

1 SEARCH FOR PRODUCTION OF A HIGGS BOSON AND A SINGLE TOP
2 QUARK IN MULTILEPTON FINAL STATES IN pp COLLISIONS AT $\sqrt{s} = 13$
3 TeV.

4 by

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Chapter 5

Statistical methods

In the course of analyzing the data sets provided by the CMS experiment and used in this thesis, several statistical tools have been employed; in this chapter, a description of these tools will be presented, starting with the general statement of the multivariate analysis methods, followed by the particularities of the Boosted Decision Trees (BDT) method and its application to the classification problem. Statistical inference methods used will also be presented. This chapter is based mainly on References [126–128].

5.1 Multivariate analysis

Multivariate data analysis (MVA) makes use of the statistical techniques developed to analyze more than one variable at once, taking into account all the correlations among variables. MVA is employed in a variety of fields like consumer and market research, quality control and process optimization. Using MVA it is possible to identify the dominant patterns in a data sample, like groups, outliers and trends, and determine to which group a set of values belong; in the particle physics context, MVA methods are used to perform the selection of certain type of events from a large data set.

Processes with small cross section, such as the tHq process ($\sigma_{SM}(\sqrt{s} = 13\text{TeV}) = 70.96 \text{ fb}$), are hard to detect in the presence of the processes with larger cross sections, $\sigma_{SM}^{t\bar{t}}(\sqrt{s} = 13\text{TeV}) = 823.44 \text{ fb}$ for instance; therefore, only a small fraction of the data contains events of interest (signal), the major part is signal-like events, which mimic signal characteristics but belong to different processes, so they are a background to the process of interest. This implies that it is not possible to say with certainty that a given event is a signal or a background and statistical methods should be involved. In that sense, the challenge can be formulated as one where a set of events have to be classified according to certain special features; these features correspond to the measurements of several parameters like energy or momentum, organized in a set of *input variables*. The measurements for each event can be written in a vector $\mathbf{x} = (x_1, \dots, x_n)$ for which

- $f(\mathbf{x}|s)$ is the probability density (*likelihood function*) that \mathbf{x} is the set of measured values given that the event is a signal event (signal hypothesis).
- $f(\mathbf{x}|b)$ is the probability density (*likelihood function*) that \mathbf{x} is the set of measured values given that the event is a background event (background hypothesis).

Figure 5.1 shows three ways to perform a classification of events for which measurements of two properties, i.e., two input variables x_1 and x_2 , have been performed; blue circles represent signal events while red triangles represent background events. The classification on the left is *cut-based* requiring $x_1 < c_1$ and $x_2 < c_2$; usually the cut values (c_1 and c_2) are chosen according to some knowledge about the event process. In the middle plot, the classification is performed using a linear function of the input variables, hence the boundary is a straight line, while in the right plot the

the relationship between input variables is not linear thus the boundary is not linear either.

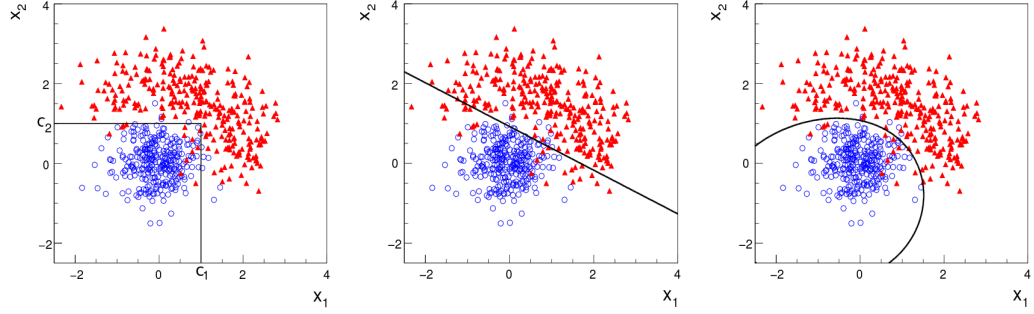


Figure 5.1: Scatter plots-MVA event classification. Distribution of two input variables x_1 and x_2 measured for a set of events; blue circles represent signal events and red triangles represent background events. The classification is based on cuts (left), linear boundary (center), and nonlinear boundary (right) [126]

In general, the boundary can be parametrized in terms of the input variables such that the cut is set on the parametrization instead of on the variables, i.e., $y(\mathbf{x}) = y_{cut}$ with y_{cut} being a constant; thus, the acceptance or rejection of an event is based on which side of the boundary the event is located. If $y(\mathbf{x})$, usually called *test statistic*, has functional form, it can be used to determine the probability distribution functions $p(y|s)$ and $p(y|b)$ and then perform a test statistic with a single cut on the scalar variable y .

