Queues

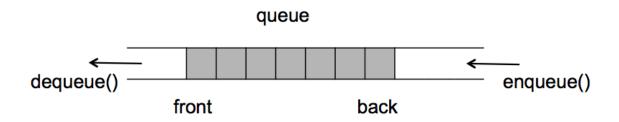
Slide Set: 8

Learning Objectives

- Implement the queue and double-ended queue classes using either an array or a linked-list data structure
- The STL deque implementation

Introduction

- A queue is a data structure of ordered entries such that entries can only be inserted at one end (called the **rear**) and removed at the other end (called the **front**)
- The entry at the front end of the queue is called the first entry
- Designed to operate in a FIFO context (first-in first-out)
- Items are taken out of the queue in the same order that they were put into the queue







- We will give two implementations of our queue class:
 - A static implementation using a fixed-sized array
 - A dynamic implementation using a linked list

Array Implementation of a Queue

- With a queue, we add entries at one end of the array and remove them from the other end
 - We access the used portion of the array at both ends
- Because we now need to keep track of both ends of the used portion of the array, we will have two variables to keep track of how much of the array is used:
 - 1. first: indicates the first index currently in use
 - 2. last: indicates the last index currently in use
- If data is the array name, then the queue entries will be in the array components:

```
data[first], data[first + 1], ... data[last]
```

Array Implementation of a Queue (Cont'd)

- To add an entry:
 - increment last by one
 - 2. store the new entry in the component data[last]
- To get the next entry:
 - retrieve data[first]
 - increment first by one, so that data[first] is then the entry that used to be second

What is the problem with this plan?

Array Implementation of a Queue (Cont'd)

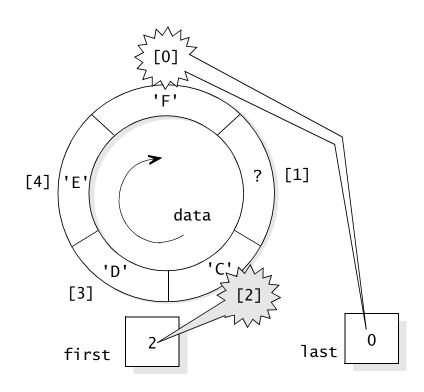
- A straightforward approach for using the freed array locations: Maintain all the queue entries so that first is always equal to 0
 - When data[0] is removed, we move all the entries in the array down one location
- This approach is inefficient: every time we remove an entry from the queue, we must move every entry in the queue
- Another approach: We can simply start reusing the available locations at the front of the array
- Think of this arrangement as if the array were bent into a circle with the first component of the array immediately after the last component
- In this circular arrangement, the free index positions are always "right after" data[last]

Array Implementation of a Queue (Cont'd)



- Circular view of the array
- It may help to actually view the array as bent into a circle, with the final array element attached back to the beginning:

An array used in this way is called a circular array



Array Implementation of a Queue (Cont'd)



Implementation of queue using a circular array:

- data: A private member variable that holds the queue's entries in an array
- The private member variables first and last hold the indexes for the front and the rear of the queue
 - Whenever the queue is non-empty, the entries begin at the location data[first]
 - If the entries reach the end of the array, then they continue at the first location, data[0]
 - In any case, data[last] is the last entry in the queue
- count: A private member variable that records the number of items that are in the queue
 - count will be used to check whether the queue is empty or full

Array Implementation of a Queue (Cont'd)

- The queue class definition uses a helper function called next_index
 - This is a private member function
 - Allows us to easily step through the array, one index after another, with wraparound at the end
 - The reason for declaring next_index is to make the other implementations easier to read
- next_index = (i+1) % CAPACITY

Header File for the Array Version of the Queue Template Class (Cont'd)



```
#ifndef SCU_COEN79_QUEUE1_H
#define SCU COEN79 QUEUE1 H
#include <cstdlib> // Provides size_t
namespace scu coen79 8B
    template <class Item>
    class queue
     public:
        typedef std::size t size type;
        typedef Item value type;
        static const size_type CAPACITY = 30;
       // CONSTRUCTOR
       queue();
```

Header File for the Array Version of the Queue Template Class (Cont'd)



```
// MODIFICATION MEMBER FUNCTIONS
        void pop( );
        void push(const Item& entry);
        // CONSTANT MEMBER FUNCTIONS
        bool empty( ) const { return (count == 0); }
        Item front( ) const;
        size_type size( ) const { return count; }
    private:
        Item data[CAPACITY]; // Circular array
        size_type first;  // Index of item at front of the queue
size_type last;  // Index of item at rear of the queue
        size_type count; // Total number of items in the queue
        // HELPER MEMBER FUNCTION
        size_type next_index(size_type i) const {return (i+1)%CAPACITY;}
    };
                                              When a class requires some small operation that
                                              is implemented as a formula, consider
#include "queue1.template"
                                              implementing the formula with a helper function
#endif
```



```
// TEMPLATE CLASS IMPLEMENTED: queue<Item>
// INVARIANT for the queue class:
// 1. The number of items in the queue is in the member variable count;
// 2. For a non-empty queue, the items are stored in a circular array
// beginning at data[first] and continuing through data[last].
// The array's total capacity is CAPACITY.
// 3. For an empty array, last is some valid index, and first is
// always equal to next index(last).
#include <cassert>
namespace scu coen79 8B {
    template <class Item>
    const typename queue<Item>::size type queue<Item>::CAPACITY;
    template <class Item>
    queue<Item>::queue( )
                                       Satisfies the invariant: For an empty queue,
        count = 0:
                                       last is some valid index, and
        first = 0;
                                       first = next index(last)
        last = CAPACITY - 1;
    }
```

