}{\kappa_t^2 + \kappa_V^2}. \quad (6.10)$$

this parameter covers the full space between -1.0 and 1.0 , with the SM expectation at 0.5 . Absolute values of 1.0 or 0.0 would correspond to purely Higgs-top and purely Higgs-V couplings, respectively.

Table 6.18 shows the points in the κ_t/κ_V and f_t parameter space that are mapped by the 51 individual κ_t and κ_V points.

The overall Higgs decay width (modified by both κ_t and κ_V) becomes irrelevant if limits are quoted as absolute cross sections rather than multiples of the expected cross section (which depends on it).

The 1D histograms of events as categorized in regions of the 2D BDTG plane are

f_t	κ_t/κ_V	$\kappa_V = 0.5$	$\kappa_V = 1.0$	$\kappa_V = 1.5$
-0.973	-6.000	-3.00		
-0.941	-4.000	-2.00		
-0.900	-3.000	-1.50	-3.00	
-0.862	-2.500	-1.25		
-0.800	-2.000	-1.00	-2.00	-3.00
-0.692	-1.500	-0.75	-1.50	
-0.640	-1.333			-2.00
-0.610	-1.250		-1.25	
-0.500	-1.000	-0.50	-1.00	-1.50
-0.410	-0.833			-1.25
-0.360	-0.750		-0.75	
-0.308	-0.667			-1.00
-0.200	-0.500	-0.25	-0.50	-0.75
-0.100	-0.333			-0.50
-0.059	-0.250		-0.25	
-0.027	-0.167			-0.25
0.000	0.000	0.00	0.00	0.00
0.027	0.167			0.25
0.059	0.250		0.25	
0.100	0.333			0.50
0.200	0.500	0.25	0.50	0.75
0.308	0.667			1.00
0.360	0.750		0.75	
0.410	0.833			1.25
0.500	1.000	0.50	1.00	1.50
0.610	1.250		1.25	
0.640	1.333			2.00
0.692	1.500	0.75	1.50	
0.800	2.000	1.00	2.00	3.00
0.862	2.500	1.25		
0.900	3.000	1.50	3.00	
0.941	4.000	2.00		
0.973	6.000	3.00		

Table 6.18: The 33 distinct values of κ_t/κ_V and f_t as mapped by the 51 κ_t and κ_V points.

then used in a maximum likelihood fit of signal and background shapes, where the tHq , tHW , and $t\bar{t}H$ signals are floating with a common signal strength modifier r , producing a 95% C.L. upper limit the observed cross section of $tHq + tHW + t\bar{t}H$.

3132 This procedure is done separately for each point (κ_t, κ_V) where the cross sections
 3133 and branching fractions are scaled accordingly in each point. Limits at fixed values
 3134 of κ_t/κ_V are by construction identical. Tables G.1–G.3 and G.4–G.6 in Appendix G
 3135 show the scalings of cross section times branching fraction, as well as branching
 3136 fractions alone for each of the Higgs decay modes and each of the signal components.

3137 6.12 Systematic uncertainties

3138 The uncertainties present in this analysis can be either of statistical nature given
 3139 the size of the samples and the probabilistic nature of the processes, or of system-
 3140 atic nature. The systematic uncertainties are associated to theoretical uncertainties
 3141 originating in the limited knowledge of the processes, and also to experimental uncer-
 3142 tainties originating for instance from the limited resolution of the detectors. In this
 3143 section, the contributions to the systematic uncertainties from all the sources in this
 3144 analysis are considered.

3145 Rate uncertainties associated to the application of scaling factors for the affected
 3146 processes, and shape uncertainties which affect not only the normalization but also
 3147 the shape of certain distributions, compose the systematic uncertainties. The latter
 3148 can affect the analysis during the event selection; therefore, these systematic shape
 3149 uncertainties are applied to the simulation samples.

3150 Experimental uncertainties.

3151 • *Luminosity.* The measurement of the luminosity delivered by the LHC is af-
 3152 fected by experimental conditions like pileup and the number of protons per
 3153 bunch. Due to variations in the LHC running parameters an uncertainty of
 3154 2.6% is applied.

- 3155 • *Lepton efficiencies.* Systematic uncertainties in the signal selection efficiency
 3156 arise from correction factors applied to the simulated events in order to better
 3157 match the measured detector performance; also from theoretical uncertainties in
 3158 the modeling of the signal process. Data/MC differences in the trigger efficiency
 3159 accounted with scale factors applied to correct for them, lepton reconstruction
 3160 and identification performance, and lepton selection efficiency carry a combined
 3161 uncertainty of about 5% per lepton.

- 3162 • *Jets related uncertainties.* Jet energy corrections affect the uncertainty in the
 3163 signal selection efficiency it is evaluated by varying the correction factors within
 3164 their uncertainties and propagating the effects to the final results by recalculat-
 3165 ing the kinematic quantities. The effects of the jet energy scale uncertainties,
 3166 ***b***-tagging efficiency and forward jet mismodeling are evaluated using dedicated
 3167 shape templates derived from a variation of the jet energy scale within its uncer-
 3168 tainty and from varying the ***b***-tagging forward jet data/MC scale factors within
 3169 their uncertainty.

3170 **Theory uncertainties**

3171 The uncertainties from unknown higher orders of tHq and tHW production are
 3172 estimated from a change in the Q^2 scale of double and half the initial value, evaluated
 3173 for each point of κ_t and κ_V . The $t\bar{t}H$ signal component has an uncertainty of about
 3174 +5.8/-9.2% from Q^2 scale variations and a further 3.6% from the knowledge of
 3175 PDFs and α_s [57]. Uncertainties related to the choice of PDF set and its scale are
 3176 estimated to be about 3.7% for tHq and about 4.0% for tHW .

3177 The theoretical uncertainties from unknown higher orders for $t\bar{t}W$ and $t\bar{t}Z$ are 12%
 3178 and 10% respectively; additional uncertainties from the knowledge of PDFs and α_s
 3179 of about 4% each for $t\bar{t}W$ and $t\bar{t}Z$ are estimated.

3180 **Backgrounds**

3181 Besides the theory uncertainties on $t\bar{t}W$ and $t\bar{t}Z$, uncertainties of the smaller irre-
 3182 ducible backgrounds and the charge mis-identification estimate are covered with flat
 3183 normalization uncertainties. The WZ contribution due to the scale factor is derived
 3184 during the background estimation using the control region.

3185 The dominant uncertainty is associated to the estimate of the non-prompt lepton
 3186 contribution using a fake rate method; the main normalization uncertainty comes from
 3187 limited statistics in the data control region, and the subtraction of residual prompt
 3188 lepton contribution as stated in section 6.7.2. Shape variations resembling data/MC
 3189 differences and deviations in closure test are evaluated as shape uncertainties.

3190 **Fake rate closure uncertainties**

3191 In order to determine the systematic uncertainties associated to the fake rates,
 3192 the BDTG classifier output shapes from a pure MC estimation of fake leptons (in
 3193 $t\bar{t}$) and from the application of fake-rates as measured in QCD MC, applied in $t\bar{t}$
 3194 MC events, are compared. The difference in the resulting normalization and output
 3195 shapes, for both trainings vs. $t\bar{t}$ and vs. $t\bar{t}V$, are estimated and propagated to the
 3196 fit as normalization and shape variations; Figures 6.27 and 6.28 show the results of
 3197 these closure tests.

3198 Table 6.19 list all the systematic uncertainties currently considered in the analysis.

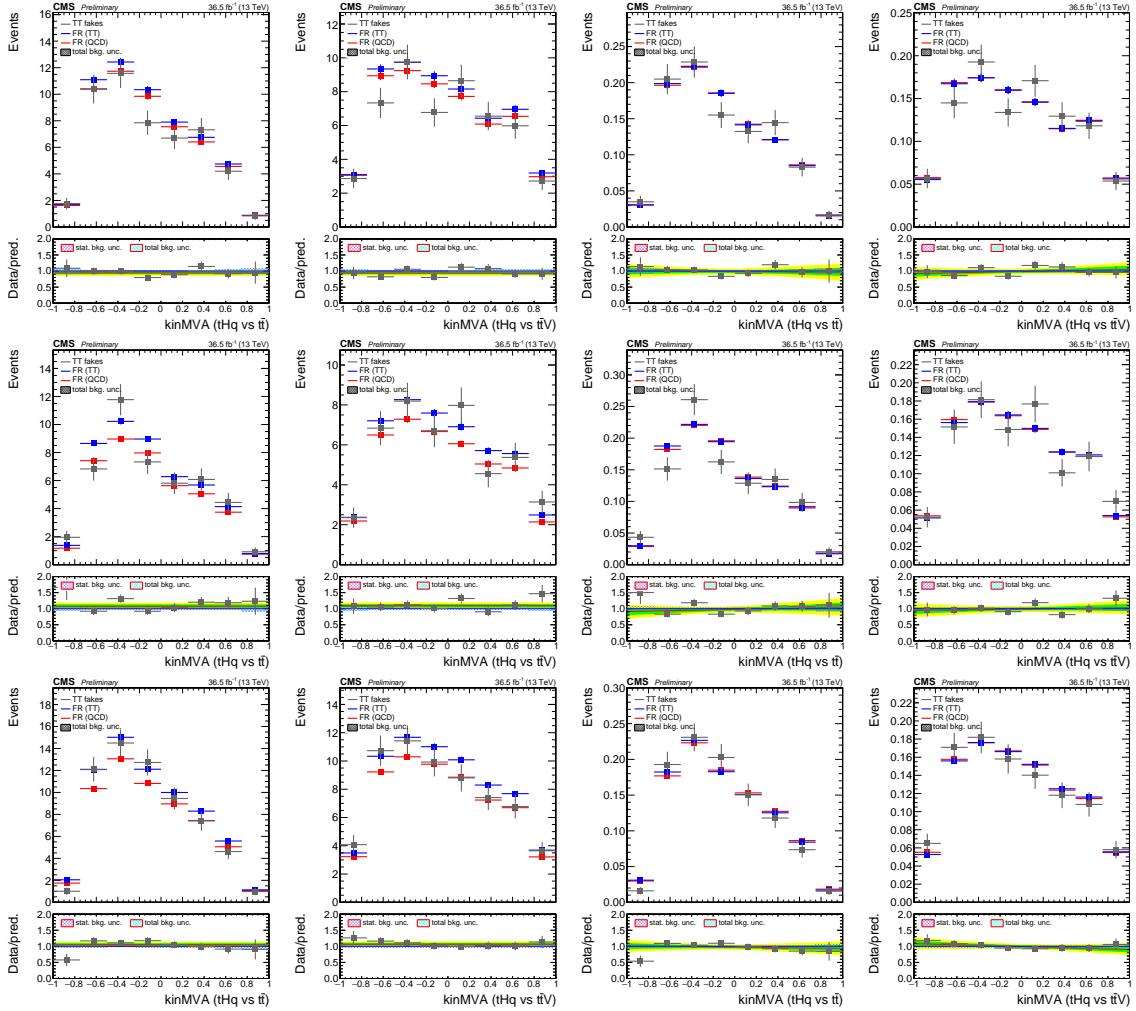


Figure 6.27: BDT outputs comparing $t\bar{t}$ MC to a fake-rate prediction using fake rates measured in QCD MC. Agreement in normalization is estimated from the plots in the two left columns, shape disagreement is estimated from the (normalized) plots in the two right columns. From top to bottom rows: same-sign $e^\pm \mu^\mp$ selection with electron fakes, same-sign $e^\pm \mu^\mp$ selection with muon fakes, same-sign $\mu^\pm \mu^\pm$ selection.

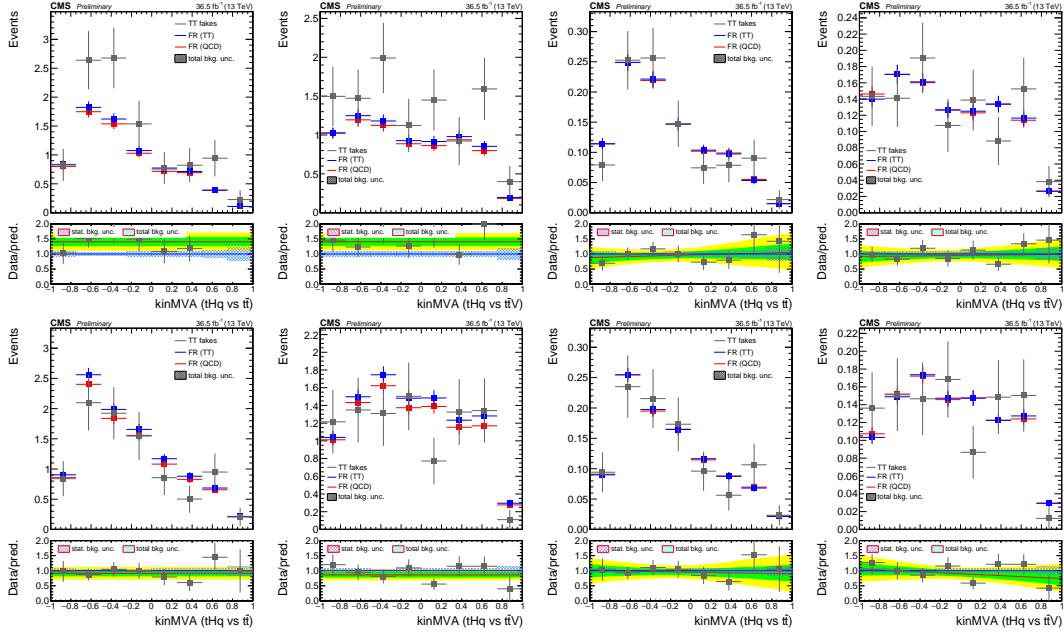


Figure 6.28: BDT outputs comparing $t\bar{t}$ MC to a fake-rate prediction using fake rates measured in QCD MC. Agreement in normalization is estimated from the plots in the two left columns, shape disagreement is estimated from the (normalized) plots in the two right columns. From top to bottom rows: three lepton selection with electron fakes, three lepton selection with muon fakes.

Source	Channel	Size
Experimental uncertainties		
Luminosity	all	1.026
Loose lepton efficiency		1.02 per lepton
Tight lepton efficiency		1.03 per lepton
Trigger efficiency	$\mu^\pm \mu^\pm$ $e^\pm \mu^\pm$ $\ell\ell\ell$	1.01 1.01 1.03
Jet energy scale	all	templates
Forward jet modeling	all	templates, see Tab. 6.17
_tagging efficiency	all	templates
Theory uncertainties		
Q^2 scale (tHq)	all	0.92–1.06 (depending on κ_t, κ_V)
Q^2 scale (tHW)	all	0.93–1.05 (depending on κ_t, κ_V)
Q^2 scale ($t\bar{t}H$)	all	0.915/1.058
Q^2 scale ($t\bar{t}W$)	all	1.12
Q^2 scale ($t\bar{t}Z$)	all	1.11
pdf ($t\bar{t}H$)	all	1.036
pdf gg ($t\bar{t}Z$)	all	0.966
pdf $q\bar{q}$ ($t\bar{t}W$)	all	1.04
pdf qg (tHq)	all	1.037
pdf qg (tHW)	all	1.040
Higgs branching fractions		
param_alphaS	all	1.012
param_mB	all	0.981
HiggsDecayWidthTHU_hqq	all	0.988
HiggsDecayWidthTHU_hvv	all	1.004
HiggsDecayWidthTHU_hll	all	1.019
Backgrounds		
WZ control region statistics	$\ell\ell\ell$	1.10
WZ control region backgrounds	$\ell\ell\ell$	1.20
WZ modeling	$\ell\ell\ell$	1.07
$WZ + 2\text{jet}$ background	$\mu^\pm \mu^\pm, e^\pm \mu^\pm$	1.50
Rare SM processes	all	1.50
Charge flips	$e^\pm \mu^\pm$	1.30
Fake rate estimate		
Electron FR measurement		templates
Muon FR measurement		templates
Electron closure	$e^\pm \mu^\pm$	0.94 norm., (0.98 ($t\bar{t}$))/1.07 ($t\bar{t}V$)) shape var.
	$\ell\ell\ell$	1.40 norm., (1.09 ($t\bar{t}$))/1.05 ($t\bar{t}V$)) shape var.
Muon closure	$\mu^\pm \mu^\pm$	1.07 norm., (0.97 ($t\bar{t}$))/0.91 ($t\bar{t}V$)) shape var.
	$e^\pm \mu^\pm$	1.09 norm., (1.06 ($t\bar{t}$))/1.03 ($t\bar{t}V$)) shape var.
	$\ell\ell\ell$	1.09 norm., (0.95 ($t\bar{t}$))/0.83 ($t\bar{t}V$)) shape var.

Table 6.19: Pre-fit size of systematic uncertainties.

3199 6.13 Results

3200 As a result of applying the event pre-selection on the dataset, 127 events are observed
 3201 in the $3l$ channel, 280 in the $2lss \mu^\pm \mu^\pm$ channel and 525 in the $2lss e^\pm \mu^\pm$ channel
 3202 as shown in Table 6.8. These events are then classified into one of ten categories,
 3203 depending on the output of the two BDTG classifiers and according to the optimized
 binning strategy.

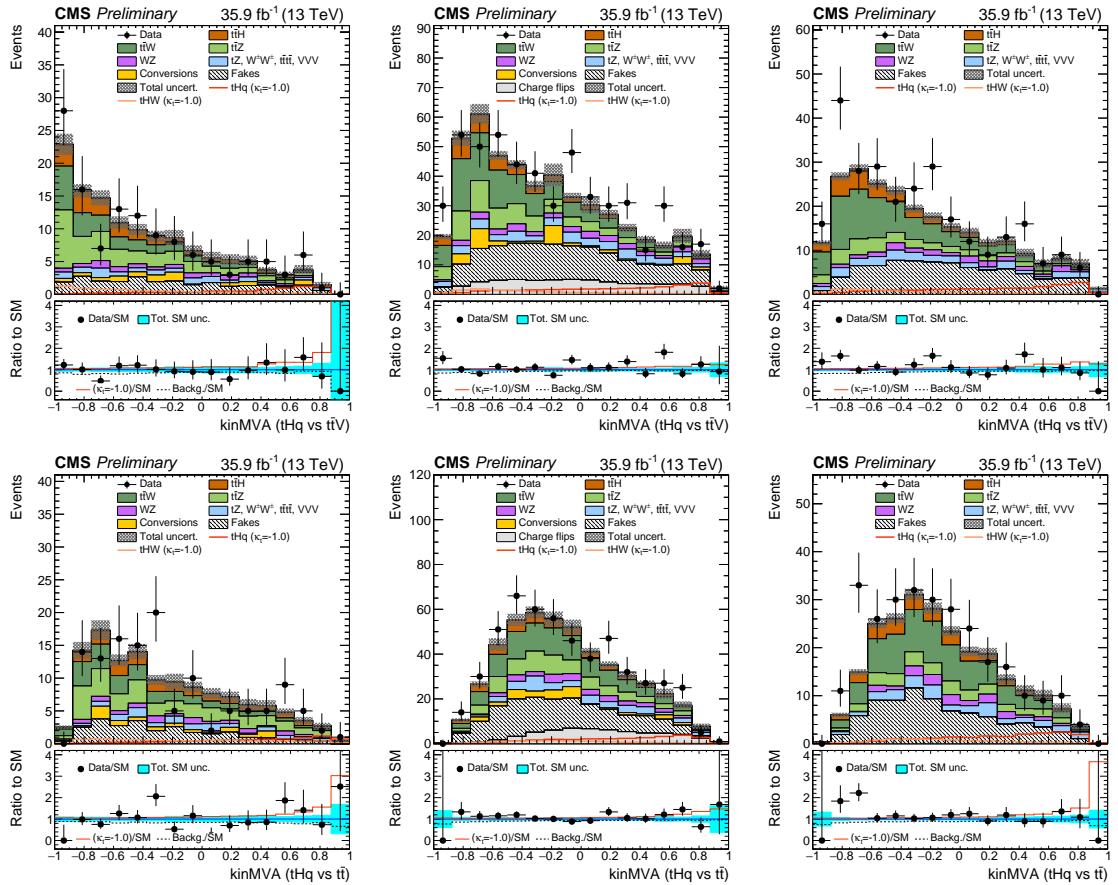


Figure 6.29: Pre-fit BDT classifier outputs, for the three-lepton channel (left), $e^\pm \mu^\pm$ (center), and $\mu^\pm \mu^\pm$ (right), for 35.9 fb^{-1} , for training against $t\bar{t}V$ (top row) and against $t\bar{t}$ (bottom row). In the box below each distribution, the ratio of the observed and predicted event yields is shown. The shape of the two tH signals for $\kappa_t = -1.0$ is shown, normalized to their respective cross sections for $\kappa_t = -1.0, \kappa_V = 1.0$. The grey band represents the unconstrained (pre-fit) statistical and systematical uncertainties.

