

5.1 - 5.4 Notes

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1 The Pythagorean theorem

$$a^2 + b^2 - 2ab \cos C = c^2 \quad (1)$$

$$a^2 + b^2 \because -2ab \cos C = 2ab \cdot 0 = 0 \quad (2)$$

$$\frac{d}{dx}(e^x) = e^x \cdot \ln e = e^x \cdot 1 \quad (3)$$

$$\therefore \ln_e e = e^1 \quad (4)$$

$$\frac{d}{dx}(b^x) = b^x \cdot \ln b = \ln b \cdot (b^x) \quad (5)$$

$$\int b^x dx = \frac{b^x}{\ln b} + C \quad (6)$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x} \quad (7)$$

$$\frac{d}{dx}(\log_b x) = \frac{d}{dx} \left(\frac{\log(x)}{\log(b)} \right) \Rightarrow \log_4(64) = \frac{\log(64)}{\log(4)} = 3 \quad (8)$$

$$\therefore = \frac{d}{dx} \left(\frac{\ln x}{\ln b} \right) \quad (9)$$

$$= \frac{d}{dx} \left(\frac{1}{\ln(b)} \right) \ln x \quad (10)$$

$$= \frac{1}{x \ln b} \quad (11)$$

2 A glance at integration by parts

$$\int \ln x dx \quad (1)$$

$$= x \ln x - x \quad (2)$$

3 01/09/24 Warm-up

1.

$$f(x) = x + \sin(x) \quad (1)$$

$$f'(x) = 1 + \cos(x) \quad (2)$$

4 The tangent integral

$$\int \tan x dx \quad (1)$$

$$= \int \frac{\sin x}{\cos x} dx, \quad u = \cos x, \quad du = -\sin x dx \quad (2)$$

$$= - \int \frac{1}{u} du \quad (3)$$

$$= -\ln |u| + C = -\ln |\cos x| + C = \ln |\sec x| + C \quad (4)$$

5 The secant integral

$$\int \sec x dx \left(\frac{\sec x + \tan x}{\sec x + \tan x} \right) \quad (1)$$

$$= \int \frac{\sec^2 x + \sec x \tan x}{\sec x + \tan x} dx \quad u = \sec x + \tan x \quad du = \sec x \tan x + \sec^2 x dx \quad (2)$$

$$\int \frac{1}{u} du \quad (3)$$

$$= \ln |u| + C \quad (4)$$

$$= \ln |\sec x + \tan x| + C \quad (5)$$

6 The cosecant integral

$$\int \csc x dx \quad (1)$$

$$= \quad (2)$$