Slide Set: 1

### **Learning Objectives**



- Write precondition/postcondition contracts for small functions, and use the C++ assert facility to test preconditions
- Recognize quadratic, linear, and logarithmic running time behavior in simple algorithms, and write big-O expressions to describe this behavior
- Create and recognize test data that is appropriate for simple problems, including testing boundary conditions and fully exercising code





- Specification of the task
- Design of a solution
- Implementation (coding) of the solution
- Analysis of the solution
- Testing and debugging
- Maintenance and evolution of the system
- Obsolescence

### Specification, Design, Implementation



- The specification is a precise description of the problem
- The design phase consists of formulating the steps to solve the problem
- The implementation is the actual C++ code that carries out the design

Specification, Design, Implementation

□Example: Display a table for converting Celsius temperatures to Fahrenheit:

For a small problem, a sample of the desired output is a sufficient specification

#### Specification, Design, Implementation



- The next step is to design a solution:
  - An algorithm is a set of instructions for solving a problem
  - □Example: An algorithm for the temperature problem will print the conversion table
  - During the design of the algorithm, the details of a particular programming language can be distracting
  - Using a mixture of English and a programming language (C++) is called pseudocode
  - When the C++ code for a step is obvious, then the pseudocode may use C++
  - When a step is clearer in English, then we will use English

#### **Design Concept: Decomposing the Problem**



- A good technique for designing an algorithm is to break down the problem at hand into a few subtasks
  - Then decompose each subtask into smaller subtasks
  - Then replace the smaller subtasks with even smaller subtasks, and so forth
  - Each subtask can be implemented as a separate piece of your program (C++ function)

**Design Concept: Decomposing the Problem (Cont'd)** 

- □Example:
- The temperature problem has at least two good subtasks:
  - 1. Converting a temperature from Celsius degrees to Fahrenheit
  - 2. Printing a line of the conversion table in the specified format

**Design Concept: Decomposing the Problem (Cont'd)** 

- The first draft of our pseudocode for the temperature problem might look like this:
  - 1. Do preliminary work to open and set up the output device properly
  - 2. Display the labels at the top of the table
  - 3. For each line in the table (using variables celsius and fahrenheit):
    - a. Set celsius equal to the next Celsius temperature of the table
    - b. fahrenheit = the celsius temperature converted to Fahrenheit
    - c. Print the Celsius and Fahrenheit values with labels on an output line

#### **Design Concept: Decomposing the Problem (Cont'd)**



- What makes a good decomposition?
  - Subtasks should help you produce short pseudocode
  - No more than a page of succinct description to solve the entire problem, and ideally much less than a page
- Two considerations for selecting good subtasks:
  - 1. The potential for **code reuse**: A function is written with sufficient generality that it can be reused elsewhere
  - 2. The possibility of future changes to the program
    - □ Example: Our temperature program might be modified to convert to Kelvin degrees instead of Fahrenheit
    - If the conversion task is performed by a separate function, much of the modification will be confined to this one function

#### **Preconditions and Postconditions**



- Frequently a programmer must communicate precisely what a function accomplishes, without any indication of how the function does its work
- Information hiding: To know only as much as you need, but no more

#### **Preconditions and Postconditions (Cont'd)**

 You are the head of a programming team and you want one of your programmers to write a function for a part of a project





- One way to specify such requirements is with a pair of statements about the function
  - The precondition statement indicates what must be true before the function is called
  - The postcondition statement indicates what will be true when the function finishes its work

- Precondition and postcondition are added to a function prototype
  - Prototype consists of the function's return type, name, and parameter list

#### **Preconditions and Postconditions (Cont'd)**



□ Example

```
void write_sqrt( double x )

// Precondition: x >= 0.

// Postcondition: The square root of x has been written to

// the standard output.

...
```

The precondition and postcondition appear as comments in program

**Preconditions and Postconditions (Cont'd)** 

□ Example

```
void write_sqrt( double x )

// Precondition: x >= 0.

// Postcondition: The square root of x has

// been written to the standard output.

...

In this example, the precondition requires that
    x >= 0 be true whenever the function is called
```

```
☐ Which of these function calls meet the precondition?
write_sqrt( -10 );
write_sqrt( 0 );
write_sqrt( 5.6 );
```

**Preconditions and Postconditions (Cont'd)** 

□ Example

```
void write_sqrt( double x)

// Precondition: x >= 0.

// Postcondition: The square root of x has

// been written to the standard output.

...
```