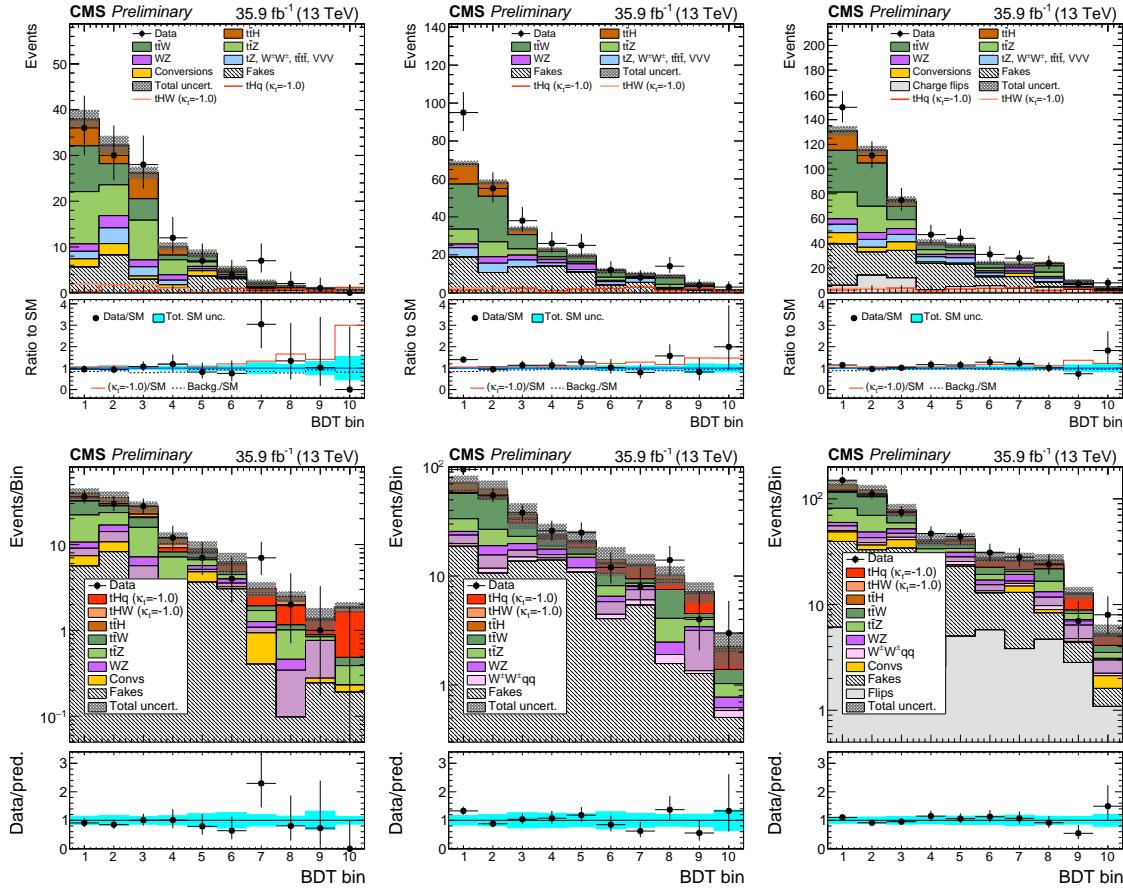


Figure 6.30: Expected (pre-fit) distributions in the final binning used for the signal extraction, for (from left to right) the three lepton channel, the $\mu^{\pm}\mu^{\pm}$ channel, and the $e^{\pm}\mu^{\pm}$ channel. Linear scale (top row), and logarithmic scale (bottom row).

3205 The pre-fit distributions of BDTG outputs are shown in Figure 6.29, while the
 3206 pre-fit distributions in the final binning used in the signal extraction are shown in
 3207 Figure 6.30.

3208 The expected signal and background shapes for the distribution in the one-dimensional
 3209 histogram (with ten bins) are fit to the observed data in a maximum likelihood fit,
 3210 for all three channels simultaneously and separately for the signal shapes for each of
 3211 the 33 κ_t/κ_V coupling configuration points.

3212 The tH and $t\bar{H}$ production cross sections and the Higgs decay branching ratios are
 3213 modified in each point with the Higgs-top (κ_t) and Higgs-vector boson (κ_V) coupling

3214 strength

3215 while the Higgs-tau coupling strength modifier (κ_τ) is assumed to be equal to κ_t ,
 3216 while the rest of the parameters are assumed to be at the SM predicted values; there-
 3217 fore, the combined signal shape is uniquely defined by the ratio of κ_t/κ_V . In the fit,
 3218 the signal components, tH and $t\bar{t}H$, are floated with a common signal strength mod-
 3219 ifier (defined as the ratio to the expected cross section) to produce a 95% confidence
 3220 level (C.L.) upper limit on the observed $tH + t\bar{t}H$ cross section times the combined
 3221 branching ratio of $H \rightarrow WW^* + ZZ^* + \tau\tau$.

3222 The post-fit categorized BDT output distributions obtained in the maximum like-
 3223 lihood fit to extract the limits, are shown in Figure 6.31.

3224 As expected, the signal contribution is very small compared to the background
 3225 contribution; however, it is possible to see the signal contribution in data by
 3226 subtracting the background from the overall BDT output distributions as shown in
 3227 Figure 6.32 for the inverted coupling scenario ($\kappa_V = 1, \kappa_t = -1$) and Figure 6.33 for the
 3228 SM-like scenario ($\kappa_V = 1, \kappa_t = -1$).

3229 The observed 95% C.L. upper limits on the $tH + ttH$ signal cross sections for
 3230 the case of inverted couplings ($\hat{I}\check{z}t/\hat{I}\check{z}V = \sqrt{1.0}$) for the individual channels are,
 3231 respectively, 1.00, 0.84, and 0.70 pb for the $\ell\ell\ell\ell$, $e\ell\ell\ell$, and trilepton final states,
 3232 corresponding to 2.3, 1.9, and 1.6 times the respective expected cross sections for $\hat{I}\check{z}V$
 3233 = 1.0. The combination of all three channels yields a limit of 0.64 pb on a signal
 3234 shape expected for $\hat{I}\check{z}t/\hat{I}\check{z}V = \sqrt{1.0}$, corresponding to 1.4 times the expected tH
 3235 + ttH cross section with $\hat{I}\check{z}t = \sqrt{1.0}$, $\hat{I}\check{z}V = 1.0$. In the standard model scenario
 3236 ($\hat{I}\check{z}t/\hat{I}\check{z}V = 1.0$), the observed upper limit on the cross section times branching ratio
 3237 is 0.56 pb, corresponding to 3.1 times the expected SM cross section of $tH + ttH$.
 3238 Table 4 summarizes the results for the inverted coupling scenario and for the standard
 3239 model. The best-fit combined signal strength for the standard model hypothesis is

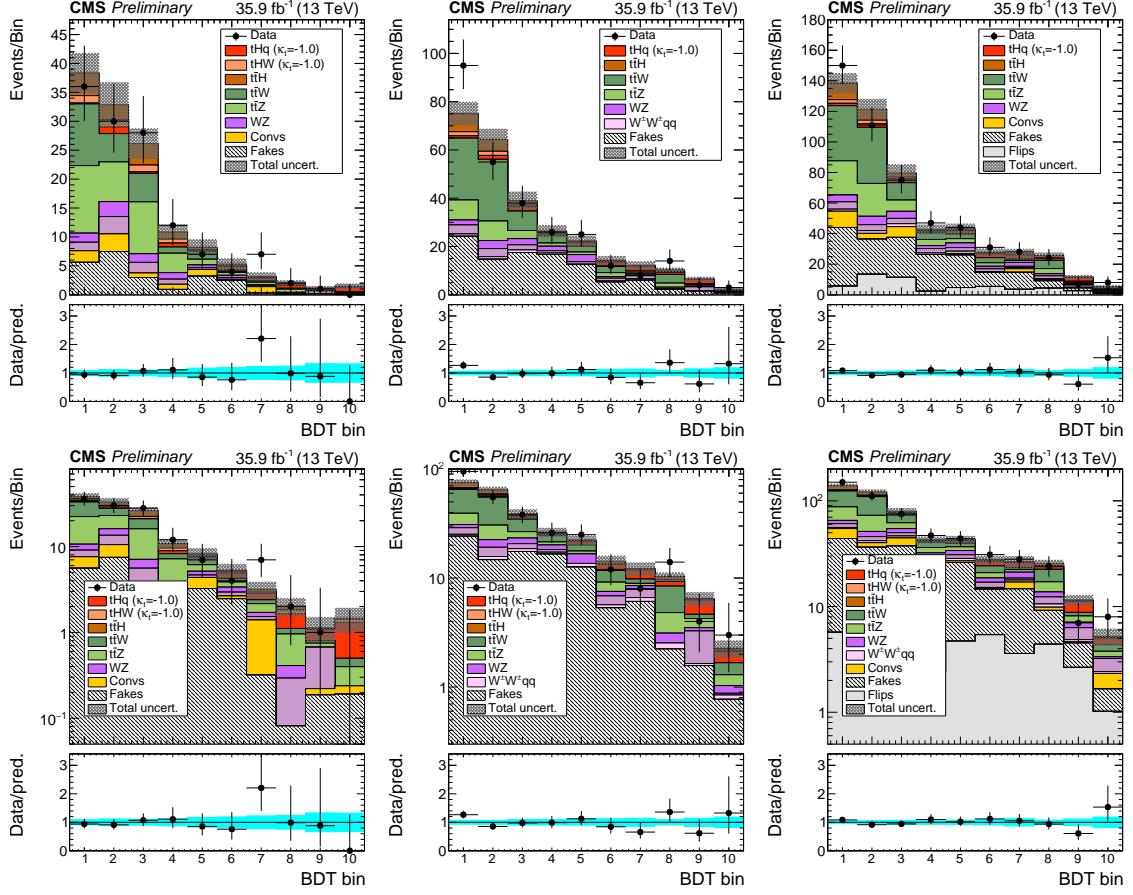


Figure 6.31: Post-fit distributions in the final binning used for the signal extraction, for (from left to right) the three lepton channel, the $\mu^\pm\mu^\pm$ channel, and the $e^\pm\mu^\pm$ channel. Linear scale (top row), and logarithmic scale (bottom row).

3240 1.8 \pm 0.3(stat.) \pm 0.6(syst.), corresponding to an observed significance of 2.7 \sqrt{C}
 3241 (1.5 \sqrt{C} expected) over a backgroundonly hypothesis. For a scenario of inverted cou-
 3242 plings ($\hat{t}z_t = \hat{t}z_1 = \hat{t}z_V$), the best fit signal strength is 0.7 \pm 0.4, correspond-
 3243 ing to a significance of 1.7 \sqrt{C} (2.5 \sqrt{C} expected), whereas the fit prefers a signal strength
 3244 compatible with 0 for a scenario with $\hat{t}z_t = 0$ (where the ttH component vanishes).
 3245 The expected and observed limits are shown in Fig. 7 as a function of $\hat{t}z_t/\hat{t}z_V$. Com-
 3246 paring the observed upper limit with the theoretical prediction of the tH + ttH cross
 3247 section times BR for $\hat{t}z_V = 1.0$ constrains the allowed range of coupling configura-
 3248 tions $\hat{t}z_t/\hat{t}z_V$ to between about ± 1.25 and ± 1.60 . The sensitivity of the analysis

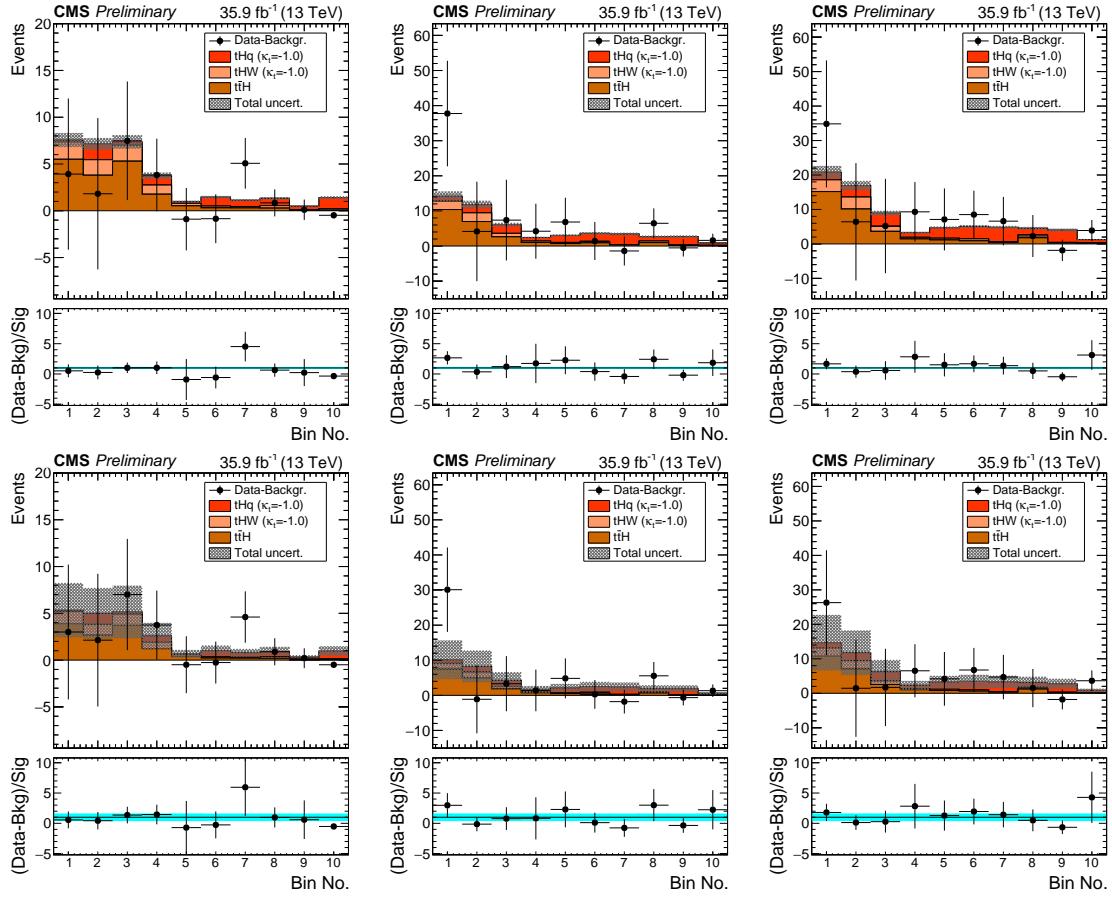


Figure 6.32: Background-subtracted pre- (top) and post-fit (bottom) distributions in the final binning used for the signal extraction, for three lepton channel (left), the $\mu^\pm\mu^\pm$ channel (center), and the $e^\pm\mu^\pm$ channel (right). For a fit in the inverted couplings scenario ($\kappa_V = 1, \kappa_t = -1$).

is limited by systematic uncertainties, predominantly by those concerning the normalizations of the main background components (the non-prompt lepton estimation, the scale uncertainties for $t\bar{t}W$ and $t\bar{t}Z$), as well as by the uncertainties on the measured lepton efficiency.

The asymptotic upper CL_S limits at 95% C.L. on the combined production cross section of tHq , tHW , and $t\bar{t}H$ (reported as an upper limit on the cross section times modified branching ratio), for each of the 51 coupling configurations, see Tab. 6.20. The limits and best-fit values of the signal cross section (and corresponding signal

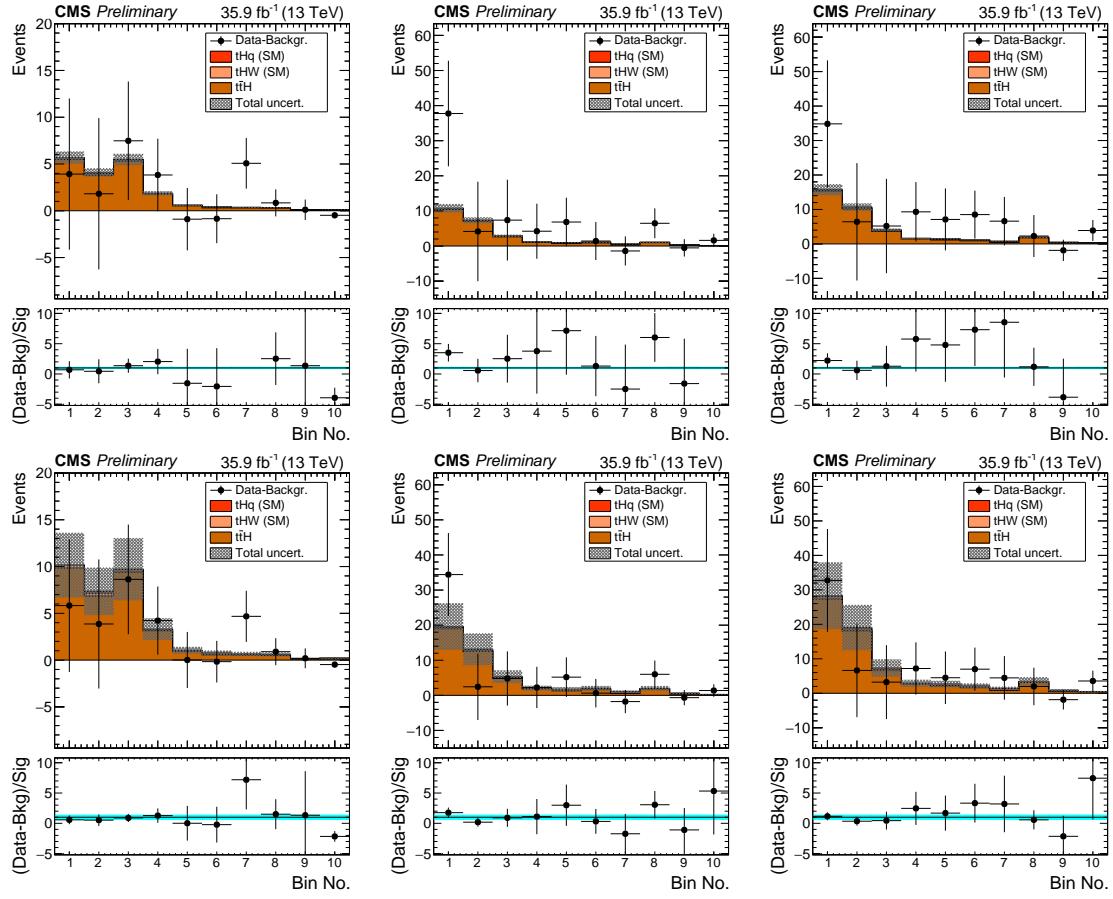


Figure 6.33: Background-subtracted pre- (top) and post-fit (bottom) distributions in the final binning used for the signal extraction, for the three lepton channel (left), the $\mu^\pm\mu^\pm$ channel (center), and the $e^\pm\mu^\pm$ channel (right). For a fit in the SM-like scenario ($\kappa_t = \kappa_V = 1$).

strength at $\kappa_V = 1.0$) for each point are given in Tab. 6.22, and in Tab. 6.21 for the two main hypotheses, split by channel. In the SM point a signal strength of $1.82^{+0.34}_{-0.33}(\text{stat.})^{+0.55}_{-0.59}(\text{syst.})$ (compared to the SM cross section at $\kappa_V = 1.0$) is obtained, corresponding to a cross section of $0.33 \pm 0.12 \text{ pb}$. The observed significance of the signal, in a background-only hypothesis, is 2.7σ , with an a-priori expected significance of 1.5σ . Without considering systematic uncertainties, the significance increases to 6.2σ . A scan of the observed and expected significances for each coupling configuration is shown in Fig. 6.37.

3265 The pulls and impacts of the most important nuisance parameters are shown in
 3266 Fig. 6.38.

Scenario	Channel	Obs. Limit	Exp. Limit				
			-2σ	-1σ	Median	$+1\sigma$	$+2\sigma$
$\kappa_V = 1.0$	$\mu^\pm \mu^\pm$	2.3	0.71	0.94	1.32	1.88	2.60
$\kappa_t = -1.0$	$e^\pm \mu^\pm$	1.9	0.65	0.87	1.21	1.71	2.32
	$\ell\ell\ell$	1.6	0.43	0.59	0.86	1.26	1.78
	Combined ($\mu\mu, 3\ell$)	1.6	0.40	0.54	0.78	1.12	1.57
	Combined ($\mu\mu, e\mu, 3\ell$)	1.4	0.37	0.50	0.71	1.03	1.43
(SM)	$\mu^\pm \mu^\pm$	4.9	1.20	1.61	2.27	3.24	4.54
$\kappa_V = 1.0$	$e^\pm \mu^\pm$	3.3	1.10	1.48	2.07	2.95	4.06
$\kappa_t = 1.0$	$\ell\ell\ell$	3.0	0.91	1.22	1.73	2.49	3.47
	Combined ($\mu\mu, 3\ell$)	3.4	0.79	1.07	1.51	2.17	3.01
	Combined ($\mu\mu, e\mu, 3\ell$)	3.1	0.71	0.96	1.36	1.94	2.70

Table 6.20: Expected and observed CLS limits (at 95% C.L.) on the signal strength of combined $tH + t\bar{t}H$ production in each channel, and for different combinations thereof, for a scenario with inverted couplings ($\kappa_V = 1.0$, $\kappa_t = -1.0$, top section), and for the standard model ($\kappa_V = \kappa_t = 1.0$, bottom section). Numbers are for $35.9 fb^{-1}$.

