Jacob M. Montgomery

Quantitative Political Methodology

Causality in Regression and Difference in

Differences

Road map

Where we have been:

- What is regression?
- How to interpret coefficients?
- ► Interactions/Dummies

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- ▶ What is regression?
- How to interpret coefficients?
- Interactions/Dummies

Today:

- Using regression for causal inference
- Using difference-in-differences to make causal claims

- ▶ We will use T to represent a treatment variable.
- ► For a categorical treatment

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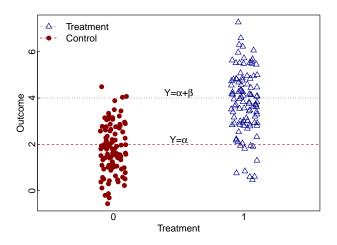
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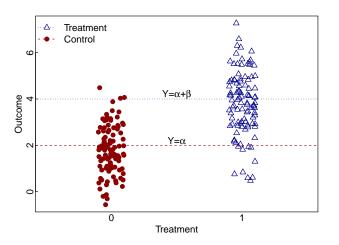
- ► We let y_i^1 represent the outcome of the ith unit if the treatment is given.
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- ▶ The causal effect of T_i on observation i will then be $y_i^1 y_i^0$

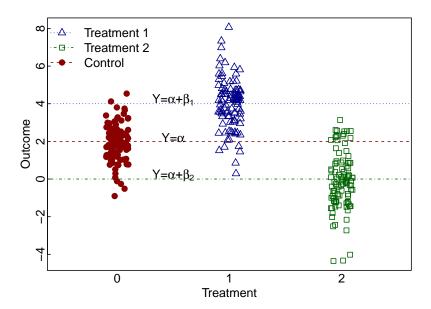


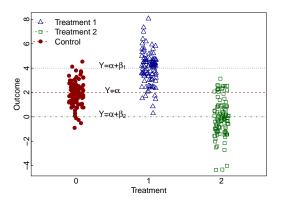


$$ATE = mean(y_i^1) - mean(y_i^0)$$

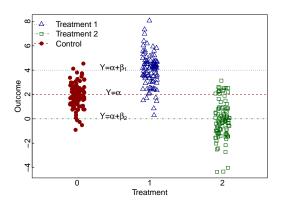
$$ATE = (\alpha + \beta) - (\alpha)$$

$$\blacktriangleright$$
 ATE = β



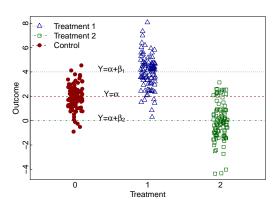


$$Y = \alpha + T_1 \beta_1 + T_2 \beta_2$$



$$Y = \alpha + T_1\beta_1 + T_2\beta_2$$

- ▶ Control: $Y = \alpha$
- ▶ Treatment 1: $Y = \alpha + \beta_1$
- ▶ Treatment 2: $Y = \alpha + \beta_2$

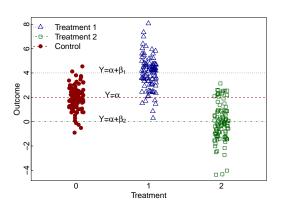


$$Y = \alpha + T_1\beta_1 + T_2\beta_2$$

$$ATE_1 = mean(y_i^1) - mean(y_i^0)$$

$$ATE_1 = (\alpha + \beta_1) - (\alpha)$$

$$ightharpoonup$$
 $ATE_1 = \beta_1$

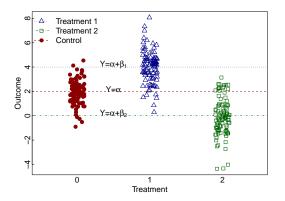


►
$$ATE_2 = mean(y_i^2) - mean(y_i^0)$$

► $ATE_2 = (\alpha + \beta_2) - (\alpha)$

$$ightharpoonup$$
 $ATE_2 = \beta_2$

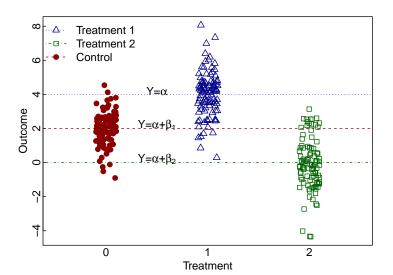
Is blue Different than green?



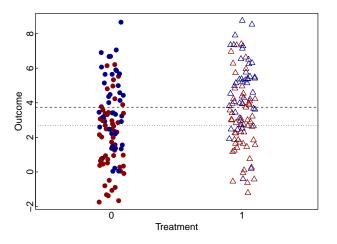
- $ATE_{2vs.1} = mean(y_i^2) mean(y_i^1)$
- $ATE_{2vs.1} = (\alpha + \beta_2) (\alpha + \beta_1)$
- $ATE_{2vs.1} = \beta_2 \beta_1$

Is blue Different than green?

