Variation in the demographic effects of grass-endophyte symbiosis along an aridity gradient

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1 Abstract

Introduction

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Plant-microbe symbioses are widespread and ecologically important. These interactions are famously context-dependent, where the direction and strength of the interaction outcome depends on the environment in which it occurs (Bronstein, 1994; Fowler et al., 2023; Hoeksema and Bruna, 2015). Plant-microbe interactions that are beneficial under stressful conditions may become parasitic under benign conditions (Giauque et al., 2019). Under biotic stress (e.g., herbivory), endophyte symbiosis can benefit host plants by facilitating the production of secondary compounds that deter feeding or exert direct toxicity, thereby reducing insect growth, survival, and oviposition (Atala et al., 2022; Bastias et al., 2017; Vega, 2008). Similarly under abiotic stress (e.g., 10 drought), symbionts can increase their host tolerance (Clay and Schardl, 2002). However, in 11 many plant-microbe interactions, host protection is not guaranteed solely by the presence of a symbionts; rather, the density of the symbiont can determine the effectiveness of this protection 13 (Laughton et al., 2014). Higher endophyte densities may lead to increased resource exploitation 14 by the symbiont, potentially imposing costs on the host, such as reduced growth or reproduction 15 (Faeth, 2009).

Context dependence raises the hypothesis that plant-microbe interactions are likely to vary 17 across environmental gradients, from range core to range edge, with significant implications 18 for host range expansion. If microbial symbiosis provides greater benefits under environmental 19 stress, then symbionts could enhance the suitability of range-edge environments, potentially extending host range limits (Allsup et al., 2023; Rudgers et al., 2020). For instance, fungal 21 endophytes improve the survival of Bromus laevipes populations in dry conditions, increasing their drought resistance at the range edge and thereby extending the species' geographic range (Afkhami et al., 2014; David et al., 2019). Even if the symbiont does not directly improve host 24 survival, it may still enhance host population growth over time by increasing relative growth and 25 reproduction, potentially offsetting the negative effects of lower survival rates (Yule et al., 2013). Conversely, if microbial symbiosis is costly for the host at range edge, symbionts could constrain host range (Bennett and Groten, 2022; Benning and Moeller, 2021*a,b*). Although context dependence, along with spatiotemporal variations in abiotic environmental conditions may reduce the effectiveness of the benefits provided by the symbiont to the host species, our understanding of the mechanisms that alter host-symbiont interactions across species geographic range remains limited.

Ecological studies of plant-microbe symbiosis typically examine interactions from the plant's 33 perspective and rarely manipulate symbiont frequency to explore how symbiont response to environmental variation might translate to effect on host demographic performance across host's range. Symbionts promotes their own fitness by influencing their host's life history traits and 36 resistance to abiotic and biotic stress (Giauque et al., 2019; Kazenel et al., 2015; Saikkonen et al., 37 1998). Therefore overlooking the role of symbionts and their potential cascading effects on the eco-evolutionary population dynamics of host species could lead to inaccurate prediction of host 39 response to global change. Moreover, studies on plant-microbe symbiosis often fail to account for the synergistic effects of abiotic and biotic factors on host dynamics across species ranges. Finally, studies of plant-microbe symbiosis have relied on methods such as inoculating sterile soil (Peacher and Meiners, 2020), excluding endophyte fungal hyphae using fine mesh or rotating cores (Chung et al., 2019), and applying fungicide (Bennett and Groten, 2022). While valuable, these approaches are often challenging to implement in field settings or on large scales. As a result, the mechanisms by which symbionts drive host range limitation and expansion are poorly understood, hindering our understanding of the potential cascading effects of symbionts 47 on eco-evolutionary species demography and range limitation in the context of global change. 48

Working across a precipitation gradient in the south-central US, we investigated how the demographic effects of endophyte symbiosis varied from core to edge of the host range. To answer these questions, we studied the symbiotic association between cool-season grass species (*Agrostis hyemalis*, *Elymus virginicus* and *Poa arachnifera*) and its vertically transmitted fungal symbiont Epichloë elymi. [Describe ecology and natural history of grass-endophyte interactions]¹. Our

¹I am not sure If we need this

experiment was design to test the following hypotheses²:

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- 1. We hypothesized that stress associated with aridity and low precipitation would strengthen the plant-fungal mutualism, such that the fitness benefits of endophyte symbiosis are maximized at the range edge.
 - 2. We hypothesized that fungal growth in planta varied from range core to range edge. If endophyte growth is limited by host photosynthesis, then environments that are stressful for hosts may correspond to poor endophyte growth. Alternatively, if active regulation by the host is required to keep symbionts "in check", then environments that are stressful for hosts may correspond to high endophyte growth.