Scenario	Channel	Obs. Limit	Exp. Limit (pb)		
			(pb)	Median	$\pm 1\sigma$
$\kappa_t/\kappa_V = -1$	$\mu^\pm \mu^\pm$	1.00	0.58	[0.42, 0.83]	[0.31, 1.15]
	$e^\pm \mu^\pm$	0.84	0.54	[0.39, 0.76]	[0.29, 1.03]
	$\ell\ell\ell$	0.70	0.38	[0.26, 0.56]	[0.19, 0.79]
	Combined	0.64	0.32	[0.22, 0.46]	[0.16, 0.64]
$\kappa_t/\kappa_V = 1$ (SM-like)	$\mu^\pm \mu^\pm$	0.87	0.41	[0.29, 0.58]	[0.22, 0.82]
	$e^\pm \mu^\pm$	0.59	0.37	[0.26, 0.53]	[0.20, 0.73]
	$\ell\ell\ell$	0.54	0.31	[0.22, 0.43]	[0.16, 0.62]
	Combined	0.56	0.24	[0.17, 0.35]	[0.13, 0.49]

Table 6.21: Expected and observed 95% C.L. upper limits on the $tH + t\bar{t}H$ production cross section times $H \rightarrow WW^* + \tau\tau + ZZ^*$ branching ratio for a scenario of inverted couplings ($\kappa_t/\kappa_V = -1.0$, top rows) and for a standard-model-like signal ($\kappa_t/\kappa_V = 1.0$, bottom rows), in pb. The expected limit is calculated on a background-only Asimov dataset and quoted with $\pm 1\sigma$ and $\pm 2\sigma$ probability ranges.

f_t	κ_t/κ_V	Exp. lim.	SM exp.	Obs. lim.	Best fit σ [pb]	Best fit r
-0.973	-6.000	0.328 $^{+0.136}_{-0.090}$	0.507 $^{+0.206}_{-0.158}$	0.603	0.305 $^{+0.155}_{-0.169}$	0.013 $^{+0.007}_{-0.007}$
-0.941	-4.000	0.335 $^{+0.137}_{-0.098}$	0.509 $^{+0.215}_{-0.166}$	0.627	0.322 $^{+0.157}_{-0.174}$	0.036 $^{+0.018}_{-0.020}$
-0.900	-3.000	0.335 $^{+0.138}_{-0.096}$	0.510 $^{+0.215}_{-0.172}$	0.639	0.334 $^{+0.160}_{-0.173}$	0.075 $^{+0.036}_{-0.039}$
-0.862	-2.500	0.334 $^{+0.139}_{-0.097}$	0.505 $^{+0.217}_{-0.173}$	0.649	0.341 $^{+0.160}_{-0.174}$	0.119 $^{+0.056}_{-0.061}$
-0.800	-2.000	0.330 $^{+0.141}_{-0.095}$	0.500 $^{+0.212}_{-0.176}$	0.656	0.345 $^{+0.165}_{-0.176}$	0.202 $^{+0.097}_{-0.103}$
-0.692	-1.500	0.325 $^{+0.139}_{-0.095}$	0.485 $^{+0.209}_{-0.172}$	0.660	0.340 $^{+0.164}_{-0.176}$	0.369 $^{+0.178}_{-0.191}$
-0.640	-1.333	0.325 $^{+0.139}_{-0.097}$	0.482 $^{+0.210}_{-0.173}$	0.659	0.334 $^{+0.169}_{-0.174}$	0.456 $^{+0.231}_{-0.238}$
-0.610	-1.250	0.321 $^{+0.140}_{-0.095}$	0.474 $^{+0.210}_{-0.169}$	0.653	0.328 $^{+0.164}_{-0.177}$	0.505 $^{+0.252}_{-0.272}$
-0.500	-1.000	0.315 $^{+0.142}_{-0.093}$	0.450 $^{+0.213}_{-0.160}$	0.638	0.304 $^{+0.175}_{-0.176}$	0.685 $^{+0.395}_{-0.396}$
-0.410	-0.833	0.312 $^{+0.138}_{-0.095}$	0.424 $^{+0.210}_{-0.147}$	0.615	0.276 $^{+0.168}_{-0.177}$	0.819 $^{+0.498}_{-0.526}$
-0.360	-0.750	0.307 $^{+0.138}_{-0.093}$	0.409 $^{+0.200}_{-0.136}$	0.593	0.256 $^{+0.170}_{-0.176}$	0.874 $^{+0.581}_{-0.601}$
-0.308	-0.667	0.301 $^{+0.138}_{-0.092}$	0.384 $^{+0.198}_{-0.124}$	0.566	0.231 $^{+0.165}_{-0.174}$	0.915 $^{+0.655}_{-0.689}$
-0.200	-0.500	0.292 $^{+0.136}_{-0.090}$	0.345 $^{+0.181}_{-0.109}$	0.497	0.166 $^{+0.163}_{-0.162}$	0.895 $^{+0.879}_{-0.871}$
-0.100	-0.333	0.278 $^{+0.132}_{-0.086}$	0.303 $^{+0.156}_{-0.092}$	0.409	0.092 $^{+0.157}_{-0.092}$	0.679 $^{+1.159}_{-0.679}$
-0.059	-0.250	0.268 $^{+0.129}_{-0.083}$	0.283 $^{+0.152}_{-0.085}$	0.365	0.059 $^{+0.148}_{-0.059}$	0.515 $^{+1.285}_{-0.515}$
-0.027	-0.167	0.260 $^{+0.125}_{-0.081}$	0.266 $^{+0.135}_{-0.077}$	0.328	0.029 $^{+0.142}_{-0.029}$	0.297 $^{+1.434}_{-0.297}$
0.000	0.000	0.254 $^{+0.123}_{-0.079}$	0.252 $^{+0.123}_{-0.073}$	0.294	0.000 $^{+0.132}_{-0.000}$	0.002 $^{+1.776}_{-0.002}$
0.027	0.167	0.275 $^{+0.132}_{-0.086}$	0.284 $^{+0.148}_{-0.084}$	0.357	0.040 $^{+0.154}_{-0.040}$	0.650 $^{+2.514}_{-0.650}$
0.059	0.250	0.297 $^{+0.141}_{-0.093}$	0.329 $^{+0.171}_{-0.099}$	0.458	0.119 $^{+0.183}_{-0.119}$	2.015 $^{+3.098}_{-2.015}$
0.100	0.333	0.322 $^{+0.148}_{-0.099}$	0.405 $^{+0.220}_{-0.135}$	0.611	0.246 $^{+0.166}_{-0.184}$	4.147 $^{+2.802}_{-3.103}$
0.200	0.500	0.324 $^{+0.141}_{-0.096}$	0.505 $^{+0.212}_{-0.181}$	0.730	0.413 $^{+0.150}_{-0.177}$	5.982 $^{+2.174}_{-2.559}$
0.308	0.667	0.281 $^{+0.122}_{-0.082}$	0.462 $^{+0.172}_{-0.159}$	0.651	0.382 $^{+0.136}_{-0.144}$	4.186 $^{+1.492}_{-1.574}$
0.360	0.750	0.268 $^{+0.116}_{-0.079}$	0.442 $^{+0.160}_{-0.154}$	0.620	0.364 $^{+0.130}_{-0.135}$	3.392 $^{+1.214}_{-1.253}$
0.410	0.833	0.258 $^{+0.112}_{-0.075}$	0.427 $^{+0.162}_{-0.147}$	0.599	0.351 $^{+0.127}_{-0.130}$	2.754 $^{+0.999}_{-1.022}$
0.500	1.000	0.244 $^{+0.105}_{-0.072}$	0.401 $^{+0.154}_{-0.137}$	0.562	0.328 $^{+0.118}_{-0.121}$	1.821 $^{+0.657}_{-0.671}$
0.610	1.250	0.240 $^{+0.104}_{-0.070}$	0.394 $^{+0.154}_{-0.133}$	0.545	0.315 $^{+0.118}_{-0.119}$	1.072 $^{+0.399}_{-0.403}$
0.640	1.333	0.242 $^{+0.105}_{-0.071}$	0.398 $^{+0.156}_{-0.136}$	0.547	0.316 $^{+0.122}_{-0.121}$	0.921 $^{+0.354}_{-0.352}$
0.692	1.500	0.244 $^{+0.106}_{-0.071}$	0.401 $^{+0.159}_{-0.136}$	0.543	0.312 $^{+0.120}_{-0.120}$	0.678 $^{+0.262}_{-0.261}$
0.800	2.000	0.256 $^{+0.109}_{-0.075}$	0.416 $^{+0.169}_{-0.138}$	0.552	0.311 $^{+0.121}_{-0.127}$	0.317 $^{+0.123}_{-0.129}$
0.862	2.500	0.268 $^{+0.114}_{-0.078}$	0.433 $^{+0.169}_{-0.142}$	0.558	0.310 $^{+0.127}_{-0.130}$	0.170 $^{+0.070}_{-0.072}$
0.900	3.000	0.276 $^{+0.118}_{-0.080}$	0.442 $^{+0.177}_{-0.144}$	0.563	0.308 $^{+0.128}_{-0.134}$	0.102 $^{+0.042}_{-0.044}$
0.941	4.000	0.290 $^{+0.122}_{-0.084}$	0.459 $^{+0.184}_{-0.149}$	0.566	0.304 $^{+0.134}_{-0.140}$	0.046 $^{+0.020}_{-0.021}$
0.973	6.000	0.306 $^{+0.122}_{-0.081}$	0.474 $^{+0.192}_{-0.150}$	0.571	0.300 $^{+0.131}_{-0.150}$	0.016 $^{+0.007}_{-0.008}$

Table 6.22: Expected (for background only, and for a SM-like Higgs signal) and observed 95% C.L. upper limits (in pb), and best fit signal strength r and corresponding best fit cross section for the combined $tH + t\bar{t}H$ cross section times modified branching ratio for the combination of all three channels, for different values of κ_t/κ_V or the equivalent f_t numbers.

$\ell\ell\ell$	$r = 1.44_{-0.84}^{+0.91}$
$e^\pm \mu^\pm$	$r = 1.42_{-1.03}^{+1.06}$
$\mu^\pm \mu^\pm$	$r = 2.75_{-1.11}^{+1.22}$
Combined	$r = 1.82_{-0.69}^{+0.76}$
Expected	$r = 1.00_{-0.65}^{+0.70}$

Table 6.23: Best-fit signal strengths for a SM-like Higgs signal for the individual channels.

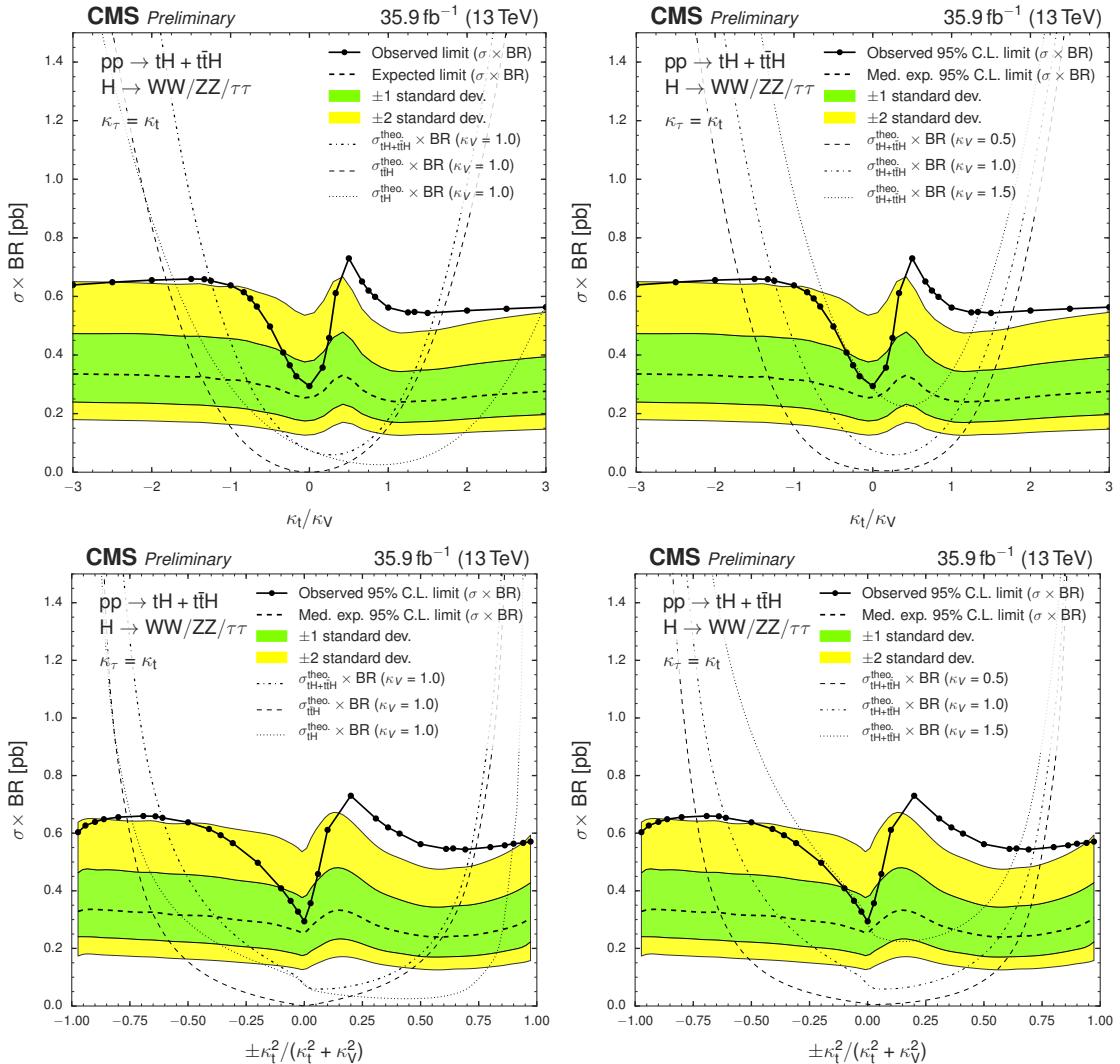


Figure 6.34: Expected (from background-only) and observed asymptotic limits on the combined $tH + t\bar{t}H$ cross section times modified BR as a function of κ_t/κ_V (top) and $\text{sign}(\kappa_t/\kappa_V) \times \frac{\kappa_t^2}{(\kappa_t^2 + \kappa_V^2)}$ (bottom) for the combination of three lepton channel, $\mu^\pm \mu^\pm$, and $e^\pm \mu^\pm$ channel.

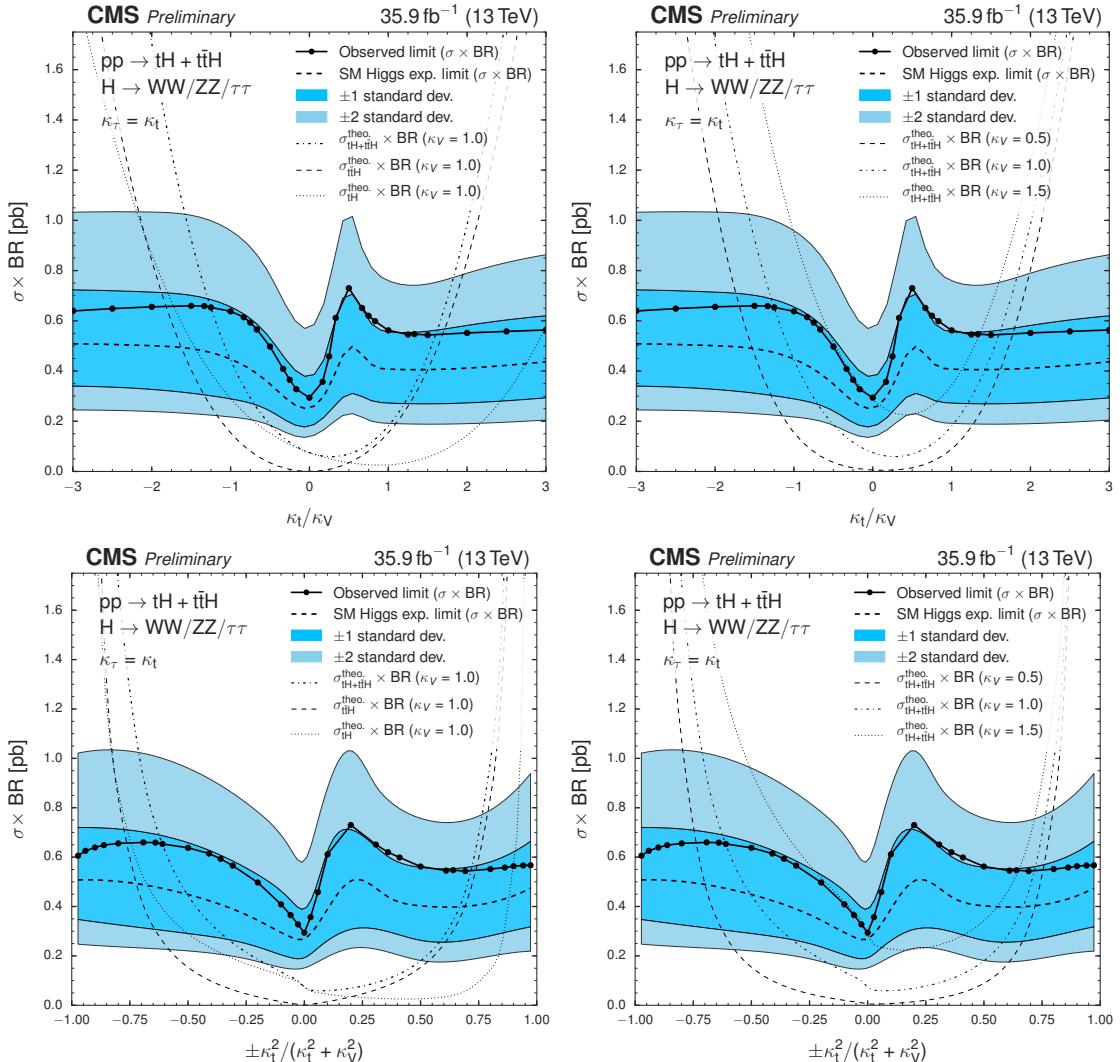


Figure 6.35: As Fig. 6.34 but calculating the expected limit on an Asimov dataset that includes SM-like $t\bar{t}H$ and tH signals.

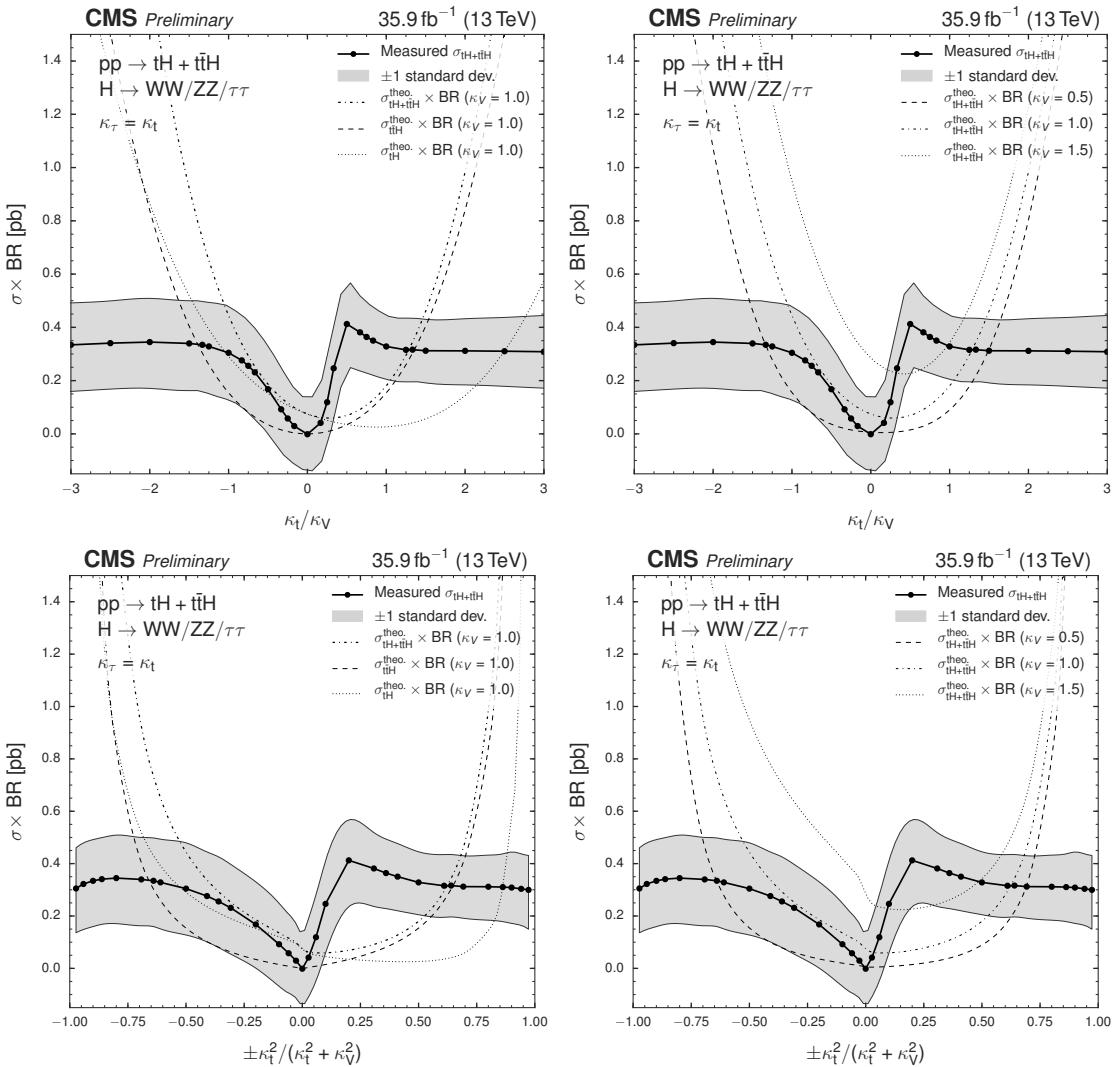


Figure 6.36: Best fit values of the combined $tH + t\bar{H}$ cross section times modified BR as a function of κ_t/κ_V (top) and $\text{sign}(\kappa_t/\kappa_V) \times \frac{\kappa_t^2}{(\kappa_t^2 + \kappa_V^2)}$ (bottom) for the combination of three lepton channel, $\mu^\pm\mu^\pm$, and $e^\pm\mu^\pm$ channel.

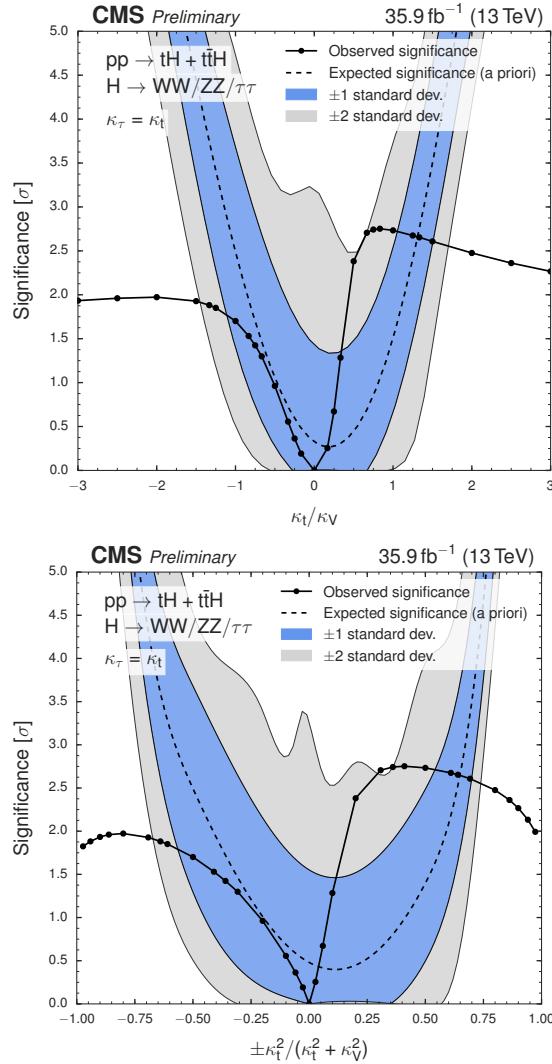


Figure 6.37: Observed and a priori expected significance of the fit result (in a background-only hypothesis) as a function of κ_t/κ_V (top) and f_t (bottom) for the combination of three lepton channel, $\mu^\pm\mu^\pm$, and $e^\pm\mu^\pm$ channel.

