

How to Analyze Data From Multiple Animals

John Fieberg, Associate Professor

Department of Fisheries, Wildlife and Conservation Biology



1. We've seen how to estimate parameters describing an individual's use of space

- ▶ RSFs
- ▶ SSFs

1. We've seen how to estimate parameters describing an individual's use of space
 - ▶ RSFs
 - ▶ SSFs
2. We may want to know what is driving any differences among animals

1. We've seen how to estimate parameters describing an individual's use of space
 - ▶ RSFs
 - ▶ SSFs
2. We may want to know what is driving any differences among animals
3. We may want to pool information across individuals to better understand population-level selection patterns

Causes of Individual Variability

- Genetic factors
 - Inherited traits
 - Heritability
 - Twin studies
 - Family studies
 - Adoption studies
 - Molecular genetics
 - Polygenic inheritance
 - Single-gene disorders
 - Chromosomal abnormalities
 - Epigenetics
 - Gene-environment interactions
- Environmental factors
 - Nutrition
 - Stress
 - Social environment
 - Physical environment
 - Cultural factors
 - Education
 - Lifestyle choices
 - Trauma
 - Substance use
 - Health care access
 - Socioeconomic status
- Developmental factors
 - Prenatal development
 - Early childhood experiences
 - Puberty
 - Aging
 - Neuroplasticity
 - Brain development
 - Hormonal changes
 - Cognitive development
 - Emotional development
 - Social development
- Measurement and methodological factors
 - Measurement error
 - Sampling bias
 - Observer bias
 - Instrumentation
 - Data collection methods
 - Statistical analysis
 - Reporting bias
 - Publication bias
 - Confounding variables
 - Correlation vs. causation

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015

Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions FREE

Pascal Marchand, Mathieu Garel, Gilles Bourgoïn, Dominique Dubray, Daniel Maillard, Anne Loison Author Notes

Behavioral Ecology, Volume 26, Issue 2, 1 March 2015, Pages 472–482,
<https://doi.org/10.1093/beheco/aru212>

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015

Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions

Pascal Marchand, Mathieu Garel, Gilles Bourgoi
Anne Loison | Author Notes

Behavioral Ecology, Volume 26, Issue 2, 1 March
<https://doi.org/10.1093/beheco/aru212>

Received: 22 August 2016 | Revised: 12 December 2016 | Accepted: 22 December 2016
DOI: 10.1093/beheco/aru212

ORIGINAL RESEARCH

WILEY *Ecology and Evolution*

Complex variation in habitat selection strategies among individuals driven by extrinsic factors

Edward J. Raynor¹ | Hawthorne L. Beyer² | John M. Briggs¹ | Anthony Joern¹

¹Division of Biology, Kansas State University,
Manhattan, KS, USA

²ABC Centre of Excellence for Environmental
Decisions, The University of Queensland,
Brisbane, Qld, Australia

Correspondence
Edward J. Raynor, Division of Biology, Kansas
State University, Manhattan, KS, USA.
Email: edwardraynor@gmail.com

Current address
Edward J. Raynor, School of Natural
Resources, University of Nebraska, Lincoln,
NE, USA

Funding information
Division of Environmental Biology, National
Science Foundation (NSF), Grant/Award
Number: DEB-1000465; NSF Korea UTR

Abstract

Understanding behavioral strategies employed by animals to maximize fitness in the face of environmental heterogeneity, variability, and uncertainty is a central aim of animal ecology. Flexibility in behavior may be key to how animals respond to climate and environmental change. Using a mechanistic modeling framework for simultaneously quantifying the effects of habitat preference and intrinsic movement on space use at the landscape scale, we investigate how movement and habitat selection vary among individuals and years in response to forage quality–quantity tradeoffs, environmental conditions, and variable annual climate. We evaluated the association of dynamic, biotic forage resources and static, abiotic landscape features with large grazer movement decisions in an experimental landscape, where forage resources vary in response to prescribed burning, grazing by a native herbivore, the plains bison (*Bison bison*), and a continental climate. Our goal was to determine how biotic and abiotic factors mediate bison movement decisions in a nutritionally heterogeneous grassland. We integrated spatially explicit relocations of GPS-collared bison and extensive vegetation surveys to relate movement paths to grassland attributes over a time pe-

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015



Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions FREE

Pascal Marchand, Mathieu Garel, Gilles Bourgoi
Anne Loison [Author Notes](#)

