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## Using Meta-analytic Structural Equation Modeling to Study Developmental Change in Relations Between Language and Literacy

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The purpose of this review was to introduce readers of *Child Development* to the meta-analytic structural equation modeling (MASEM) technique. Provided are a background to the MASEM approach, a discussion of its utility in the study of child development, and an application of this technique in the study of reading comprehension (RC) development. MASEM uses a two-stage approach: first, it provides a composite correlation matrix across included variables, and second, it fits hypothesized a priori models. The provided MASEM application used a large sample ( $N = 1,205,581$ ) of students (ages 3.5–46.225) from 155 studies to investigate the factor structure and relations among components of RC. The practical implications of using this technique to study development are discussed.

Meta-analysis is not a new technique in the study of child development, particularly as related to educational research. Indeed, Gene Glass (1976) first coined the term meta-analysis: “[meta-analysis is] a rigorous alternative to the causal, narrative discussions of research studies which typify our attempts to make sense of the rapidly expanding research literature” (p. 3). In education, meta-analyses have pooled effect sizes from studies examining the effectiveness of programs designed for struggling readers (e.g., Lee & Tsai, 2017; Wanzek, Wexler, Vaughn, & Ciullo, 2010), the effects of vocabulary training on reading comprehension (RC; e.g., Elleman, Lindo, Morphy, & Compton, 2009), and the effectiveness of spelling instruction (e.g., Graham & Santangelo, 2014), to name only a few.

Meta-analysis is not limited to the pooling of effect sizes like Hedge’s  $g$  or Cohen’s  $d$  and can also be used to pool correlation coefficients across studies. For example, recent correlational meta-analyses involving reading skills have considered rapid naming ability and reading (Araújo, Reis, Petersson, & Faisca, 2015), word decoding and RC (García & Cain, 2014), and second language correlates of RC (e.g., Jeon & Yamashita, 2014). However, these studies investigated the univariate relations between one predictor and one outcome (or in the case of Jeon & Yamashita, multiple-univariate analyses). These studies, particularly Jeon and Yamashita (2014), are missing valuable information provided by correlations that were unmeasured in a univariate meta-analysis framework.

Education researchers can use meta-analytic techniques and a structural equation modeling (SEM) framework to test multivariate models using a multivariate framework to address the limitations of univariate methods (e.g., Becker & Schram, 1994; Viswesvaran & Ones, 1995). The purpose of this article was to introduce the multivariate meta-analytic

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SEM (MASEM) approach, to discuss its usefulness in the study of child development, and to apply MASEM to the study of a multivariate skill (RC).

### *MASEM: A Primer*

In a univariate approach, each element of a correlation matrix is treated as independent within a study, and correlations are thus pooled separately (e.g., Araújo et al., 2015; García & Cain, 2014). Becker (2000, 2009) proposed a model-based meta-analysis approach: a pooled correlation matrix is estimated under a random effects model, and variation between studies is included in the confidence intervals of the estimates. The relations among variables that considers their covariances can be estimated through multiple-regression models (Becker, 2000, 2009). This generalized least squares (GLS) approach extended univariate meta-analysis, but resulted in the question: How do you choose an appropriate sample size for these analyses? Does one choose the average sample size, the harmonic mean of sample sizes, or another option?

Cheung and Chan (2005) extended the GLS method to a two-stage SEM (TSSEM) approach to address the question of choosing a sample size. TSSEM uses multiple-group SEM to pool correlation matrices in the first stage, and then uses weighted least squares (WLS) estimation in fitting the a priori proposed SEM(s) in the second stage. Using WLS, the sampling covariance matrix is used to assign different weights to the correlation matrix cells depending on their precision (i.e., the size of their variances). Thus, there is no need to decide on one sample size to use for the estimation of model effects (Cheung, 2015b).

### *The Utility of MASEM in the Study of Child Development*

The number of effect sizes reported in primary studies can vary greatly, as researchers have different research questions and use different methods and samples to answer them. Multivariate approaches are exceptionally useful for education researchers, as the types of curricula, minutes or hours spent teaching various subjects, and even classroom environments are different across schools, districts, and states. The usefulness of MASEM is further emphasized by the increasing use of latent variables to extract common variance across similar, but separately norm-referenced educational tests. One example is a recent extension of the direct and inferential mediated effects (DIME) model of RC (Cromley & Azevedo, 2007). The DIME model defines direct and indirect pathways

between vocabulary, decoding, background knowledge, inference, strategy usage, and RC using single manifest measures. Ahmed et al. (2016) extended the DIME model using multiple measures of each construct to create latent variables in a large sample of students, thus extracting the common variance among similar measures to create a more reliable model of RC. Multivariate MASEM aims to increase the reliability of correlational meta-analyses in a similar manner that the inclusion of latent variables brought to path analyses.

### *MASEM Application: Component Skills of RC*

RC is vital for educational attainment (National Center for Education Statistics, 2013). According to the Simple View of Reading (SVR; Gough & Tunmer, 1986; Hoover & Gough, 1990), skilled RC is the product of sufficient decoding and linguistic comprehension skills. Both decoding and linguistic comprehension are necessary for RC, but each component alone is not sufficient. Decoding, or word recognition, is the ability to interpret printed letters and words using the alphabetic principle (Adams, 1990) and to transform them into their phonetic code (Perfetti, 1985). Fluent and accurate decoding, at the word level and in the context of sentences or passages, facilitates RC (LaBerge & Samuels, 1974). Linguistic comprehension includes oral language skills such as listening comprehension and vocabulary knowledge. Listening comprehension is the ability to interpret the meaning of oral lexical information (Gough & Tunmer, 1986), and makes significant contribution to RC ability above word reading (Kim, 2015). Vocabulary knowledge is one of the most important predictors of RC (Anderson & Freebody, 1981; Beck & McKeown, 1991; Ouellette, 2006) and accounts for a large proportion of variance in listening comprehension ability at kindergarten (Florit, Roch, & Levorato, 2013, 2014). Vocabulary knowledge is also important for word recognition and facilitates reading (Chiappe, Chiappe, & Gottardo, 2004; Metsala & Walley, 1998). Failures in either decoding (i.e., reading impairment) or linguistic comprehension (i.e., language impairment) can result in delayed or impaired comprehension of written text (Gough & Tunmer).

