The Fundamental Counting Principle

If one operation can be performed in m ways and a second operation can be performed in n ways, then the number of ways to perform the sequence of two operations is $m \cdot n$.

This rule can be extended to any number of operations performed in sequence.

Example 1. A section of an exam contains four true—false questions.

A completed exam paper is selected at random, and the four answers are recorded.

How many answers are possible? (That is, find the number of all possible outcomes.)

Questions: Q1 Q2 Q3 Q4
Possible answers: T or F T or F T or F

Number of outcomes: $2 \times 2 \times 2 = 16$

Example 2. Three fair coins are tossed. What is the number of all possible outcomes?

Coins: Coin 1 Coin 2 Coin 3

Possible outcomes: H or T H or T H or T

Number of outcomes: $2 \times 2 \times 2 = 8$