

Answer the following 4 questions and submit your answers online:

1. [10 points] Analysis

There are n pancakes to be fried on a small grill that can hold only two pancakes at a time. Each pancake has to be fried on both sides; frying one side of a pancake takes 1 minute, regardless of whether one or two pancakes are fried at the same time. Consider the following recursive algorithm for executing this task in the minimum amount of time. If $n \leq 2$, fry the pancake or the two pancakes together on each side. If $n > 2$, fry any two pancakes together on each side and then apply the same procedure recursively to the remaining $n - 2$ pancakes.

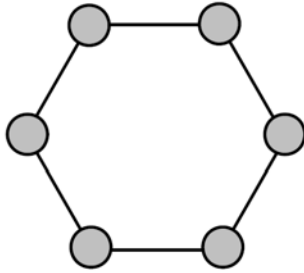
a. Set up and solve the recurrence for the amount of time this algorithm needs to fry n pancakes.

b. Explain why this algorithm does not fry the pancakes in the minimum amount of time for all $n > 0$.

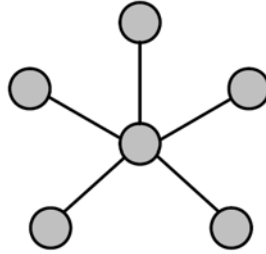
c. Give a correct recursive algorithm that executes the task in the minimum amount of time.

2. [10 points] Exhaustive Search

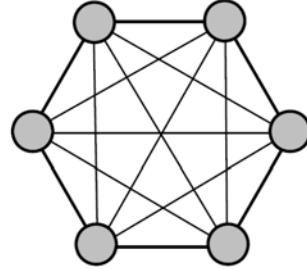
A network topology specifies how computers, printers, and other devices are connected over a network. The figure below illustrates three common topologies of networks: Ring, Star, and Fully Connected Mesh.



Ring



Star



Fully Connected Mesh

You are given a boolean matrix $A[0..n-1, 0..n-1]$, where $n > 3$, which is supposed to be the adjacency matrix of a graph modeling a network with one of these topologies. Your task is to determine which of these three topologies, if any, the matrix represents. Design a brute-force algorithm for this task and indicate its time efficiency class.

3. [10 points] Decrease and Conquer

- a. Show that the disk moves made in the classic recursive algorithm for the Towers of Hanoi puzzle can be used for generating the binary reflected Gray code.
- b. Show how the binary reflected Gray code can be used for solving the Towers of Hanoi puzzle.

4. [10 points] Divide and Conquer

How many lines does his algorithm print? Write a recurrence and solve it.

```
function printaton(n: an integer power of 2) {  
    if n > 1 {  
        printaton(n/2)  
        printaton(n/2)  
        printaton(n/2)  
        for i = 1 to n ^ 4 do  
            printline("are we done yet")  
    }  
}
```

- a. Use Master's theorem to obtain an asymptotic solution.
- b. Derive an exact solution by expanding the recurrence.