Figure 5.2 shows an example of what would be the probability distribution functions under the signal and background hypotheses for a scalar test statistic with a cut on the classifier y . Note that the tails of the distributions indicate that some signal events fall in the rejection region and some background events fall on the acceptance region; therefore, it is convenient to define the *efficiency* with which events of a given type are accepted. The signal and background efficiencies are given by

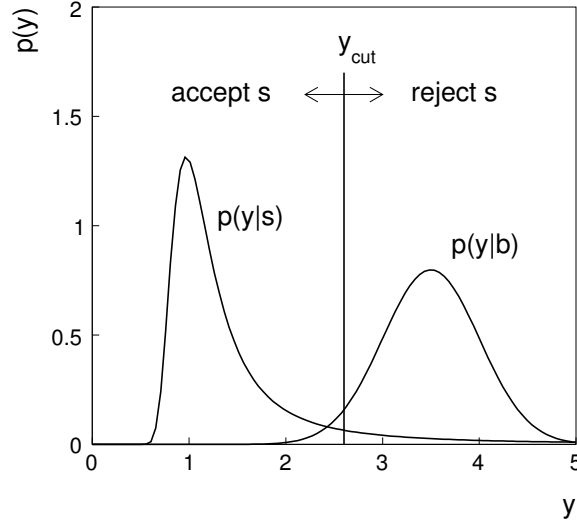


Figure 5.2: Distributions of the scalar test statistic $y(\mathbf{x})$ under the signal and background hypotheses. [126]

$$\varepsilon_s = P(\text{accept event}|s) = \int_A f(\mathbf{x}|s) d\mathbf{x} = \int_{-\infty}^{y_{\text{cut}}} p(y|s) dy, \quad (5.1)$$

$$\varepsilon_b = P(\text{accept event}|b) = \int_A f(\mathbf{x}|b) d\mathbf{x} = \int_{-\infty}^{y_{\text{cut}}} p(y|b) dy, \quad (5.2)$$

104 where A is the acceptance region. If the background hypothesis is the *null hypothesis*
 105 (H_0), the signal hypothesis would be *alternative hypothesis* (H_1); in this context, the
 106 background efficiency corresponds to the significance level of the test (α) and describes
 107 the misidentification probability, while the signal efficiency corresponds to the power
 108 of the test $(1-\beta)^1$ and describes the probability of rejecting the background hypothesis
 109 if the signal hypothesis is true. What is sought in an analysis is to maximize the power
 110 of the test relative to the significance level, i.e., set a selection with the largest possible
 111 selection efficiency and the smallest possible misidentification probability.

¹ β is the fraction of signal events that fall out of the acceptance region

5.1.1 Decision trees

For this thesis, the implementation of the MVA strategy, described above, is performed through decision trees by using the TMVA software package [127] included in the ROOT analysis framework [129]. In a simple picture, a decision tree classifies events according to their input variables values by setting a cut on each input variable and checking which events are on which side of the cut, just as proposed in the MVA strategy, but in addition, as a machine learning algorithm, decision trees offer the possibility to be trained and then perform the classification efficiently.

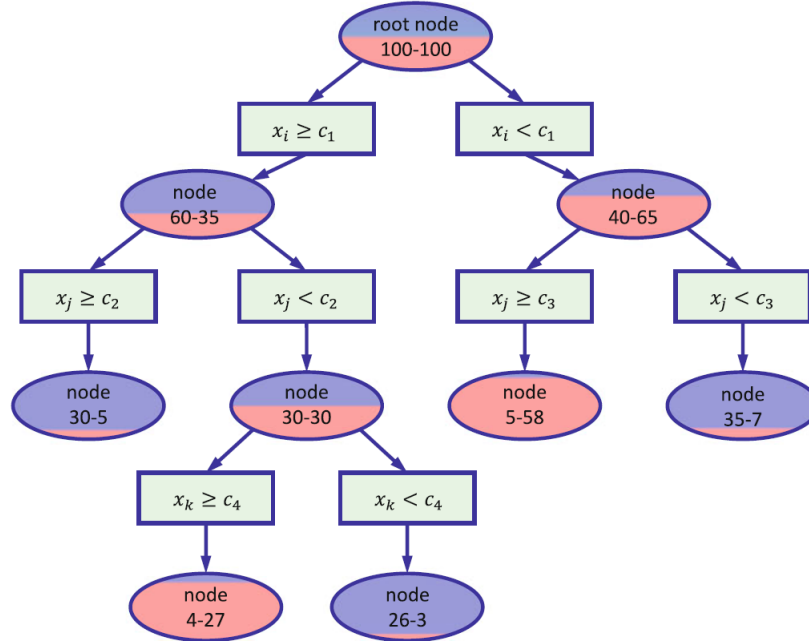


Figure 5.3: Example of a decision tree. Each node is fed with a MC sample mixing signal and background events (left-right numbers); nodes colors represent the relative number of signal/background events [128].

The training or growing of a decision tree is the process where the rules for classifying events are defined; this process is represented in Figure 5.3 and consists of several steps:

- take MC samples of signal and background events and split them into two parts

each; the first parts will be used in the decision tree training, while the second parts will be used for testing the final classifier obtained from the training. Each event has associated a set of input variables $\mathbf{x} = (x_1, \dots, x_n)$ which serve to distinguish between signal and background events. The training sample is taken in at the *root node*.