- The postcondition always indicates what work the function has accomplished
- In this case, when the function returns, the square root of x has been written

#### **Preconditions and Postconditions (Cont'd)**



#### **Example**

```
bool is_vowel( char letter )
// Precondition: letter is an uppercase or lowercase letter
// (in the range 'A' ... 'Z' or 'a' ... 'z') .
// Postcondition: The value returned by the function is true if
// Letter is a vowel; otherwise the value returned by the
// function is false.
```

```
is_vowel( 'A' ); true
is_vowel(' Z' ); false
is_vowel( '?' ); Nobody knows, the precondition has been violated
```

**Preconditions and Postconditions (Cont'd)** 

- The programmer who calls the function is responsible for ensuring that the precondition is valid when the function is called
- When we pretend that we do not know how a function is implemented, we are using a form of information hiding called procedural abstraction

AT THIS POINT, MY
PROGRAM CALLS YOUR
FUNCTION, AND I MAKE
SURE THAT THE
PRECONDITION IS
VALID.



**Preconditions and Postconditions (Cont'd)** 

 The programmer who writes the function counts on the precondition being valid, and ensures that the postcondition becomes true at the function's end THEN MY FUNCTION
WILL EXECUTE, AND
WHEN IT IS DONE, THE
POSTCONDITION WILL BE
TRUE.
I GUARANTEE IT.



- When you write a function, you should detect when a precondition has been violated
- If you detect that a precondition has been violated, then print an error message and halt the program
  - ... to avoid crashing the program with an unknown error



- During program development, functions should be designed to help programmers find errors as easily as possible
- As part of this effort, the first action of a function should be to check that its precondition is valid
- If the precondition fails, then:
  - The function prints a message
  - Either halts the entire program, or performs some other error actions before returning
- The assert facility is a good approach to detecting invalid data at an early point
  - Includes this directive: #include <cassert>
  - You can turn off all assertions by: #define NDEBUG



```
void write sqrt( double x)
// Precondition: x >= 0.
// Postcondition: The square root of x has been written
// to the standard output.
                       If (x >= 0)
                       x is valid and the assertion takes no action
  assert(x >= 0);
                       If (x < 0)
                       The precondition has been violated,
                       a message is printed and the program is halted
```

#### **Preconditions and Postconditions (Cont'd)**



#### □ Example

```
#include <iostream>
// uncomment to disable assert()
// #define NDEBUG
#include <cassert>

int main()
{
    assert(10+10==20);
    std::cout << "Execution continues past the first assert\n";
    assert(12+12==20);
    std::cout << "Execution continues past the second assert\n";
}</pre>
```

```
output:
Execution continues past the first assert
test: test.cc:10: int main(): Assertion `12+12==20' failed.
Aborted
```

- Succinctly describes the behavior of a function...
  - without cluttering up your thinking with details of how the function works
- At a later point, you may re-implement the function in a new way ...
  - ... but programs (which only depend on the precondition/postcondition) will still work with no changes

#### The Temperature Conversion Program

```
#include <iostream> // Provides cout
#include <iomanip> // Provides setw function for setting
                       // output width
#include <cstdlib>
                       // Provides EXIT SUCCESS
#include <cassert> // Provides assert function
using namespace std; // Allows all standard library items to
                        // be used
                                        A function for temperature conversion
double celsius_to_fahrenheit(double c)
// Precondition: c is a Celsius temperature no less than
// absolute zero (-273.16).
// Postcondition: The return value is the temperature c
// converted to Fahrenheit degrees.
    const double MINIMUM CELSIUS = -273.16; // Absolute zero in
                                             // Celsius degree
    assert(c >= MINIMUM CELSIUS);
                                      It is a declared constant, which means
    return (9.0 / 5.0) * c + 32;
}
                                      that its value will never be changed
                                      while the program is running
```

#### The Temperature Conversion Program (Cont'd)

A function to setup the output format

```
void setup_cout_fractions(int fraction_digits)
// Precondition: fraction digits is not negative.
// Postcondition: All double or float numbers printed to cout
// will now be rounded to the specified digits on the right of the
// decimal.
    assert(fraction digits > 0);
                                        Determines how many digits are
    cout.precision(fraction digits);
                                        printed for each number
                                              Causes numbers to be printed
    cout.setf(ios::fixed, ios::floatfield);
                                              in fixed-point notation
    if (fraction digits == 0)
        cout.unsetf(ios::showpoint);
    else
                                       Set the showpoint flag to show the
        cout.setf(ios::showpoint);
                                       decimal point
}
```