Other important predictors of RC that were not explicitly included in the original SVR include background knowledge, working memory, and reasoning and inference skills. Background knowledge affects RC (e.g., Dole, Valencia, Greer, & Wardrop, 1991; Spire & Donley, 1998), and more strongly facilitates RC as a reader ages (Evans, Floyd,

McGrew, & Leforgee, 2001). Second, working memory (see Baddeley, Eysenck, & Anderson, 2009, for a review; Baddeley, 1992) is a foundational cognitive skill that supports comprehension monitoring and inference making (e.g., Oakhill, Hartt, & Samols, 2005) and is an important predictor of RC (Cain, Oakhill, & Bryant, 2004; Seigneuric & Ehrlich, 2005; Swanson & Berninger, 1995). Third, reasoning skills are important for understanding spoken language, and verbal and nonverbal reasoning tasks are significantly correlated with reading (Pammer & Kevan, 2007). Inference uses background knowledge to interpolate or extrapolate missing information and is important for RC (Cain et al., 2004; Kendeou, Bohn-Gettler, White, & Van Den Broek, 2008; Oakhill & Cain, 2012; Tompkins, Guo, & Justice, 2013; Yuill & Oakhill, 1988). In contrast to the SVR, other multivariate models of RC such as the multicomponent view of reading (Cain, 2009; Cain et al., 2004), the DIME model (Cromley & Azevedo, 2007), the verbal efficiency theory (Perfetti, 1985), and the construction-integration model (Kintsch, 1988) provide evidence for the inclusion background knowledge, working memory, and reasoning and inference as separate from or in addition to the original SVR components.

### *This Study*

Within the present application, we used the two-stage MASEM approach to analyze the correlations between common components of RC to answer the following questions:

1. What are the meta-analytic correlations between RC and its predictors?
2. What is the factor structure of the hypothesized predictors, and how much variance do these factors account for in RC?
3. Are there differences in the model structure or relations between younger and older children?

## **Method**

### *Literature Base*

We used a multistep process to identify relevant articles. The original literature search was conducted on March 25, 2015; it was then updated on April 3, 2016.

### *Search Criteria*

Using PsycINFO, ProQuest (Dissertations and Theses), and the Education Resources Information

Center (ERIC), a primary search of the literature was conducted to identify studies that included *one* of the following phrases in the title of the document: *reading comprehension* OR *text comprehension* OR *simple view of reading* OR *simple view*. To ensure retrieval of empirical studies, the abstract must have also contained *predict\** or *develop\** or *assoc\** OR *relat\** OR *depend\** OR *connect\** OR *occur\** (the asterisk is to denote all extensions of the word are acceptable, e.g., prediction, development). All studies must have been published from 1990 on, as methods for teaching reading and measuring reading ability differed substantially prior to this time. Additionally, studies must have had one or more key words related to the predictor variables as a subject (e.g., *decoding*, *working memory*, *background knowledge*, *vocabulary knowledge*).

We identified 4,258 articles using these criteria; 2,404 studies after removing duplicate sources (1,350 from PsycINFO and ProQuest and 1,054 from ERIC). Due to issues with retrieval, the total number of studies subjected to exclusionary criteria was reduced to 1,815.

### *Exclusion Criteria*

Exclusionary criteria were applied in two steps. Within the first step, the titles of the articles were screened for three exclusionary criteria (see Figure 1): special population status (e.g., traumatic brain injury, autism spectrum disorder, intellectual disability, hearing or vision impairments), being unrelated to the meta-analysis (e.g., nonempirical, single-case studies, corrigendum, commentaries), or English language learners (ELL) or foreign language populations. We excluded studies with ELL samples because the relations between decoding and comprehension can be affected by transfer effects across languages (García & Cain, 2014), and foreign language populations were excluded because different writing systems may produce different relations between the included variables (Florit & Cain, 2011). An additional 212 studies could not be retrieved from the server. Applying these exclusionary criteria to the titles resulted in the exclusion of 1,117 total studies (see Figure 1).

We consulted the full texts of the remaining 1,287 studies to determine eligibility for analysis using the following criteria. Studies must have measured individual constructs (i.e., no composite scores) and measures must have been collected within the same year (i.e., only concurrent correlations). Studies must have had a correlation