Materials and methods

Study species

Elymus virginicus (Poaceae) is a cool season perennial grass native to woodland and prairie habitats of eastern North America (Shaw, 2011). The westernmost range limits of this species correspond to the longitudinal aridity gradient in the central and southern Great Plains (fig. 1). Throughout its range, the species is symbiotic with the seed-transmitted fungal endophyte (Epichloë spp.) (Rudgers and Swafford, 2009). Across natural populations in Texas, endophyte prevalence (fraction of plants that are endophyte-symbiotic) in Elymus virginicus ranged from 10% to 100%, with a mean of 53% (Sneck et al., 2017). Fungal genotyping indicated that the endophytes are capable of synthesizing secondary compounds such as peramine, loline, and ergot alkaloids, which may confer resistance against drought and herbivory (Beaudry, 1951). In addition, the species is capable of both self-pollination and outcrossing (Church, 1958).

² I need to update these hypotheses by adding the herbivory effect

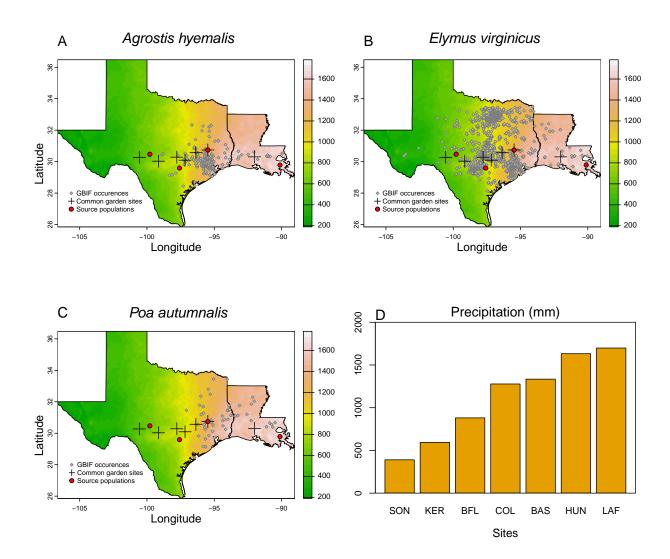


Figure 1: Distribution of common garden sites across the longitudinal aridity gradient in the central and southern Great Plains. Red dots represent the locations of source populations, while grey dots represent the GBIF locations of the species across the study area.

Study design

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Experimental Design. To understand the demographic effects of endophyte symbiosis from core to edge of the host range, we established common gardens at 7 sites across the geographic range of Elymus virginicus (fig. 1). Experimental sites spanned an aridity gradient (temperature gradi-

ent). Common gardens were established in 8 plots per site. Plots were 1.5m * 1.5m and the area was tilled of existing vegetation to control for native plant competition. Plots were also selected in shaded areas under tree canopy or near shrubs to mimic the natural environmental of the 81 species. In each plot, we planted 15 individuals of E. virginicus approximately 15 cm deep in an evenly spaced 4*4 grid pattern, with positions randomly assigned. For each plot, we randomly 83 assigned a starting endophyte frequency (80%, 60%, 40%, 20%)³ and herbivory treatment (herbi-84 vores exclusion and herbivores accessibility). We ensured that all plots had comparable quantities 85 of source populations. After establishing the plots, we watered the plants and recorded initial tiller counts, flowering status and plot position, endophyte status, source population of each in-87 dividual plant. For herbivory exclusion plots, we enclosed them with 1.2m tall mesh fencing to prevent browsing by vertebrate herbivores and sprayed the plots with insecticide. For herbivores accessibility plots (control treatment), we half enclosed the plots with the mesh netting. We stationed one HOBO MX2307 data logger at each site to collect temperature and volumetric water 91 content in the soil every hour.