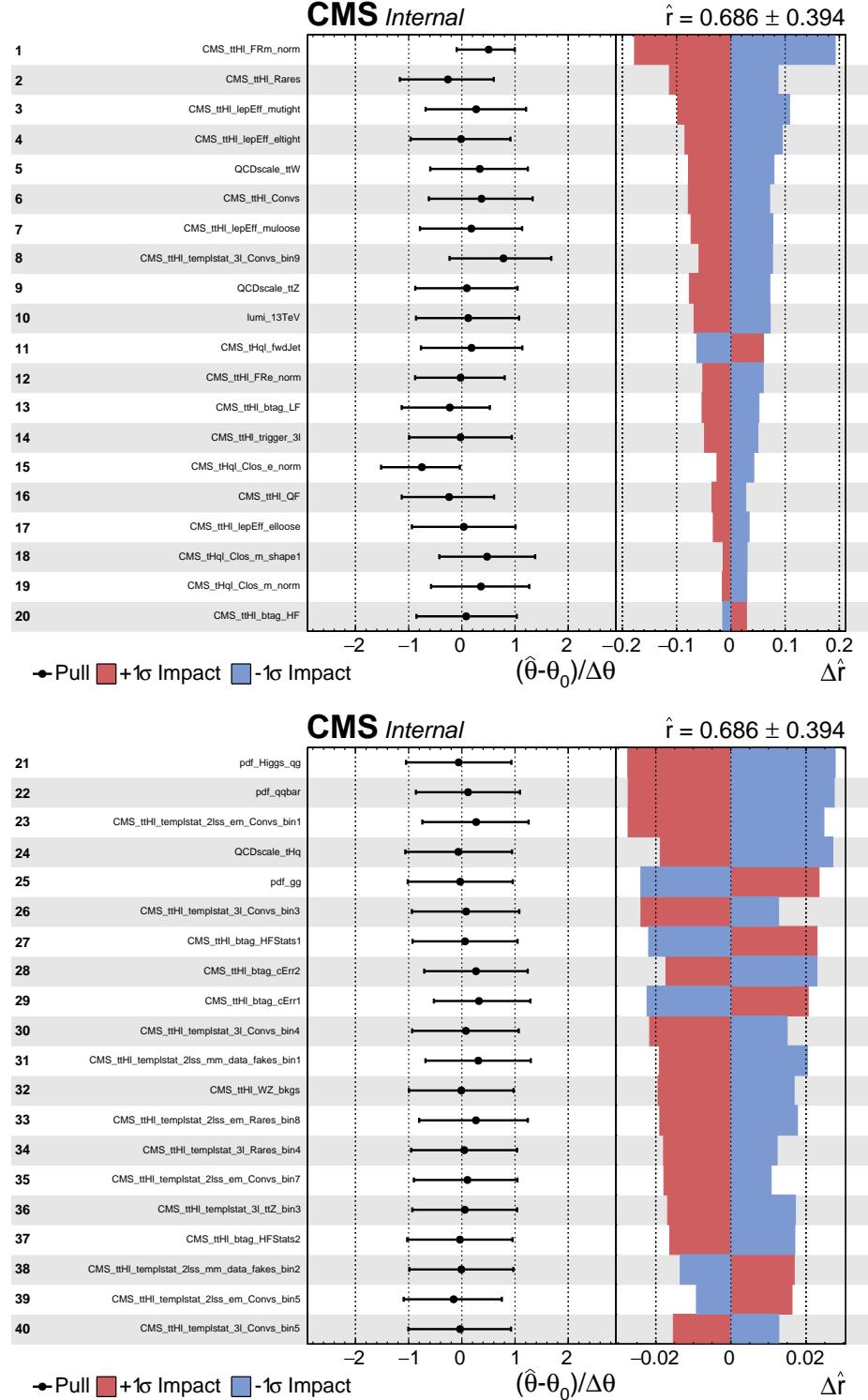


Figure 6.38: Post-fit pulls and impacts of the 40 nuisance parameters with largest impacts for the fit on the observed data, for the $\kappa_t/\kappa_V = -1.0$ hypothesis.

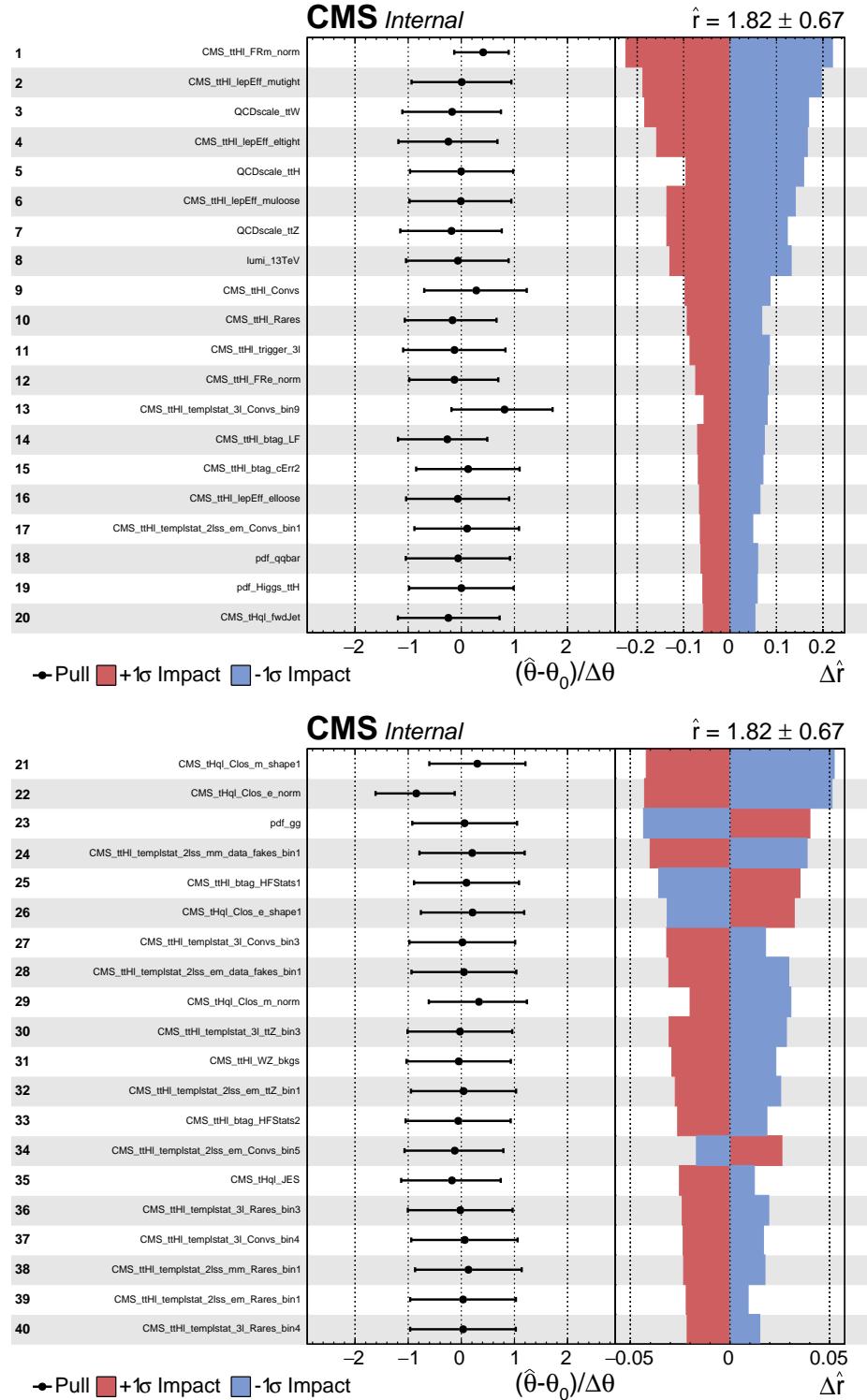


Figure 6.39: Post-fit pulls and impacts of the 40 nuisance parameters with largest impacts for the fit on the observed data, for the standard model ($\kappa_t/\kappa_V = 1.0$) hypothesis.

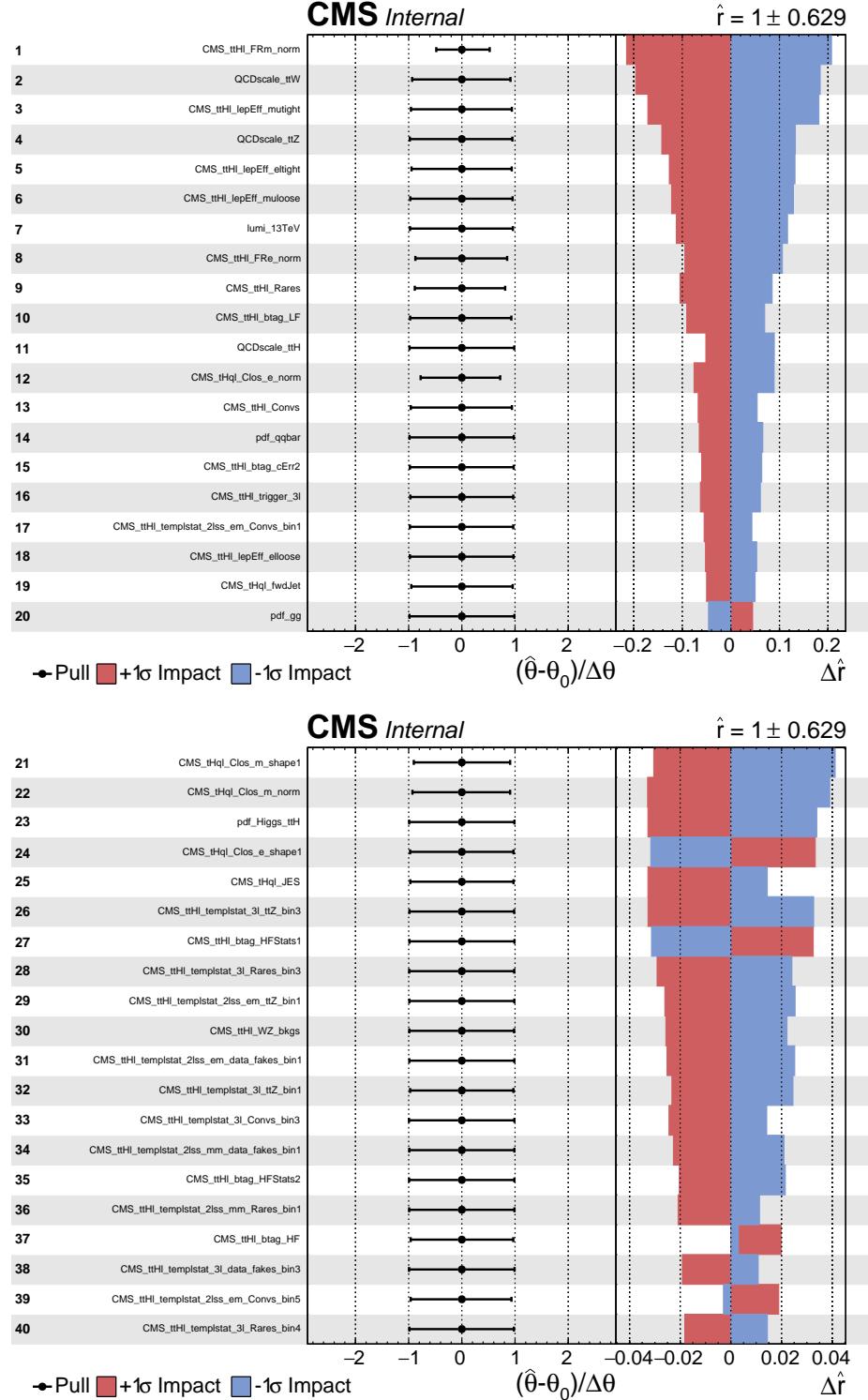


Figure 6.40: Post-fit pulls and impacts of the 40 nuisance parameters with largest impacts for a fit to the Asimov dataset with fixed signal strength, for the $\kappa_t/\kappa_V = -1.0$ hypothesis.

³²⁶⁷ **Appendix A**

³²⁶⁸ **Datasets and triggers**

Dataset name
/JetHT/Run2016X-23Sep2016-vY/MINIAOD
/HTMHT/Run2016X-23Sep2016-vY/MINIAOD
/MET/Run2016X-23Sep2016-vY/MINIAOD
/SingleElectron/Run2016X-23Sep2016-vY/MINIAOD
/SingleMuon/Run2016X-23Sep2016-vY/MINIAOD
/SinglePhoton/Run2016X-23Sep2016-vY/MINIAOD
/DoubleEG/Run2016X-23Sep2016-vY/MINIAOD
/MuonEG/Run2016X-23Sep2016-vY/MINIAOD
/DoubleMuon/Run2016X-23Sep2016-vY/MINIAOD
/Tau/Run2016B-23Sep2016-v3/MINIAOD
/JetHT/Run2016H-PromptReco-v3/MINIAOD
/HTMHT/Run2016H-PromptReco-v3/MINIAOD
/MET/Run2016H-PromptReco-v3/MINIAOD
/SingleElectron/Run2016H-PromptReco-v3/MINIAOD
/SingleMuon/Run2016H-PromptReco-v3/MINIAOD
/SinglePhoton/Run2016H-PromptReco-v3/MINIAOD
/DoubleEG/Run2016H-PromptReco-v3/MINIAOD
/MuonEG/Run2016H-PromptReco-v3/MINIAOD
/DoubleMuon/Run2016H-PromptReco-v3/MINIAOD

Table A.1: Full 2016 dataset used in the analysis. In the first section of the table are listed the 23Sep2016 samples; in the Run2016X-23Sep-vY label, X:B-G tag the run while Y:1,3 tag the version of the data sample. Second section list the PromptReco version of the dataset.

Same-sign dilepton (==2 muons)
HLT_Mu17_TrkIsoVVL_Mu8_TrkIsoVVL_DZ_v*
HLT_Mu17_TrkIsoVVL_TkMu8_TrkIsoVVL_DZ_v*
HLT_IsoMu22_v*
HLT_IsoTkMu22_v*
HLT_IsoMu22_eta2p1_v*
HLT_IsoTkMu22_eta2p1_v*
HLT_IsoMu24_v*
HLT_IsoTkMu24_v*
Same-sign dilepton (==2 electrons)
HLT_Ele23_Ele12_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_Ele27_eta2p1_WP Loose_Gsf_v*
HLT_Ele27_WPTight_Gsf_v*
HLT_Ele25_eta2p1_WPTight_Gsf_v*
Same-sign dilepton (==1 muon, ==1 electron)
HLT_Mu23_TrkIsoVVL_Ele8_CaloIdL_TrackIdL_IsoVL_v*
HLT_Mu8_TrkIsoVVL_Ele23_CaloIdL_TrackIdL_IsoVL_v*
HLT_Mu23_TrkIsoVVL_Ele8_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_Mu8_TrkIsoVVL_Ele23_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_IsoMu22_v*
HLT_IsoTkMu22_v*
HLT_IsoMu22_eta2p1_v*
HLT_IsoTkMu22_eta2p1_v*
HLT_IsoMu24_v*
HLT_IsoTkMu24_v*
HLT_Ele27_WPTight_Gsf_v*
HLT_Ele25_eta2p1_WPTight_Gsf_v*
HLT_Ele27_eta2p1_WP Loose_Gsf_v*
Three lepton
HLT_DiMu9_Ele9_CaloIdL_TrackIdL_v*
HLT_Mu8_DiEle12_CaloIdL_TrackIdL_v*
HLT_TripleMu_12_10_5_v*
HLT_Ele16_Ele12_Ele8_CaloIdL_TrackIdL_v*
HLT_Mu23_TrkIsoVVL_Ele8_CaloIdL_TrackIdL_IsoVL_v*
HLT_Mu23_TrkIsoVVL_Ele8_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_Mu8_TrkIsoVVL_Ele23_CaloIdL_TrackIdL_IsoVL_v*
HLT_Mu8_TrkIsoVVL_Ele23_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_Ele23_Ele12_CaloIdL_TrackIdL_IsoVL_DZ_v*
HLT_Mu17_TrkIsoVVL_Mu8_TrkIsoVVL_DZ_v*
HLT_Mu17_TrkIsoVVL_TkMu8_TrkIsoVVL_DZ_v*
HLT_IsoMu22_v*
HLT_IsoTkMu22_v*
HLT_IsoMu22_eta2p1_v*
HLT_IsoTkMu22_eta2p1_v*
HLT_IsoMu24_v*
HLT_IsoTkMu24_v*
HLT_Ele27_WPTight_Gsf_v*
HLT_Ele25_eta2p1_WPTight_Gsf_v*
HLT_Ele27_eta2p1_WP Loose_Gsf_v*

Table A.2: Table of high-level triggers considered in the analysis.

		<i>tHq</i>			<i>tHW</i>		
κ_V	κ_t	sum of weights	cross section [pb]	sum of weights	cross section [pb]	LHE weights	
1.0	-3.0	35.700022	2.991	11.030445	0.6409	LHEweight_wgt[446]	
1.0	-2.0	20.124298	1.706	5.967205	0.3458	LHEweight_wgt[447]	
1.0	-1.5	14.043198	1.205	4.029093	0.2353	LHEweight_wgt[448]	
1.0	-1.25	11.429338	0.9869	3.208415	0.1876	LHEweight_wgt[449]	
1.0	-1.0		0.7927		0.1472		
1.0	-0.75	7.054998	0.6212	1.863811	0.1102	LHEweight_wgt[450]	
1.0	-0.5	5.294518	0.4723	1.339886	0.07979	LHEweight_wgt[451]	
1.0	-0.25	3.818499	0.3505	0.914880	0.05518	LHEweight_wgt[452]	
1.0	0.0	2.627360	0.2482	0.588902	0.03881	LHEweight_wgt[453]	
1.0	0.25	1.719841	0.1694	0.361621	0.02226	LHEweight_wgt[454]	
1.0	0.5	1.097202	0.1133	0.233368	0.01444	LHEweight_wgt[455]	
1.0	0.75	0.759024	0.08059	0.204034	0.01222	LHEweight_wgt[456]	
1.0	1.0	0.705305	0.07096	0.273617	0.01561	LHEweight_wgt[457]	
1.0	1.25	0.936047	0.0839	0.442119	0.02481	LHEweight_wgt[458]	
1.0	1.5	1.451249	0.1199	0.709538	0.03935	LHEweight_wgt[459]	
1.0	2.0	3.335034	0.2602	1.541132	0.08605	LHEweight_wgt[460]	
1.0	3.0	10.516125	0.8210	4.391335	0.2465	LHEweight_wgt[461]	
1.5	-3.0	45.281492	3.845	13.426212	0.7825	LHEweight_wgt[462]	
1.5	-2.0	27.606715	2.371	7.809713	0.4574	LHEweight_wgt[463]	
1.5	-1.5	20.476088	1.784	5.594971	0.3290	LHEweight_wgt[464]	
1.5	-1.25	17.337465	1.518	4.635978	0.2749	LHEweight_wgt[465]	
1.5	-1.0	14.483302	1.287	3.775902	0.2244	LHEweight_wgt[466]	
1.5	-0.75	11.913599	1.067	3.014744	0.1799	LHEweight_wgt[467]	
1.5	-0.5	9.628357	0.874	2.352505	0.1410	LHEweight_wgt[468]	
1.5	-0.25	7.627574	0.702	1.789184	0.1081	LHEweight_wgt[469]	
1.5	0.0	5.911882	0.5577	1.324946	0.08056	LHEweight_wgt[470]	
1.5	0.25	4.479390	0.4365	0.959295	0.05893	LHEweight_wgt[471]	
1.5	0.5	3.331988	0.3343	0.692727	0.04277	LHEweight_wgt[472]	
1.5	0.75	2.469046	0.2558	0.525078	0.03263	LHEweight_wgt[473]	
1.5	1.0	1.890565	0.2003	0.456347	0.02768	LHEweight_wgt[474]	
1.5	1.25	1.596544	0.1689	0.486534	0.02864	LHEweight_wgt[475]	
1.5	1.5	1.586983	0.1594	0.615638	0.03509	LHEweight_wgt[476]	
1.5	2.0	2.421241	0.2105	1.170602	0.06515	LHEweight_wgt[477]	
1.5	3.0	7.503280	0.5889	3.467546	0.1930	LHEweight_wgt[478]	
0.5	-3.0	27.432685	2.260	8.929074	0.5136	LHEweight_wgt[479]	
0.5	-2.0	13.956013	1.160	4.419093	0.2547	LHEweight_wgt[480]	
0.5	-1.5	8.924438	0.7478	2.757611	0.1591	LHEweight_wgt[481]	
0.5	-1.25	6.835341	0.5726	2.075247	0.1204	LHEweight_wgt[482]	
0.5	-1.0	5.030704	0.4273	1.491801	0.08696	LHEweight_wgt[483]	
0.5	-0.75	3.510528	0.2999	1.007273	0.05885	LHEweight_wgt[484]	
0.5	-0.5	2.274811	0.1982	0.621663	0.03658	LHEweight_wgt[485]	
0.5	-0.25	1.323555	0.1189	0.334972	0.01996	LHEweight_wgt[486]	
0.5	0.0	0.656969	0.06223	0.147253	0.008986	LHEweight_wgt[487]	
0.5	0.25	0.274423	0.02830	0.058342	0.003608	LHEweight_wgt[488]	
0.5	0.5	0.176548	0.01778	0.068404	0.003902	LHEweight_wgt[489]	
0.5	0.75	0.363132	0.03008	0.177385	0.009854	LHEweight_wgt[490]	
0.5	1.0	0.834177	0.06550	0.385283	0.02145	LHEweight_wgt[491]	
0.5	1.25	1.589682	0.1241	0.692099	0.03848	LHEweight_wgt[492]	
0.5	1.5	2.629647	0.2047	1.097834	0.06136	LHEweight_wgt[493]	
0.5	2.0	5.562958	0.4358	2.206057	0.1246	LHEweight_wgt[494]	
0.5	3.0	14.843102	1.177	5.609519	0.3172	LHEweight_wgt[495]	

Table A.3: κ_V and κ_t combinations generated for the two signal samples and their NLO cross sections. The *tHq* cross section is multiplied by the branching fraction of the enforced leptonic decay of the top quark (0.324) [150].