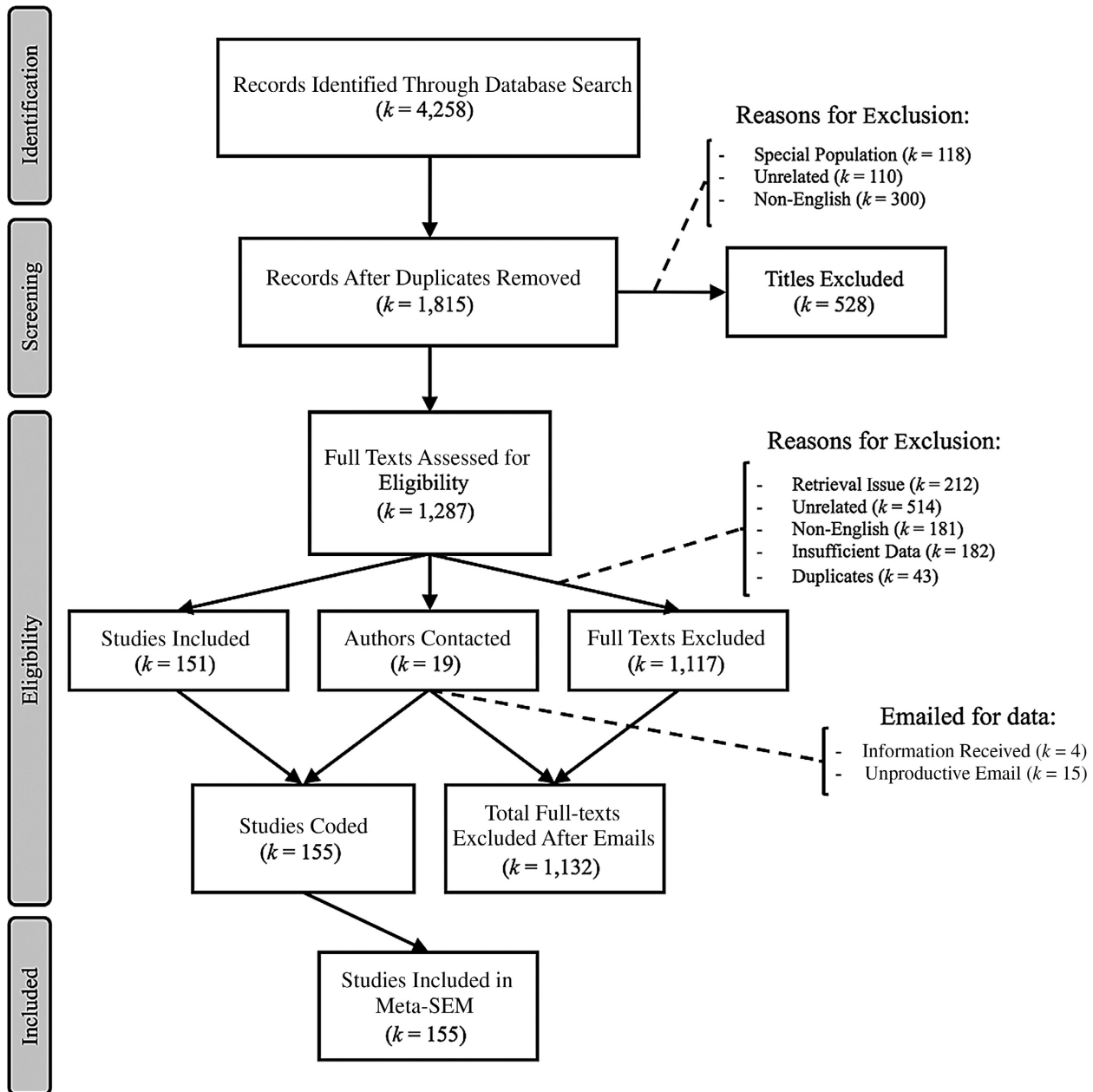


Figure 1. Flow chart of the record screening process. Reasons for exclusion are included in brackets to the right of the excluded boxes.

coefficient between a measure of RC and at least one predictor variable, and must have met the exclusionary criteria applied to the article titles that may have been missed during the first step. The authors of 19 of 182 studies with insufficient data could be contacted, but 15 could no longer provide the data. In total  $k = 155$  studies, denoted with asterisks within the References (references used in the study that were not cited in text are included in Appendix S1 to preserve space), were included in the present analyses.

#### Moderator Variables

Both average age of the sample and reader ability status (e.g., reading or learning disability, typical readers) were coded. While there was enough information to group the correlation matrices by average age, there was not enough information to create full composite correlation matrices separately for the typical sample of readers and for readers with learning or reading disabilities. As such, we conducted moderator analyses using only average age.



### *Coding Scheme*

Each study was coded for the following information: Study name and year, sample size of students, age, reader status (e.g., reading disability, typical readers), and available correlations between RC and the eight predictor variables (word reading accuracy, word reading fluency, text reading fluency, vocabulary knowledge, listening comprehension, background knowledge, reasoning and inference, and working memory). Where correlations were missing from a study, we left the cell blank, and still included any available information in the coding scheme. Multivariate MASEM allows for missing correlations to be handled in the missing at random (MAR) framework when the correlation matrix is estimated in the first stage of the MASEM. This allows models to be fit using maximum likelihood estimation methods (Cheung, 2015b; Enders, 2010). If a cell had more than one correlation, we adopted the method used by the National Reading Panel (National Institute of Child Health and Human Development [NICHD], 2000) by averaging the effect sizes together. See Appendix S2 for a discussion on model robustness and correlation coverage across the included matrices.

### *Reliability of Coding*

To assess reliability, a graduate student independently coded 20 of the identified studies to establish acceptable interrater reliability. The mean kappa was .94 (.82–1) for the matrices, 1 for age, .95 for reader ability designation, and 1 for sample size.

### *Meta-analytic Structural Equation Models*

#### *Fixed Versus Random Effects Models*

It was reasonable to expect that there were study-specific differences in correlations due to variations in samples, measures, and study designs. As such, a random effects model was adopted. Additionally, a random effects model allows for the generalization of findings to be outside of the studies used in a meta-analysis. The R package metaSEM (Cheung, 2015a) provides a TSSEM method to first calculate the sampling covariance matrix of the correlations and to estimate a pooled correlation matrix. The second stage of the TSSEM analyzes the pooled correlation matrix according to the user's hypothesized models. Using metaSEM, the  $I^2$  statistic was estimated to quantify heterogeneity in correlations using the Q test of homogeneity (see Cheung, 2015b). After creating the pooled correlations using the first step,

the estimated values of the Stage 1 results were treated as sample statistics in the Stage 2 analysis.

### *Hypothesized A Priori Models*

Structural models fit using metaSEM differ from traditional SEMs fit in other programs in several ways. Traditional SEM fitting specifies latent variables to represent common variance across *measures* or *items* of the same construct. In metaSEM, since the data are represented as correlations and not as scores on a particular measure, higher order factors capture the common variance across *constructs*. Therefore, residual variances and disturbance terms in metaSEM represent the amount of variance unaccounted for in the constructs that may be attributable to heterogeneity in sampling and measurement.

### *Confirmatory Factor Analyses*

We first explored the factor structure of the predictor variables before including RC. We fit a two-factor model to test the true SVR (one factor for linguistic comprehension and a second factor for decoding) and a three-factor model with the original two components of the SVR and a separate factor for the cognitive components (working memory and reasoning and inference). We include more information about the fitting of these models, including tests of model fit, in Supporting Information (Appendix S3).