Behavioral Ecology, Volume 26, Issue 2, 1 March
<https://doi.org/10.1093/beheco/aru212>

Received: 22 August 2016 | Revised: 12 December 2016 | Accepted: 22 December 2016
DOI: 10.1093/beheco/aru212

ORIGINAL RESEARCH

WILEY *Ecology and Evolution*

Complex variation in habitat selection strategies among individuals driven by extrinsic factors

| John M. Briggs¹ | Anthony Joern¹

[Evolutionary Ecology](#)

March 1989, Volume 3, [Issue 1](#), pp 80–94 | [Cite as](#)

Density-dependent habitat selection: Testing the theory with fitness data

Authors

Authors and affiliations

Douglas W. Morris

Journal of Animal Ecology, 2016, 85, 1–11
Number: 00000000; NGP Korea LTER

bison bison), and a continental climate. Our goal was to determine how biotic and abiotic factors mediate bison movement decisions in a nutritionally heterogeneous grassland. We integrated spatially explicit relocations of GPS-collared bison and extensive vegetation surveys to relate movement paths to grassland attributes over a time pe-

oral strategies employed by animals to maximize fitness in the heterogeneity, variability, and uncertainty is a central aim of lity in behavior may be key to how animals respond to climate nge. Using a mechanistic modeling framework for simultane-ffects of habitat preference and intrinsic movement on space ale, we investigate how movement and habitat selection vary years in response to forage quality–quantity tradeoffs, environ- l variable annual climate. We evaluated the association of dy- sources and static, abiotic landscape features with large grazer n an experimental landscape, where forage resources vary in l burning, grazing by a native herbivore, the plains bison (Bison

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015

Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions FREE

Pascal Marchand, Mathieu Garel, Gilles Bourgois
Anne Loison Author Notes

Behavioral Ecology, Volume 26, Issue 2, 1 March
<https://doi.org/10.1093/beheco/aru212>

Received: 22 August 2016 | Revised: 12 December 2016 | Accepted: 22 December 2016
DOI: 10.1093/beheco/aru212

ORIGINAL RESEARCH

WILEY *Ecology and Evolution*

Complex variation in habitat selection strategies among individuals driven by extrinsic factors

| John M. Briggs¹ | Anthony Joern¹



OIKOS 92: 542–554. Copenhagen 2001

Habitat selection by predators and prey in communities with asymmetrical intraguild predation

Michael R. Heithaus

Heithaus, M. R. 2001. Habitat selection by predators and prey in communities with asymmetrical intraguild predation. – *Oikos* 92: 542–554.

exploited by animals to maximize fitness in the
reliability, and uncertainty is a central aim of
y be key to how animals respond to climate
statistical modeling framework for simultane-
reference and intrinsic movement on space
e how movement and habitat selection vary
o forage quality–quantity tradeoffs, environ-
imate. We evaluated the association of dy-
abiotic landscape features with large grazer
landscape, where forage resources vary in
ry a native herbivore, the plains bison (Bison
ir goal was to determine how biotic and ab-
itions in a nutritionally heterogeneous grass-
cations of GPS-collared bison and extensive
aths to grassland attributes over a time pe-

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015

Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions FREE

Pascal Marchand, Mathieu Garel, Gilles Bourgoi

Anne Loison Author Notes

Behavioral Ecology, Volume 26
<https://doi.org/10.1093/behe>

Received: 22 August 2016 | Revised: 12 December 2016 | Accepted: 22 December 2016
DOI: 10.1093/behe/2764

WILEY *Ecology and Evolution*

Vol. 137, Supplement

The American Naturalist

June 1991



OIKOS 92: 542–554. Copenhagen 2001

Habitat selection by predators asymmetrical intraguild predation

Michael R. Heithaus

Heithaus, M. R.
asymmetrical ir

GENETIC VARIATION FOR HABITAT PREFERENCE: EVIDENCE AND EXPLANATIONS

JOHN JAENIKE AND ROBERT D. HOLT

Department of Biology, University of Rochester, Rochester, New York 14627;
Museum of Natural History and Department of Systematics and Ecology,
University of Kansas, Lawrence, Kansas 66045