Sample	σ [pb]	*
TTWJetsToLNu_TuneCUETP8M1_13TeV-amcatnloFXFX-madspin-pythia8	0.2043	*
TTZToLLNuNu_M-10_TuneCUETP8M1_13TeV-amcatnlo-pythia8	0.2529	*
/store/cmst3/group/susy/gpetrucc/13TeV/u/TTLL_m1to10_L0_NoMS_for76X/	0.0283	
WGToLNuG_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	585.8	
ZGTo2LG_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	131.3	
TGJets_TuneCUETP8M1_13TeV_amcatnlo_madspin_pythia8	2.967	
TGJets_TuneCUETP8M1_13TeV_amcatnlo_madspin_pythia8	2.967	
TTGJets_TuneCUETP8M1_13TeV-amcatnloFXFX-madspin-pythia8	3.697	
WpWpJJ_EWK-QCD_TuneCUETP8M1_13TeV-madgraph-pythia8	0.03711	
ZZZ_TuneCUETP8M1_13TeV-amcatnlo-pythia8	0.01398	
WWZ_TuneCUETP8M1_13TeV-amcatnlo-pythia8	0.1651	
WZZ_TuneCUETP8M1_13TeV-amcatnlo-pythia8	0.05565	
WW_DoubleScattering_13TeV-pythia8	1.64	
tZq_ll_4f_13TeV-amcatnlo-pythia8_TuneCUETP8M1	0.0758	
ST_tW1l_5f_L0_13TeV-MadGraph-pythia8	0.01123	
TTTT_TuneCUETP8M1_13TeV-amcatnlo-pythia8	0.009103	
WZTo3LNu_TuneCUETP8M1_13TeV-powheg-pythia8	4.4296	
ZZTo4L_13TeV_powheg_pythia8	1.256	
TTJets_SingleLeptFromTbar_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	182.1754	*
TTJets_SingleLeptFromT_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	182.1754	*
TTJets_DiLept_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	87.3	*
DYJetsToLL_M-10to50_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	18610	
DYJetsToLL_M-50_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	6024	
WJetsToLNu_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	61526.7	
ST_tW_top_5f_inclusiveDecays_13TeV-powheg-pythia8_TuneCUETP8M1	35.6	
ST_tW_antitop_5f_inclusiveDecays_13TeV-powheg-pythia8_TuneCUETP8M1	35.6	
ST_t-channel_4f_leptonDecays_13TeV-amcatnlo-pythia8_TuneCUETP8M1	70.3144	
ST_t-channel_antitop_4f_leptonDecays_13TeV-powheg-pythia8_TuneCUETP8M1	26.2278	
ST_s-channel_4f_leptonDecays_13TeV-amcatnlo-pythia8_TuneCUETP8M1	3.68064	
WWTo2L2Nu_13TeV-powheg	10.481	
ttWJets_13TeV_madgraphMLM	0.6105	
ttZJets_13TeV_madgraphMLM	0.5297/0.692	

Table A.4: List of background samples used in this analysis (CMSSW 80X). The first section of the table lists the samples used in simulation to extract the final yields and shapes; the second section lists the samples of the processes for which the yields are estimated from data. The MC simulation is used to design the data driven methods and in the derivation of the associated systematic uncertainties. The third section list the leading order $t\bar{t}W$ and $t\bar{t}Z$ samples, which in addition to the ones market with a *, where used in the BDT training.

³²⁶⁹ **Appendix B**

³²⁷⁰ **Aditional plots**

³²⁷¹ **B.1 Pre-selection kinematic variables**

³²⁷² Figures B.1, B.2 and B.3 show the distributions of some relevant kinematic variables,
³²⁷³ normalized to the cross section of the respective processes and to the integrated
³²⁷⁴ luminosity.

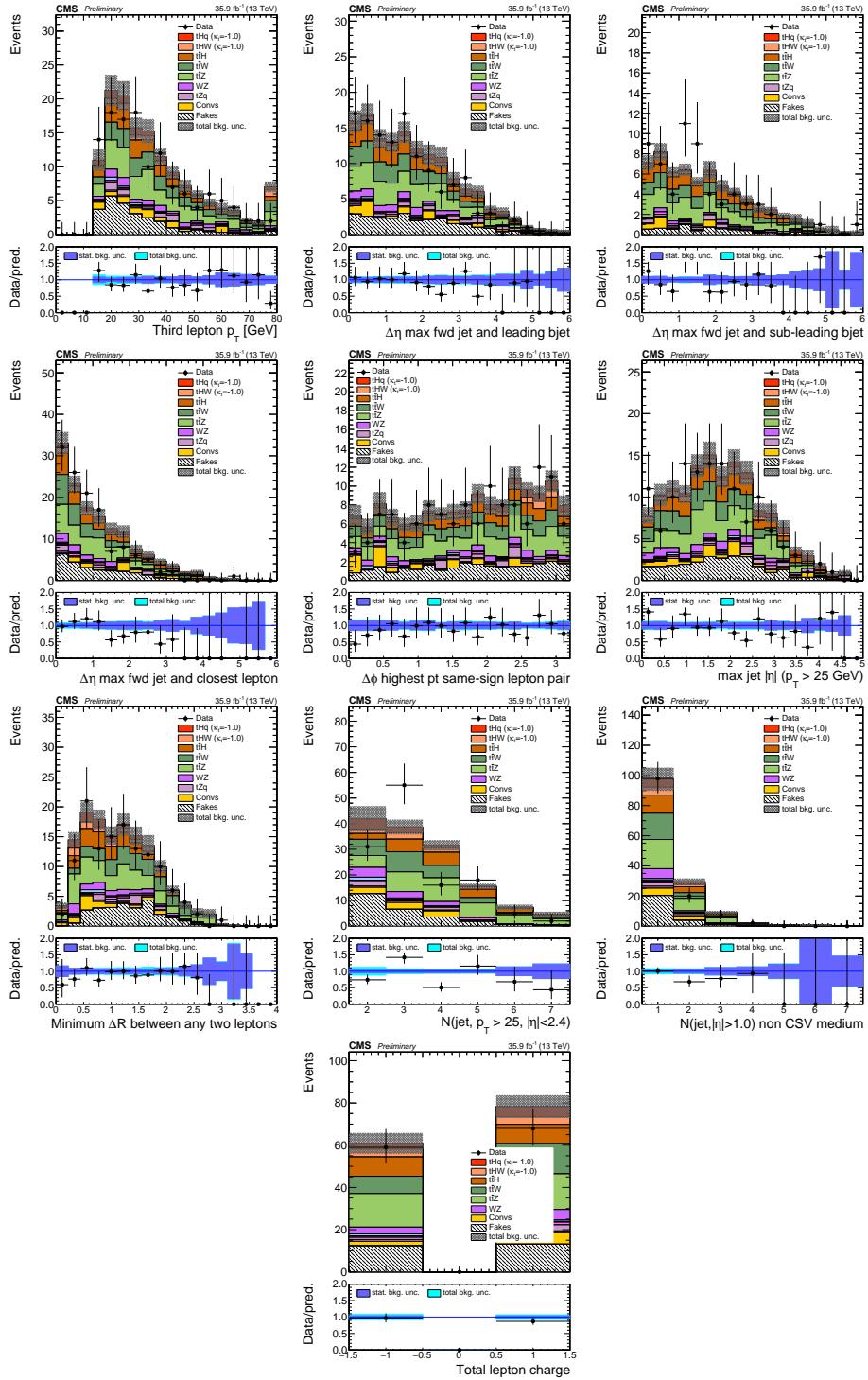


Figure B.1: Distributions of input variables to the BDT for signal discrimination, three lepton channel, normalized to their cross section and to 35.9 fb^{-1} .

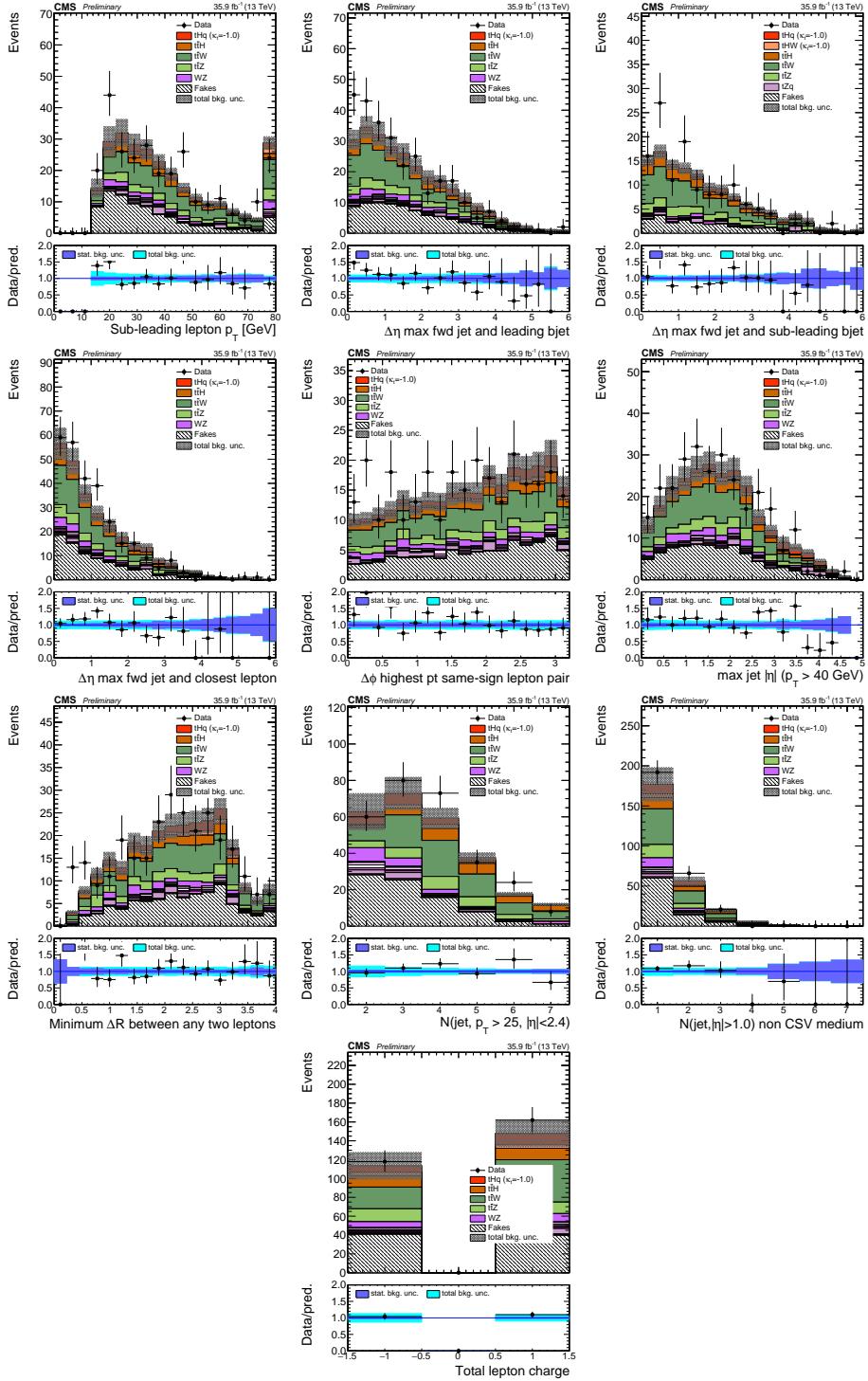


Figure B.2: Distributions of input variables to the BDT for signal discrimination, in $\mu^\pm \mu^\pm$ channel, normalized to their cross section and to 35.9 fb^{-1} .

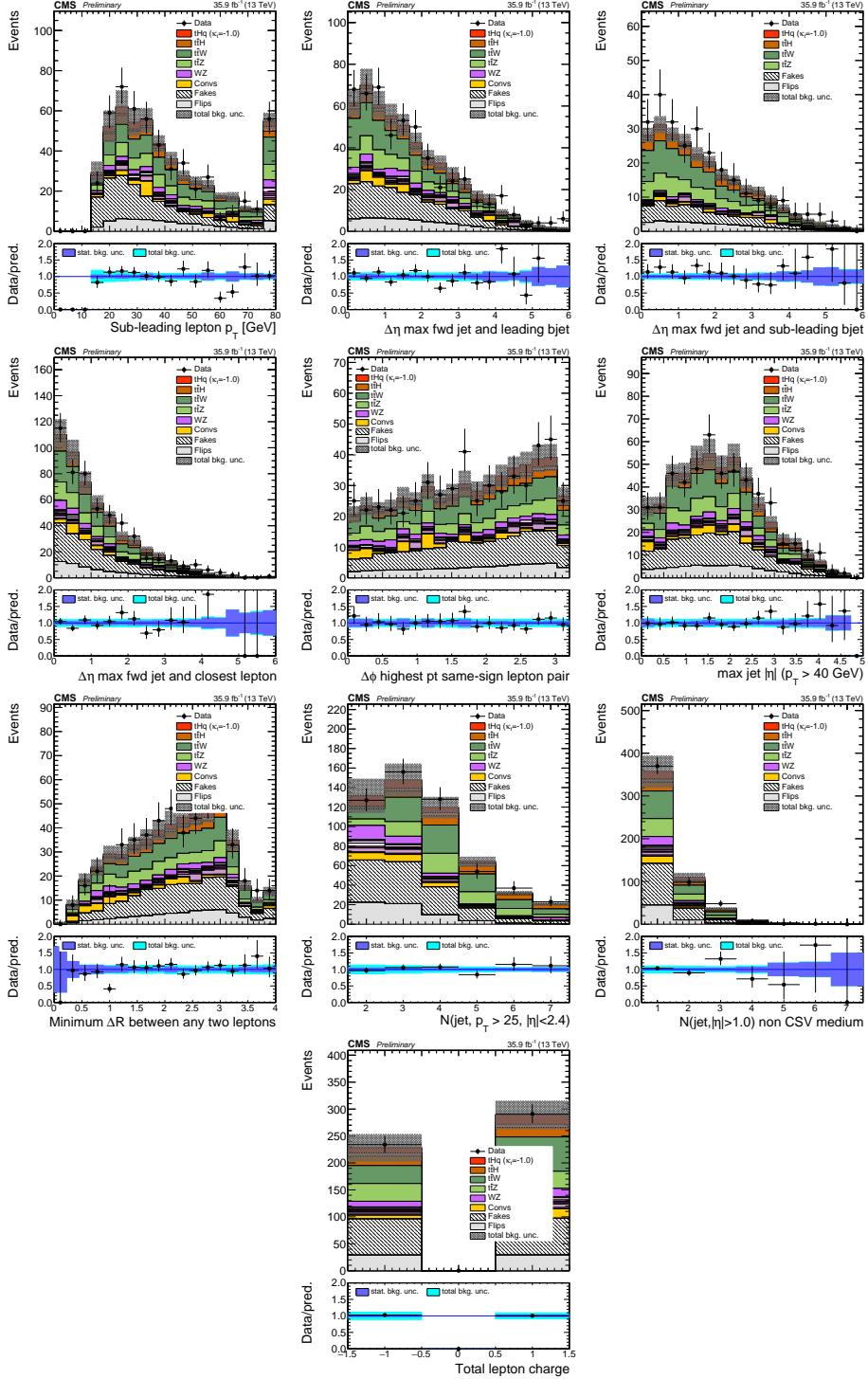


Figure B.3: Distributions of input variables to the BDT for signal discrimination, in $e^\pm\mu^\pm$ channel, normalized to their cross section and to 35.9 fb^{-1} .

3275 **B.2 BDTG input variables for $2lss$ channel**

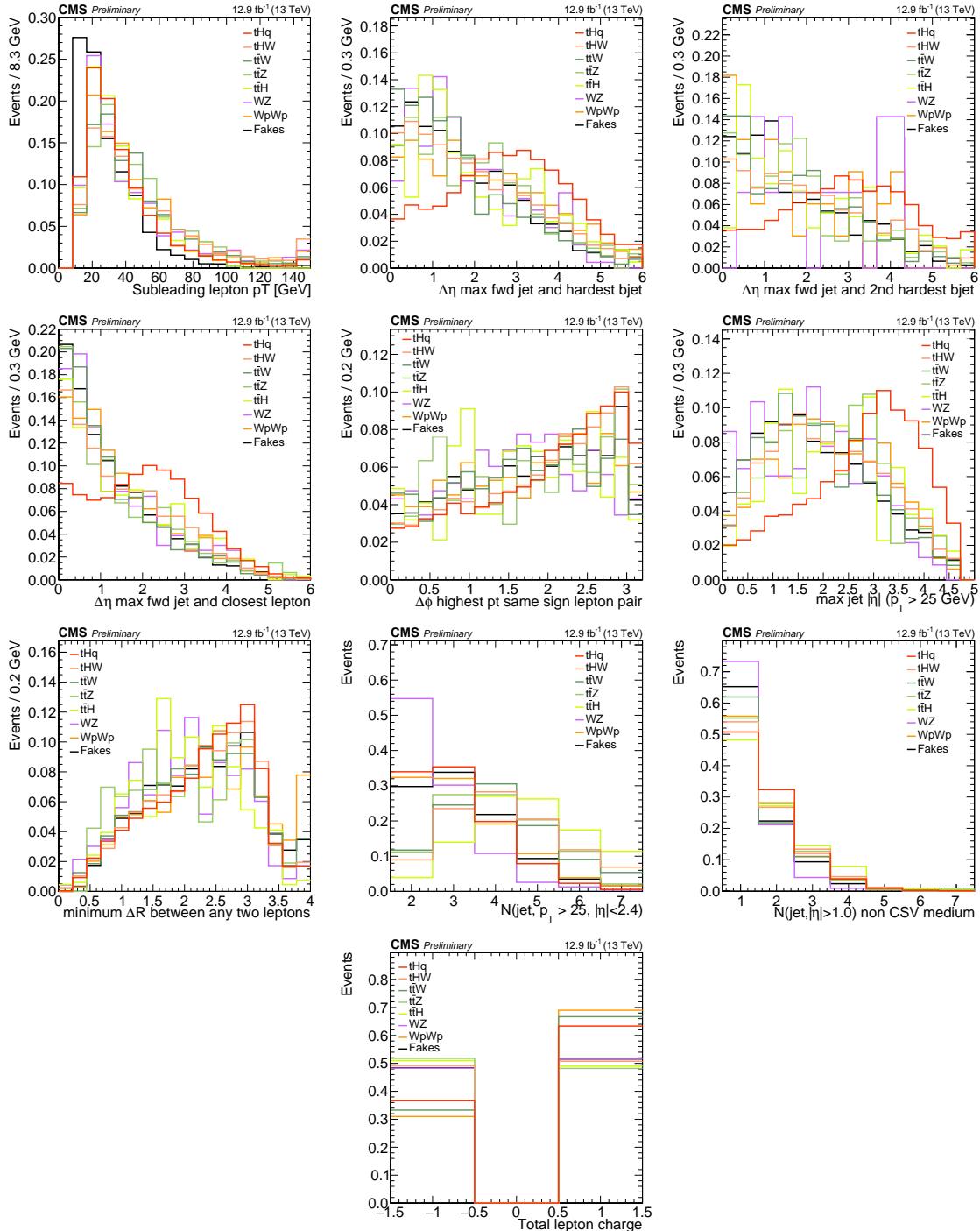


Figure B.4: Distributions of input variables to the BDT for signal discrimination, two lepton same sign channel.

3276 **B.3 Input variables distributions from BDTG**
 3277 classifiers

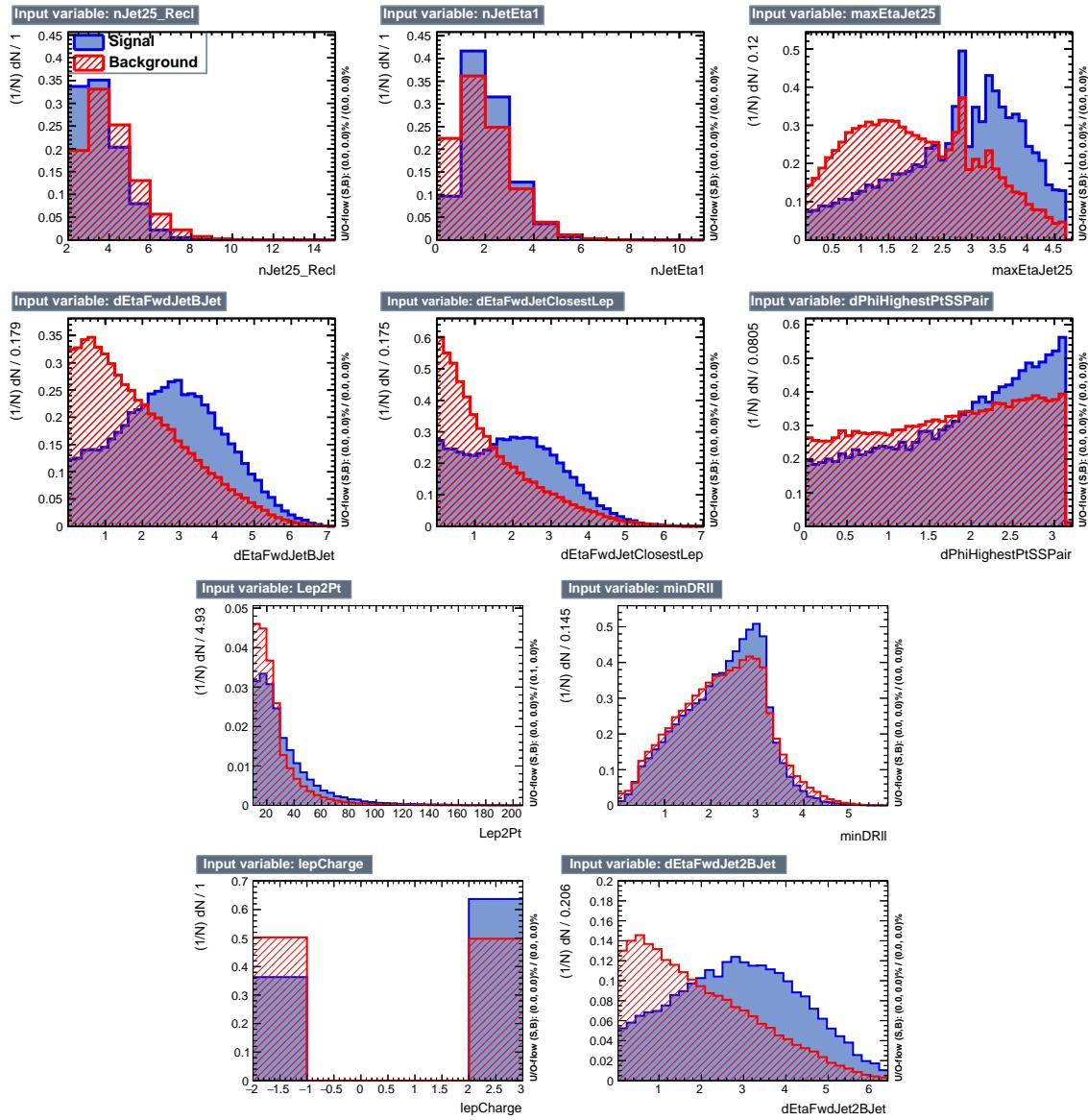


Figure B.5: BDT input variables as seen by BDTG classifier for the $2lss$ channel, tHq signal (blue) discriminated against $t\bar{t}$ background (red).