### *RC Model*

A modified version of the SVR was fit to the complete set of matrices ( $k = 214$ ). Three higher order factors were created from the eight predictors: a decoding factor was indicated by word reading fluency, text reading fluency, and word decoding accuracy, a linguistic comprehension factor was indicated by vocabulary knowledge and morphology, listening comprehension, and background knowledge, and a cognitive factor was represented by working memory and reasoning and inference. We then regressed RC onto these three factors.

### *Moderator Analyses*

We used age as a moderator during the fitting of these models. We created two groups: a younger group including samples with average ages below 11 years (below the sixth grade) and an older group including samples with average ages at or above 11 years (at or above Grade 6). We applied this method due

issues with variable coverage in the correlation matrix (explained in detail in the Results section).

### *Model Fit*

We assessed model fit with the chi-square test of model fit, the confirmatory fit index (CFI), the standardized root mean square residual (SRMR), and the root mean square error of approximation (RMSEA) and its confidence interval. Maximized CFI values ( $> .95$ ), minimized RMSEA and SRMR values ( $< .08$ ), and a low ratio of the chi-square value to its degrees of freedom ( $\leq 2$ ) were preferred (Kline, 2016).

## **Results**

### *First Stage Results*

#### *Descriptive Statistics*

Table 1 contains the results of the first stage of the TSSEM approach. Correlations (presented in the bottom half of Table 1) between the nine predictor variables ranged from low to moderate (.265–.695). The correlation between word reading fluency and listening comprehension was homogenous ( $I^2 = .000$ ). A homogenous correlation indicates that the relation between word reading fluency and listening comprehension was captured in a similar way across the studies that included these variables. All other correlations were heterogeneous across studies ( $I^2s > .82$ , see the top half of Table 1). The average sample size across all included studies was  $n = 5,530$ . The harmonic mean sample size was  $n = 114$ . A total of  $N = 1,205,581$  participants from  $k = 155$  studies were included in the present meta-analysis. The average age for the participants was 12.533 years (range: 3.5–46.225).

#### *Second Stage Results*

The three-factor model of RC was fit to the Stage 1 results of the TSSEM approach. This model provided excellent fit to the data,  $\chi^2(20) = 61.4902$ ,  $p < .001$ , CFI = .9969, RMSEA = .0012 [.0009, .0016], SRMR = .0310. Figure 2 includes the path coefficients and factor loadings. The loadings of word reading fluency ( $\lambda = .702$ ,  $p < .001$ ), decoding accuracy ( $\lambda = .785$ ,  $p < .001$ ), and text reading fluency ( $\lambda = .865$ ,  $p < .001$ ) were all significant and positive, indicating that the latent construct of decoding captured significant common variance across the included studies. A similar pattern of loadings for vocabulary knowledge ( $\lambda = .766$ ,  $p < .001$ )

background knowledge ( $\lambda = .676$ ,  $p < .001$ ), and listening comprehension ( $\lambda = .641$ ,  $p < .001$ ) were estimated, indicating that the construct of linguistic comprehension was also capturing significant common variance between these three indicators.

The standardized regression pathways from the higher order factors of linguistic comprehension ( $\beta = .394$ ,  $p < .001$ ) and decoding ( $\beta = .283$ ,  $p < .001$ ) were significant and positive. For every 1 *SD* increase in linguistic comprehension and in decoding, RC increased by .394 and .283 *SD* units, respectfully. After accounting for individual differences in decoding and linguistic comprehension, the factor that included the cognitive components (working memory and reasoning and inference) did not account for significant additional variance in RC ( $\beta = .137$ ,  $p = .129$ ). Approximately 56.8% of the variance in RC was accounted for by this model ( $R^2 = 1 - d$ ).

#### *Moderator Analyses*

The first stage of the TSSEM approach was used to create separate composite correlation matrices for these two groups. The expanded SVR model was then fit separately to these matrices in the second stage. To create two groups of matrices according to age, we dichotomized age at 11 years. This dichotomization represents children in approximately fifth grade and below for the younger sample (average age = 8.76 years, range = 3.5–10.67) and approximately sixth grade and older for the older sample (average age = 16.80, range = 11.0–46.23).

#### *Younger Sample*

The composite correlation matrix and heterogeneity estimates for the younger children are contained in Table 2. Correlations ranged from low to moderately high (.278–.740). Three correlations were homogenous (denoted in bold in Table 2). During the first stage model fitting, it was discovered that there was not enough information across the included studies ( $k = 79$ ) to estimate the meta-correlations for background knowledge. The first stage model failed to converge. For the purposes of this portion of the meta-analysis, background knowledge was removed from the models for the younger cohort.

The two-factor model provided excellent fit to the data,  $\chi^2(18) = 31.0251$ ,  $p = .0285$ , CFI = .9985, RMSEA = .0012 [.0004, .0018], SRMR = .0347. Increasing the model complexity to create three factors did not improve model fit (see Appendix S3, Table C2). Figure 3 presents the path coefficients for this model. Both the linguistic comprehension

Table 1  
Correlations and Heterogeneity Statistics for the Nine Included Constructs

Construct	1	2	3	4	5	6	7	8	9
1. RC	—	.988	.989	.992	.986	.980	.978	.963	.982
2. WRF	.475	—	.990	.990	.975	<b>.000</b>	.823	.945	.983
3. TRF	.581	.695	—	.991	.990	.934	.973	.966	.989
4. DA	.540	.588	.579	—	.977	.971	.988	.972	.977
5. V/M	.553	.411	.520	.480	—	.987	.986	.980	.992
6. LC	.495	<b>.316</b>	.401	.365	.482	—	.963	.982	.949
7. R/I	.452	.265	.392	.339	.403	.386	—	.985	.990
8. WM	.336	.286	.349	.327	.331	.331	.350	—	.976
9. BGK	.471	.381	.417	.423	.535	.433	.379	.329	—

Note. Correlations are below the diagonal; heterogeneity statistics are above the diagonal. Bolded values indicate homogenous correlations. RC = reading comprehension; WRF = word reading fluency; TRF = text reading fluency; DA = decoding accuracy; V/M = vocabulary and morphological knowledge; LC = listening comprehension. R/I = reasoning and inference; WM = working memory; BGK = background knowledge.

