Lecture 10: Hypothesis Testing 3

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Quantitative Political Methodology

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Roadmap

Last class:

- Hypothesis tests with small samples
- Types of errors
- Discussion of one-sided/two-sided tests

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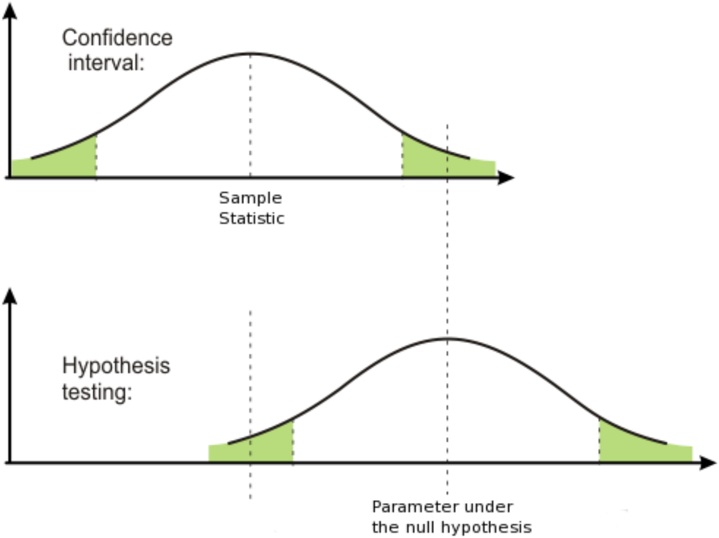
- Types of errors
- Discussion of one-sided/two-sided tests

This class:

- Relationship between CI and NHPT
- Working more examples

Visualizing confidence intervals and null-hypothesis testing}



Example: Confidence interval approach #1

According to a union agreement, the mean income for all senior-level assembly-line workers in a large company equals \$525 per week. A representative of a women's group decides to analyze whether the mean income μ for female employees matches this norm. For a random sample of 36 female employees, $\bar{y} = \$495$ and $s = \$75$.

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Research projects

First, think of a research question!

- What topics interest you?
- What phenomenon do you want to explain?
- If you don't care about the question itself, then the project will be miserable to complete.