- Pick one variable, say x_i .
- Pick one value of x_i , each event has its own value of x_i , and split the training sample into two subsamples B_1 and B_2 ; B_1 contains events for which $x_i < c_1$ while B_2 contains the rest of the training events;
- scan all possible values of x_i and find the splitting value that provides the *best* classification², i.e., B_1 is mostly made of signal events while B_2 is mostly made of background events.
- It is possible that variables other than the picked one produce a better classification, hence, all the variables have to be evaluated. Pick the next variable, say x_j , and repeat the scan over its possible values.
- At the end, all the variables and their values will have been scanned, the *best* variable and splitting value will have been identified, say x_1, c_1 , and there will be two nodes fed with the subsamples B_1 and B_2 .

Nodes are further split by repeating the decision process until a given number of final nodes is obtained, nodes are largely dominated by either signal or background events, or nodes have too few events to continue. Final nodes are called *leaves* and they are classified as signal or background leaves according to the class of the majority of events in them. Each *branch* in the tree corresponds to a sequence of cuts.

² Quality of the classification will be treated in the next paragraph.

147 The quality of the classification at each node is evaluated through a separation
 148 criteria; there are several of them but the *Gini Index* (G) is the one used in the
 149 decision trees trained for the analysis in this thesis. G is written in terms of the
 150 purity (P), i.e., the fraction of signal events in the samples after the separation is
 151 made; it is given by

$$G = P(1 - P) \quad (5.3)$$

152 note that $P=0.5$ at the root node while $G=0$ for pure leaves. For a node A split into
 153 two nodes B_1 and B_2 the G gain is

$$\Delta G = G(A) - G(B_1) - G(B_2). \quad (5.4)$$

154 The *best* classification corresponds to that for which the gain of G is maximized;
 155 hence, the scanning over all the variables in an event and their values is of great
 156 importance.

157 In order to provide a numerical output for the classification, events in a sig-
 158 nal(background) leaf are assigned an score of 1(-1) each, defining in this way the
 159 decision tree *classifier/weak learner* as

$$f(\mathbf{x}) = \begin{cases} 1 & \mathbf{x} \text{ in signal region,} \\ -1 & \mathbf{x} \text{ in background region.} \end{cases}$$

160 Figure 5.4 shows an example of the classification of a sample of events, containing
 161 two variables, performed by a decision tree.