Source populations and Identification of individual endophyte status. Plants used in the common gar-93 den experiment were derived from natural populations throughout the native range in the southcentral US (fig.1, Table X^4). At each of these natural populations we collected seeds. Some of the 95 seeds of E. virginicus were heat treated to produce endophyte negative plants (E^-) . To do so, we placed these seeds in a drying oven set at 60°C for approximately five days (120 hours). While 97 this method eliminates the endophytes from all individuals, it does not affect seed viability. All 98 seeds (both heat-treated and non-heat-treated) were planted in the Rice University greenhouse. Seedlings were regularly fertilized every two weeks. The seedlings were then vegetatively prop-100 agated to produce enough individuals for your experiment (N = 840). Before planting in the 101 field, we confirmed the endophyte status (E^+ or E^-) of all seedlings using either microscopy or 102 an immunoblot assay. This was necessary due to the varying success of the heat treatment and 103

³Do we need a schematic of one replicate of the experimental design?

⁴We need this table in the Appendix

differences in the prevalence of endophytes between the natural populations. Leaf tissues were stained with aniline blue lactic acid and viewed under a compound microscope at 200x-400x to identify fungal hyphae. The immunoblot assay (Phytoscreen field tiller endophyte detection kit, Agrinostics Ltd. Co.) uses monoclonal antibodies that target proteins of Epichloë spp. and chromagen to visually indicate presence or absence. Both methods yield similar detection rates.

109 Climatic data

To characterize the stress gradient with respect to climatic conditions, we collected the hourly temperature and soil moisture at each site using the HOBO MX2307 data loggers. We used this hourly variable to calculate the daily mean temperature (°C) and soil moisture (%)(fig. 3). We calculated the mean soil moisture and the coefficient of variation from the time the plants were placed on the ground to the time we collected demographic data⁵. The coefficient of variation of soil moisture was estimated to capture season variability in climatic data (Medvigy and Beaulieu, 2012; Meshram et al., 2017).

Demographic data

We collected demographic data including survival, growth, and reproduction during June 2023, which coincided with the flowering season of *E. virginicus*. On each individual, survival of plants was recorded as a binary (death or alive) and the size of the plant was recorded as the number of living tillers, indicated by the presence of green coloration. We recorded the number of inflorescences per plant and the number of spikelets on up to three inflorescences from three reproducing plants. We limited the spikelets count to three reproducing tillers per plot due to the time consuming nature of this measurement process. We used the number of spikelets for these three tillers to estimate the number the average number of spikelets per plants.

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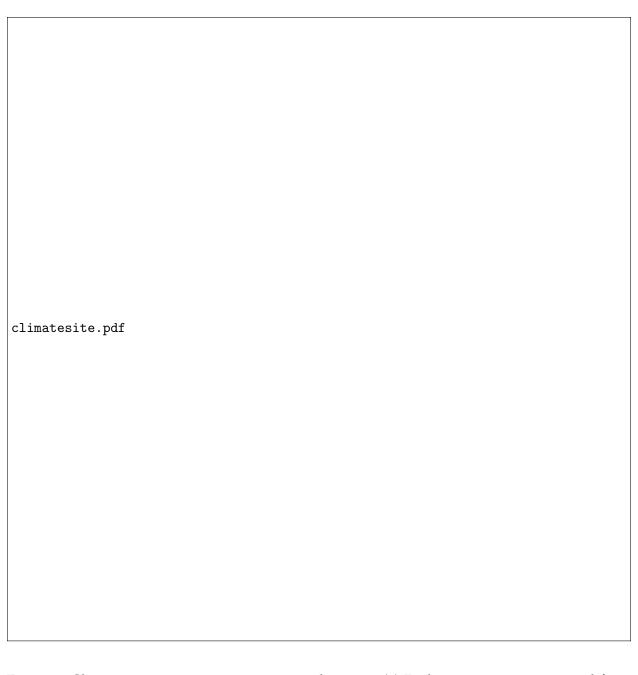


Figure 2: Climate variation across common garden sites. (a) Daily temperature, estimated from average hourly data collected by HOBO data loggers. (b) Daily soil moisture, estimated from average hourly data collected by HOBO data loggers.

