Wanat_Assignment2_final

July 7, 2019

```
In [1]: # Jump-Start for the Bank Marketing Study
        # as described in Marketing Data Science: Modeling Techniques
        # for Predictive Analytics with R and Python (Miller 2015)
        # jump-start code revised by Thomas W. Milller (2018/10/07)
        # Scikit Learn documentation for this assignment:
        # http://scikit-learn.org/stable/auto examples/classification/
          plot_classifier_comparison.html
        # http://scikit-learn.org/stable/modules/generated/
            sklearn.naive\_bayes.BernoulliNB.html\#sklearn.naive\_bayes.BernoulliNB.score
        # http://scikit-learn.org/stable/modules/generated/
            sklearn.linear_model.LogisticRegression.html
        # http://scikit-learn.org/stable/modules/model_evaluation.html
        # http://scikit-learn.org/stable/modules/generated/
        # sklearn.model_selection.KFold.html
        # prepare for Python version 3x features and functions
        # comment out for Python 3.x execution
        # from __future__ import division, print_function
        # from future_builtins import ascii, filter, hex, map, oct, zip
        # seed value for random number generators to obtain reproducible results
        RANDOM SEED = 1
        # import base packages into the namespace for this program
        import numpy as np
        import pandas as pd
        import pandas_profiling
        import matplotlib
        import matplotlib.pyplot as plt # static plotting
        import seaborn as sns # pretty plotting, including heat map
        from sklearn.linear_model import LogisticRegression
        from sklearn.model_selection import train_test_split
        from sklearn import metrics
        from sklearn.metrics import classification_report
        from sklearn.metrics import roc_curve
```

```
from sklearn.preprocessing import binarize
from sklearn.metrics import precision_recall_curve
from sklearn.naive_bayes import BernoulliNB
#from sklearn.cross_validation import cross_val_score
from sklearn.model_selection import cross_val_score
import math
```

0.1 Defined functions

```
In [2]: # correlation heat map setup for seaborn
        def corr_chart(df_corr):
            corr=df_corr.corr()
            #screen top half to get a triangle
            top = np.zeros_like(corr, dtype=np.bool)
            top[np.triu_indices_from(top)] = True
            fig=plt.figure()
            fig, ax = plt.subplots(figsize=(12,12))
            sns.heatmap(corr, mask=top, cmap='coolwarm',
                center = 0, square=True,
                linewidths=.5, cbar_kws={'shrink':.5},
                annot = True, annot_kws={'size': 9}, fmt = '.3f')
           plt.xticks(rotation=45) # rotate variable labels on columns (x axis)
            plt.yticks(rotation=0) # use horizontal variable labels on rows (y axis)
           plt.title('Correlation Heat Map')
           plt.savefig('plot-corr-map.pdf',
                bbox_inches = 'tight', dpi=None, facecolor='w', edgecolor='b',
                orientation='portrait', papertype=None, format=None,
                transparent=True, pad_inches=0.25, frameon=None)
        np.set_printoptions(precision=3)
In [3]: # define a function to return model metrics for evaluation
        def model_metrics(y_known, y_pred):
            y_test = y_known
            y_pred_class = y_pred
            confusion = metrics.confusion_matrix(y_test, y_pred_class)
           TP = confusion[1, 1]
            TN = confusion[0, 0]
           FP = confusion[0, 1]
           FN = confusion[1, 0]
            accuracy = metrics.accuracy_score(y_test, y_pred_class)
            class_error = 1 - metrics.accuracy_score(y_test, y_pred_class)
            sensitivity = metrics.recall_score(y_test, y_pred_class)
            specificity = TN / (TN + FP)
            false_positive_rate = FP / float(TN + FP)
            precision = TP / float(TP + FP)
            f1_score = metrics.f1_score(y_test, y_pred_class)
```

```
F1 = 2*precision*sensitivity/(precision + sensitivity)
            print('The model metrics are:',
                 '\naccuracy:', accuracy,
                 '\nclassification error:', class_error,
                 '\nsensitivity:', sensitivity,
                 '\nspecificity:', specificity,
                 '\nfalse positive rate:', false positive rate,
                 '\nprecision:', precision,
                  '\nF1 score:', f1 score,
                   ' \ nF1 \ by \ hand:', \ F1,
        #
                 '\nconfusion matrix:')
            return(confusion)
In [4]: # define a function that accepts a threshold and
        # prints sensitivity and specificity
        def evaluate threshold(threshold):
            print('Sensitivity:', tpr[thresholds > threshold][-1])
            print('Specificity:', 1 - fpr[thresholds > threshold][-1])
In [5]: # define a function that accepts the fpr and tpr values
        # from the roc_curve function and plot the ROC curve
        def plot_roc_curve(fpr, tpr, label=None):
            plt.plot(fpr, tpr, linewidth=2, label=label)
            plt.plot([0, 1], [0, 1], 'k--')
            plt.axis([0, 1, 0, 1])
            plt.xlabel('False Positive Rate')
            plt.ylabel('True Positive Rate')
            plt.title('ROC curve for response')
In [6]: # define a function that accepts the recall and precision values
        # from the precision_recall_curve function and plot the PR curve
        def plot_pr_curve(recall, precision, label=None):
            plt.plot(recall, precision, linewidth=2, label=label)
            plt.plot([0, 1], [0, 1], 'k--')
            plt.axis([0, 1, 0, 1])
            plt.xlabel('Recall')
            plt.ylabel('Precision')
            plt.title('PR curve for response')
In [7]: # define a function that accepts the scores from the cross validation
        # and print the scores, mean, and standard deviation
        def display_scores(scores):
            print("Scores:", scores)
            print("Mean:", scores.mean())
            print("Standard deviation:", scores.std())
```