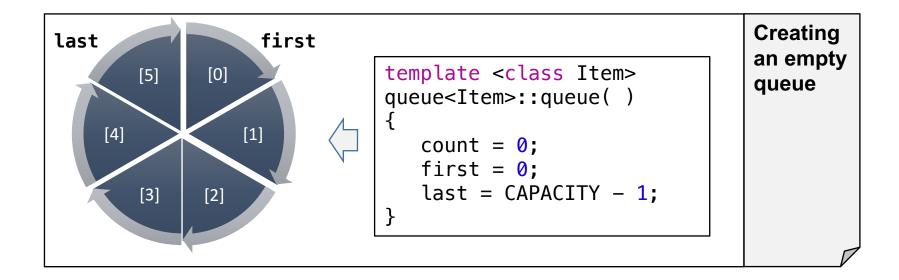


```
template <class Item>
Item queue<Item>::front( ) const
// Library facilities used: cassert
{
    assert(!empty( ));
    return data[first];
}
template <class Item>
void queue<Item>::pop( )
// Library facilities used: cassert
{
    assert(!empty( ));
    first = next index(first);
    --count;
}
```

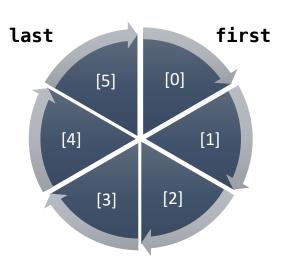


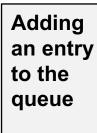
```
template <class Item>
void queue<Item>::push(const Item& entry)
// Library facilities used: cassert
{
    assert(size() < CAPACITY);
    last = next_index(last);
    data[last] = entry;
    ++count;
}</pre>
```







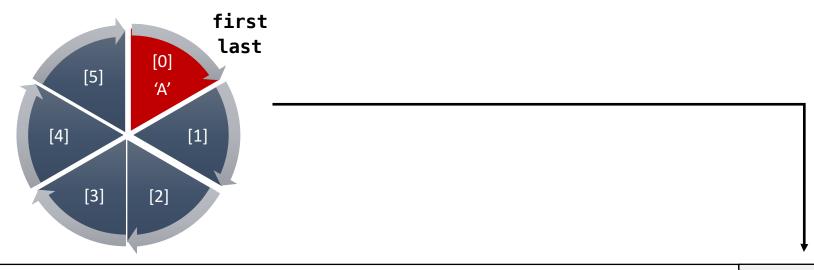


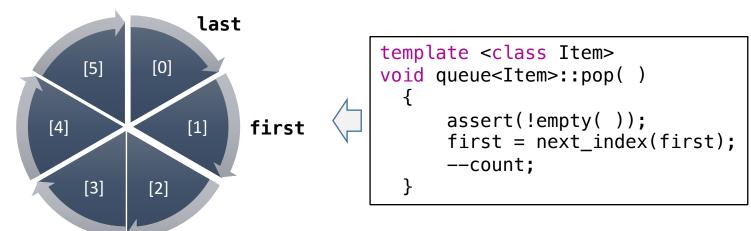


```
first
                                                                      last
template <class Item>
                                                                   [0]
void queue<Item>::push(const Item& entry)
                                                            [5]
                                                                   Ά'
{
    assert(size( ) < CAPACITY);</pre>
                                                         [4]
                                                                      [1]
    last = next_index(last);
    data[last] = entry;
    ++count;
                                                            [3]
                                                                  [2]
```

Implementation of the Array Version of the Queue Template Class (Cont'd)

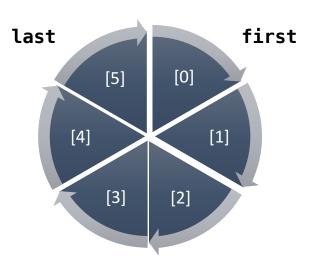






Removing an entry from the queue

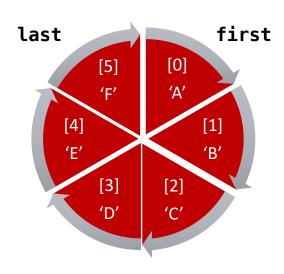




- An empty queue
- first = next_index (last)

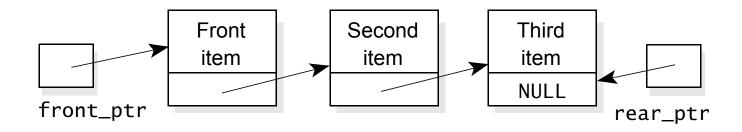
$$count = 0$$

- A full queue
- first = next index (last)



Linked-List Implementation of a Queue

- A queue can also be implemented as a linked list
- One end of the linked list is the front, and the other end is the rear of the queue
- The approach uses two pointers:
 - front ptr: To the first node
 - rear_ptr: To the last node



Header File for the Linked-List Version of the Queue Template Class



```
// FILE: queue2.h (part of the namespace
// TEMPLATE CLASS PROVIDED: queue<Item> (a queue of items)
#ifndef SCU COEN79 QUEUE2 H
                               // Prevent duplicate definition
#define SCU COEN79 QUEUE2 H
#include <cstdlib>
                               // Provides std::size t
#include "node2.h"
                                // Node template class
namespace scu_coen79_8C
    template <class Item>
    class queue
    public:
        // TYPEDEFS
        typedef std::size_t size_type;
        typedef Item value_type;
```