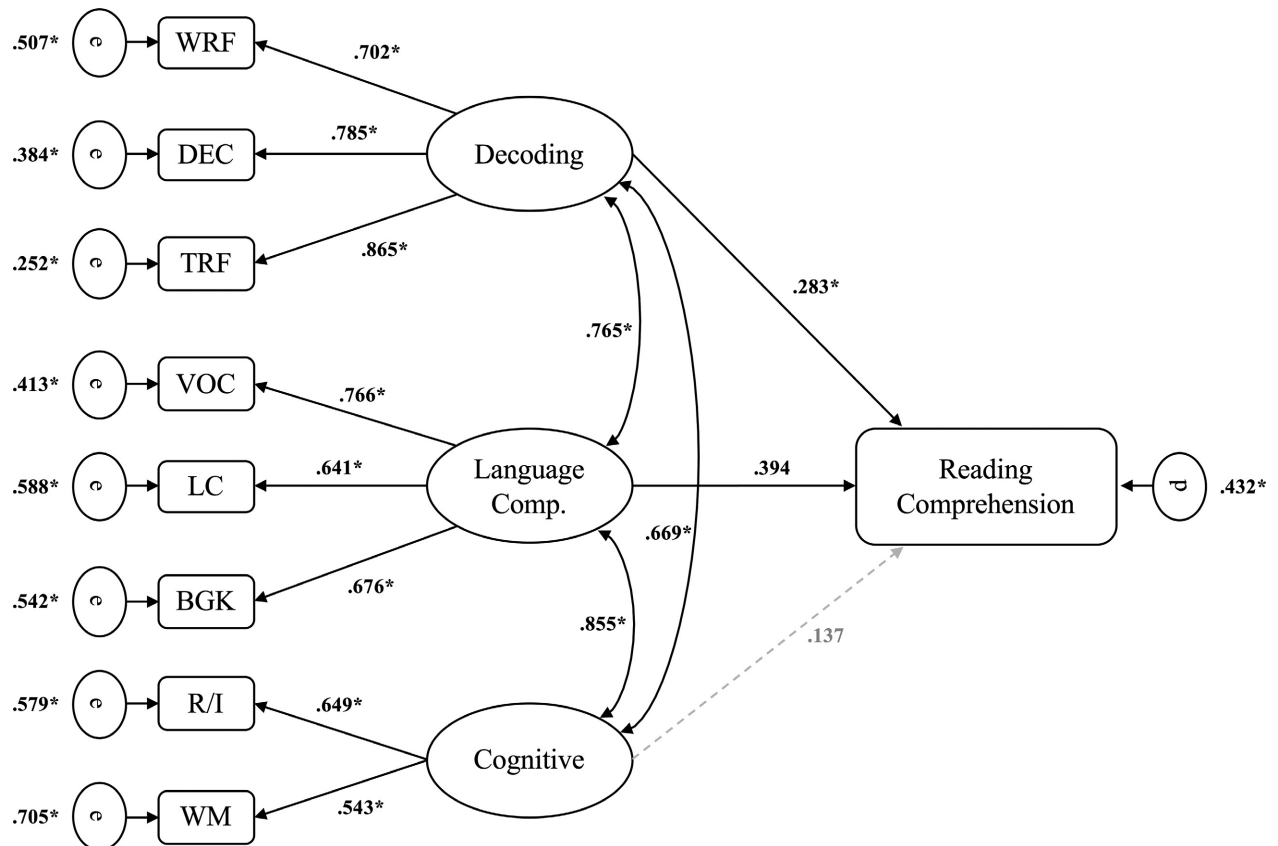


Figure 2. Meta-SEM path diagram for the three-factor model. Dashed, gray pathway is not significant. SEM = structural equation modeling; WRF = word reading fluency; DEC = decoding accuracy; TRF = text reading fluency; VOC = vocabulary knowledge; LC = listening comprehension; BGK = background knowledge; WM = working memory; R/I = reasoning and inference; e = residual variance error terms; d = disturbance term.

\* $p < .001$ .

and decoding factors captured significant common variance across their respective indicators with medium to high loadings ( $\lambda$ s = .511–.877). The

regression pathways from the linguistic comprehension factor ( $\beta = .457$ ,  $p < .001$ ) and decoding factor ( $\beta = .376$ ,  $p < .001$ ) were both significant and

Table 2  
Correlations and Heterogeneity Statistics for the Younger Cohort

Construct	1	2	3	4	5	6	7	8
1. RC	—	.979	.958	.986	.979	.973	.941	.911
2. WRF	.569	—	.984	.988	.984	<b>.000</b>	.946	<b>.000</b>
3. TRF	.621	.740	—	.982	.991	.939	.984	<b>.000</b>
4. DA	.610	.593	.642	—	.968	.972	.986	.881
5. V/M	.542	.450	.533	.470	—	.987	.983	.976
6. LC	.498	<b>.311</b>	.405	.376	.483	—	.967	.970
7. R/I	.480	.278	.412	.360	.398	.412	—	.881
8. WM	.360	<b>.312</b>	<b>.318</b>	.312	.367	.380	.329	—

Note. Correlations are below the diagonal; heterogeneity statistics are above the diagonal. Bolded values indicate homogenous correlations. RC = reading comprehension; WRF = word reading fluency; TRF = text reading fluency; DA = decoding accuracy; V/M = vocabulary and morphological knowledge; LC = listening comprehension; R/I = reasoning and inference; WM = working memory.

