

## 1.0 Introduction

**Well Ordering Principle:** Every nonempty set  $S$  of non-negative integers contains a least element; that is there is some integer  $a$  in  $S$  such that  $a \leq b$  for all  $b$ 's belonging to  $S$

**Theorem 1.1:** Archimedian property. If  $a$  and  $b$  are any positive integers, then there exists a positive integer  $n$  such that  $na \geq b$ .

**Theorem 1.2** First Principle of Finite Induction. Let  $S$  be the set of positive integers.

- (a) The integer 1 belongs to  $S$
- (b) Whenever the integer  $k$  is in  $S$ , the next integer  $k + 1$  must also be in  $S$

**Theorem 1.2** Second Principle of Finite Induction. Let  $S$  be the set of positive integers.

- (a) The integer 1 belongs to  $S$
- (b') If  $k$  is a positive integer such that  $1, 2, \dots, k$  for  $k \in S$ , then  $k + 1$  must also be in  $S$ .

Thus  $S$  is the set of all positive integers.