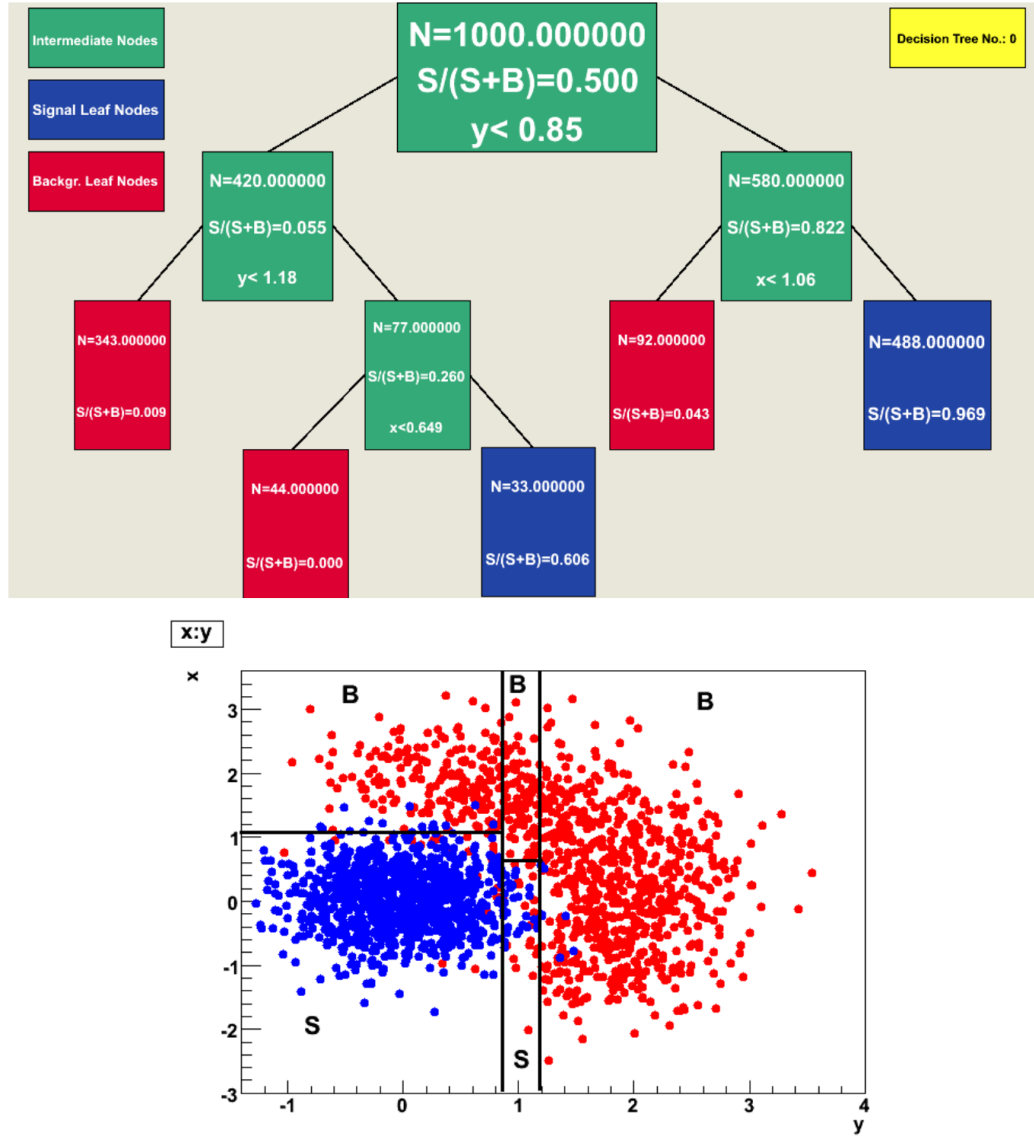


Figure 5.4: Example of a decision tree output. Each leaf, blue for signal events and red for background events, is represented by a region in the variables phase space [130].

162 5.1.2 Boosted decision trees (BDT).

163 Event misclassification occurs when a training event ends up in the wrong leaf, i.e., a
 164 signal event ends up in a background leaf or a background event ends up in a signal
 165 leaf. A way to correct it is to assign a weight to the misclassified events and train
 166 a second tree using the reweighted events; the event reweighting is performed by a

167 boosting algorithm in such a way that when used in the training of a new decision
 168 tree the *boosted events* get correctly classified. The process is repeated iteratively
 169 adding a new tree to the forest and creating a set of classifiers, which are combined
 170 to create the next classifier; the final classifier offers more stability³ and has a smaller
 171 misclassification rate than any individual ones. The resulting tree collection is known
 172 as a *boosted decision tree (BDT)*.

173 Thus, purity of the sample is generalized to

$$P = \frac{\sum_s w_s}{\sum_s w_s + \sum_b w_b} \quad (5.5)$$

174 where w_s and w_b are the weights of the signal and background events respectively;
 175 the Gini index is also generalized

$$G = \left(\sum_i^n w_i \right) P(1 - P) \quad (5.6)$$

176 with n the number of events in the node. The final score of an event, after pass-
 177 ing through the forest, is calculated as the renormalized sum of all the individual
 178 (possibly weighted) scores; thus, high(low) score implies that the event is most likely
 179 signal(background).

180 The boosting procedure, implemented in the *Gradient boosting* algorithm used in
 181 this thesis, produces a classifier $F(\mathbf{x})$ which is the weighted sum of the individual
 182 classifiers obtained after each iteration, i.e.,

$$F(\mathbf{x}) = \sum_{m=1}^M \beta_m f(\mathbf{x}; a_m) \quad (5.7)$$

183 where M is the number of trees in the forest. The *loss function* $L(F, y)$ represents the

³ Decision trees suffer from sensitivity to statistical fluctuations in the training sample which may lead to very different results with an small change in the training samples.

184 deviation between the classifier $F(\mathbf{x})$ response and the true value y obtained from the
 185 training sample (1 for signal events and -1 for background event), according to

$$L(F, y) = \ln(1 + e^{-2F(\mathbf{x})y}) \quad (5.8)$$

186 thus, the reweighting is employed to ensure the minimization of the loss function; a
 187 more detailed description of the minimization procedure can be found in Reference
 188 [131]. The final classifier output is later used as a final discrimination variable, labeled
 189 as *BDT output/response*.

190 5.1.3 Overtraining

191 Decision trees offer the possibility to have as many nodes as desired in order to
 192 reduce the misclassification to zero (in theory); however, when a classifier is too much
 193 adjusted to a particular training sample, the classifier's response to a slightly different
 194 sample may leads to a completely different classification results; this effect is know
 195 as *overtraining*.

196 An alternative to reduce the overtraining in BDTs consists in pruning the tree
 197 by removing statistically insignificant nodes after the tree growing is completed but
 198 this option is not available for BDTs with gradient boosting in the TMVA-toolkit,
 199 therefore, the overtraining has to be reduced by tuning the algorithm, number of
 200 nodes, minimum number of events in the leaves, etc. The overtraining can be evalu-
 201 ated by comparing the responses of the classifier when running over the training and
 202 test samples.

5.1.4 Variable ranking

BDTs have a couple of particular advantages related to the input variables; they are relatively insensitive to the number of input variables used in the vector \mathbf{x} . The ranking of the BDT input variables is determined by counting the number of times a variable is used to split decision tree nodes; in addition, the separation gain-squared achieved in the splitting and the number of events in the node are accounted by applying a weighting to that number. Thus, those variables with small or no power to separate signal and background events are rarely chosen to split the nodes, i.e., are effectively ignored.