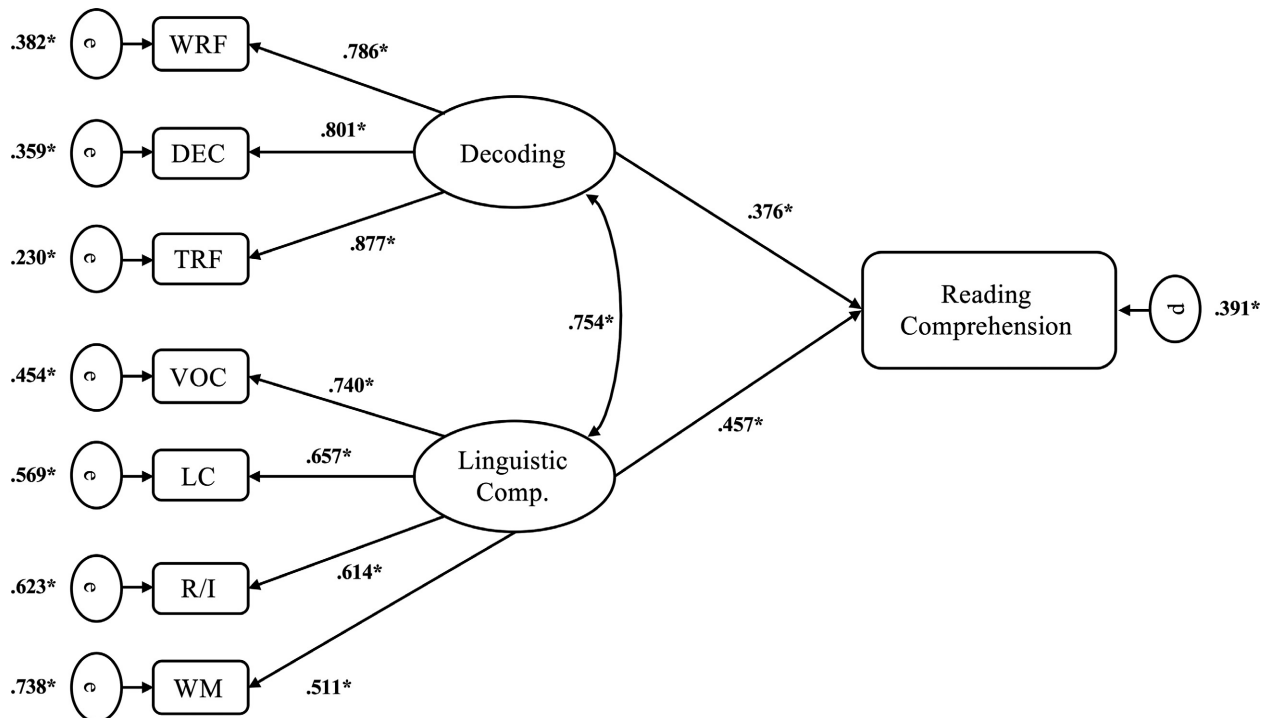


Figure 3. Meta-SEM path diagram for the younger sample. Dashed, gray pathways are not significant. SEM = structural equation modeling; WRF = word reading fluency; DEC = decoding accuracy; TRF = text reading fluency; VOC = vocabulary and morphological knowledge; LC = listening comprehension; WM = working memory; R/I = reasoning and inference; e = residual variance error terms; d = disturbance term.

\* $p < .001$ .

positive, indicating that decoding and linguistic comprehension independently predict variance in RC. These units are standardized: for every 1 *SD* unit increase in linguistic comprehension and in decoding, RC increases by .457 and .376 *SD* units, respectively. The two-factor model accounted for 60.9% of the variance in RC for younger children.

#### Older Cohort

The first stage of the TSSEM was conducted in R on the studies with samples of older children ( $k = 86$ ). The composite correlation matrix and associated heterogeneity statistics for this sample are presented in Table 3. The correlations ranged from



low to moderate ( $r = .243-.596$ ). There were four homogenous correlations (indicated in bold).

The three-factor expanded SVR model provided an excellent fit to the data,  $\chi^2(22) = 53.8364$ ,  $p < .001$ , CFI = .9951, RMSEA = .0015 [.0010, .0020], SRMR = .0451. The results of this model are presented in Figure 4. The loadings of each indicator were moderate to high (range = .641–.844). Linguistic comprehension ( $\beta = .466$ ,  $p < .001$ ) and decoding ( $\beta = .178$ ,  $p < .001$ ) accounted for significant unique variance in RC. For every 1 *SD* increase in linguistic comprehension and in decoding, RC increases by .466 and .178 *SD* units, respectfully. The linguistic comprehension factor accounted for a significantly larger portion of variance in RC than decoding. After accounting for decoding and linguistic comprehension, the cognitive component was not a unique predictor of RC ( $\beta = .135$ ,  $p = .130$ ). The three-factor model accounted for 52.6% of the variance in RC for the older sample.

### Discussion

This study used a relatively new and advanced meta-analytic SEM approach to analyze correlation matrices from 155 studies with over 1 million students. The two-stage modeling approach supported a three-factor model that accounted for 57% of the variance in RC in the full sample. This estimate is similar to other relevant accounts of the SVR (e.g., Hoover & Gough, 1990). Once decoding and linguistic comprehension were accounted for, a cognitive factor made of reasoning and inference and working memory was a separable, but nonsignificant predictor of additional variance in RC. The factor structure

was different across development: For the younger sample of students, the original specifications of the SVR were supported, whereby a two-factor model (decoding and linguistic comprehension) was the best fit to the data and accounted for 60% of the variance in RC. For the older students, the three-factor solution with a separate cognitive factor accounted for approximately 53% of the variance in RC. That we accounted for 50%–60% of the variance in RC is impressive in itself: the portion of variance unaccounted for included error and measurement variance due to differences in samples, measures, and missing constructs.

Our expansion of the SVR was based on similar models of RC that include separate variables for background knowledge, working memory, and reasoning and inference (e.g., Cain, 2009; Cain et al., 2004; Cromley & Azevedo, 2007; Kintsch, 1988; Perfetti, 1985). However, the SVR argues that constructs not specifically relevant for word reading are subsumed under the linguistic comprehension factor. Background knowledge is argued to be a separate predictor important for RC (e.g., Cromley & Azevedo, 2007), but this construct loaded best on the factor for linguistic comprehension. While the SVR posits that constructs such as reasoning and inference and working memory should load on to the linguistic comprehension factor, we only supported this for the younger sample of students. The older sample supported a full three-factor model with a cognitive factor separate from the linguistic comprehension factor. We did not include all of the necessary additional components to compare our models properly to these other relevant models of RC, so our interpretations are limited in scope to the original specifications of the SVR (Gough & Tunmer, 1986; Hoover & Gough, 1990).