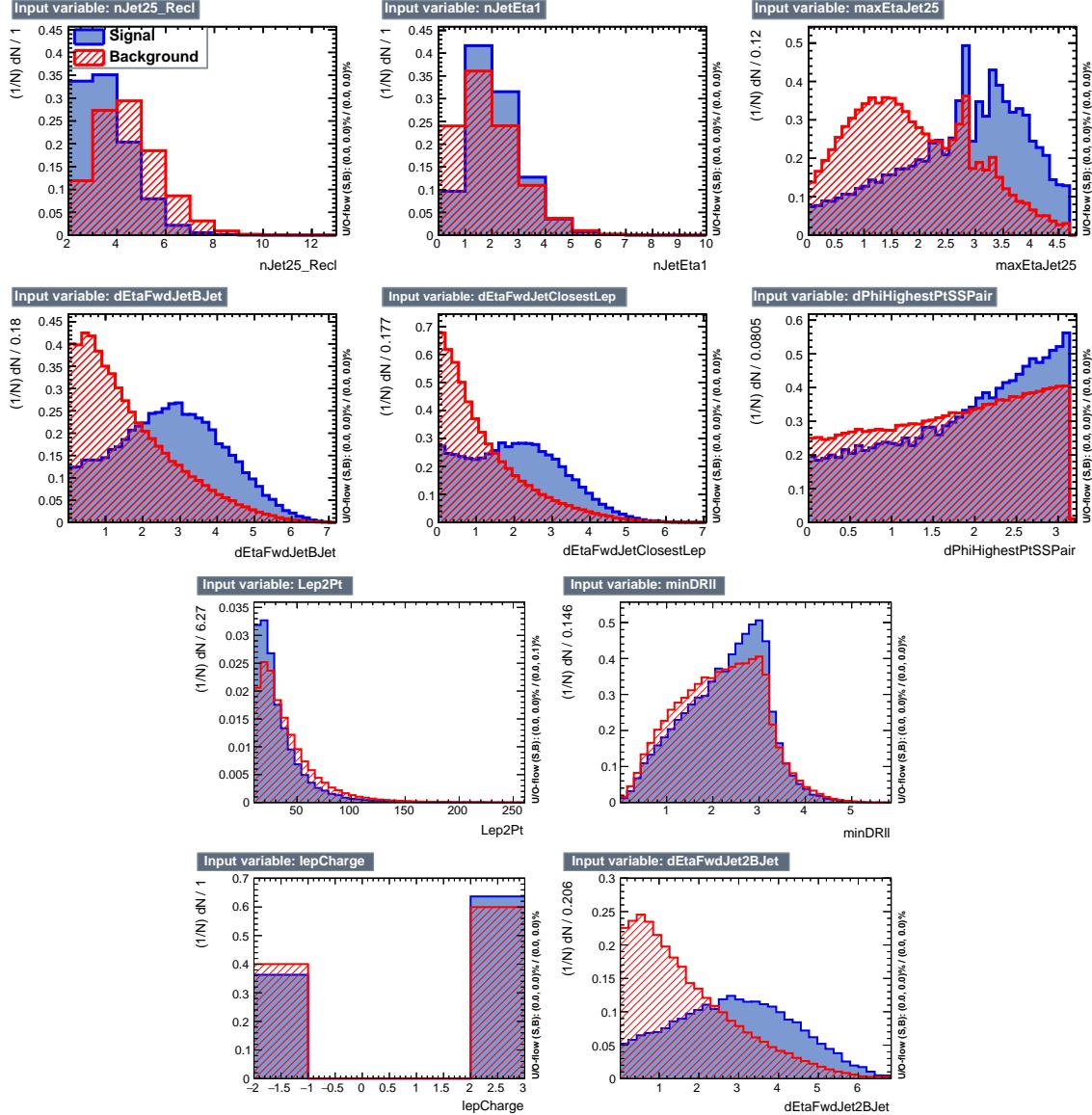


Figure B.6: BDT input variables as seen by BDTG classifier for the $2lss$ channel, tHq signal(blue) discriminated against $t\bar{t}V$ background (red).

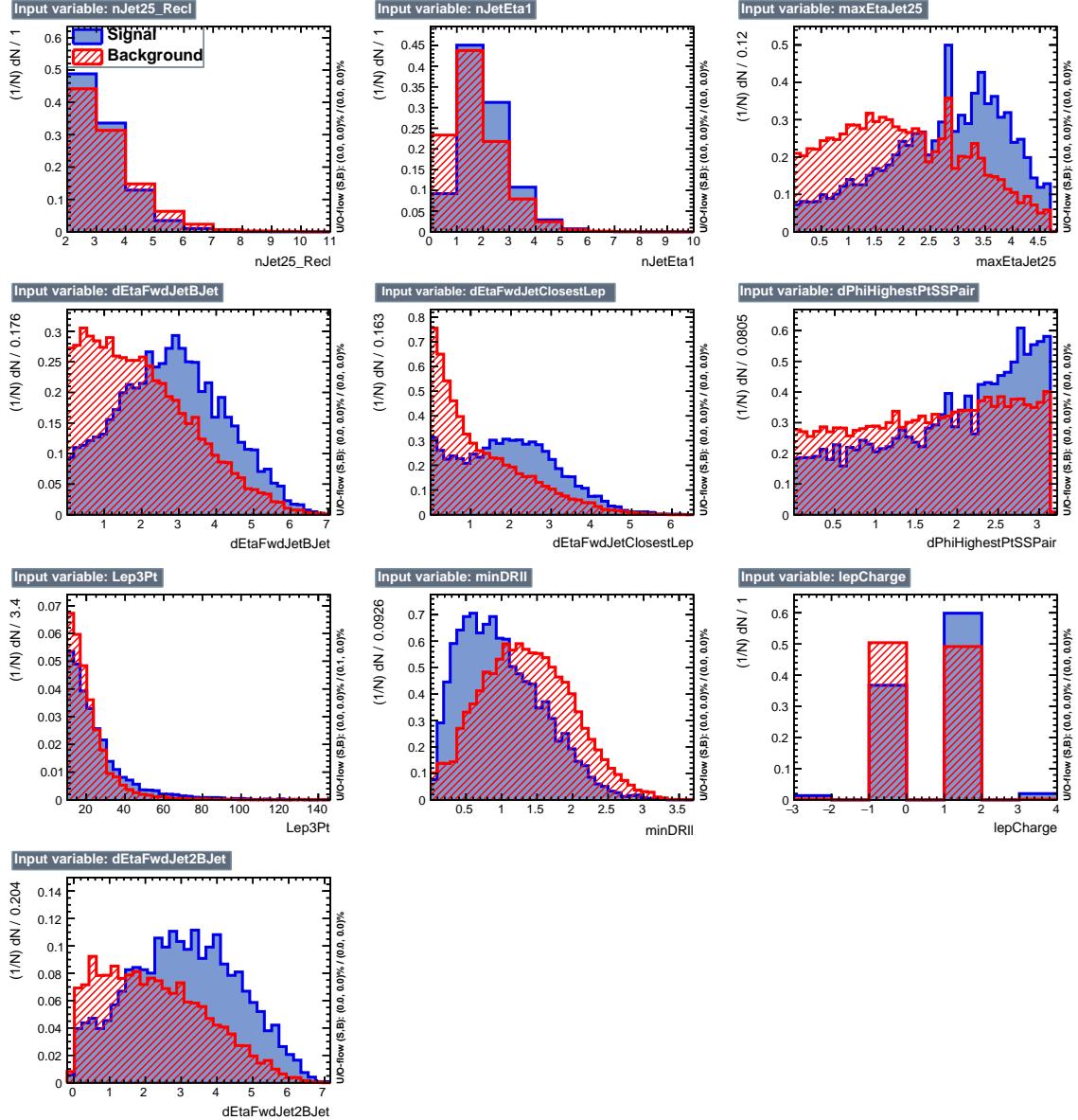


Figure B.7: BDT input variables as seen by BDTG classifier for the $3l$ channel, tHq signal (blue) discriminated against $t\bar{t}$ background (red).

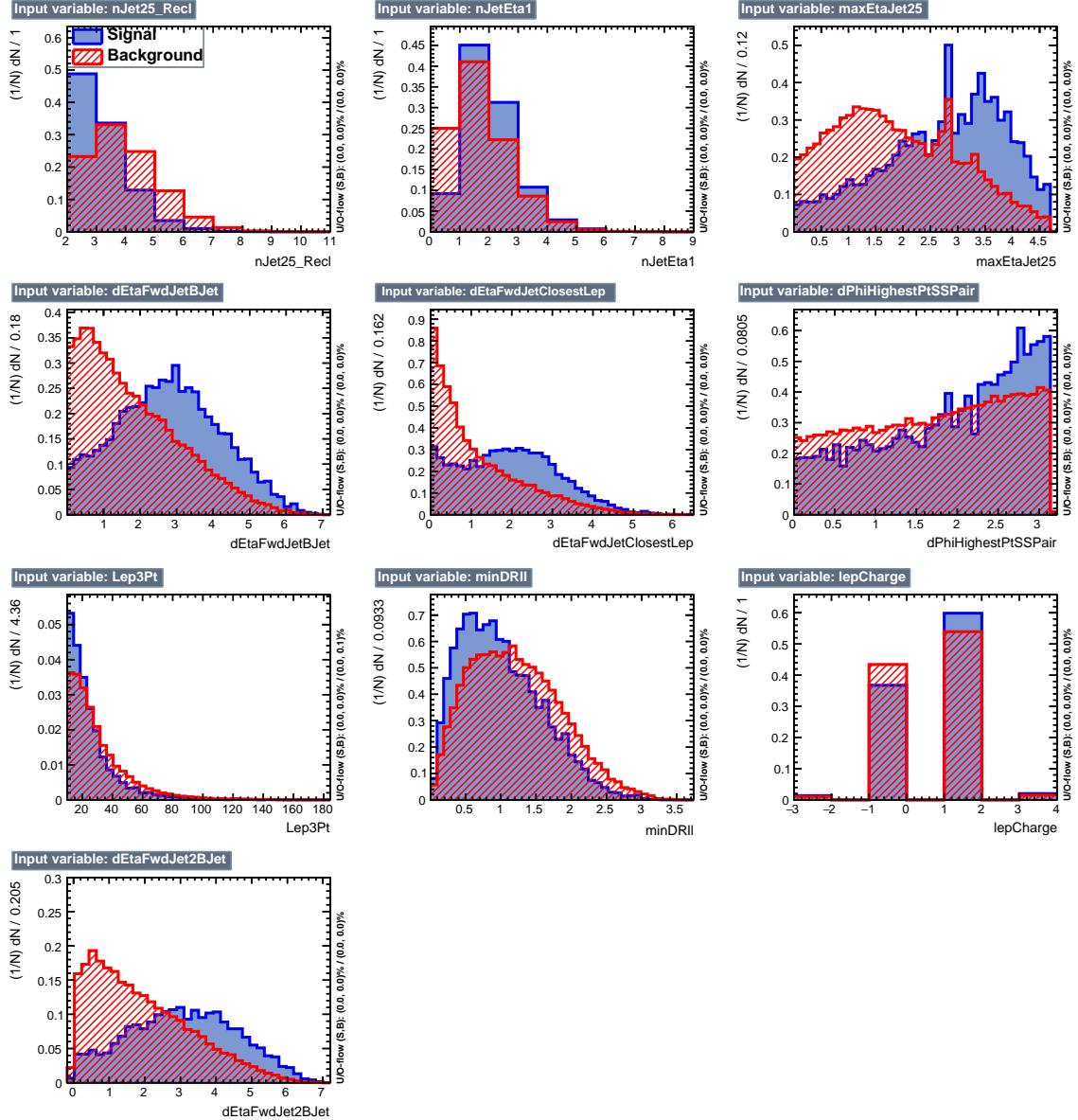


Figure B.8: BDT input variables as seen by BDTG classifier for the $3l$ channel, tHq signal (blue) discriminated against $t\bar{t}V$ background (red).

3278 **Appendix C**

3279 **Other binning strategies**

3280 Two additional strategies of clustering regions in the 2D plane of $BDTG_{tt}$ vs $BDTG_{ttV}$
3281 into bins were attempted, following studies done and documented in great detail in
3282 Reference [149]. A brief description is provided in the following.

3283 **Clustering by S/B ratio** In this method, the 2D plane is clustered into a given
3284 number of bins corresponding to regions where S/B is within a certain range. The
3285 bin borders are determined such that the number of background events in each bin is
3286 approximately equal. The resulting regions for $2lss$ and $3l$ events are shown in Figure
3287 C.1, while the expected distribution of signal and dominant backgrounds are shown
3288 in Figure C.2.

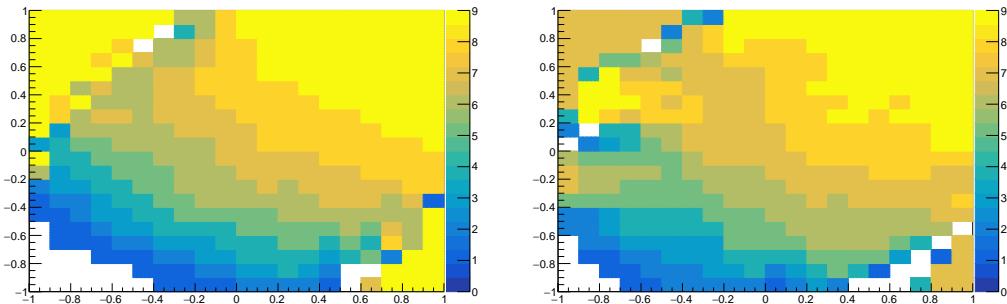


Figure C.1: Binning by S/B regions for $2lss$ (left) and $3l$ (right).

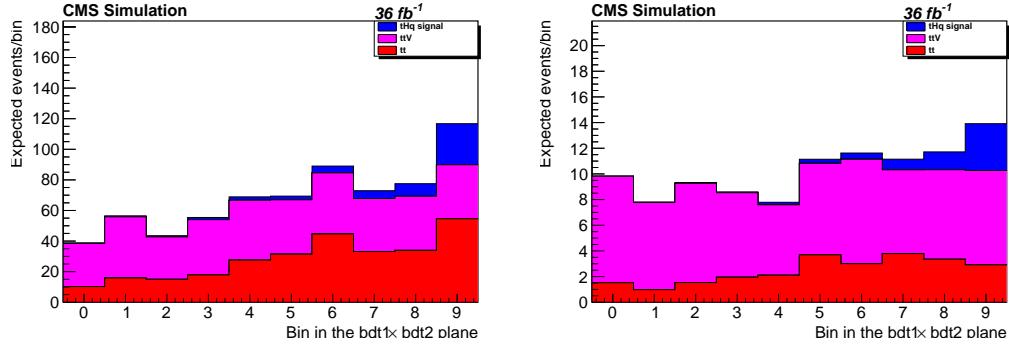


Figure C.2: Final bins (corresponding to S/B regions in the 2D plane) for $2lss$ and $3l$ (right).

Using this method, the resulting limits (for the $\kappa_t = -1, \kappa_V = 1$ scenario) are about 20% worse than with the binning in Section 6.9.6: $\mu^\pm\mu^\pm$ changed from 1.82 to 2.15, $3l$ changed from 1.52 to 1.75.

***k*-Means geometric clustering** This method employs a recursive application of the k -means algorithm (see Appendix D in Reference [149]) to separate the 2D plane into geometric regions. The resulting clustering (using the $t\bar{t}H$ multilepton code on tHq signal and $t\bar{t}$ and $t\bar{t}V$ background events) are shown in Figure C.3. The expected distribution of events for the signal and dominant backgrounds in these bins is shown in Fig. C.4.

Similarly to the S/B ratio binning, the limits using the k -means clustering are significantly worse than those of the bins described before. In the $\mu^\pm\mu^\pm$ channel, the limit deteriorates from 1.82 to 2.05, whereas in $3l$ it changes from 1.58 to 1.78.

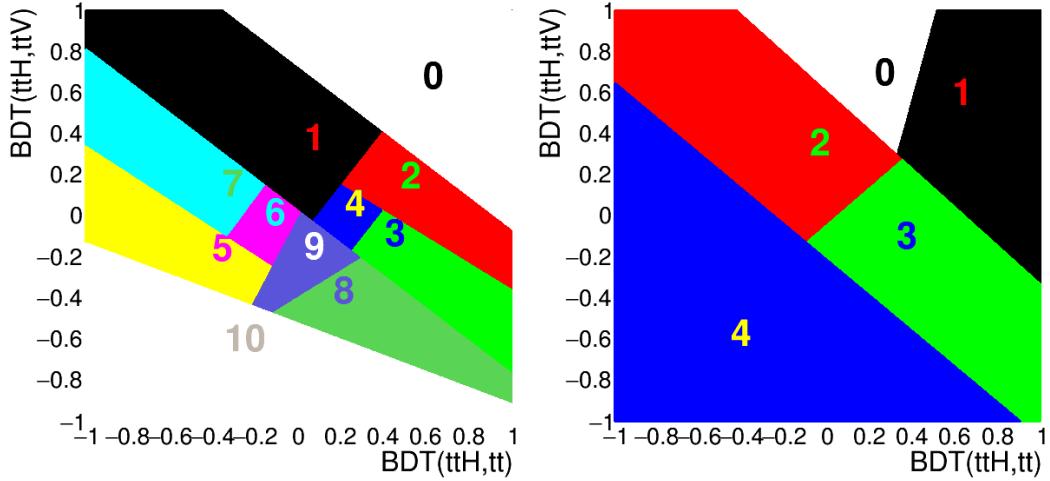


Figure C.3: Binning into geometric regions using a k -means algorithm for $2lss$ (left) and $3l$ (right).

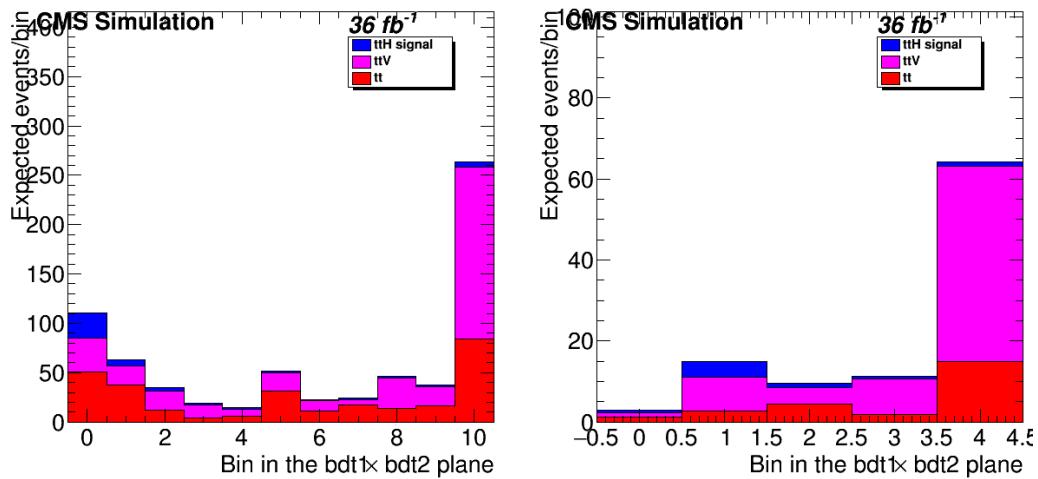


Figure C.4: Final bins using a k -means algorithm for $2lss$ (left) and $3l$ (right). Note that the bin numbering here is such that signal-like bins are lower.

3301 **Appendix D**

3302 **BDTG output variation with κ_V/κ_t**

3303 The BDTG classifier output was described in Section in the $\kappa_t = -1, \kappa_V = 1$ scenario;
3304 the change of BDTG classifiers output shape when varying the κ_V/κ_t coupling sce-
3305 nario is shown in Figure D.1 in the $3l$ channel for five different values of κ_t , with κ_V fixed at 1.0.