Abstract.—Because adaptive shifts may often be initiated by evolutionary changes in behavior, it is of interest to determine the extent to which natural populations harbor genetic variation for ecologically important behaviors. Habitat preference is an especially significant behavior, because it determines the regime of natural selection acting on loci that affect adaptation to the environment. A survey of the literature reveals that genetic variation for habitat selection is common, especially in arthropods and mollusks, the groups that have been studied most frequently. Possible adaptive mechanisms by which this variation could be maintained within populations include a genetic correlation between density-independent fitness in a habitat and a preference for it; and soft selection, whereby density-dependent population regulation occurs independently in separate habitats. Several studies have documented a phenotypic correlation between habitat preference and fitness, but few studies have documented a genetic correlation between these traits.

in the
aim of
climate
space
n vary
viron-
of dy-
grazer
rare in
(Bison
nd abi-
grass-
ensive
ne pe-

Functional Response in Habitat Selection

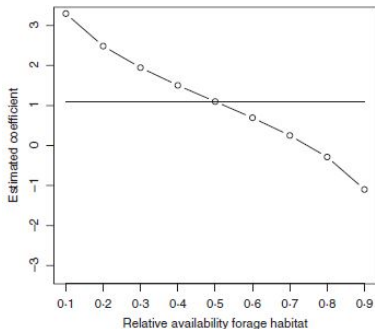
Assume animals needed a constant amount of a particular resource (e.g., water).

What would you expect to see if you plotted animal-specific RSF parameters against availability of that resource?

Functional Response in Habitat Selection

Assume animals needed a constant amount of a particular resource (e.g., water).

What would you expect to see if you plotted animal-specific RSF parameters against availability of that resource?



Aarts, G., Fieberg, J., Brasseur, S., & Matthiopoulos, J. (2013). Quantifying the effect of habitat availability on species distributions. *Journal of animal ecology*, 82(6), 1135-1145.

Methods for Modeling Data From Multiple Individuals

1. Fit models to pooled data, ignoring the fact that we have repeated measures, but use “robust SEs” (Generalized Estimating Equations or a “cluster-level bootstrap”) for inference

Methods for Modeling Data From Multiple Individuals

1. Fit models to pooled data, ignoring the fact that we have repeated measures, but use “robust SEs” (Generalized Estimating Equations or a “cluster-level bootstrap”) for inference
2. Fit models to individual animals and treat the estimates as data (two-step approach)

Methods for Modeling Data From Multiple Individuals

1. Fit models to pooled data, ignoring the fact that we have repeated measures, but use “robust SEs” (Generalized Estimating Equations or a “cluster-level bootstrap”) for inference
2. Fit models to individual animals and treat the estimates as data (two-step approach)
3. Mixed models (aka hierarchical models, random effect models): allow parameters to vary by animal

Individual Variability is Important

1. Fit models to pooled data, ignoring the fact that we have repeated measures, but use "robust SEs" (Generalized Estimating Equations or a "cluster-level bootstrap")
2. Fit models to individual animals and treat the estimates as data (two-step approach)
3. Mixed models, hierarchical models, random effect models: allow parameters to vary by animal

Two-step Approach

Mixed models

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(\textit{elev}(s)\beta_i + \textit{popD}(s)\gamma_i + \textit{forest}(s)\tau_i)$$

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Step 2: Do statistics on $(\hat{\beta}_i, \hat{\gamma}_i, \hat{\tau}_i)$

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Step 2: Do statistics on $(\hat{\beta}_i, \hat{\gamma}_i, \hat{\tau}_i)$

- calculate their variance/covariance (biased high due to sampling variability)

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Step 2: Do statistics on $(\hat{\beta}_i, \hat{\gamma}_i, \hat{\tau}_i)$

- ▶ calculate their variance/covariance (biased high due to sampling variability)
- ▶ relate coefficients to animal-specific characteristics (e.g., age, sex) using say `lm`

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Step 2: Do statistics on $(\hat{\beta}_i, \hat{\gamma}_i, \hat{\tau}_i)$

- ▶ calculate their variance/covariance (biased high due to sampling variability)
- ▶ relate coefficients to animal-specific characteristics (e.g., age, sex) using say `lm`
- ▶ plot coefficients against availability to explore functional responses

Fit models to individual animals

- ▶ Often a useful starting point (exploratory data analysis)

Fit models to individual animals

- ▶ Often a useful starting point (exploratory data analysis)
- ▶ Fewer parametric assumptions (no distributional assumptions about random effects)

Fit models to individual animals

- ▶ Often a useful starting point (exploratory data analysis)
- ▶ Fewer parametric assumptions (no distributional assumptions about random effects)

For justification of 2-step approach, see: Murtaugh, P. A. (2007). Simplicity and complexity in ecological data analysis. *Ecology*, 88(1), 56-62.