In addition, variables correlations play an important role for some MVA methods like the Fisher discriminant algorithm in which the first step consist of performing a linear transformation to a phase space where the correlations between variables are removed; in the case of BDT algorithm, correlations do not affect the performance.

5.1.5 BDT output example

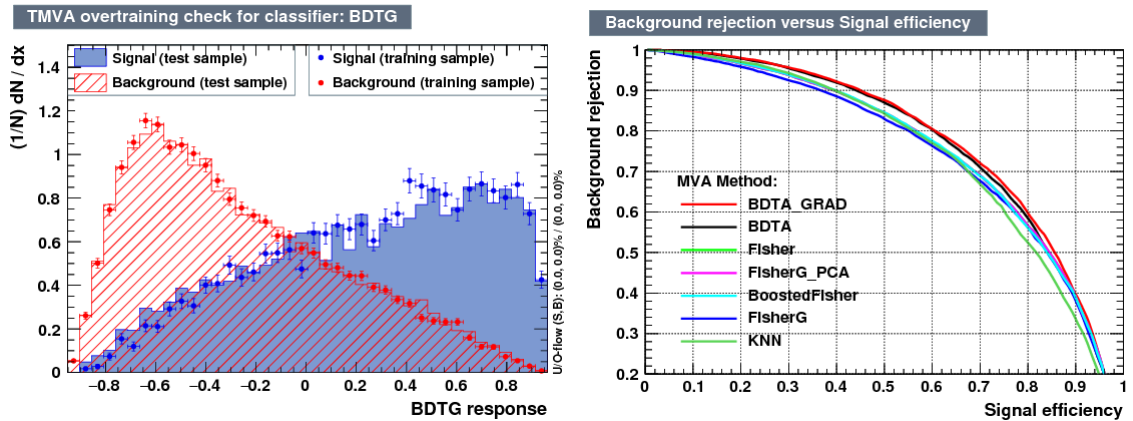


Figure 5.5: Left: Output distributions for the gradient boosted decision tree (BDTG) classifier using a sample of signal ($pp \rightarrow tHq$) and background ($pp \rightarrow t\bar{t}$) events. Right: Background rejection vs signal efficiency (ROC curves) for various MVA classifiers running over the same sample used to produce the plot on the left.

217 The left side of figure 5.5 shows the BDT output distributions for signal ($pp \rightarrow$
 218 tHq) and background ($pp \rightarrow t\bar{t}$) events; this plot is the equivalent to the one showed
 219 in Figure 5.2. A forest with 800 trees, maximum depth per tree = 3, and gradient
 220 boosting have been used as training parameters. The BDTG classifier offers a good
 221 separation power. There is a small overtraining in the signal distribution, while the
 222 background distribution is very well predicted which might indicate that the sample
 223 is composed of more background than signal events.

224 The right side of figure 5.5 shows the background rejection vs signal efficiency
 225 curves for several combinations of MVA classifiers-boosting algorithms running over
 226 the same MC sample; these curves are known as ROC curves and give an indication
 227 of the performance of the classifier. In this particular example, the best performance
 228 is achieved with the BDTG classifier (BDTA_GRAD), which motivate its use in this
 229 thesis.

230 5.2 Statistical inference

231 Once events are classified, the next step consists of finding the parameters that define
 232 the likelihood functions $f(\mathbf{x}|s), f(\mathbf{x}|b)$ for signal and background events respectively.
 233 In general, likelihood functions depend not only on the measurements but also on
 234 parameters (θ_m) that define their shapes; the process of estimating these *unknown*
 235 *parameters* and their uncertainties from the experimental data is called *inference*.

236 The statistical inference tools used in this analysis are implemented in the RooFit
 237 toolkit [132] and COMBINE package [133] included in the CMSSW software frame-
 238 work.

239 5.2.1 Nuisance parameters

240 The unknown parameter vector $\boldsymbol{\theta}$ is made of two types of parameters: those pa-
 241 rameters that provide information about the physical observables of interest for the
 242 experiment or *parameters of interest*, and the *nuisance parameters* that are not of
 243 direct interest for the experiment but that need to be included in the analysis in
 244 order to achieve a satisfactory description of the data; they represent effects of the
 245 detector response like the finite resolutions of the detection systems, miscalibrations,
 246 and in general any source of uncertainty introduced in the analysis.

247 Nuisance parameters can be estimated from experimental data; for instance, data
 248 samples from a test beam are usually employed for calibration purposes. In cases
 249 where experimental samples are not available, the estimation of nuisance parameters
 250 makes use of dedicated simulation programs to provide the required samples.

251 The estimation of the unknown parameters involves certain deviations from their
 252 true values, hence, the measurement of the nuisance parameter is written in terms
 253 of an estimated value, also called central value, $\hat{\theta}$ and its uncertainty $\delta\theta$ using the
 254 notation

$$\theta = \hat{\theta} \pm \delta\theta \quad (5.9)$$

255 where the interval $[\hat{\theta} - \delta\theta, \hat{\theta} + \delta\theta]$ is called *confidence interval*; it is usually interpreted,
 256 in the limit of infinite number of experiments, as the interval where the true value
 257 of the unknown parameter θ is contained with a probability of 0.6827 (if no other
 258 convention is stated); this interval represents the area under a Gaussian distribution
 259 in the interval $\pm 1\sigma$.