Header File for the Linked-List Version of the Queue Template Class (Cont'd)

```
// CONSTRUCTORS and DESTRUCTOR
         queue();
        queue(const queue<Item>& source);
        ~queue();
        // MODIFICATION MEMBER FUNCTIONS
        void pop( );
        void push(const Item& entry);
       void operator =(const queue<Item>& source);
        // CONSTANT MEMBER FUNCTIONS
        bool empty( ) const { return (count == 0); }
        Item front( ) const;
        size_type size( ) const { return count; }
    private:
        scu_coen79_6B::node<Item> *front_ptr;
        scu_coen79_6B::node<Item> *rear_ptr;
        size_type count;  // Total number of items in the queue
    };
#include "queue2.template" // Include the implementation
#endif
```

Invariant of the Queue Class (Linked-List Version)

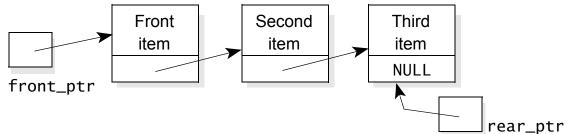


Invariants:

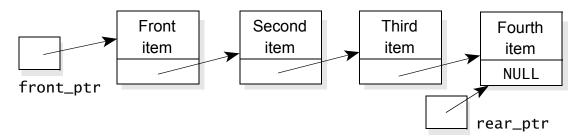
- The number of items in the queue is stored in the member variable count
- The items in the queue are stored in a linked list, with the front of the queue stored at the head node, and the rear of the queue stored at the final node
- 3. Pointers:
 - front_ptr is the head pointer
 - For a non-empty queue, the member variable rear_ptr is the tail pointer of the linked list; for an empty list, we don't care what's stored in rear ptr (as front ptr is NULL)

Implementation Details (Cont'd)

- Push member function. Adds a node at the rear of the queue
- □Example: Suppose we start with three items:



After adding a fourth item, the list would look like this:



The item is added at the end of the list through:

```
list_insert(rear_ptr, entry);
rear_ptr = rear_ptr->link();
```

Implementation Details (Cont'd)

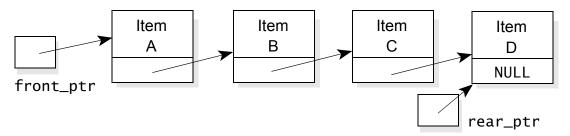
 To add the first item, we need a slightly different approach because the empty list has no rear pointer

```
if (empty())
{ // Insert first entry.
    scu_coen79_6B::list_head_insert(front_ptr, entry);
    rear_ptr = front_ptr;
}
else
{ // Insert an entry that is not the first.
    scu_coen79_6B::list_insert(rear_ptr, entry);
    rear_ptr = rear_ptr->link();
}
```

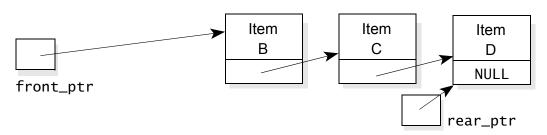
You also need to add one to the count member variable

Implementation Details (Cont'd)

- Pop member function. Removes a node from the front of the queue
- □Example: We start with this queue:



• The pop function will remove the item that is labeled "Item A", when pop returns, the list will have only three items



The implementation of pop uses list_head_remove

Linked-List Version Implementation of the Queue Template Class

```
// FILE: queue2.template
// TEMPLATE CLASS IMPLEMENTED: Queue<Item> (see queue2.h for
// documentation)
// INVARIANT for the Queue class:
// 1. The number of items in the queue is stored in the member variable
// count.
// 2. The items in the queue are stored in a linked list, with the
// front of the gueue stored at the head node, and the rear of the
// queue stored at the final node.
// 3. The member variable front_ptr is the head pointer of the linked
// list of items. For a non-empty queue, the member variable rear ptr
// is the tail pointer of the linked list; for an empty list, we don't
// care what's stored in rear ptr.
```

Note that it is important to document this "Don't Care" situation



```
#include <cassert> // Provides assert
#include "node2.h" // Node template class
namespace scu_coen79_8C
{
    template <class Item>
    queue<Item>::queue( )
                              For an empty list, we don't care
        count = 0:
                              what's stored in rear_ptr
        front ptr = NULL;
    }
    template <class Item>
    queue<Item>::queue(const queue<Item>& source)
    // Library facilities used: node2.h
        count = source.count;
        list copy(source.front ptr, front ptr, rear ptr);
    }
```



```
template <class Item>
queue<Item>::~queue( )
    list clear(front ptr);
}
template <class Item>
void queue<Item>::operator =(const queue<Item>& source)
// Library facilities used: node2.h
    if (this == &source) // Handle self-assignment
        return:
    list_clear(front_ptr);
    list_copy(source.front_ptr, front_ptr, rear_ptr);
    count = source.count;
```



```
template <class Item>
Item queue<Item>::front( ) const
// Library facilities used: cassert
    assert(!empty( ));
    return front_ptr->data( );
}
template <class Item>
void queue<Item>::pop( )
// Library facilities used: cassert, node2.h
    assert(!empty( ));
    list_head_remove(front_ptr);
    --count;
}
```



```
template <class Item>
void queue<Item>::push(const Item& entry)
// Library facilities used: node2.h
    if (empty( ))
    { // Insert first entry.
        list_head_insert(front_ptr, entry);
        rear_ptr = front_ptr;
    }
    else
        // Insert an entry that is not the first.
        list_insert(rear_ptr, entry);
        rear_ptr = rear_ptr->link( );
    }
    ++count;
```

Implementation of the Array Version of the Queue Template Class (Cont'd)



 What are the iterator invalidation rules for the linked-list version of the queue class?