Fit models to individual animals

- ▶ Often a useful starting point (exploratory data analysis)
- ▶ Fewer parametric assumptions (no distributional assumptions about random effects)

For justification of 2-step approach, see: Murtaugh, P. A. (2007). Simplicity and complexity in ecological data analysis. *Ecology*, 88(1), 56-62.

In the context of step-selection functions:

- ▶ Craiu, R. V., T. Duchesne, D. Fortin, and S. Baillargeon (2011). Conditional logistic regression with longitudinal follow-up and individual-level random coefficients: A stable and efficient two-step estimation method. *Journal of Computational and Graphical Statistics* 20, 767-784.
- ▶ Craiu, R. V., T. Duchesne, D. Fortin, and S. Baillargeon (2016). TwoStepCLogit: Conditional Logistic Regression: A Two-Step Estimation Method. R package version 1.2.5.

Two-step Approach

- Quick and easy using the `amt` package in conjunction with `tidyverse` in R

```
## # A tibble: 8 x 7
##   id      n Elevation forest `log(sl_)` PopDens      sl_
##   <fct> <int>      <dbl>   <dbl>      <dbl>      <dbl>      <dbl>
## 1 F1      6391  0.0337    17.4      0.751 -0.00208  0.00272
## 2 F2     22165  0.0467   -0.274     0.687 -0.00112 -0.00338
## 3 F3     10169  0.0868   -0.591     0.603 -0.00225  0.000765
## 4 M1      4697  0.0776   -0.219     0.510  0.000583  0.00352
## 5 M2     10709  0.0292   -0.258     0.441 -0.00258  0.00193
## 6 M3     15547  0.0485    0.470     0.532 -0.00157  0.00272
## 7 M4     54810  0.0153    0.213     0.644 -0.000511 0.00197
## 8 M5     52303  0.00350   NA        0.848 -0.0232   0.00444
```

Two-step Approach

Mixed models

Mixed models

$$f_i^u(s) \propto \exp(\textit{elev}(s)\beta_i + \textit{popD}(s)\gamma_i + \textit{forest}(s)\tau_i)$$

Mixed models

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Further assume:

$$(\beta_i, \gamma_i, \tau_i) \sim N(\mu, \psi)$$

Mixed models

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Further assume:

$$(\beta_i, \gamma_i, \tau_i) \sim N(\mu, \psi)$$

Similar 2-step approach, but assume the regression parameters come from a common normal distribution.

Mixed models

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Further assume:

$$(\beta_i, \gamma_i, \tau_i) \sim N(\mu, \psi)$$

Similar 2-step approach, but assume the regression parameters come from a common normal distribution.

Advantages:

- inference at individual- and population-level with single model

Mixed models

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Further assume:

$$(\beta_i, \gamma_i, \tau_i) \sim N(\mu, \psi)$$

Similar 2-step approach, but assume the regression parameters come from a common normal distribution.

Advantages:

- ▶ inference at individual- and population-level with single model
- ▶ can “borrow strength” across individuals when estimating $(\beta_{1i}, \dots, \beta_{2i})$

Mixed models

$$f_i^u(s) \propto \exp(\text{elev}(s)\beta_i + \text{popD}(s)\gamma_i + \text{forest}(s)\tau_i)$$

Further assume:

$$(\beta_i, \gamma_i, \tau_i) \sim N(\mu, \psi)$$

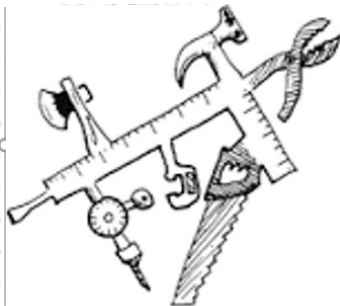
Similar 2-step approach, but assume the regression parameters come from a common normal distribution.