#### The Temperature Conversion Program (Cont'd)

```
int main( )
   // Heading for table's 1st column
   const char HEADING1[] = " Celsius";
   // Heading for table's 2nd column
   const char HEADING2[] = "Fahrenheit";
   // Label for numbers in 1st column
   const char LABEL1 = 'C':
   // Label for numbers in 2nd column
   const char LABEL2
                           = 'F':
   // The table's first Celsius temp.
   const double TABLE BEGIN = -50.0;
  // The table's final Celsius temp.
   const double TABLE END = 50.0;
```

The main function uses the two functions described earlier

#### The Temperature Conversion Program (Cont'd)

```
// Increment between temperatures
const double TABLE STEP = 10.0;
const int WIDTH = 9; // Number chars in output numbers
const int DIGITS = 1; // Number digits right of decimal pt
double value1; // A value from the table's first column
double value2; // A value from the table's second column
// Set up the output for fractions and print the table headings.
setup cout fractions(DIGITS);
cout << "CONVERSIONS from " << TABLE BEGIN << " to " << TABLE END
                                                      << endl;
cout << HEADING1 << " " << HEADING2 << endl;</pre>
```

#### Note:

Whenever you write the end1 object, the output buffer is automatically flushed

#### The Temperature Conversion Program (Cont'd)

```
// Each iteration of the loop prints one line of the table.
for (value1 = TABLE BEGIN; value1 <= TABLE END; value1 +=</pre>
                                                    TABLE STEP)
{
    value2 = celsius_to_fahrenheit(value1);
                        setw(WIDTH) sets the preferred number of output
                        characters to be used when the item is printed
    cout << setw(WIDTH) << value1 << LABEL1 << " ";</pre>
    cout << setw(WIDTH) << value2 << LABEL2 << endl;</pre>
}
                                Use "EXIT SUCCESS" in a Main Program
                                Same as return 0
return EXIT SUCCESS;
```

}

### The Standard Library and the Standard Namespace



- Standard Library aids programmers in writing portable code that can be compiled and run with many different compilers on different machines
- To use one of the library facilities, a program places an "include directive" at the top of the file that uses the facility
  - For example, to use the usual C++ input/output facilities: #include <iostream>
  - Some additional input/output items require a second include directive: #include <iomanip>

The Standard Library and the Standard Namespace (Cont'd)

#### **Note: Older Names for the Header Files**

- Older C++ compilers used slightly different names for header files
- For example, older compilers used iostream.h instead of simply iostream

#### The Standard Library and the Standard Namespace (Cont'd)



### **The Standard Namespace**

- All of the items in the new header files are part of a feature called the standard namespace, also called std
- When you use one of the new header files, your program should also have this statement after the include directives: using namespace std;
  - Note: There are other alternatives that we will talk about later

#### The Standard Library and the Standard Namespace (Cont'd)



```
return EXIT SUCCESS;
```

- Defined in cstdlib (or stdlib.h)
- The return value of EXIT\_SUCCESS tells the operating system that the program ended normally, and the operating system can then proceed with its next task
- For most operating systems, this constant is defined as zero (which
  is why you may have used return 0 in other programming

### Another example:

- Assume that a process A starts a process B, and waits for the successful completion of B
- If B does not return an EXIT\_SUCCESS, then A might try again running this process, or it might simply exit with a failure code



# **Running Time Analysis**

- Time analysis consists of reasoning about an algorithm's speed:
  - 1. Does the data structure or algorithm work fast enough for my needs?
  - 2. How much longer does the method take when the input gets larger?
  - 3. Which of several different methods is fastest?



- For a time analysis of a program, we do not usually measure the actual time taken to run the program
  - Because the number of seconds can depend on too many extraneous factors (e.g., processor speed, the effect of other processes)
- The analysis counts the number of operations required
  - An operation:
    - As simple as the execution of a single program statement
    - Arithmetic operation (addition, multiplication, etc.)
  - For most programs, the number of operations depends on the input size
    - For example, a program that sorts a list of numbers is quicker with a short list than with a long list

### **Big-O Notation**



- Often it is enough to know in a rough manner how the number of operations is affected by the input size
- We can express this kind of information in a format called big-O notation which is the order of an algorithm
- The order analysis is often enough to compare algorithms to estimate how running time is affected by changing data size
- □For example, the complexity of insertion into a linked list is O(1), while the complexity of insertion into a sorted array is O(n)