STL deque Class

Implementing the STL deque Class



- A variation of queue is a double-ended queue, also called a deque
- Entries can be quickly inserted and removed at both ends
- This differs from:
 - A stack (which uses only one end)
 - An ordinary queue (in which items enter at one end and leave at the other)

Implementing the STL deque Class

```
template< class T, class Allocator = std::allocator<T> >
class deque;
```

- std::deque (double-ended queue) is an indexed sequence container that allows fast insertion and deletion at both its beginning and its end
- Insertion and deletion at either end of a deque never invalidates pointers or references to the rest of the elements
- As opposed to std::vector, the elements of a deque are not stored contiguously
 - Typical implementations use a sequence of individually allocated fixedsize arrays (we will show the implementation later)
- Expansion of a deque is cheaper than the expansion of a std::vector because it does not involve copying of the existing elements to a new memory location

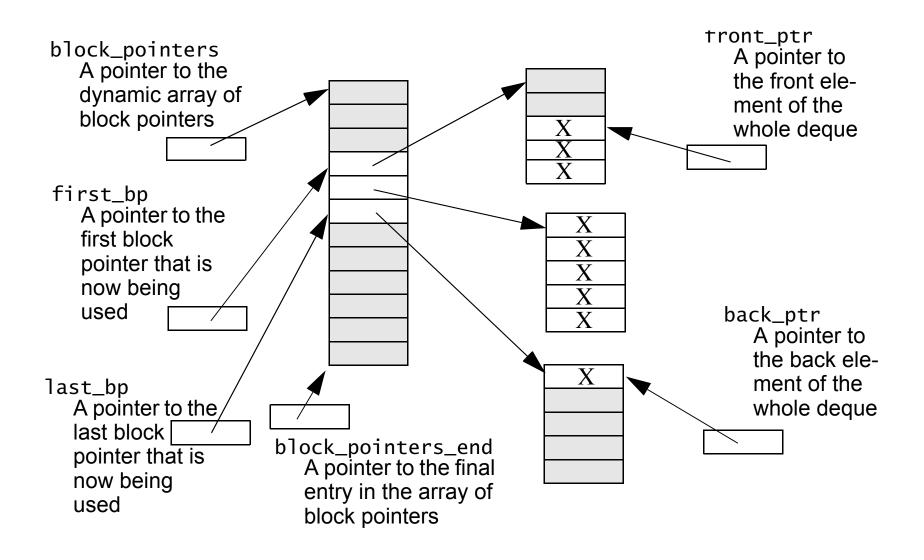


```
#include <iostream>
#include <deque>
int main()
{
    // Create a deque containing integers
    std::deque<int> d = \{1, 2, 3, 4\};
    // Add an integer to the beginning and end of the deque
    d.push front(0);
    d.push back(5);
    // Iterate and print values of deque
    for(std::deque<int>::iterator it = d.begin(); it != d.end(); ++it)
                                                               Output:
        std::cout << *it << '\n':
                                                               0
```



- STL uses a more complicated deque implementation
- A dynamic array of a fixed size called block is initially allocated to hold the elements
- If more space is needed, the block is not resized, instead, a second block of the same fixed size is allocated
- More and more blocks are allocated as needed, and pointers to all these blocks are kept together in a separate array of pointers







- The deque of the previous slide is using 3 blocks
- Each block is a dynamic array containing a constant number of items (five in our example, although a real implementation would have a larger block size)
- The shaded array locations at the start of the first block and the end of the last block are not currently being used
- The dynamic array on the left is an array of pointers to the blocks
 - Currently capable of holding up to 12 pointers, although only 3 are being used now
 - If more than 12 blocks are needed, then that array of pointers can be expanded



- The complexity (efficiency) of common dequeu operations:
 - Random access: constant O(1)
 - Insertion or removal of elements at the end or beginning: constant O(1)
 - Insertion or removal of elements: linear O(n)



- deque provides a functionality similar to vectors, but with efficient insertion and deletion of elements also at the beginning of the sequence, and not only at its end
- deques are not guaranteed to store all its elements in contiguous storage locations
 - vectors use a single array that needs to be occasionally reallocated for growth
 - The elements of a deque can be scattered in different chunks of storage
- For operations that involve frequent insertion or removals of elements at positions other than the beginning or the end, deques perform worse and have less consistent iterators and references than lists and forward lists

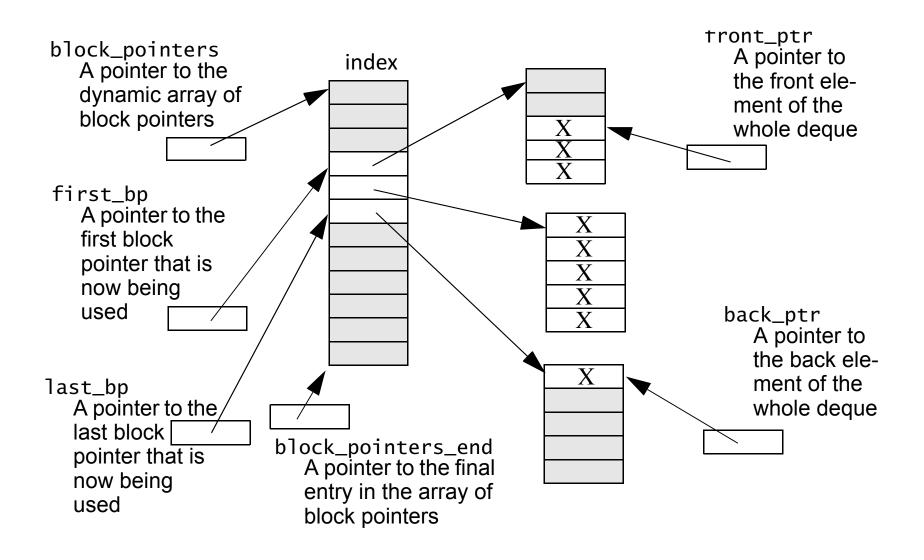
A Possible Data Structure for the STL deque Class (Cont'd)