Advantages:

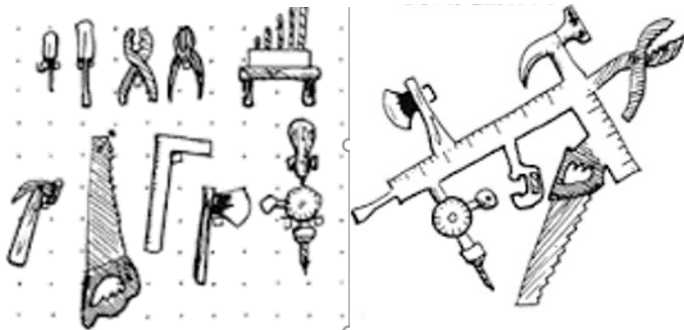
- ▶ inference at individual- and population-level with single model
- ▶ can “borrow strength” across individuals when estimating $(\beta_{1i}, \dots, \beta_{2i})$

But... more assumptions, added complexity

Two-step versus Mixed Effects Models



Two-step versus Mixed Effects Models



"If you can't explain it simply, you don't understand it well enough" - Albert Einstein

Random Effects and Models of Habitat Selection

- ▶ Random effects were proposed for RSFs over 10 years ago¹

¹Gillies et al. "Application of random effects to the study of resource selection by animals." *Journal of Animal Ecology* 75.4 (2006): 887-898.

Random Effects and Models of Habitat Selection

- Random effects were proposed for RSFs over 10 years ago¹

The screenshot shows a Google Scholar search interface. The search bar is empty. Below the search bar, the text 'Articles' is displayed with a blue diamond icon. To the right, it says 'About 35,200 results (0.11 sec)'. On the left side, there are filters for 'Any time', 'Since 2018', 'Since 2017', 'Since 2014', and 'Custom range...'. The main search result is for the article 'Application of random effects to the study of resource selection by animals' by Gillies, M. Hebblewhite, and S.E. Nielsen, published in the Journal of Animal Ecology in 2006. The article is highlighted in blue. Below the title, there is a brief abstract: 'Most frequently, individual animals are monitored and pooled to estimate population-level effects without regard to group or individual-level variation. Pooling assumes that both observations and their errors are independent, and resource selection is constant given individual variation ...'. Below the abstract, there are icons for a star, a document, and a link, followed by the text 'Cited by 479', 'Related articles', and 'All 23 versions'.

Google Scholar

Articles About 35,200 results (0.11 sec)

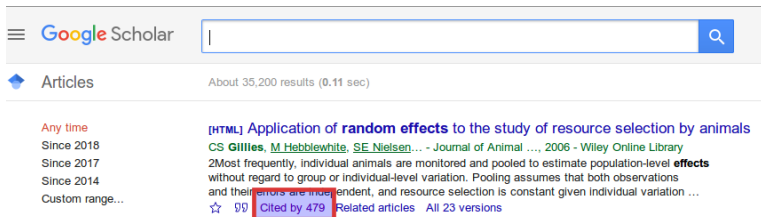
Any time
Since 2018
Since 2017
Since 2014
Custom range...

[HTML] Application of random effects to the study of resource selection by animals
CS Gillies, M Hebblewhite, SE Nielsen... - Journal of Animal ..., 2006 - Wiley Online Library
2Most frequently, individual animals are monitored and pooled to estimate population-level effects without regard to group or individual-level variation. Pooling assumes that both observations and their errors are independent, and resource selection is constant given individual variation ...
☆ 99 Cited by 479 Related articles All 23 versions

¹Gillies et al. "Application of random effects to the study of resource selection by animals." Journal of Animal Ecology 75.4 (2006): 887-898.

Random Effects and Models of Habitat Selection

- Random effects were proposed for RSFs over 10 years ago¹



The screenshot shows a Google Scholar search interface. The search bar is empty. Below the search bar, the text 'Articles' is displayed with a blue diamond icon. To the right, it says 'About 35,200 results (0.11 sec)'. On the left side, there are filters for 'Any time', 'Since 2018', 'Since 2017', 'Since 2014', and 'Custom range...'. The main search result is for the article 'Application of random effects to the study of resource selection by animals' by Gillies, M. Hebblewhite, and S.E. Nielsen, published in the Journal of Animal Ecology in 2006. The article is highlighted in green. Below the title, there is a brief description: 'Most frequently, individual animals are monitored and pooled to estimate population-level effects without regard to group or individual-level variation. Pooling assumes that both observations and their errors are independent, and resource selection is constant given individual variation ...'. To the right of the description, there are icons for 'Cited by 479', 'Related articles', and 'All 23 versions'.

- Majority of studies (80 % since 2016) only include random intercept and no random slope(s).