260 The uncertainties associated with nuisance parameters produce *systematic uncer-*
 261 *tainties* in the final measurement, while the uncertainties related only to fluctuations

in data and that affect the determination of parameters of interest produce *statistical uncertainties*.

5.2.2 Maximum likelihood estimation method

The estimation of the unknown parameters that are in best agreement with the observed data is performed through a function of the data sample that returns the estimate of those parameters; that function is called an *estimator*. Estimators are usually constructed using mathematical expressions encoded in algorithms.

In this thesis, the estimator used is the likelihood function $f(\mathbf{x}|\boldsymbol{\theta})^4$ which depends on a set of measured variables \mathbf{x} and a set of unknown parameters $\boldsymbol{\theta}$. The likelihood function for N events in a sample is the combination of all the individual likelihood functions, i.e.,

$$L(\boldsymbol{\theta}) = \prod_{i=1}^N f(\mathbf{x}^i|\boldsymbol{\theta}) = \prod_{i=1}^N f(x_1^i, \dots, x_n^i; \theta_1, \dots, \theta_m) \quad (5.10)$$

and the estimation method used is the *Maximum Likelihood Estimation* method (MLE); it is based on the combined likelihood function defined by eqn. 5.10 and the procedure seeks for the parameter set that corresponds to the maximum value of the combined likelihood function, i.e., the *maximum likelihood estimator* of the unknown parameter vector $\boldsymbol{\theta}$ is the function that produces the vector of *best estimators* $\hat{\boldsymbol{\theta}}$ for which the likelihood function $L(\boldsymbol{\theta})$ evaluated at the measured \mathbf{x} is maximum.

Usually, the logarithm of the likelihood function is used in numerical algorithm implementations in order to avoid underflow the numerical precision of the computers due to the product of low likelihoods. In addition, it is common to minimize the negative logarithm of the likelihood function, therefore, the negative log-likelihood

⁴ analogue to the likelihood functions described in previous sections

283 function is

$$F(\boldsymbol{\theta}) = -\ln L(\boldsymbol{\theta}) = -\sum_{i=1}^N f(\mathbf{x}^i | \boldsymbol{\theta}). \quad (5.11)$$

284 The minimization process is performed by the software MINUIT [134] imple-
 285 mented in the ROOT analysis framework. In case of data samples with large number
 286 of measurements, the computational resources necessary to calculate the likelihood
 287 function are too big; therefore, the parameter estimation is performed using binned
 288 distributions of the variables of interest for which the *binned likelihood function* is
 289 given by

$$L(\mathbf{x}|r, \boldsymbol{\theta}) = \prod_{i=1} \frac{(r \cdot s_i(\boldsymbol{\theta}) + b_i(\boldsymbol{\theta}))^{n_i}}{n_i!} e^{-r \cdot s_i(\boldsymbol{\theta}) - b_i(\boldsymbol{\theta})} \prod_{j=1} \frac{1}{\sqrt{2\pi}\sigma_{\theta_j}^2} e^{-(\theta_j - \theta_{0,j})^2 / 2\sigma_{\theta_j}^2}, \quad (5.12)$$

290 with s_i and b_i the expected number of signal and background yields for the bin i , n_i
 291 is the observed number of events in the bin i and $r = \sigma/\sigma_{SM}$ is the signal strength.
 292 Note that the number of entries per bin follows a Poisson distribution. The effect
 293 of the nuisance parameters have been included in the likelihood function through
 294 the multiplication by a Gaussian distribution that models the nuisance. The three
 295 parameters, r , s_i and b_i are jointly fitted to estimate the value of r .

296 5.3 Upper limits

297 In this analysis, two hypotheses are considered; the background only hypothesis
 298 ($H_0(b)$) and the signal plus background hypothesis ($H_1(s+b)$), i.e., the sample of
 299 events is composed of background only events ($r=0$) or it is a mixture of signal plus
 300 background events ($r=1$). The exclusion of one hypothesis against the other means
 301 that the observed data sample better agrees with H_0 or rather with H_1 . In order
 302 to discriminate these hypotheses, a test statistic is constructed on the basis of the

303 likelihood function evaluated for each of the hypothesis.