Models building and models selection

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To assess how stress associated with aridity affect plant-fungal mutualism, we developed four candidates models for each vital rate (survival, growth, flowering, fertility). Each vital rate was

modeled with the grand mean intercept (β_0), slopes for variation in each covariate ($\beta_1...\beta_3$) as well 129 as the interaction between covariates ($\beta_4...\beta_6$): Each model includes normally distributed random 130 effects for site-to-site variation ($\phi \sim N(0, \sigma_{site})$), plot to plot variation ($\rho \sim N(0, \sigma_{site})$), and 131 source-to-source variation that is related to the provenance of the transplants used to establish 132 the common garden ($\omega \sim N(0, \sigma_{source})$) (Eq.1). 133

$$model1 = \beta_{0} + \beta_{1}T_{mean} + \beta_{2}E + \beta_{3}H + \beta_{4}E * T_{mean} + \beta_{5}H * E + \beta_{6}H * T_{mean} + \phi + \omega + \rho$$

$$model2 = \beta_{0} + \beta_{1}T_{CV} + \beta_{2}E + \beta_{3}H + \beta_{4}E * T_{CV} + \beta_{5}H * E + \beta_{6}H * T_{CV} + \phi + \omega + \rho$$

$$model3 = \beta_{0} + \beta_{1}M_{mean} + \beta_{2}E + \beta_{3}H + \beta_{4}E * M_{mean} + \beta_{5}H * E + \beta_{6}H * M_{mean} + \phi + \omega + \rho$$

$$model4 = \beta_{0} + \beta_{1}M_{CV} + \beta_{2}E + \beta_{3}H + \beta_{4}E * M_{CV} + \beta_{5}H * E + \beta_{6}H * M_{CV} + \phi + \omega + \rho$$

$$(1)$$

We modeled survival using a Bernoulli distribution, growth with a Gaussian distribution, 134 flower with a negative binomial and fertility (number of spikelet) with a negative binomial dis-135 tribution. To check whether the fitted models are compatible with the observed data, we used the posterior predictive checks (Berkhof et al., 2000; Gelman et al., 2000). All models do a good job of capturing relevant aspects of the data, such as means, standard deviations, and quantiles (fig.A1, fig.A2, fig.A3, fig.A4). 139

To select the best model for each vital rate, we compared the four models using the leaveone-out cross-validation (LOOCV)⁶ (Vehtari et al., 2017). LOOCV combines both validation and training methods. In this approach, one observation is used for validation while the training set consists of n-1 observations. This process is repeated for each observation, resulting in n estimated models (Silva and Zanella, 2024). The estimate of test error from LOOCV is calculated by averaging the errors across these n models (Eq.2).

$$CV_n = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$
 (2)

All models were performed in R (R Core Team, 2023) and Stan (Stan Development Team, 146 2024). 147

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⁶I need to add something about difference in models

148 Results

Table 1: Candidate models of *E. virginicus* vital rates (growth, flowering, spikelet and survival).

Vital rate Model ∆elpd ∆se Survival model3 0.0 0.0 Survival model2 -0.5 0.5 Survival model4 -0.9 0.9 Survival model1 -2.2 1.9 Growth model2 0.0 0.0 Growth model3 -0.3 0.4 Growth model3 -0.3 0.4 Flowering model2 0.0 0.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2 Spiket model4 -1.2 1.2				
Survival model2 -0.5 0.5 Survival model4 -0.9 0.9 Survival model1 -2.2 1.9 Growth model2 0.0 0.0 Growth model4 0.0 0.8 Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Vital rate	Model	Δelpd	Δse
Survival model4 -0.9 0.9 Survival model1 -2.2 1.9 Growth model2 0.0 0.0 Growth model4 0.0 0.8 Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Survival	model3	0.0	0.0
Survival model1 -2.2 1.9 Growth model2 0.0 0.0 Growth model4 0.0 0.8 Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Survival	model2	-0.5	0.5
Growth model2 0.0 0.0 Growth model4 0.0 0.8 Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Survival	model4	-0.9	0.9
Growth model4 0.0 0.8 Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model4 -4.3 1.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Survival	model1	-2.2	1.9
Growth model3 -0.3 0.4 Growth model1 -0.4 0.4 Flowering model2 0.0 0.0 Flowering model4 -4.3 1.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Growth	model2	0.0	0.0
Growthmodel1-0.40.4Floweringmodel20.00.0Floweringmodel4-4.31.0Floweringmodel3-6.51.4Floweringmodel3-6.51.4Spiketmodel20.00.0Spiketmodel3-0.50.6Spiketmodel1-0.71.2	Growth	model4	0.0	0.8
Floweringmodel20.00.0Floweringmodel4-4.31.0Floweringmodel3-6.51.4Floweringmodel3-6.51.4Spiketmodel20.00.0Spiketmodel3-0.50.6Spiketmodel1-0.71.2	Growth	model3	-0.3	0.4
Flowering model4 -4.3 1.0 Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Growth	model1	-0.4	0.4
Flowering model3 -6.5 1.4 Flowering model3 -6.5 1.4 Spiket model2 0.0 0.0 Spiket model3 -0.5 0.6 Spiket model1 -0.7 1.2	Flowering	model2	0.0	0.0
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Spiketmodel20.00.0Spiketmodel3-0.50.6Spiketmodel1-0.71.2	Flowering	model3	-6.5	1.4
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Spiket model1 -0.7 1.2	Spiket	model2	0.0	0.0
1	Spiket	model3	-0.5	0.6
Spiket model4 -1.2 1.2	Spiket	model1	-0.7	1.2
	Spiket	model4	-1.2	1.2