### **Big-O Notation (Cont'd)**



• If the largest term in a formula is a constant times n (i.e.,  $a \times n$ ), then the algorithm is said to be "big-O of n" written O(n), and the algorithm is called linear

■ Example: What is the big-O notation for this formula? 100n+5 : O(n)

### **Big-O Notation (Cont'd)**



• If the largest term in a number of operations' formula is no more than a constant times  $n^2$ , then the algorithm is said to be "big-O of  $n^2$ ," written  $O(n^2)$ , and the algorithm is called **quadratic** 

☐ What is the big-O notation for this formula?  $n^2+5n$  :  $O(n^2)$ 

### **Big-O Notation (Cont'd)**



 If the largest term in a formula is a constant times a logarithm of n, then the algorithm is "big-O of the logarithm of n," written O(log n), and the algorithm is called logarithmic

☐ What is the big-O notation for this formula? The number of digits in n : O(log n)

Note: digits = floor( log10( number ) ) + 1;

### **Big-O Comparison of Algorithms**



Highest complexity

Function	Common name	
n!	factorial	
$2^n$	exponential	
$n^d, d > 3$	polynomial	
$n^3$	cubic	
$n^2$	quadratic	
$n\sqrt{n}$		
$n \log n$	quasi-linear	
$\mid n \mid$	linear	
$\sqrt{n}$	root - n	
$\log n$	logarithmic	
1	constant	

Lowest complexity

### **Big-O Notation (Cont'd)**

### **Examples**

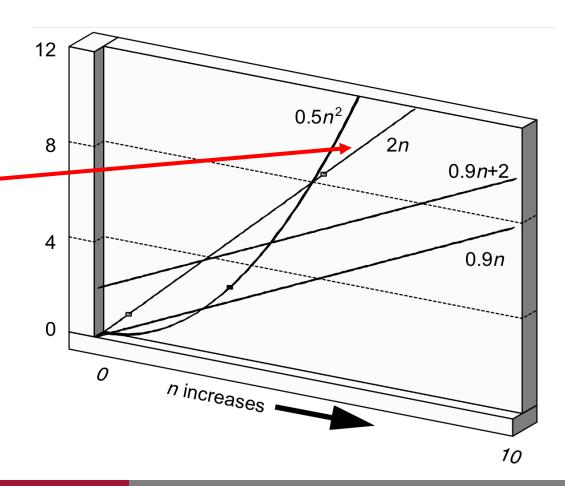
T(n)	Complexity
$5n^3 + 200n^2 + 15$	$O(n^3)$
$3n^2 + 2^{300}$	$O(n^2)$
$5\log_2 n + 15\ln n$	$O(\log n)$
$2\log n^3$	$O(\log n)$
$4n + \log n$	O(n)
$2^{64}$	O(1)
$\log n^{10} + 2\sqrt{n}$	$O(\sqrt{n})$
$2^n + n^{1000}$	$O(2^n)$

### **Big-O Comparison of Algorithms**



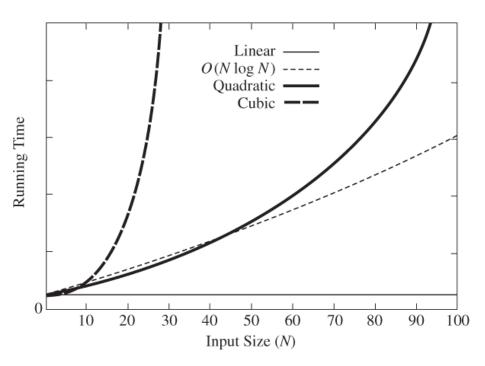
Different algorithms perform the same task with different big-O times

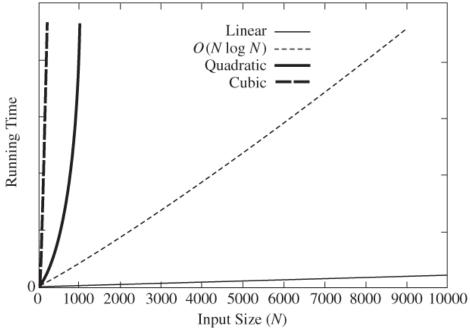
With a sufficiently large input, the algorithm with the better big-O analysis will perform faster