The private member pointers might be declared in this way:

```
// Number of value_type items in each block
static const size t block size = 5;
// The elements in the deque
typedef int value type;
// A pointer to a dynamic array of value_type items
typedef value type* vtp;
// A pointer to the dynamic array of block pointers
vtp* block pointers;
// A pointer to the final entry in the array of block pointers
vtp* block_pointers_end;
// A pointer to the first block pointer that's now being used
vtp* first bp;
// A pointer to the last block pointer that's now being used
vtp* last bp;
vtp front_ptr; // A pointer to the front element of the whole deque
vtp back ptr; // A pointer to the back element of the whole deque
```





Pointer Arithmetic used in the Implementation of the deque Class



Use pointer arithmetic in the implementation:

- If p is a pointer into an array and n is an integer, then the expression p+n gives a new pointer that is n elements beyond *p
- In this case, the expression ++p changes p so that it points to the next element in the array, and --p changes p so that it points to the previous element
- If p and q are both pointers into the same array, then the expression q p gives an integer that indicates the distance between q and p
- \square Example: If *q is the element after *p, then q p is 1

Constructor



```
template <class Item>
deque<Item>::deque (int init bp array size, int init block size)
{
        bp array size = init bp array size;
        block size = init block size;
        //set a pointer the start of the array of block pointers
        block pointers = new value type* [bp array size];
        for (size type index = 0; index < bp array size; ++index)</pre>
            block pointers[index] = NULL;
        }
        //set a pointer the end of the array of block pointers
        block pointers end = block pointers + (bp_array_size - 1);
        first bp = last bp = NULL;
        front ptr = back ptr = NULL;
    }
```

Destructor



```
emplate <class Item>
deque<Item>::~deque ()
{
   for (size type index = 0; index < bp array size; ++index)</pre>
        if (block pointers[index] != NULL)
                delete [] block pointers[index];
    delete [] block pointers;
    first bp = last bp = NULL;
    block pointers end = block pointers = NULL;
    front ptr = back ptr = NULL;
```

Clear



```
template <class Item>
void deque<Item>::clear ()
   for (size type index = 0; index < bp array size; ++index)</pre>
        delete [] block pointers[index];
        block pointers[index] = NULL;
    }
    first bp = last bp = NULL;
    front ptr = back ptr = NULL;
```

Implementation of the deque's pop_back Function



```
void mydeque::pop_back( )
{
   // An empty deque has a NULL back_ptr:
   assert (back_ptr != NULL);
```

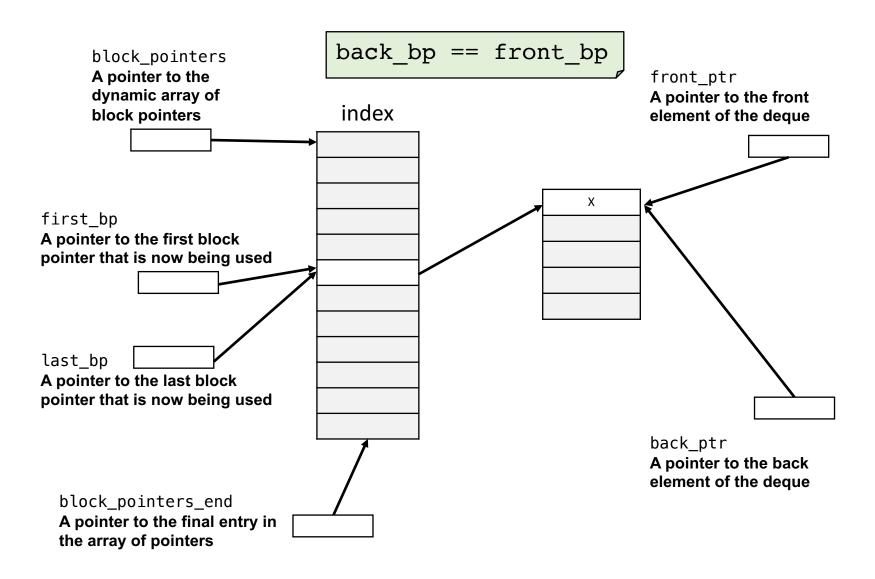
Case 1: There is just one block with just one element, so delete it, and reset things back to the start

See the next slide

```
if (back_ptr == front_ptr)
  {
    clear( );
}
```

Implementation of the deque's pop_back Function





Implementation of the deque's pop_back Function



Case 2: back_ptr is pointing to the first element of the last block in the deque:

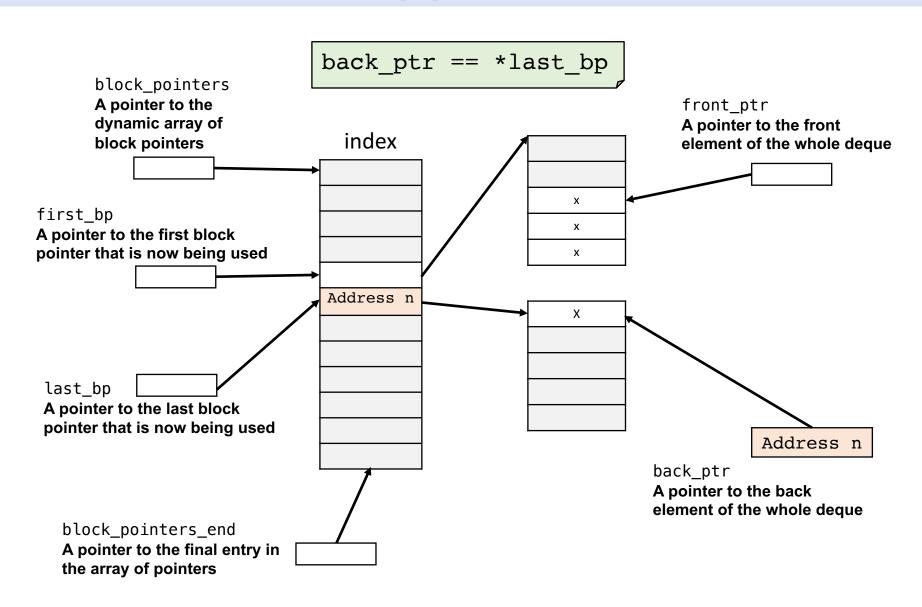
- Remove the entire last block. Note that this will call the destructor for each item in the block: delete [] back_ptr;
- The last block pointer that we are using is now one spot earlier in the array of block pointers: --last_bp;
- The new back element is now the last element in the last block

```
else if (back_ptr == *last_bp)
{
    delete [] *last_bp;
    *last_bp = NULL;
    --last_bp;
    back_ptr = (*last_bp) + (BLOCK_SIZE - 1);
}
```

See the next slide

Implementation of the deque's pop_back Function





Implementation of the deque's pop_back Function



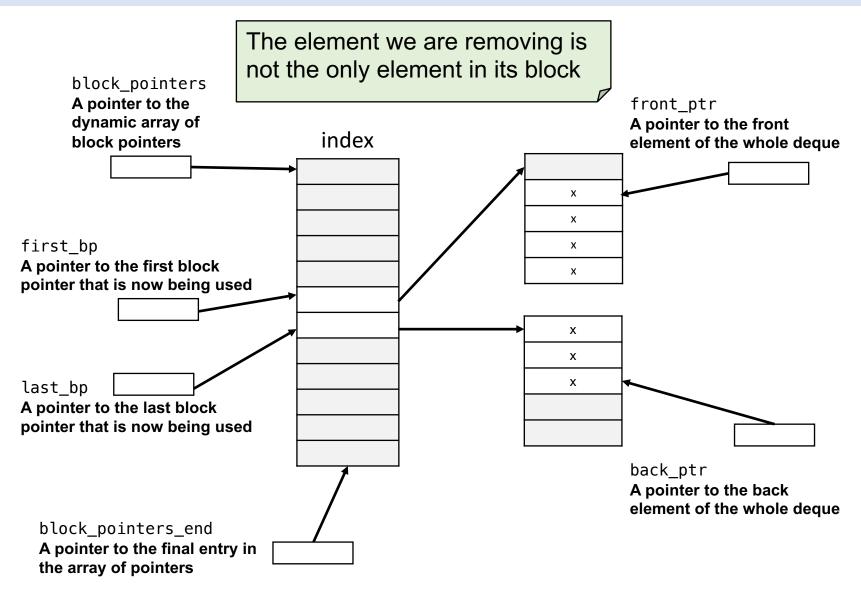
Case 3: The element we are removing is not the only element in its block, so we just move the back_ptr backward

```
else
{
     --back_ptr;
}
```

See the next slide

Implementation of the deque's pop_back Function





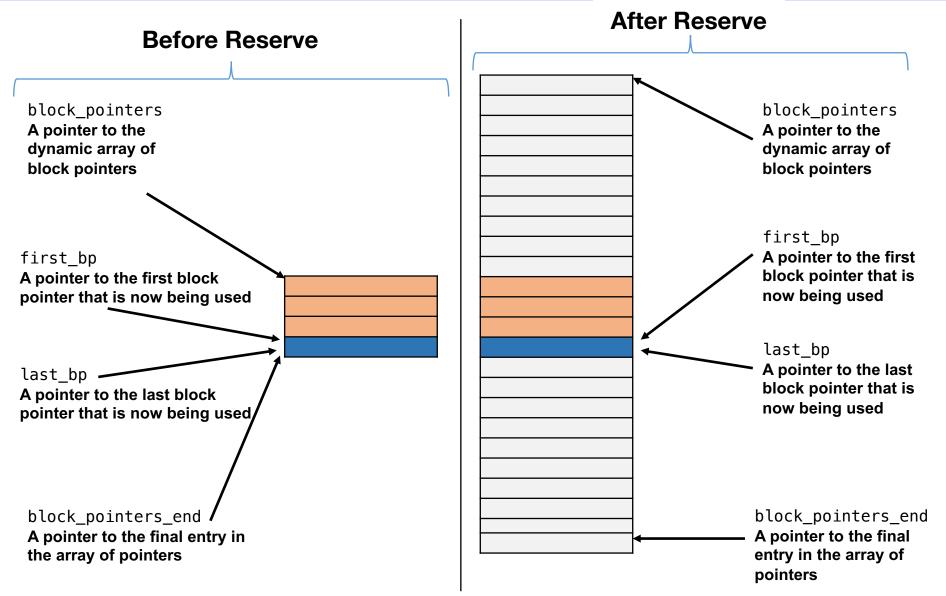
Reserve



- To increase the size of the deque (i.e., reserve function)
 - We plan to increase the size of the deque by 20 X BLCOK_SIZE
 - Therefore, we need to increase the size of the array of block pointers by 20
 - We also copy the existing array of block pointers to the middle of the new array of block pointers to improve the flexibility of adding at the two ends of the deque