¹Gillies et al. "Application of random effects to the study of resource selection by animals." Journal of Animal Ecology 75.4 (2006): 887-898.

RSFs: Random Intercept-Only Models

1. Intercept in RSFs is not of interest and depends heavily on the sampling ratio of used versus available points

⁵Schielzeth, H. and W. Forstmeier (2009). Conclusions beyond support: Overconfident estimates in mixed models. *Behavioral Ecology* 20, 416-420.

RSFs: Random Intercept-Only Models

1. Intercept in RSFs is not of interest and depends heavily on the sampling ratio of used versus available points
2. Cannot (by definition) account for among-animal variation in the regression slopes (i.e., functional responses)!

⁵Schielzeth, H. and W. Forstmeier (2009). Conclusions beyond support: Overconfident estimates in mixed models. *Behavioral Ecology* 20, 416-420.

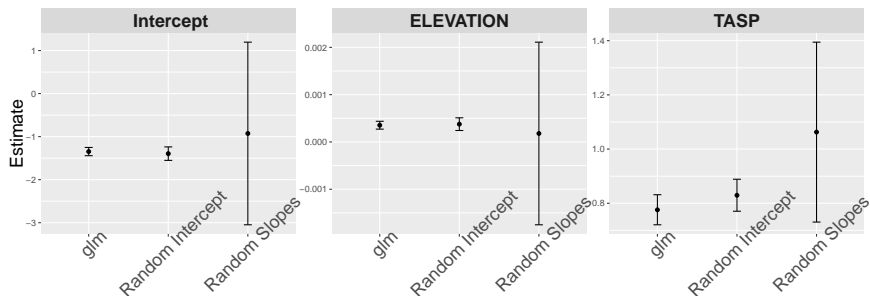
RSFs: Random Intercept-Only Models

1. Intercept in RSFs is not of interest and depends heavily on the sampling ratio of used versus available points
2. Cannot (by definition) account for among-animal variation in the regression slopes (i.e., functional responses)!
3. SEs will be too small, particularly with lots of observations for each animal⁵

⁵Schielzeth, H. and W. Forstmeier (2009). Conclusions beyond support: Overconfident estimates in mixed models. *Behavioral Ecology* 20, 416-420.

Example: Goat RSFs⁶

```
glm <- glm(STATUS ~ TASP + ELEVATION, family=binomial(),  
          data = goats)  
glmer_int <- glmmTMB(STATUS ~ TASP + ELEVATION + (1|ID),  
                    family=binomial(), data = goats)  
glmer_randcoef <- glmmTMB(STATUS ~ TASP + ELEVATION +  
                          (1+TASP+ELEVATION|ID),  
                          family=binomial(), data = goats)
```



⁶Lele & Keim, (2006) Weighted distributions and estimation of resource selection probability functions. Ecology 87, 3021–3028.


SSFs: Mixed Effects

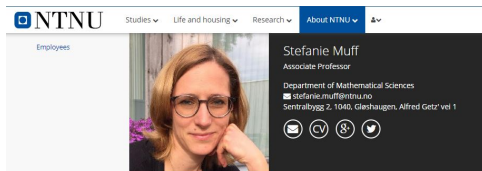
Conditional logistic regression with random effects is computationally prohibitive for most data sets.

Options:

- ▶ `coxme` for small numbers of strata
- ▶ `TwoStepCLogit::Ts.estim()`, a two-step approach

Accounting for individual-specific variation in habitat-selection studies: Efficient estimation of mixed-effects models using Bayesian or frequentist computation

Stefanie Muff^{1,2}  | Johannes Signer³  | John Fieberg⁴ 



Norwegian University of Science and Technology

Mixed SSF Trick

Reformulation SSFs as a Poisson model with stratum-specific intercepts α_{nt} ⁵

- ▶ Same likelihood kernel as condition logistic regression likelihood, same $\hat{\beta}$, same $SE(\hat{\beta})$

⁵Armstrong et al. "Conditional Poisson models: a flexible alternative to conditional logistic case cross-over analysis." BMC medical research methodology 14.1 (2014): 122.

Mixed SSF Trick

Reformulation SSFs as a Poisson model with stratum-specific intercepts α_{nt} ⁵

- ▶ Same likelihood kernel as condition logistic regression likelihood, same $\hat{\beta}$, same $SE(\hat{\beta})$
- ▶ But, then lots of intercepts to estimate (one for every used location!)