### **Big-O Comparison of Algorithms**







#### **Time Analysis of C++ Functions**

- The first step of the time analysis is to decide precisely what we will count as a single operation
  - For C++ functions, a good choice is to count the total number of C++ operations (such as an assignment, the < operation, or the << operation) plus the number of function calls (such as the call to assert)
  - If the function calls did complex work themselves, then we would also need to count the operations that are carried out there

### **Big-O Notation (Cont'd)**



```
    i = 0, 1, ..., N -1, the last time it check that i = N and stops
    Runs N times
```

- Total number of operations = N + (N + 1)
- The complexity of this code is O(N)

The complexity of this code is O(N<sup>2</sup>)

### **Big-O Notation (Cont'd)**



```
for (int i = 1; i <= n; ++i)
{
    for (int j = 1; j <= i; ++j)
        statement;
}</pre>
```

What is the time complexity of the above code?

- Worst-case analysis: determines the maximum number of operations required for the inputs of a given size n
- Average-case analysis: determines the average number of operations required for the inputs of a given size n
- **Best-case analysis**: determines the fewest number of operations required for the inputs of a given size *n*

### **Sample Actual Execution Time**

 If an operation can be run in 1 ns, then the execution time of different algorithms against data size is:

	Time			
Function	$(n=10^3)$	$(n=10^4)$	$(n=10^5)$	
$\log_2 n$	10 ns	$13.3 \mathrm{\ ns}$	16.6 ns	
$\sqrt{n}$	$31.6  \mathrm{ns}$	$100 \mathrm{\ ns}$	316 ns	
$\mid n \mid$	$1~\mu \mathrm{s}$	$10~\mu\mathrm{s}$	$100~\mu\mathrm{s}$	
$n \log_2 n$	$10~\mu \mathrm{s}$	$133~\mu\mathrm{s}$	$1.7 \mathrm{\ ms}$	
$n^2$	$1 \mathrm{\ ms}$	$100 \mathrm{\ ms}$	10 s	
$n^3$	1 s	$16.7  \mathrm{min}$	11.6 days	
$n^4$	$16.7  \mathrm{min}$	$116  \mathrm{days}$	3171 yr	
$2^n$	$3.4 \cdot 10^{284} \text{ yr}$	$6.3 \cdot 10^{2993} \text{ yr}$	$3.2 \cdot 10^{30086} \text{ yr}$	



- Program testing occurs when you run a program and observe its behavior
- Part of the science of software engineering is the systematic construction of a set of test inputs that is likely to discover errors, and such test inputs are the topic of this section

#### **Choosing Test Data**

- To serve as good test data, your test inputs need two properties:
  - You must know what output a correct program should produce for each test input
  - 2. The test inputs should include those inputs that are most likely to cause errors

#### **Choosing Test Data (Cont'd)**



Two methods for finding test data that is most likely to cause errors:

- First Method: Based on identifying and testing inputs called boundary values, which are particularly apt to cause errors
- A boundary value of a problem is an input that is one step away from a different kind of behavior

```
□Example:
```

```
int time_check(int hour);
// Precondition: hour lies in the
// range 0 <= hour <= 23</pre>
```

Two boundary values for time\_check are hour equal to 0 and hour equal to 23

#### **Choosing Test Data (Cont'd)**

- If you cannot test all possible inputs, at least test the boundary values
- For example, if legal inputs range from 0 to 1000000, then be sure to test input 0 and input 1000000
- It is a good idea also to consider 0, 1, and -1 to be boundary values whenever they are legal input

#### **Choosing Test Data (Cont'd)**



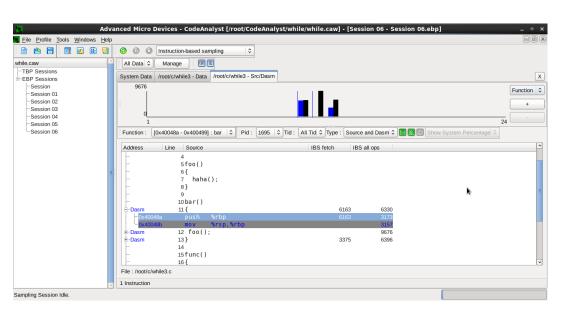
Second Method: Fully exercising code requires intimate knowledge of how a program has been implemented

This technique is simple, with two rules:

- Make sure that each line of your code is executed at least once by some of your test data
- If there is some part of your code that is sometimes skipped altogether, then make sure that there is at least one test input that actually does skip this part of your code