304 The *Neyman-Pearson* lemma [135] states that the test statistic that provides the
 305 maximum power for H_1 for a given significance level (background misidentification
 306 probability α), is given by the ratio of the likelihood functions $L(\mathbf{x}|H_1)$ and $L(\mathbf{x}|H_0)$;
 307 however, in order to use that definition it is necessary to know the true likelihood
 308 functions, which in practice is not always possible. Approximate functions obtained
 309 by numerical methods, like the BDT method described above, have to be used, so
 310 that the *profile likelihood* test statistic is defined by

$$\lambda(\mathbf{r}) = \frac{L(\mathbf{x}|r, \hat{\boldsymbol{\theta}}(r))}{L(\mathbf{x}|\hat{r}, \hat{\boldsymbol{\theta}})}, \quad (5.13)$$

311 where, \hat{r} and $\hat{\boldsymbol{\theta}}$ maximize the likelihood function, and $\hat{\boldsymbol{\theta}}$ maximizes the likelihood
 312 function for a given value of the signal strength modifier r . In practice, the test
 313 statistic t_r

$$t_r = -2\ln\lambda(r) \quad (5.14)$$

314 is used to evaluate the presence of signal in the sample, since the minimum of t_r at
 315 $r = \hat{r}$ suggests the presence of signal with signal strength \hat{r} . The uncertainty interval
 316 for r is determined by the values of r for which $t_r = +1$.

317 The expected probability density function (p.d.f) $f(t_r|r, \boldsymbol{\theta})$ of the test statistic t_r
 318 can be obtained numerically by generating MC samples where one hypothesis, $H_0(b)$
 319 or $H_1(s+b)$, is assumed; thus, MC samples contain the possible values of t_r obtained
 320 from *pseudo-experiments* as shown in Figure 5.6. The probability that t_r takes a value
 321 equal or greater than the observed value ($t_{r,obs}$) when a signal with a signal modifier
 322 r is present in the data sample, is called the *p-value* of the observation; it can be
 323 calculated using

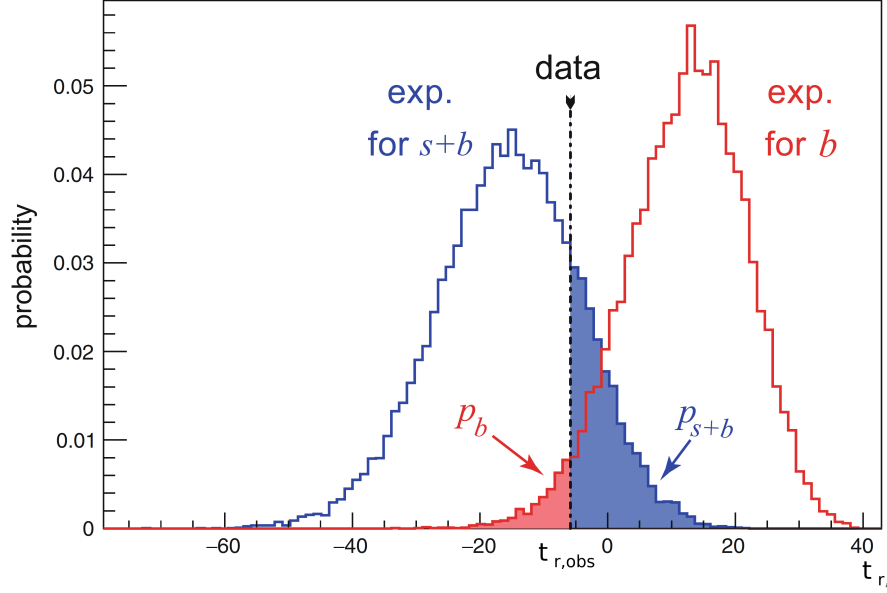


Figure 5.6: t_r p.d.f. from MC pseudo experiments assuming H_0 (red) and H_1 (blue). The black dashed line shows the value of the test statistic as measured from data. Adapted from Reference [128].

$$p_r = \int_{t_{r,obs}}^{\infty} f(t'_r|r, \boldsymbol{\theta}) dt'_r, \quad (5.15)$$

thus, $p_r < 0.05$ means that, for that particular value of r , H_1 could be excluded at 95% Confidence Level (CL). The corresponding background-only p-value is given by

$$1 - p_b = \int_{t_{r,obs}}^{\infty} f(t'_r|0, \boldsymbol{\theta}) dt'_r, \quad (5.16)$$

If the t_r p.d.f.s for both hypotheses are well separated, as shown in the top side of Figure 5.7, the experiment is sensitive to the presence of signal in the sample. If the signal presence is small, both p.d.f.s will be largely overlapped (bottom of Figure ??) and either the signal hypothesis could be rejected with not enough justification because the experiment is not sensitive to the signal or a fluctuation of the background could be misinterpreted as presence of signal with the corresponding rejection of the