⁵Armstrong et al. "Conditional Poisson models: a flexible alternative to conditional logistic case cross-over analysis." BMC medical research methodology 14.1 (2014): 122.

Mixed SSF Trick

Reformulation SSFs as a Poisson model with stratum-specific intercepts α_{nt} ⁵

- ▶ Same likelihood kernel as condition logistic regression likelihood, same $\hat{\beta}$, same $SE(\hat{\beta})$
- ▶ But, then lots of intercepts to estimate (one for every used location!)
- ▶ Trick: $\alpha_{nt} \sim N(0, 10^6)$ (avoids shrinkage and explicit estimation)

⁵Armstrong et al. "Conditional Poisson models: a flexible alternative to conditional logistic case cross-over analysis." BMC medical research methodology 14.1 (2014): 122.

Applied Example



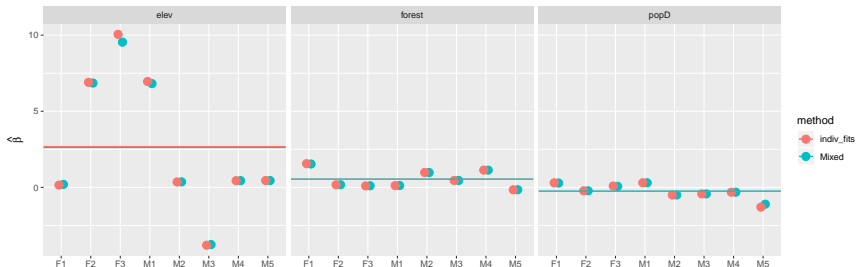
Covariates:

- ▶ elevation
- ▶ population density
- ▶ forest (yes/no)

Compare two-step approaches and mixed models:

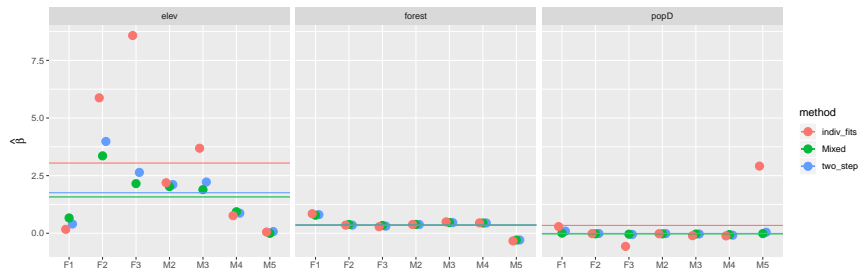
- ▶ individual estimates
- ▶ estimated mean coefficients
- ▶ estimated variance of the coefficients across animals

RSFs



Variance estimates	$sd(\beta_{\text{elev}})$	$sd(\beta_{\text{popD}})$	$sd(\beta_{\text{forest}})$
naive two-step (indiv_fits)	4.69	0.523	0.608
mixed model	4.21	0.443	0.564

SSFs



Variance estimates	$\text{sd}(\beta_{\text{elev}})$	$\text{sd}(\beta_{\text{popD}})$	$\text{sd}(\beta_{\text{forest}})$
naive two-step (indiv_fits)	2.49	1.02	0.339
formal two-step ('TS.Estim')	1.67	0.036	0.228
mixed model	1.35	0.0000019	0.312

Summary

Naive two-step approach:

- ▶ simple and easy to understand
- ▶ estimators of variance components biased high

Summary

Naive two-step approach:

- ▶ simple and easy to understand
- ▶ estimators of variance components biased high

Ts.Estimation (formal two-step approach):

- ▶ FAST, can estimate of variance components (but not their uncertainty), can share information across individuals
- ▶ can fail with categorical predictors (all individuals need to encounter all factor levels)

Summary

Naive two-step approach:

- ▶ simple and easy to understand
- ▶ estimators of variance components biased high

Ts.Estimation (formal two-step approach):

- ▶ FAST, can estimate of variance components (but not their uncertainty), can share information across individuals
- ▶ can fail with categorical predictors (all individuals need to encounter all factor levels)

Poisson trick:

- ▶ fast, can estimate variance components (and their uncertainty), can share information across individuals
- ▶ formal one-step framework for fitting mixed-effect RSFs and SSFs

Implementation

- ▶ Two-step methods: tidyverse and via Ts.estim
- ▶ Frequentist mixed models: glmmTMB

See paper and associated code for a Bayesian implementation using INLA and Stan.