#### **Choosing Test Data (Cont'd)**

- Many compilers have a software tool called a profiler to help fully exercise code
- A typical profiler will generate a listing indicating how often each statement of your program was executed
- This can help you spot parts of your program that were not tested
- Valgrind
- Oprofile
- Gprof
- AMD Code Analyst



#### **Debugging (Cont'd)**

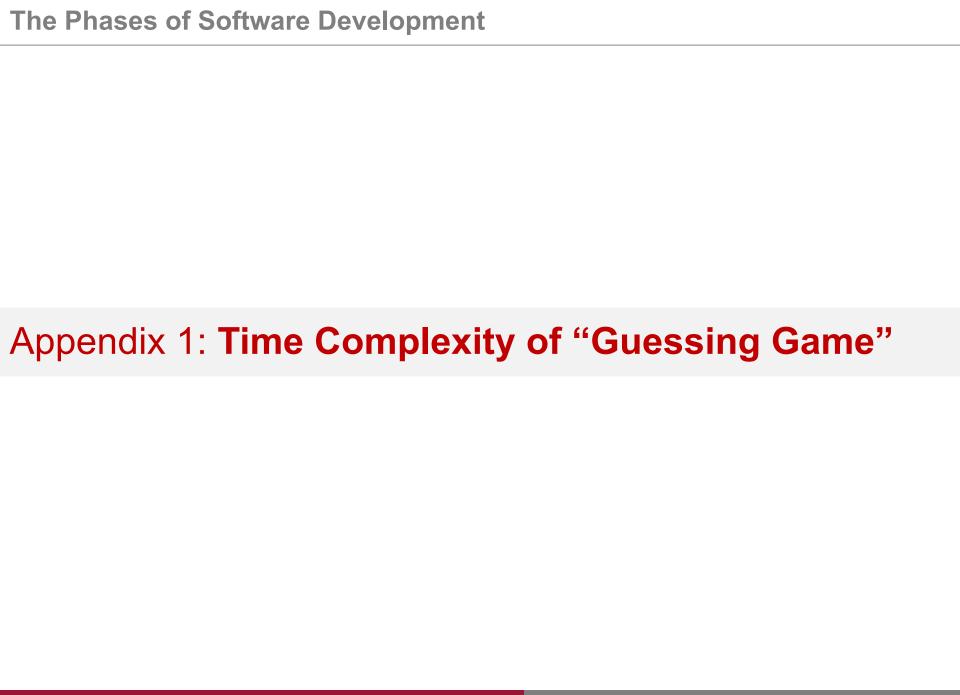


- After an erroneous test input is found, you still must determine exactly why the "bug" occurs, and then "debug the program"
- Debugging Tip:
  - 1. Never start changing suspicious code on the hope that the change "might work better"
  - 2. Instead, discover exactly why a test case is failing and limit your changes to corrections of known errors
  - 3. Once you have corrected a known error, all test cases should be rerun
- Use a software tool called a debugger to help track down exactly why an error occurs

### Summary



- One good method for specifying what a function is supposed to do is to provide a precondition and postcondition for the function
- Understanding and using the C++ Standard Library can make program development easier
- Time analysis is an analysis of how many operations an algorithm requires
- Three important examples of big-O analyses are **linear** (O(n)), quadratic  $(O(n^2))$ , and logarithmic  $(O(\log n))$ .
- An important testing technique is to identify and test boundary values
- A second important testing technique is to ensure that your test cases are fully exercising the code



#### **Guessing Game Function for the Time Analysis Example**

```
#include <cassert> // Provides assert
#include <iostream> // Provides cout and cin
#include <cstdlib> // Provides EXIT_SUCCESS
using namespace std; // Allows all Standard Library items to be used
// Prototype for the function used in this program
void guess_game(int n);
// Precondition: n > 0.
// Postcondition: The user has been asked to think of a number
// between 1 and n. The function asks a series of questions,
// until the number is found.
int main( )
    quess qame(100);
    return EXIT SUCCESS;
```

Guessing Game Function for the Time Analysis Example (Cont'd)

```
void guess game(int n)
// Library facilities used: cassert, iostream
    int guess;
    char answer;
    assert(n >= 1); One comparison, one call to assert = 2 operations
                                                       4 output operations
    cout << "Think of a whole number from 1 to " << n << "." << endl;
                     One assignment operation
    answer = 'N':
```

Guessing Game Function for the Time Analysis Example (Cont'd)

#### **Loop initialization = 1 operation**

Guessing Game Function for the Time Analysis Example (Cont'd)

#### References

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