Reserve

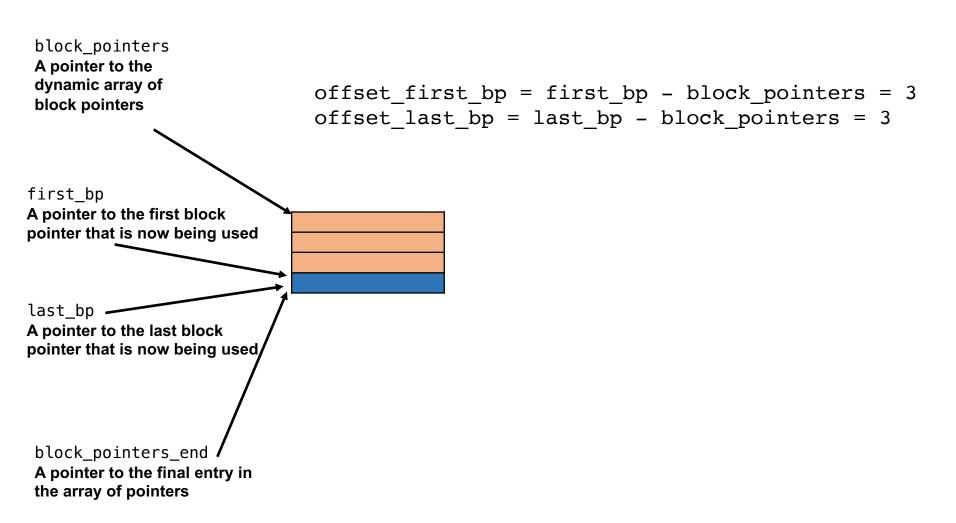




Increasing the Size of deque

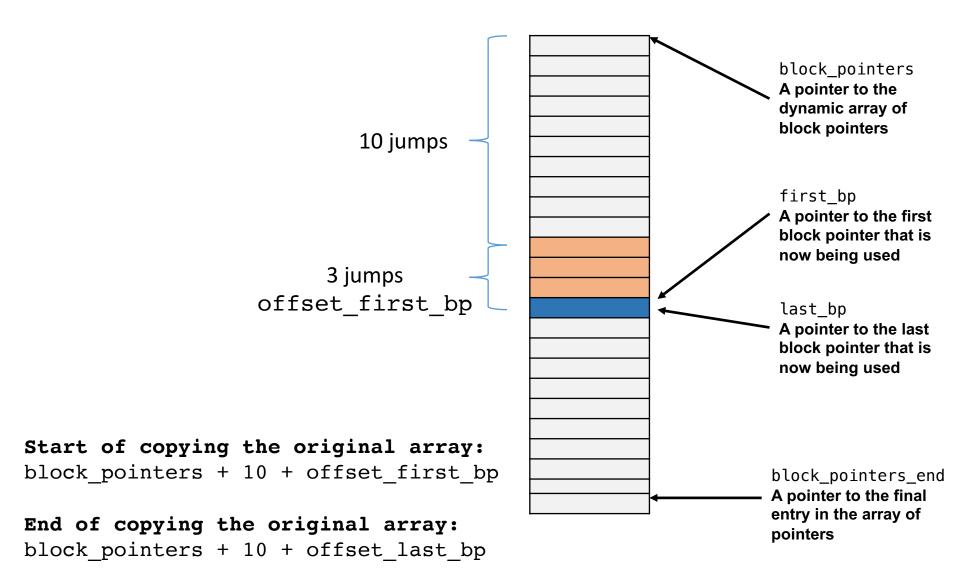


Before Reserve



Increasing the Size of deque





Reserve



```
template <class Item>
void deque<Item>::reserve() {
   size type newSize = bp array size + 20;
   value type** new block pointers = new value type* [newSize];
   for (size type index = 0; index < newSize; ++index)</pre>
        new block pointers[index] = NULL;
   size type offsett first bp = first bp - block pointers;
   size type offsett last bp = last bp - block pointers;
   std::copy(first bp, last bp + 1,
             new block pointers + 10 + offsett first bp);
        delete [] block pointers;
        block pointers = new block pointers;
        bp array size = newSize;
        block pointers end = block pointers + bp array size - 1;
        first bp = block pointers + offsett first bp + 10;
        last bp = block pointers + offsett last bp + 10;
}
```

Iterator Invalidation Rules for STL's deque



- Note that an iterator pointing to an item of a deque cannot be implemented by only using a pointer to an item
- The iterator needs to know which array it is part of, and where the index is, so it can find the next/previous arrays

Insertion:

- All iterators and references are invalidated because existing elements must be shifted
- If inserted member is at the front or back of the deque, all iterators are invalidated, but references to elements are unaffected
 - It fills out the first/last array, and then adds another one when necessary, so it never needs to move existing elements
 - However, the index vector might be copied and reallocated when resized

Iterator Invalidation Rules for STL's deque



Erasure:

 All iterators and references are invalidated, unless the erased members are at the front or back of the deque (in which case only iterators and references to the erased members are invalidated)

Uses for Queues (Cont'd)