Table 3  
*Correlations and Heterogeneity Statistics for the Older Cohort*

Construct	1	2	3	4	5	6	7	8	9
1. RC	—	.963	.990	.992	.987	.981	.984	.971	.981
2. WRF	.394	—	.992	.988	.920	<b>.000</b>	<b>.000</b>	.939	<b>.000</b>
3. TRF	.527	.596	—	.991	.983	.865	.963	.976	.972
4. DA	.438	.589	.522	—	.981	.955	.981	.982	.964
5. V/M	.562	.382	.514	.485	—	.986	.987	.979	.989
6. LC	.494	<b>.313</b>	.393	.346	.477	—	.862	.981	<b>.000</b>
7. R/I	.434	<b>.243</b>	.362	.304	.401	.358	—	.989	.992
8. WM	.324	.272	.363	.336	.316	.292	.352	—	.979
9. BGK	.436	<b>.302</b>	.288	.356	.526	<b>.517</b>	.376	.323	—

*Note.* Correlations are below the diagonal; heterogeneity statistics are above the diagonal. Bolded values indicate homogenous correlations. RC = reading comprehension; WRF = word reading fluency; TRF = text reading fluency; V/M = vocabulary and morphological knowledge; LC = listening comprehension; R/I = reasoning and inference; WM = working memory; BGK = background knowledge.

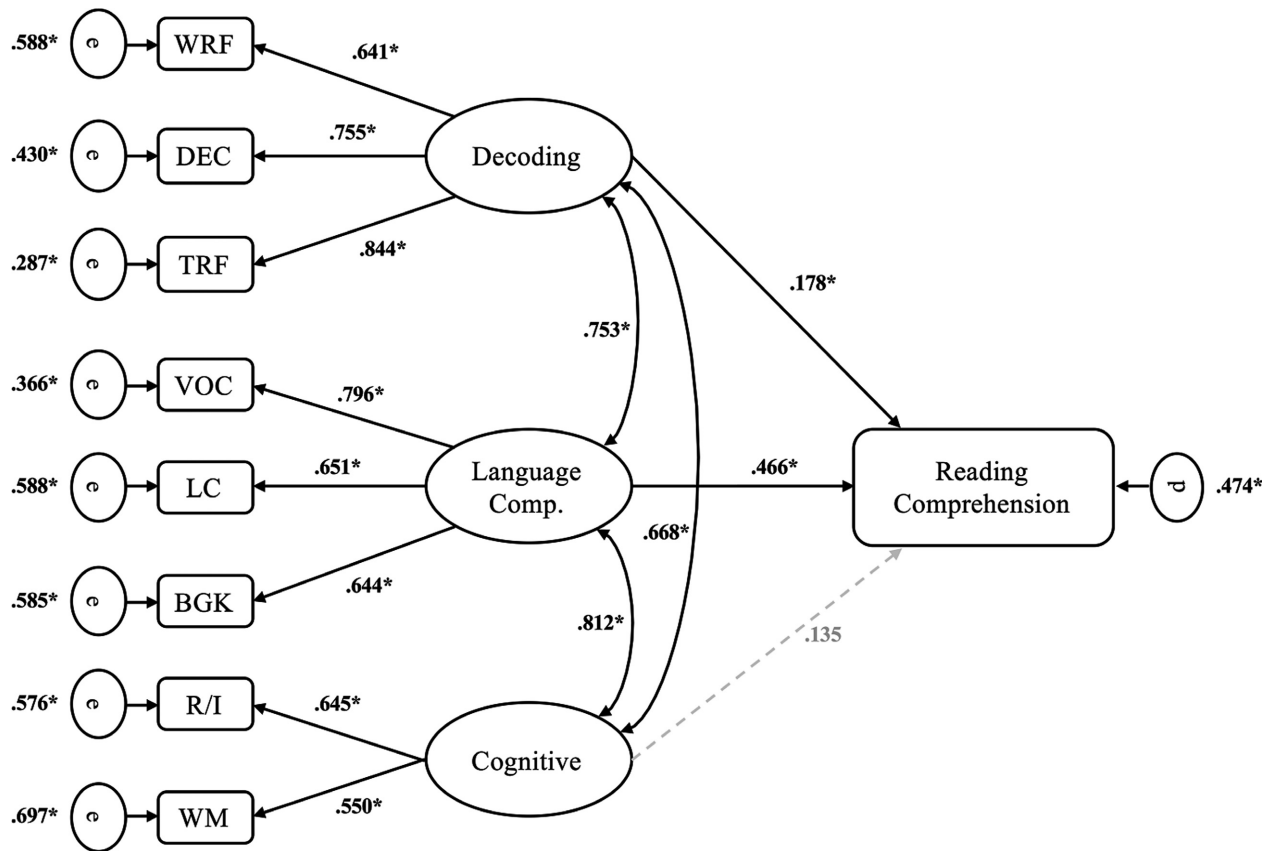


Figure 4. Meta-SEM path diagram of Model 2 for the older sample. Dashed, gray pathways are not significant. SEM = structural equation modeling; WM = working memory; R/I = reasoning and inference; BGK = background knowledge; WRF = word reading fluency; DEC = decoding accuracy; TRF = text reading fluency; VOC = vocabulary knowledge; LC = listening comprehension; e = residual variance error terms; d = disturbance term.

\* $p < .001$ .

### *Strengths of the MASEM Approach*

There are multiple strengths and benefits for researchers who use SEM or meta-analytic approaches and want to incorporate a method that uses both in to their statistical toolbox.