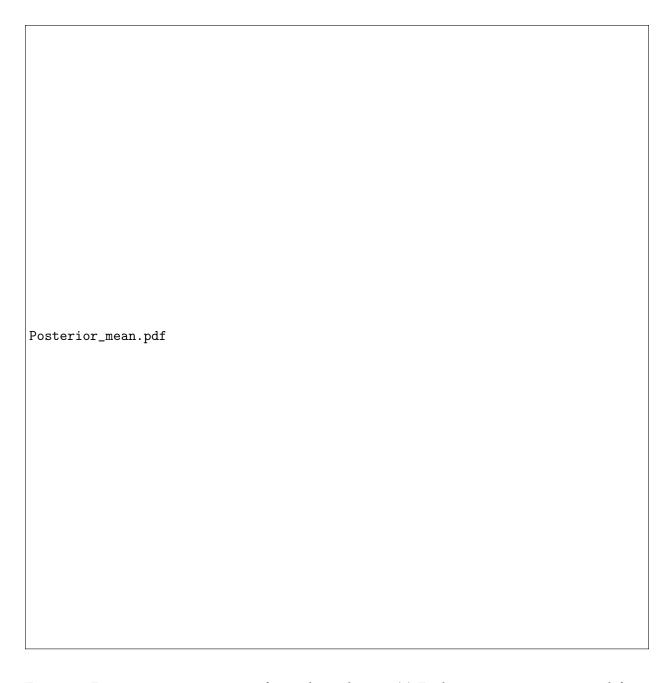


Figure 3: Posterior mean estimates for each vital rate. (a) Daily temperature, estimated from average hourly data collected by HOBO data loggers. (b) Daily soil moisture, estimated from average hourly data collected by HOBO data loggers.

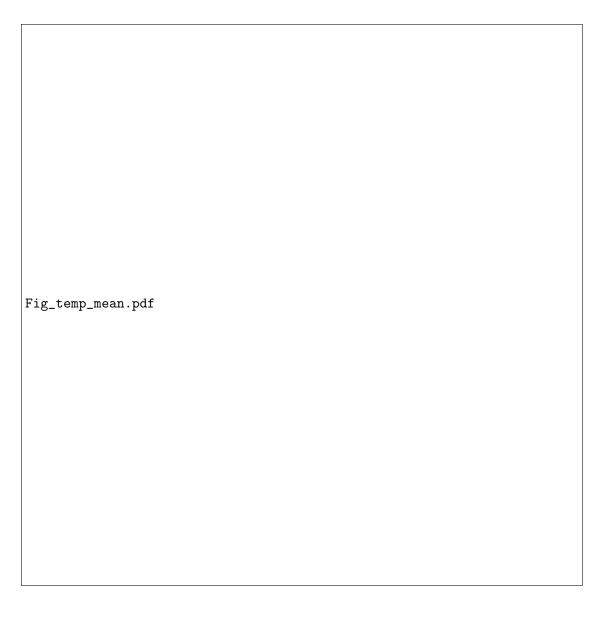


Figure 4: Variation in vital rates across a temperature gradient.

Acknowledgments

Statement of Authorship

Data and Code Availability

Appendix A

Figure A1: Comparison of the observed survival data with the posterior predictions from the survival models for each climate variable

Figure A2: Comparison of the observed growth data with the posterior predictions from the growth models for each climate variable

Figure A3: Comparison of the observed spikelet data with the posterior predictions from the spikelet models for each climate variable

Figure A4: Comparison of the observed flowering data with the posterior predictions from the flowering models for each climate variable

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