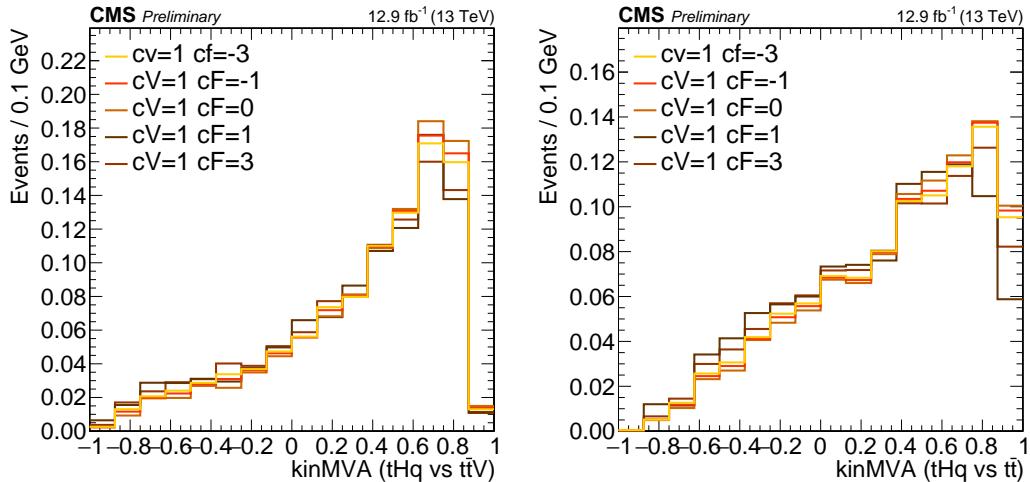


Figure D.1: Change of the BDTG classifiers output when varying κ_t coupling (κ_V is fixed at 1.0). Training vs. $tt\bar{V}$ (right) and vs. $tt\bar{t}$ (left).

3306

3307 Complete this section !!!!!!! ask about this !

3308 **Appendix E**

3309 **tHq - $t\bar{t}H$ overlap**

3310 This section provides a quick overview of the differences and commonalities in event
3311 selections between this analysis and the $t\bar{t}H$ multilepton search [149]. The object
3312 selections of the two analysis are perfectly synchronized due to shared frameworks
3313 and samples. The only exception is the usage of forward jets ($|\eta| > 2.4, p_T > 40$ GeV)
3314 in this analysis. Such jets are not considered in the $t\bar{t}H$ analysis.

3315 Table E.1 gives an overview of the main differences in the event selections. Here,
3316 $E_T^{miss}_{LD}$ is defined as $E_T^{miss} \times 0.00397 + H_T^{miss} \times 0.00265$. Un-tagged jets in the tHq
3317 analysis are jets that do not pass the CSV loose working point and are either central
3318 ($|\eta| < 2.4, p_T > 25$ GeV) or forward ($|\eta| < 2.4, p_T > 40$ GeV). All jets in the $t\bar{t}H$ analysis
3319 are selected with $p_T > 25$ GeV. Lepton p_T cuts and the trigger selections are identical.

Channel	tHq	$t\bar{t}H$
3l	Z veto, 15bGeV $N_{jets}^{b, med.} \geq 1$ ≥ 1 un-tagged jet	Z veto, 10 GeV $N_{jets}^{b, med.} \geq 1$ OR $N_{jets}^{b, loose} \geq 2$ $E_T^{miss}_{LD} > 0.2$ OR $N_{jets}^{centr.} \geq 4$
2lss	$N_{jets}^{b, med.} \geq 1$ ≥ 1 un-tagged jet	$N_{jets}^{b, med.} \geq 1$ OR $N_{jets}^{b, loose} \geq 2$ $N_{jets}^{central} \geq 4$

Table E.1: Differences in event selection between this analysis and the $t\bar{t}H$ multilepton analysis.

3320 Table E.2 shows the total events yields in the individual channels, and the yield
 3321 of shared events between each channel, for the tHq signal sample, the $t\bar{t}H$ signal
 3322 sample, and the data. In the data, for the $3l$ channel, about 80% of events passing
 3323 the tHq selection also pass the $t\bar{t}H$ selection, constituting about 70% of that channel.
 3324 In the $2lss$ channel, about 50% of data events passing the tHq selection also pass the
 3325 $t\bar{t}H$ selection, but these events constitute almost 90% of the $t\bar{t}H$ selection in those
 3326 channels. Similar overlaps are also seen in the tHq and $t\bar{t}H$ signal samples.

3327 There is no migration between different channels and different selections, i.e. no
 3328 events passing the selection of a given tHq channel pass the selection of any other
 3329 channels of $t\bar{t}H$ and vice versa.

tHq sample	tHq	$t\bar{t}H$	Common	(% tHq)	(% $t\bar{t}H$)
$\mu^\pm\mu^\pm$	7400	2353	2166	29.3	92.1
$e^\pm\mu^\pm$	11158	3600	3321	29.8	92.2
$e^\pm e^\pm$	3550	1106	1025	28.9	92.7
$\ell\ell\ell$	3115	2923	2347	75.3	80.3

$t\bar{t}H$ sample	tHq	$t\bar{t}H$	Common	(% tHq)	(% $t\bar{t}H$)
$\mu^\pm\mu^\pm$	32612	28703	26547	81.4	92.5
$e^\pm\mu^\pm$	48088	42521	39164	81.4	92.1
$e^\pm e^\pm$	15476	12869	11896	76.9	92.4
$\ell\ell\ell$	26627	30598	25288	95.0	82.6

Data	tHq	$t\bar{t}H$	Common	(% tHq)	(% $t\bar{t}H$)
$\mu^\pm\mu^\pm$	280	160	140	50.0	87.5
$e^\pm\mu^\pm$	525	280	242	46.1	86.4
$e^\pm e^\pm$	208	90	79	38.0	87.8
$\ell\ell\ell$	126	154	104	82.5	67.5

Table E.2: Individual and shared event yields between this analysis (tHq) and $t\bar{t}H$ multilepton selections.

3330 **Appendix F**

3331 **Forward jet impact plots**

3332 The impact of the data/MC disagreement for forward jet η is observed to reduce with
3333 higher p_T cuts; Figures F.1, F.2 and F.3 show this reduction in the impact of the
3334 forward jet η nuisance in the fit.

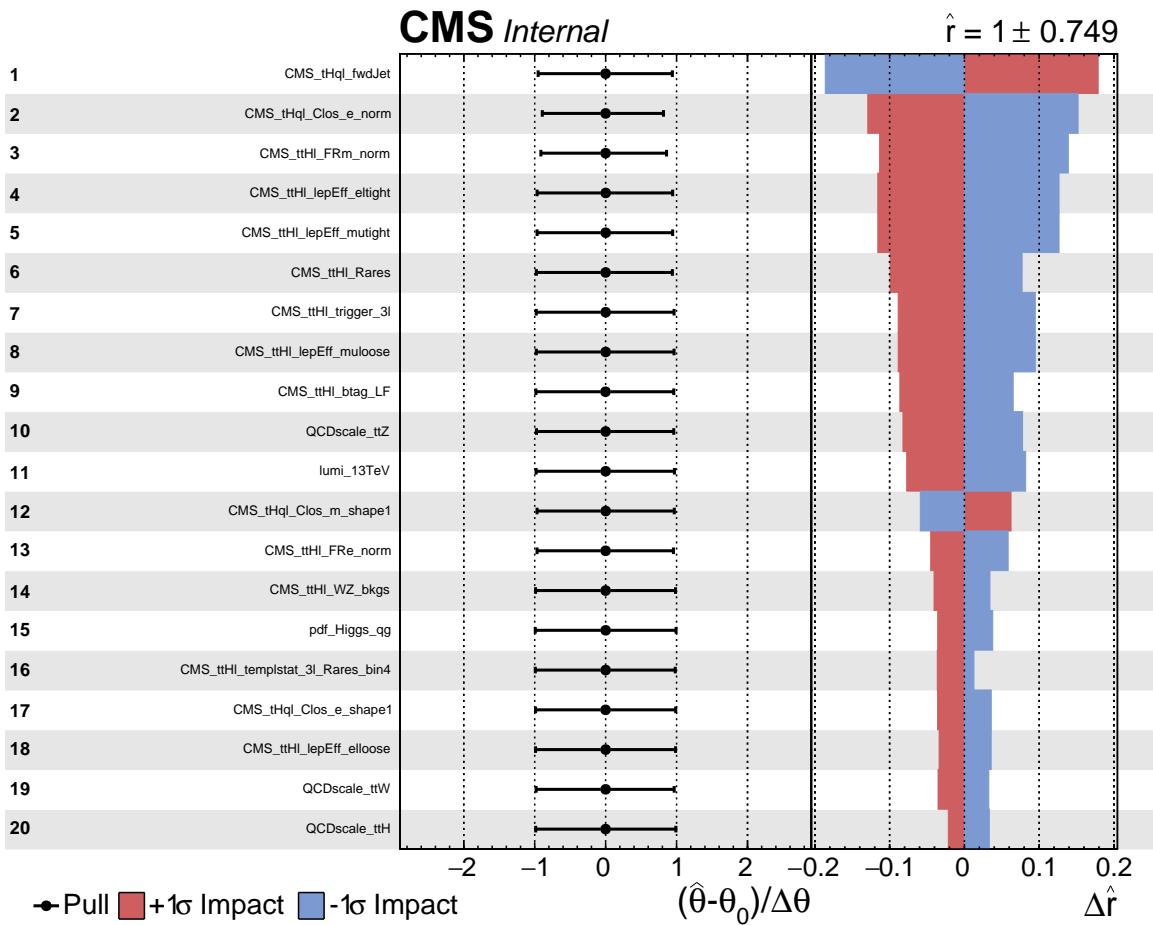


Figure F.1: Post-fit pulls and impacts of the 20 nuisance parameters with p_T cut 25 GeV for the forward jet.

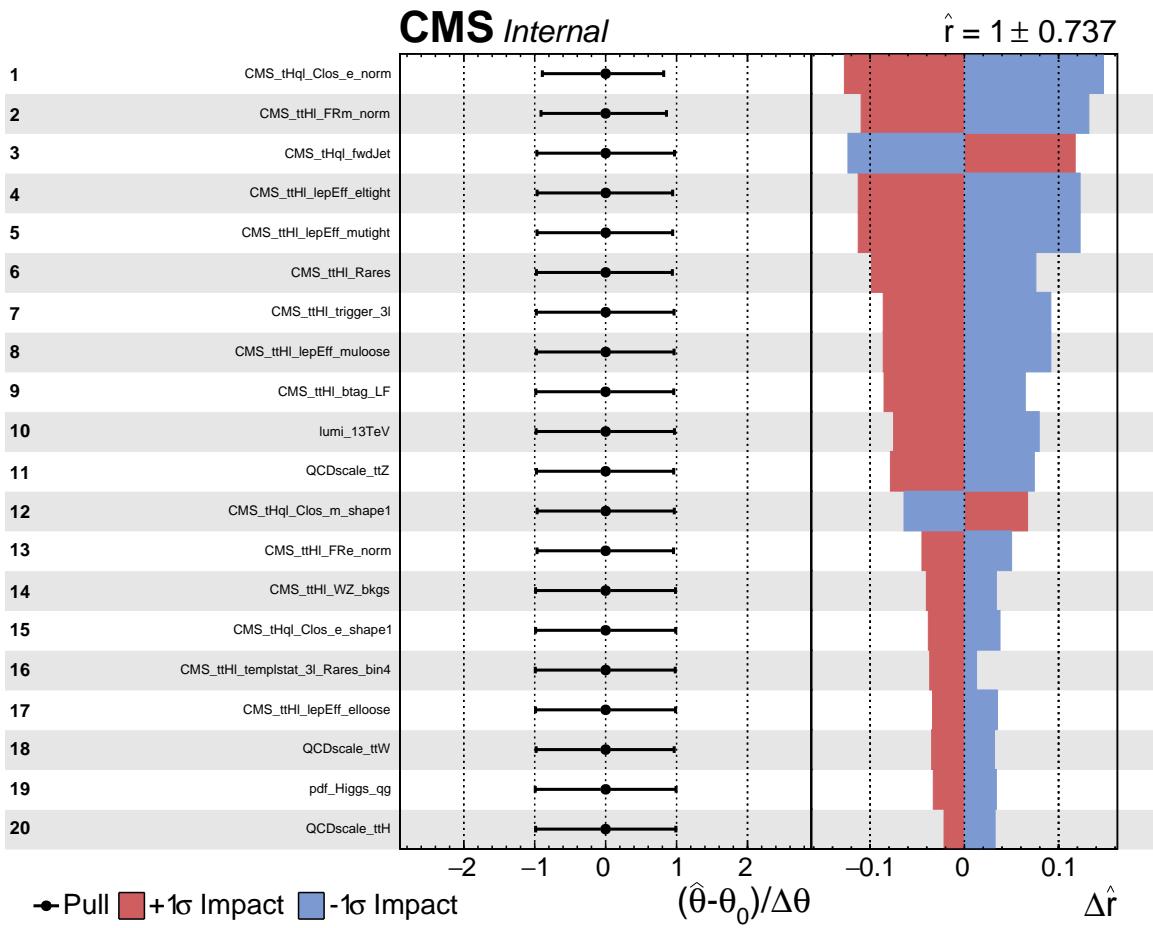


Figure F.2: Post-fit pulls and impacts of the 20 nuisance parameters with p_T cut 30 GeV for the forward jet.

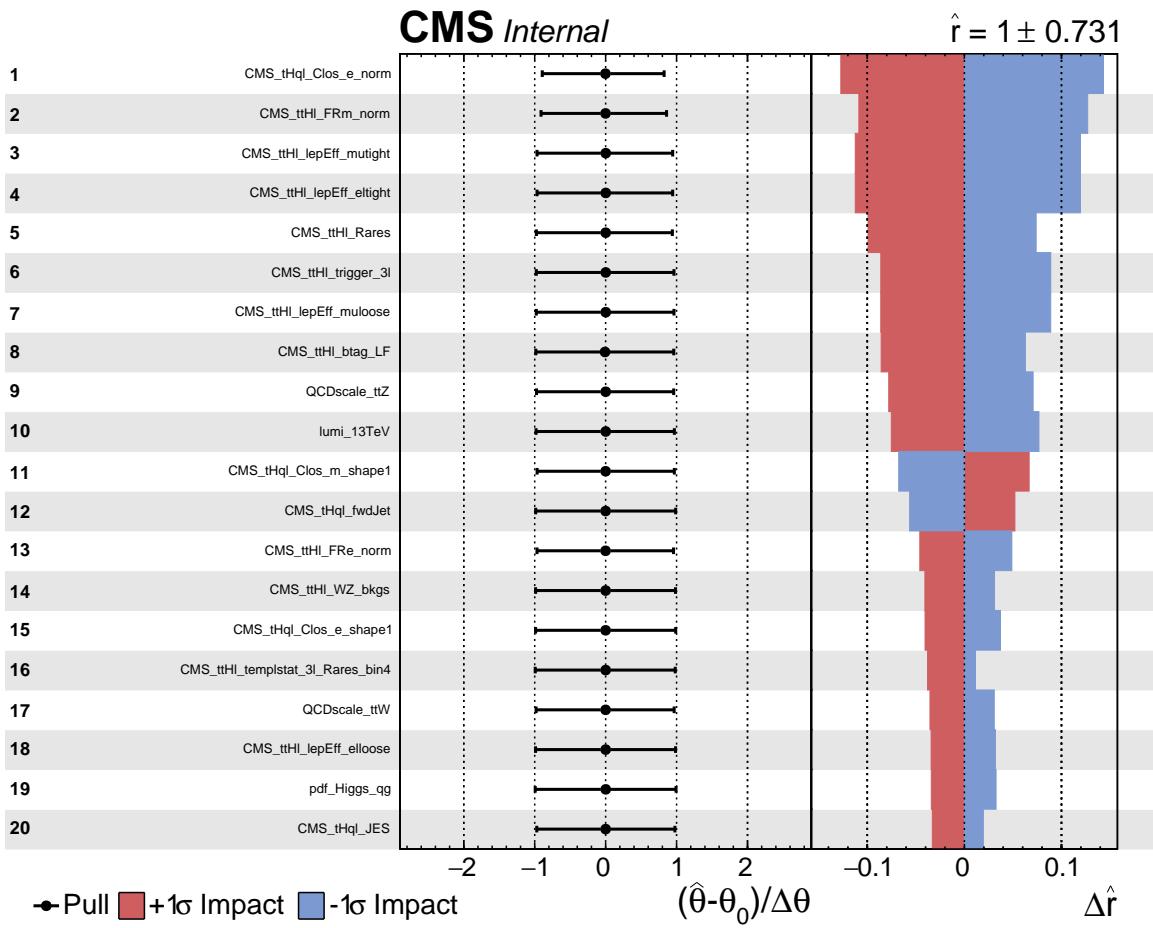


Figure F.3: Post-fit pulls and impacts of the 20 nuisance parameters with p_T cut 40 GeV for the forward jet.

³³³⁵ **Appendix G**

³³³⁶ **Cross sections and Branching**

³³³⁷ **ratios scalings**

κ_V	κ_t	HWW	HZZ	H $\tau\tau$	H $\mu\mu$	Hbb	Hcc	H $\gamma\gamma$	HZ γ	Hgg
0.5	-6.0	0.0827	0.0827	11.9098	11.9098	0.3308	0.3308	0.3308	0.3308	0.3308
0.5	-4.0	0.1417	0.1417	9.0699	9.0699	0.5669	0.5669	0.5669	0.5669	0.5669
0.5	-3.0	0.1889	0.1889	6.7999	6.7999	0.7555	0.7555	0.7555	0.7555	0.7555
0.5	-2.5	0.2173	0.2173	5.4325	5.4325	0.8692	0.8692	0.8692	0.8692	0.8692
0.5	-2.0	0.2478	0.2478	3.9647	3.9647	0.9912	0.9912	0.9912	0.9912	0.9912
0.5	-1.5	0.2782	0.2782	2.5034	2.5034	1.1126	1.1126	1.1126	1.1126	1.1126
0.5	-1.333	0.2877	0.2877	2.0448	2.0448	1.1508	1.1508	1.1508	1.1508	1.1508
0.5	-1.25	0.2922	0.2922	1.8264	1.8264	1.1689	1.1689	1.1689	1.1689	1.1689
0.5	-1.0	0.3048	0.3048	1.2194	1.2194	1.2194	1.2194	1.2194	1.2194	1.2194
0.5	-0.833	0.3122	0.3122	0.8665	0.8665	1.2487	1.2487	1.2487	1.2487	1.2487
0.5	-0.75	0.3154	0.3154	0.7097	0.7097	1.2617	1.2617	1.2617	1.2617	1.2617
0.5	-0.667	0.3184	0.3184	0.5666	0.5666	1.2736	1.2736	1.2736	1.2736	1.2736
0.5	-0.5	0.3235	0.3235	0.3235	0.3235	1.2938	1.2938	1.2938	1.2938	1.2938
0.5	-0.333	0.3272	0.3272	0.1451	0.1451	1.3087	1.3087	1.3087	1.3087	1.3087
0.5	-0.25	0.3285	0.3285	0.0821	0.0821	1.3139	1.3139	1.3139	1.3139	1.3139
0.5	-0.167	0.3294	0.3294	0.0367	0.0367	1.3177	1.3177	1.3177	1.3177	1.3177
0.5	0.0	0.3302	0.3302	0.0000	0.0000	1.3207	1.3207	1.3207	1.3207	1.3207
0.5	0.167	0.3294	0.3294	0.0367	0.0367	1.3177	1.3177	1.3177	1.3177	1.3177
0.5	0.25	0.3285	0.3285	0.0821	0.0821	1.3139	1.3139	1.3139	1.3139	1.3139
0.5	0.333	0.3272	0.3272	0.1451	0.1451	1.3087	1.3087	1.3087	1.3087	1.3087
0.5	0.5	0.3235	0.3235	0.3235	0.3235	1.2938	1.2938	1.2938	1.2938	1.2938
0.5	0.667	0.3184	0.3184	0.5666	0.5666	1.2736	1.2736	1.2736	1.2736	1.2736
0.5	0.75	0.3154	0.3154	0.7097	0.7097	1.2617	1.2617	1.2617	1.2617	1.2617
0.5	0.833	0.3122	0.3122	0.8665	0.8665	1.2487	1.2487	1.2487	1.2487	1.2487
0.5	1.0	0.3048	0.3048	1.2194	1.2194	1.2194	1.2194	1.2194	1.2194	1.2194
0.5	1.25	0.2922	0.2922	1.8264	1.8264	1.1689	1.1689	1.1689	1.1689	1.1689
0.5	1.333	0.2877	0.2877	2.0448	2.0448	1.1508	1.1508	1.1508	1.1508	1.1508
0.5	1.5	0.2782	0.2782	2.5034	2.5034	1.1126	1.1126	1.1126	1.1126	1.1126
0.5	2.0	0.2478	0.2478	3.9647	3.9647	0.9912	0.9912	0.9912	0.9912	0.9912
0.5	2.5	0.2173	0.2173	5.4325	5.4325	0.8692	0.8692	0.8692	0.8692	0.8692
0.5	3.0	0.1889	0.1889	6.7999	6.7999	0.7555	0.7555	0.7555	0.7555	0.7555
0.5	4.0	0.1417	0.1417	9.0699	9.0699	0.5669	0.5669	0.5669	0.5669	0.5669
0.5	6.0	0.0827	0.0827	11.9098	11.9098	0.3308	0.3308	0.3308	0.3308	0.3308

Table G.1: Scalings of Higgs decay branching ratios vs. κ_t and $\kappa_V = 0.5$ for the resolved model.