A much easier way to do this, is to change what is the "control" and leave that out.

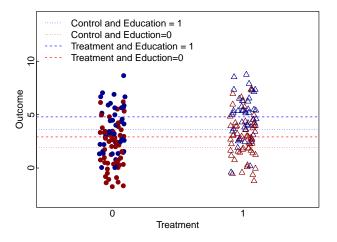


Control variables



$$Y = \alpha + T\beta_1 + X\beta_2$$

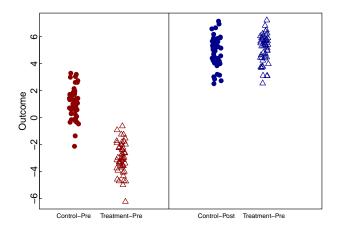
Control variables



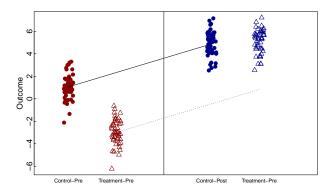
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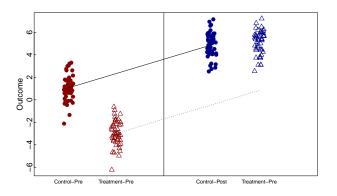
Adding control variables improves precision

	No Control	Control
Intercept	2.67	1.89
	(0.22)	(0.24)
Treatment	1.43	1.42
	(0.31)	(0.29)
Covariate		1.78
		(0.29)
R^2	0.056	0.136

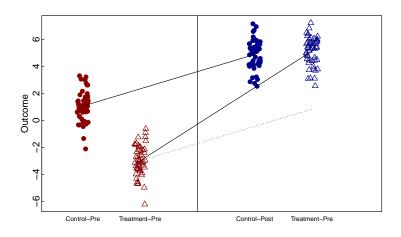


$$Y = \alpha + Treatment\beta_1 + Pre/Post\beta_2 + (T \times PP)\beta_3$$





- Assume parallel paths
- ► The treatment group would have moved in parallel to the control group in the absence of the intervention.
- ▶ We can estimate the effect of the treatment on the treated



- We need to model both what happened and what would have happened
- $Y = \alpha + Treatment\beta_1 + Pre/Post\beta_2 + (T \times PP)\beta_3$

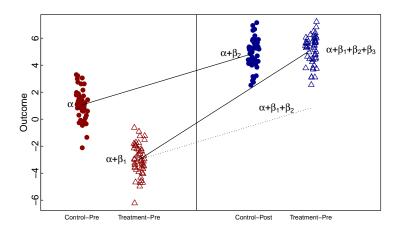
Diff-in-diff model

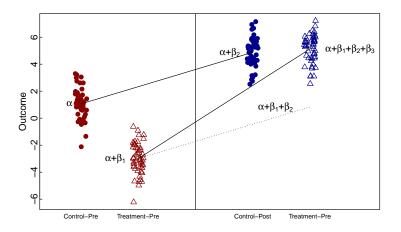
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	1.0591	0.1547	6.84	0.0000
Assignment	-4.0522	0.2188	-18.52	0.0000
PrePost	3.8202	0.2188	17.46	0.0000
Assignment:PrePost	4.2994	0.3095	13.89	0.0000

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Let's write down the prediction equation on the board.





The difference between what we observed $(\alpha + \beta_1 + \beta_2 + \beta_3)$ and what we would have observed $(\alpha + \beta_1 + \beta_2)$ is

$$(\alpha + \beta_1 + \beta_2 + \beta_3) - (\alpha + \beta_1 + \beta_2) = \beta_3$$

Difference in difference: Discussion

▶ Despite being tricky to think about it, it is simple to estimate.

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- ▶ Despite being tricky to think about it, it is simple to estimate.
- ▶ Does *not require* that the treatment and control group be similar, only that that they would have had parallel paths.
- ► You can (and should) also control for other factors, which will help improve your estimates.

Applied Example: Minimum wage laws

What is the effect of increasing the minimum wage on low-wage workers?

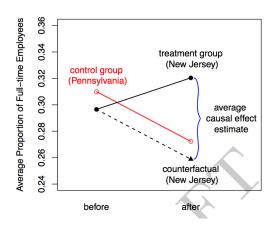
- ► Side 1?
- ► Side 2?

Study basics:

- ► In 1992, New Jersey increased the minimum wage from \$4.25/hour to \$5.05/hour.
- Researchers collected information about the number of full time employees (as a proportion of total number of employees) at various fast food chains before and after the reform.

Study basics:

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- ► Researchers collected information about the number of full time employees (as a proportion of total number of employees) at various fast food chains before and after the reform.
- Researchers also collected the same information from the same chains in Pennsylvania to serve as a counterfactual.
- Are New Jersey and Pennsylvania perfect counterfactuals for each other?



- ▶ Divide up into your groups.
- ► Interpret this plot. What was the effect of the wage increase in New Jersey? Be ready to answer.