### *Multivariate Approach*

MASEM can be applied in a univariate or multivariate framework. However, the multivariate approach allows a researcher to analyze more than one effect size per study, presenting an increase in information that can be retained from a single study and incorporated in to a large meta-analysis. Similar to the models we fit, researchers can analyze data from correlation matrices across studies to test their theoretical model that provides an estimate of heterogeneity due to differences in measures, samples, and settings. Furthermore, it is possible that researchers from the primary studies

to be included in the analyses are interested in different construct relations. This can present as a missing data issue, whereby Study A may be interested in X related to Y, Study B is interested in Z related to Y, and Study C is interested in the interrelations between X, Y, and Z. Multivariate applications allow for missing correlations to be handled in the MAR framework, so that the models can be fit using maximum likelihood estimation methods (Cheung, 2015b; Enders, 2010). In doing so, researchers do not have to only include studies that measure all variables (Study C) and instead can include all studies that include any of the variables (Studies A, B, and C).

### *Model Robustness*

We were in a unique position to attempt a test of robustness for our models given the large number of studies and large number of subjects. We randomly selected half (107) of the total number of

matrices (220) for these tests; however, there was an issue of coverage for background knowledge across the included matrices, much like what was seen when we split the matrices according to age. Cheung (2015b) has reported that a minimum of four values are needed in each cell to properly estimate the value and its confidence interval. We decided to run the robustness tests on the remaining constructs; the results of these models are highly similar to those found in the overall model and separate models for age. These tests of robustness are further discussed in Appendix S2.

#### *Limitations of the MASEM Approach*

The limitations of the MASEM approach can apply to any researchers who use this method regardless of topic or field. We state limitations specific to our results and explain how these limitations may affect researchers of any background.

##### *Range Restriction*

We included studies from only the past 26 years. This reduces the amount of studies that would meet criteria had studies been accepted from years prior to 1990. The MASEM approach has the ability to include continuous and categorical moderators. Future applications of this method should consider publication year or a range of publication years as a moderator to test for historical differences in populations, settings, and measures.

##### *Dichotomization*

We dichotomized age to produce a matrix for children who were below age 11 and for children who were aged 11 and older. Dichotomizing continuous variables has been criticized (e.g., MacCallum, Zhang, Preacher, & Rucker, 2002; Maxwell & Delaney, 2004), as it produces a loss of effect size and power, loss of information regarding individual differences, and loss of measurement reliability. However, most of these criticisms are directed at dichotomizing scales that are normally distributed (e.g., using cut-points on a continuous scale of ability or skill). The solution in this study is justified in that there are reasons to believe children younger than older children will have different patterns of predictor importance. However, we could not directly compare the model for the younger cohort to the model for the older cohort due to inability to analyze the same covariance structure in the models.

##### *Reader Ability Status*

We coded reader ability status for all studies but we were not able to include it as a moderator in the MASEM analyses. This limited our ability to investigate whether the parameter estimates and model structure were different across separable groups of impairment, which represents an important distinction. An additional study on the differences between these groups is warranted and necessary. Future applications of this method may encounter this same issue, and researchers should be aware of this limitation when considering subgroup analyses.

##### *Coding of Listening Comprehension Measures*

We accounted for a smaller amount of variance (41%) in the construct of listening comprehension at the study level than we anticipated. One hypothesis is that the listening comprehension variable was coded to include tasks that measured students' oral grammatical and syntactical skills in addition to tasks measuring their understanding of oral language. As a result, this construct was heterogeneous across studies. Researchers should exercise caution when coding for broad concepts, and carefully consider the ways in which primary studies measure their constructs of interest.

##### *Reliability of Measurement*

One final limitation was that the reliability of the measures was not controlled for at the individual study level. Decoding, linguistic comprehension, and cognitive abilities were privileged in the final model, since these variables had their reliability accounted for through the estimation of latent variables. RC was a single-criterion variable, even though every study included a measure of RC. Researchers should consider multiple indicators of constructs to create latent variables free of measurement error, or consider correcting for study level reliability where feasible.

Despite its limitations, but given the likelihood that a researcher will encounter these limitations, the results still provide researchers the basic tools needed to not only conduct their own MASEMs but to understand and consider the methodological constraints and complexities.

##### *Implications for Education Research*

We were unable to test for potential indirect effects from the cognitive component to RC

through either of the SVR components due to the usage of correlational data. However, previous research has suggested that improvements in reading fluency can reduce the demands on working memory, indirectly improving RC by reducing cognitive load (Swanson & O'Connor, 2009). Furthermore, two of the linguistic comprehension components (vocabulary knowledge, background knowledge) have previously been indirectly linked to RC through inferencing skills (Ahmed et al., 2016; Cromley & Azevedo, 2007). Although a direct pathway was not supported, and an indirect pathway could not be estimated, there were large correlations between the cognitive component and decoding and linguistic comprehension. Additionally, previous studies have shown that text reading fluency fully mediates the relation between word reading and RC, and partially mediates the relation between listening comprehension and RC (e.g., Kim & Wagner, 2015). Further testing is needed to determine if there are constructs involved in indirect pathways that could benefit from targeted instruction and intervention. The usage of MASEM techniques with longitudinal data may be better suited for determining indirect and direct pathways in the development of RC skills.

#### *Concluding Remarks: The Utility of MASEMs*

The MASEM results were estimated from the first multivariate, large-scale meta-analysis to be conducted on individual differences in RC. The MASEM approach provided a composite correlation matrix of the included variables and fit multiple models to the data that supported both the original and expanded versions of the SVR. This promising two-stage statistical approach can benefit researchers of any field, but is particularly beneficial for the education sciences, where curricula, measures, and samples can vary extremely between studies. The two-stage approach to combining correlation matrices across multiple studies and considering the covariances between correlations provides a unique way to account for stochastic dependence and heterogeneity that has previously been ignored or underutilized.

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### Supporting Information

Additional supporting information may be found in the online version of this article at the publisher's website:

**Appendix S1.** References Used in the Meta-Analytic Structural Equation Modeling Application

**Appendix S2.** Results of Model Robustness Checks

**Appendix S3.** Results of the Confirmatory Factor Analyses (CFA) Model Testing