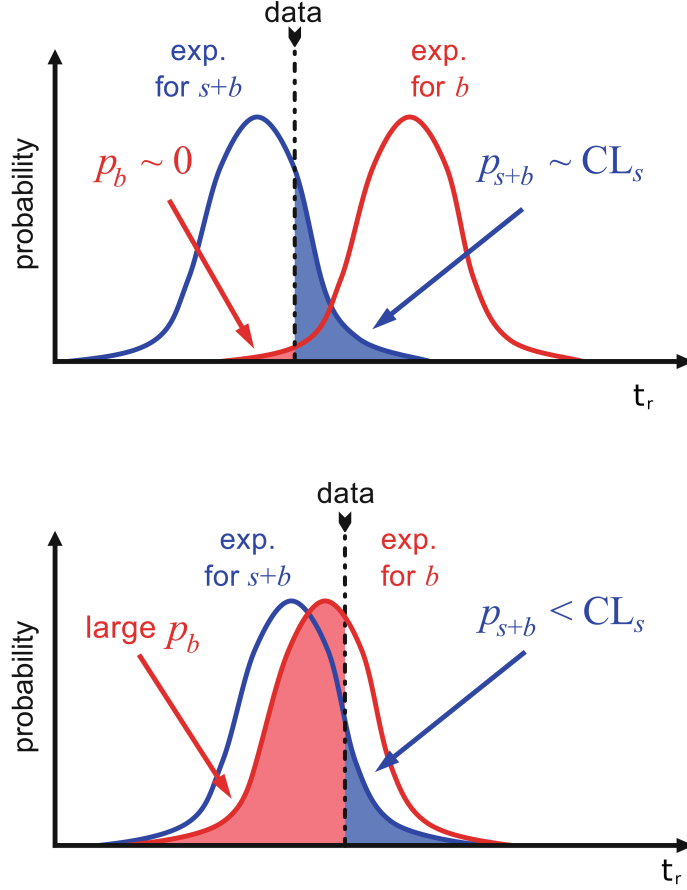


Figure 5.7: CL_s limit illustration. When the test statistic p.d.f. for the two hypotheses H_0 and H_1 are well separated (top) and when they are largely overlapped (bottom). Adapted from Reference [128].

332 background-only hypothesis. These issues are corrected by using the modified p-
 333 value [136]

$$p'_r = \frac{p_r}{1 - p_b} \equiv CL_s. \quad (5.17)$$

334 If H_1 is true, then p_b is small, $CL_s \simeq p_r$ and H_0 is rejected; if there is large
 335 overlap and an statistical fluctuation cause that p_b is large, then both numerator and
 336 denominator in Eqn. 5.17 become small but CL_s would allow the rejection of H_1
 337 even if there is poor sensitivity to signal.

338 The upper limit of the parameter of interest r^{up} is determined by excluding the
 339 range of values of r for which $CL_s(r, \theta)$ is lower than the confidence level desired,
 340 normally 90% or 95%, e.g, scanning over r and finding the value for which $p_r^{up} =$
 341 0.05. The expected upper limit can be calculated using pseudo-experiments based on
 342 the background-only hypothesis and obtaining a distribution for r_{ps}^{up} ; the median of
 343 that distribution corresponds to the expected upper limit, while the $\pm 1\sigma$ and $\pm 2\sigma$
 344 deviations correspond to the values of the distribution that defines the 68% and 95%
 345 of the area under the distribution centered in the median. It is usual to present all
 346 the information about the expected and observed limits in the so-called *Brazilian-flag*
 347 *plot* as the one showed in Figure 5.8. The solid line represent the observed CL_s

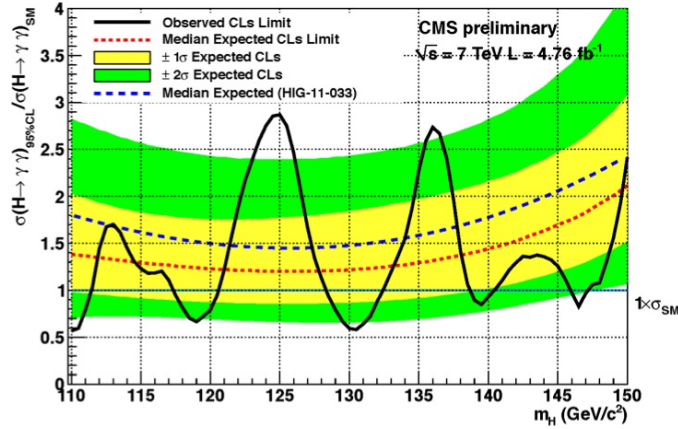


Figure 5.8: Brazilian flag plot of CMS experiment limits for Higgs boson decaying to photons [137].

348 5.4 Asymptotic limits

349 As said before, the complexity of the likelihood functions, the construction of test
 350 statistics, and the calculation of the limits and their uncertainties is not always man-
 351 ageable and requires extensive computational resources; in order to overcome those
 352 issues, asymptotic approximations for likelihood-based test statistics, like the ones

353 described in previous sections, have been developed [138, 139] using Wilks' theorem.
354 Asymptotic approximations replace the construction of the test statistics p.d.f.s using
355 MC pseudo-experiments, with the approximate calculation of the test statistics p.d.f.s
356 by employing the so-called *Asimov dataset*.

357 The Asimov dataset is defined as the dataset that produce the true values of the
358 nuisance parameters when it is used to evaluate the estimators for all the parameters;
359 it is obtained by setting the values of the variables in the dataset to their expected
360 values [139].

361 Limits calculated by using the asymptotic approximation and the Asimov dataset
362 are know as *asymptotic limits*.

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