- Queues are frequently used in simulation programs
 - □ Example: A program to simulate the traffic at an intersection might use a software queue to simulate the real-life situation of a growing line of automobiles waiting for a traffic light to change from red to green
- Queues also appear in computer system software, such as the operating system that runs on your PC
 - □Example: For buffering input characters
- In a computer system in which more than one process or component uses a single resource, a queue is often used so that the processes or components wait in line and are served on a "first-come, first-served" basis

Programming Example: Recognizing Palindromes



- Palindrome is a string that reads the same forward and backward
- □Example: "radar" is a palindrome
- □A more complicated example: Able was I ere I saw Elba
- Suppose we want a program to read a line of text and tell us if the line is a palindrome
- We can do this by using: a stack and a queue
- We will read the line of text into both a stack and a queue, and then
 write out the contents of the stack and the contents of the queue
- The line that is written using the queue is written forward, and the line that is written using the stack is written backward
- Now, if those two output lines are the same, then the input string must be a palindrome



```
// FILE: pal.cxx
// Program to test whether an input line is a palindrome. Spaces,
// punctuation, and the difference between upper- and lowercase are
// ignored.
#include <cassert> // Provides assert
#include <cctype> // Provides isalpha, toupper
#include <cstdlib> // Provides EXIT_SUCCESS
#include <iostream> // Provides cout, cin, peek
#include <queue> // Provides the queue template class
#include <stack> // Provides the stack template class
using namespace std;
int main( )
   queue<char> q;
    stack<char> s;
    char letter;
    queue<char>::size type mismatches = 0; // Mismatches between queue
                                          // and stack
```



```
cout << "Enter a line and I will see if it's a palindrome:" << endl;</pre>
while (cin.peek( ) != '\n')
  {
                                         returns true if its single argument is
      cin >> letter;
                                         one of the alphabetic characters
      if (isalpha(letter))
      {
           q.push(toupper(letter));
           s.push(toupper(letter));
                                         converts a lowercase letter to
                                         corresponding uppercase letter and
                                         returns this value
while ((!q.empty( )) && (!s.empty( )))
  {
      if (q.front() != s.top())
           ++mismatches;
      q.pop();
      s.pop();
```

```
if (mismatches == 0)
    cout << "That is a palindrome." << endl;
else
    cout << "That is not a palindrome." << endl;
return EXIT_SUCCESS;
}</pre>
```

A Program to Recognize Palindromes (Cont'd)

Sample Dialogues from the Palindrome Program

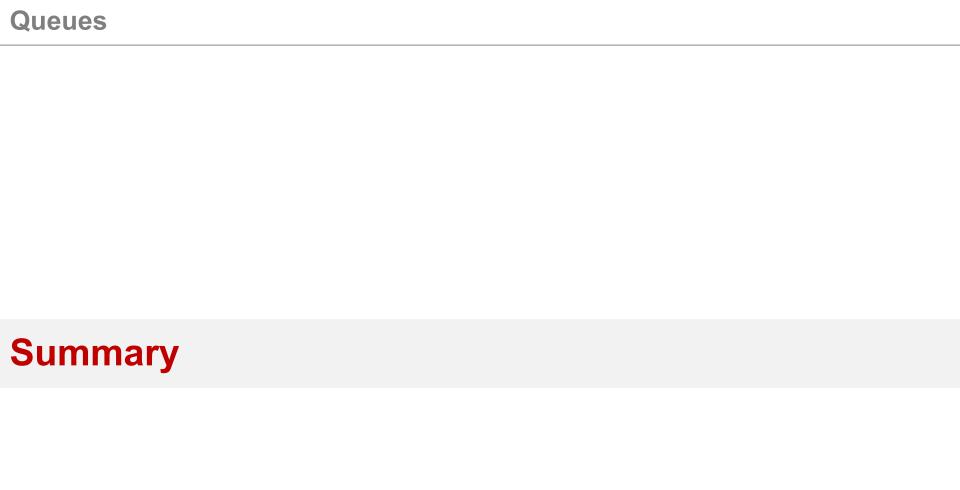
First Sample Dialogue

```
Enter a line and I will see if it's a palindrome: Straw? No, too stupid a fad. I put soot on warts. That is a palindrome.
```

Second Sample Dialogue

```
Enter a line and I will see if it's a palindrome: Able were you ere you saw Elba. That is not a palindrome.
```

- Our program also ignores spaces and punctuation, requiring only that the letters on the line read the same forward and backward
- □ Example: You might not immediately recognize the following as a palindrome: Straw? No, too stupid a fad. I put soot on warts
- Our program ignores blanks and punctuation, so, according to our program, the above is a palindrome
- The function, called isalpha, returns true if its single argument is one of the alphabetic characters
 - From <cctype>



Summary

- A queue is a First-In/First-Out data structure
- A queue can be used to buffer data that is being sent from a fast computer component to a slower component
- Queues have many other applications: in simulation programs, operating systems, and elsewhere
- A queue can be implemented as a partially filled circular array
- A queue can be implemented as a linked list
- When implementing a queue, you need to keep track of both ends of the list
- A deque (or "double-ended queue") allows quick removal and insertion of elements from both ends
 - It can be implemented with a circular array, a doubly linked list or more complex structures of pointers

References

- Data Structures and Other Objects Using C++, Michael Main, Walter Savitch, 4th Edition
- 2) Data Structures and Algorithm Analysis in C++, by Mark A. Weiss, $\mathbf{4}^{\text{TH}}$ Edition
- 3) C++: Classes and Data Structures, by Jeffrey Childs
- 4) http://en.cppreference.com
- 5) http://www.cplusplus.com
- 6) https://isocpp.org