κ_V	κ_t	HWW	HZZ	H $\tau\tau$	H $\mu\mu$	Hbb	Hcc	H $\gamma\gamma$	HZ γ	Hgg
1.0	-6.0	0.3122	0.3122	11.2408	11.2408	0.3122	0.3122	0.3122	0.3122	0.3122
1.0	-4.0	0.5144	0.5144	8.2305	8.2305	0.5144	0.5144	0.5144	0.5144	0.5144
1.0	-3.0	0.6651	0.6651	5.9862	5.9862	0.6651	0.6651	0.6651	0.6651	0.6651
1.0	-2.5	0.7517	0.7517	4.6979	4.6979	0.7517	0.7517	0.7517	0.7517	0.7517
1.0	-2.0	0.8412	0.8412	3.3647	3.3647	0.8412	0.8412	0.8412	0.8412	0.8412
1.0	-1.5	0.9271	0.9271	2.0859	2.0859	0.9271	0.9271	0.9271	0.9271	0.9271
1.0	-1.333	0.9534	0.9534	1.6941	1.6941	0.9534	0.9534	0.9534	0.9534	0.9534
1.0	-1.25	0.9658	0.9658	1.5091	1.5091	0.9658	0.9658	0.9658	0.9658	0.9658
1.0	-1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.0	-0.833	1.0196	1.0196	0.7075	0.7075	1.0196	1.0196	1.0196	1.0196	1.0196
1.0	-0.75	1.0283	1.0283	0.5784	0.5784	1.0283	1.0283	1.0283	1.0283	1.0283
1.0	-0.667	1.0362	1.0362	0.4610	0.4610	1.0362	1.0362	1.0362	1.0362	1.0362
1.0	-0.5	1.0495	1.0495	0.2624	0.2624	1.0495	1.0495	1.0495	1.0495	1.0495
1.0	-0.333	1.0593	1.0593	0.1175	0.1175	1.0593	1.0593	1.0593	1.0593	1.0593
1.0	-0.25	1.0627	1.0627	0.0664	0.0664	1.0627	1.0627	1.0627	1.0627	1.0627
1.0	-0.167	1.0652	1.0652	0.0297	0.0297	1.0652	1.0652	1.0652	1.0652	1.0652
1.0	0.0	1.0672	1.0672	0.0000	0.0000	1.0672	1.0672	1.0672	1.0672	1.0672
1.0	0.167	1.0652	1.0652	0.0297	0.0297	1.0652	1.0652	1.0652	1.0652	1.0652
1.0	0.25	1.0627	1.0627	0.0664	0.0664	1.0627	1.0627	1.0627	1.0627	1.0627
1.0	0.333	1.0593	1.0593	0.1175	0.1175	1.0593	1.0593	1.0593	1.0593	1.0593
1.0	0.5	1.0495	1.0495	0.2624	0.2624	1.0495	1.0495	1.0495	1.0495	1.0495
1.0	0.667	1.0362	1.0362	0.4610	0.4610	1.0362	1.0362	1.0362	1.0362	1.0362
1.0	0.75	1.0283	1.0283	0.5784	0.5784	1.0283	1.0283	1.0283	1.0283	1.0283
1.0	0.833	1.0196	1.0196	0.7075	0.7075	1.0196	1.0196	1.0196	1.0196	1.0196
1.0	1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.0	1.25	0.9658	0.9658	1.5091	1.5091	0.9658	0.9658	0.9658	0.9658	0.9658
1.0	1.333	0.9534	0.9534	1.6941	1.6941	0.9534	0.9534	0.9534	0.9534	0.9534
1.0	1.5	0.9271	0.9271	2.0859	2.0859	0.9271	0.9271	0.9271	0.9271	0.9271
1.0	2.0	0.8412	0.8412	3.3647	3.3647	0.8412	0.8412	0.8412	0.8412	0.8412
1.0	2.5	0.7517	0.7517	4.6979	4.6979	0.7517	0.7517	0.7517	0.7517	0.7517
1.0	3.0	0.6651	0.6651	5.9862	5.9862	0.6651	0.6651	0.6651	0.6651	0.6651
1.0	4.0	0.5144	0.5144	8.2305	8.2305	0.5144	0.5144	0.5144	0.5144	0.5144
1.0	6.0	0.3122	0.3122	11.2408	11.2408	0.3122	0.3122	0.3122	0.3122	0.3122

Table G.2: Scalings of Higgs decay branching ratios vs. κ_t and $\kappa_V = 1.0$ for the resolved model.

κ_V	κ_t	HWW	HZZ	H $\tau\tau$	H $\mu\mu$	Hbb	Hcc	H $\gamma\gamma$	HZ γ	Hgg
1.5	-6.0	0.6424	0.6424	10.2785	10.2785	0.2855	0.2855	0.2855	0.2855	0.2855
1.5	-4.0	1.0028	1.0028	7.1307	7.1307	0.4457	0.4457	0.4457	0.4457	0.4457
1.5	-3.0	1.2477	1.2477	4.9909	4.9909	0.5545	0.5545	0.5545	0.5545	0.5545
1.5	-2.5	1.3802	1.3802	3.8338	3.8338	0.6134	0.6134	0.6134	0.6134	0.6134
1.5	-2.0	1.5115	1.5115	2.6870	2.6870	0.6718	0.6718	0.6718	0.6718	0.6718
1.5	-1.5	1.6322	1.6322	1.6322	1.6322	0.7254	0.7254	0.7254	0.7254	0.7254
1.5	-1.333	1.6682	1.6682	1.3175	1.3175	0.7414	0.7414	0.7414	0.7414	0.7414
1.5	-1.25	1.6851	1.6851	1.1702	1.1702	0.7489	0.7489	0.7489	0.7489	0.7489
1.5	-1.0	1.7310	1.7310	0.7693	0.7693	0.7693	0.7693	0.7693	0.7693	0.7693
1.5	-0.833	1.7570	1.7570	0.5419	0.5419	0.7809	0.7809	0.7809	0.7809	0.7809
1.5	-0.75	1.7684	1.7684	0.4421	0.4421	0.7860	0.7860	0.7860	0.7860	0.7860
1.5	-0.667	1.7788	1.7788	0.3517	0.3517	0.7906	0.7906	0.7906	0.7906	0.7906
1.5	-0.5	1.7962	1.7962	0.1996	0.1996	0.7983	0.7983	0.7983	0.7983	0.7983
1.5	-0.333	1.8089	1.8089	0.0891	0.0891	0.8039	0.8039	0.8039	0.8039	0.8039
1.5	-0.25	1.8133	1.8133	0.0504	0.0504	0.8059	0.8059	0.8059	0.8059	0.8059
1.5	-0.167	1.8165	1.8165	0.0225	0.0225	0.8073	0.8073	0.8073	0.8073	0.8073
1.5	0.0	1.8191	1.8191	0.0000	0.0000	0.8085	0.8085	0.8085	0.8085	0.8085
1.5	0.167	1.8165	1.8165	0.0225	0.0225	0.8073	0.8073	0.8073	0.8073	0.8073
1.5	0.25	1.8133	1.8133	0.0504	0.0504	0.8059	0.8059	0.8059	0.8059	0.8059
1.5	0.333	1.8089	1.8089	0.0891	0.0891	0.8039	0.8039	0.8039	0.8039	0.8039
1.5	0.5	1.7962	1.7962	0.1996	0.1996	0.7983	0.7983	0.7983	0.7983	0.7983
1.5	0.667	1.7788	1.7788	0.3517	0.3517	0.7906	0.7906	0.7906	0.7906	0.7906
1.5	0.75	1.7684	1.7684	0.4421	0.4421	0.7860	0.7860	0.7860	0.7860	0.7860
1.5	0.833	1.7570	1.7570	0.5419	0.5419	0.7809	0.7809	0.7809	0.7809	0.7809
1.5	1.0	1.7310	1.7310	0.7693	0.7693	0.7693	0.7693	0.7693	0.7693	0.7693
1.5	1.25	1.6851	1.6851	1.1702	1.1702	0.7489	0.7489	0.7489	0.7489	0.7489
1.5	1.333	1.6682	1.6682	1.3175	1.3175	0.7414	0.7414	0.7414	0.7414	0.7414
1.5	1.5	1.6322	1.6322	1.6322	1.6322	0.7254	0.7254	0.7254	0.7254	0.7254
1.5	2.0	1.5115	1.5115	2.6870	2.6870	0.6718	0.6718	0.6718	0.6718	0.6718
1.5	2.5	1.3802	1.3802	3.8338	3.8338	0.6134	0.6134	0.6134	0.6134	0.6134
1.5	3.0	1.2477	1.2477	4.9909	4.9909	0.5545	0.5545	0.5545	0.5545	0.5545
1.5	4.0	1.0028	1.0028	7.1307	7.1307	0.4457	0.4457	0.4457	0.4457	0.4457
1.5	6.0	0.6424	0.6424	10.2785	10.2785	0.2855	0.2855	0.2855	0.2855	0.2855

Table G.3: Scalings of Higgs decay branching ratios vs. κ_t and $\kappa_V = 1.5$ for the resolved model.

κ_V	κ_t	ttHWW	ttHZZ	ttH $\tau\tau$	tHqWW	tHqZZ	tHq $\tau\tau$	tHWWW	tHWZZ	tHW $\tau\tau$
0.5	-6.0	2.9775	2.9775	428.7530	9.2066	9.2066	1325.7460	9.7660	9.7660	1406.3049
0.5	-4.0	2.2675	2.2675	145.1182	7.5740	7.5740	484.7357	7.8819	7.8819	504.4411
0.5	-3.0	1.7000	1.7000	61.1988	6.1214	6.1214	220.3702	6.2562	6.2562	225.2227
0.5	-2.5	1.3581	1.3581	33.9529	5.1857	5.1857	129.6430	5.2277	5.2277	130.6931
0.5	-2.0	0.9912	0.9912	15.8589	4.1227	4.1227	65.9633	4.0762	4.0762	65.2197
0.5	-1.5	0.6259	0.6259	5.6327	2.9838	2.9838	26.8544	2.8645	2.8645	25.7805
0.5	-1.333	0.5112	0.5112	3.6333	2.6025	2.6025	18.4974	2.4648	2.4648	17.5190
0.5	-1.25	0.4566	0.4566	2.8538	2.4154	2.4154	15.0962	2.2700	2.2700	14.1878
0.5	-1.0	0.3048	0.3048	1.2194	1.8696	1.8696	7.4784	1.7078	1.7078	6.8310
0.5	-0.833	0.2166	0.2166	0.6012	1.5271	1.5271	4.2386	1.3605	1.3605	3.7760
0.5	-0.75	0.1774	0.1774	0.3992	1.3657	1.3657	3.0729	1.1987	1.1987	2.6970
0.5	-0.667	0.1417	0.1417	0.2521	1.2111	1.2111	2.1553	1.0451	1.0451	1.8598
0.5	-0.5	0.0809	0.0809	0.0809	0.9236	0.9236	0.9236	0.7640	0.7640	0.7640
0.5	-0.333	0.0363	0.0363	0.0161	0.6720	0.6720	0.2981	0.5249	0.5249	0.2328
0.5	-0.25	0.0205	0.0205	0.0051	0.5618	0.5618	0.1405	0.4231	0.4231	0.1058
0.5	-0.167	0.0092	0.0092	0.0010	0.4622	0.4622	0.0516	0.3334	0.3334	0.0372
0.5	0.0	0.0000	0.0000	0.0000	0.2953	0.2953	0.0000	0.1909	0.1909	0.0000
0.5	0.167	0.0092	0.0092	0.0010	0.1755	0.1755	0.0196	0.1010	0.1010	0.0113
0.5	0.25	0.0205	0.0205	0.0051	0.1339	0.1339	0.0335	0.0762	0.0762	0.0191
0.5	0.333	0.0363	0.0363	0.0161	0.1043	0.1043	0.0463	0.0647	0.0647	0.0287
0.5	0.5	0.0809	0.0809	0.0809	0.0809	0.0809	0.0809	0.0809	0.0809	0.0809
0.5	0.667	0.1417	0.1417	0.2521	0.1044	0.1044	0.1859	0.1480	0.1480	0.2634
0.5	0.75	0.1774	0.1774	0.3992	0.1329	0.1329	0.2991	0.1993	0.1993	0.4485
0.5	0.833	0.2166	0.2166	0.6012	0.1720	0.1720	0.4775	0.2620	0.2620	0.7272
0.5	1.0	0.3048	0.3048	1.2194	0.2811	0.2811	1.1243	0.4200	0.4200	1.6801
0.5	1.25	0.4566	0.4566	2.8538	0.5119	0.5119	3.1993	0.7270	0.7270	4.5438
0.5	1.333	0.5112	0.5112	3.6333	0.6041	0.6041	4.2939	0.8449	0.8449	6.0051
0.5	1.5	0.6259	0.6259	5.6327	0.8096	0.8096	7.2863	1.1020	1.1020	9.9179
0.5	2.0	0.9912	0.9912	15.8589	1.5402	1.5402	24.6428	1.9827	1.9827	31.7238
0.5	2.5	1.3581	1.3581	33.9529	2.3549	2.3549	58.8716	2.9329	2.9329	73.3233
0.5	3.0	1.7000	1.7000	61.1988	3.1686	3.1686	114.0678	3.8625	3.8625	139.0502
0.5	4.0	2.2675	2.2675	145.1182	4.6200	4.6200	295.6829	5.4873	5.4873	351.1881
0.5	6.0	2.9775	2.9775	428.7530	6.6207	6.6207	953.3740	7.6698	7.6698	1104.4467

Table G.4: Scalings of cross section times BR for the resolved model, for the different $t\bar{t}H$, tHq , tHW signal components and $\kappa_V = 0.5$.

κ_V	κ_t	ttHWW	ttHZZ	ttH $\tau\tau$	tHqWW	tHqZZ	tHq $\tau\tau$	tHWWW	tHWZZ	tHW $\tau\tau$
1.0	-6.0	11.2408	11.2408	404.6686	40.4768	40.4768	1457.1666	41.3681	41.3681	1489.2533
1.0	-4.0	8.2305	8.2305	131.6886	34.2339	34.2339	547.7422	33.8480	33.8480	541.5676
1.0	-3.0	5.9862	5.9862	53.8759	28.5396	28.5396	256.8562	27.3983	27.3983	246.5850
1.0	-2.5	4.6979	4.6979	29.3616	24.8511	24.8511	155.3195	23.3557	23.3557	145.9734
1.0	-2.0	3.3647	3.3647	13.4590	20.6360	20.6360	82.5440	18.8497	18.8497	75.3987
1.0	-1.5	2.0859	2.0859	4.6933	16.0557	16.0557	36.1254	14.0919	14.0919	31.7068
1.0	-1.333	1.6941	1.6941	3.0102	14.4942	14.4942	25.7545	12.5059	12.5059	22.2216
1.0	-1.25	1.5091	1.5091	2.3579	13.7201	13.7201	21.4377	11.7273	11.7273	18.3239
1.0	-1.0	1.0000	1.0000	1.0000	11.4220	11.4220	11.4220	9.4484	9.4484	9.4484
1.0	-0.833	0.7075	0.7075	0.4909	9.9372	9.9372	6.8953	8.0059	8.0059	5.5552
1.0	-0.75	0.5784	0.5784	0.3254	9.2212	9.2212	5.1869	7.3200	7.3200	4.1175
1.0	-0.667	0.4610	0.4610	0.2051	8.5229	8.5229	3.7917	6.6579	6.6579	2.9620
1.0	-0.5	0.2624	0.2624	0.0656	7.1807	7.1807	1.7952	5.4076	5.4076	1.3519
1.0	-0.333	0.1175	0.1175	0.0130	5.9375	5.9375	0.6584	4.2814	4.2814	0.4748
1.0	-0.25	0.0664	0.0664	0.0042	5.3616	5.3616	0.3351	3.7730	3.7730	0.2358
1.0	-0.167	0.0297	0.0297	0.0008	4.8163	4.8163	0.1343	3.3009	3.3009	0.0921
1.0	0.0	0.0000	0.0000	0.0000	3.8183	3.8183	0.0000	2.4676	2.4676	0.0000
1.0	0.167	0.0297	0.0297	0.0008	2.9624	2.9624	0.0826	1.7981	1.7981	0.0501
1.0	0.25	0.0664	0.0664	0.0042	2.5928	2.5928	0.1620	1.5284	1.5284	0.0955
1.0	0.333	0.1175	0.1175	0.0130	2.2612	2.2612	0.2507	1.3014	1.3014	0.1443
1.0	0.5	0.2624	0.2624	0.0656	1.7115	1.7115	0.4279	0.9742	0.9742	0.2435
1.0	0.667	0.4610	0.4610	0.2051	1.3198	1.3198	0.5871	0.8188	0.8188	0.3643
1.0	0.75	0.5784	0.5784	0.3254	1.1834	1.1834	0.6657	0.8042	0.8042	0.4524
1.0	0.833	0.7075	0.7075	0.4909	1.0852	1.0852	0.7530	0.8301	0.8301	0.5760
1.0	1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.0	1.25	1.5091	1.5091	2.3579	1.1380	1.1380	1.7782	1.5278	1.5278	2.3872
1.0	1.333	1.6941	1.6941	3.0102	1.2492	1.2492	2.2197	1.7691	1.7691	3.1434
1.0	1.5	2.0859	2.0859	4.6933	1.5628	1.5628	3.5163	2.3434	2.3434	5.2727
1.0	2.0	3.3647	3.3647	13.4590	3.1023	3.1023	12.4092	4.6362	4.6362	18.5449
1.0	2.5	4.6979	4.6979	29.3616	5.2667	5.2667	32.9167	7.4799	7.4799	46.7493
1.0	3.0	5.9862	5.9862	53.8759	7.7435	7.7435	69.6914	10.5403	10.5403	94.8625
1.0	4.0	8.2305	8.2305	131.6886	12.7892	12.7892	204.6276	16.4642	16.4642	263.4266
1.0	6.0	11.2408	11.2408	404.6686	20.9516	20.9516	754.2573	25.5403	25.5403	919.4497

Table G.5: Scalings of cross section times BR for the resolved model, for the different $t\bar{t}H$, tHq , tHW signal components and $\kappa_V = 1.0$.

κ_V	κ_t	ttHWW	ttHZZ	ttH $\tau\tau$	tHqWW	tHqZZ	tHq $\tau\tau$	tHWWW	tHWZZ	tHW $\tau\tau$
1.5	-6.0	23.1266	23.1266	370.0260	96.1923	96.1923	1539.0768	95.1080	95.1080	1521.7272
1.5	-4.0	16.0441	16.0441	114.0913	81.6690	81.6690	580.7570	77.3512	77.3512	550.0531
1.5	-3.0	11.2295	11.2295	44.9178	68.8703	68.8703	275.4812	62.9086	62.9086	251.6344
1.5	-2.5	8.6261	8.6261	23.9614	60.7939	60.7939	168.8720	54.1622	54.1622	150.4505
1.5	-2.0	6.0458	6.0458	10.7481	51.7152	51.7152	91.9381	44.6227	44.6227	79.3293
1.5	-1.5	3.6725	3.6725	3.6725	41.9469	41.9469	41.9469	34.6991	34.6991	34.6991
1.5	-1.333	2.9643	2.9643	2.3410	38.6171	38.6171	30.4971	31.4016	31.4016	24.7987
1.5	-1.25	2.6330	2.6330	1.8284	36.9629	36.9629	25.6687	29.7807	29.7807	20.6810
1.5	-1.0	1.7310	1.7310	0.7693	32.0233	32.0233	14.2326	25.0144	25.0144	11.1175
1.5	-0.833	1.2192	1.2192	0.3760	28.7953	28.7953	8.8803	21.9653	21.9653	6.7740
1.5	-0.75	0.9948	0.9948	0.2487	27.2234	27.2234	6.8058	20.5014	20.5014	5.1254
1.5	-0.667	0.7914	0.7914	0.1565	25.6778	25.6778	5.0772	19.0767	19.0767	3.7720
1.5	-0.5	0.4491	0.4491	0.0499	22.6628	22.6628	2.5181	16.3435	16.3435	1.8159
1.5	-0.333	0.2006	0.2006	0.0099	19.7986	19.7986	0.9758	13.8117	13.8117	0.6807
1.5	-0.25	0.1133	0.1133	0.0031	18.4397	18.4397	0.5122	12.6364	12.6364	0.3510
1.5	-0.167	0.0507	0.0507	0.0006	17.1281	17.1281	0.2123	11.5203	11.5203	0.1428
1.5	0.0	0.0000	0.0000	0.0000	14.6443	14.6443	0.0000	9.4640	9.4640	0.0000
1.5	0.167	0.0507	0.0507	0.0006	12.3858	12.3858	0.1535	7.6760	7.6760	0.0951
1.5	0.25	0.1133	0.1133	0.0031	11.3529	11.3529	0.3154	6.8916	6.8916	0.1914
1.5	0.333	0.2006	0.2006	0.0099	10.3820	10.3820	0.5117	6.1783	6.1783	0.3045
1.5	0.5	0.4491	0.4491	0.0499	8.6227	8.6227	0.9581	4.9621	4.9621	0.5513
1.5	0.667	0.7914	0.7914	0.1565	7.1299	7.1299	1.4098	4.0411	4.0411	0.7990
1.5	0.75	0.9948	0.9948	0.2487	6.4888	6.4888	1.6222	3.6932	3.6932	0.9233
1.5	0.833	1.2192	1.2192	0.3760	5.9148	5.9148	1.8241	3.4176	3.4176	1.0540
1.5	1.0	1.7310	1.7310	0.7693	4.9627	4.9627	2.2057	3.0782	3.0782	1.3681
1.5	1.25	2.6330	2.6330	1.8284	4.0340	4.0340	2.8014	3.0873	3.0873	2.1440
1.5	1.333	2.9643	2.9643	2.3410	3.8531	3.8531	3.0429	3.2206	3.2206	2.5434
1.5	1.5	3.6725	3.6725	3.6725	3.6725	3.6725	3.6725	3.6725	3.6725	3.6725
1.5	2.0	6.0458	6.0458	10.7481	4.4580	4.4580	7.9254	6.3144	6.3144	11.2255
1.5	2.5	8.6261	8.6261	23.9614	6.8533	6.8533	19.0368	10.4359	10.4359	28.9887
1.5	3.0	11.2295	11.2295	44.9178	10.3536	10.3536	41.4143	15.4728	15.4728	61.8913
1.5	4.0	16.0441	16.0441	114.0913	18.9646	18.9646	134.8595	26.5208	26.5208	188.5926
1.5	6.0	23.1266	23.1266	370.0260	35.9359	35.9359	574.9741	46.2619	46.2619	740.1909

Table G.6: Scalings of cross section times BR for the resolved model, for the different $t\bar{t}H$, tHq , tHW signal components and $\kappa_V = 1.5$.

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