0.2 Import data set and prepare for analysis

```
In [8]: # initial work with the smaller data set
        bank = pd.read_csv('bank.csv', sep = ';') # start with smaller data set
        # examine the shape of original input data
        print(bank.shape)
(4521, 17)
In [9]: #total number of NaN values in each column
        bank.isnull().sum()
Out [9]: age
                     0
        job
                     0
        marital
                     0
        education
                     0
        default
                     0
        balance
                     0
                     0
        housing
        loan
                     0
                     0
        contact
        day
                     0
        month
                     0
        duration
                     0
        campaign
                     0
                     0
        pdays
        previous
                     0
                     0
        poutcome
        response
        dtype: int64
In [10]: print(bank.response.head())
0
     no
1
     no
2
     no
3
     no
4
Name: response, dtype: object
In [11]: display(bank.head())
                               education default
                                                  balance housing loan
   age
                job marital
    30
                                                      1787
0
         unemployed married
                                 primary
                                                                no
                                              no
                                                                     no
1
    33
           services married
                               secondary
                                              no
                                                      4789
                                                               yes
                                                                    yes
2
    35
         management
                      single
                                tertiary
                                                      1350
                                                               yes
                                              no
                                                                     no
         management married
                                tertiary
                                                     1476
                                              no
                                                               yes yes
```

```
blue-collar married secondary
                                                no
                                                           0
                                                                 yes
                                                                        no
             day month
                         duration
                                    campaign
                                                      previous poutcome response
    contact
                                               pdays
  cellular
               19
                                79
                                            1
                                                  -1
                                                              0
                                                                 unknown
                    oct
   cellular
                               220
                                            1
                                                              4
                                                                 failure
1
               11
                    may
                                                 339
                                                                                no
2
   cellular
                               185
                                            1
                                                 330
                                                              1
                                                                 failure
               16
                    apr
                                                                                no
    unknown
                                                                 unknown
3
                3
                    jun
                               199
                                            4
                                                  -1
                                                              0
                                                                                no
    unknown
                5
                    may
                               226
                                                  -1
                                                                 unknown
                                                                                nο
In [12]: bank.describe()
Out[12]:
                                    balance
                                                       day
                                                               duration
                                                                             campaign
                          age
                                                                          4521.000000
                 4521.000000
                                4521.000000
                                              4521.000000
                                                            4521.000000
         count
         mean
                   41.170095
                                1422.657819
                                                15.915284
                                                             263.961292
                                                                             2.793630
                                                             259.856633
         std
                   10.576211
                                3009.638142
                                                 8.247667
                                                                             3.109807
         min
                   19.000000
                               -3313.000000
                                                 1.000000
                                                               4.000000
                                                                             1.000000
         25%
                   33.000000
                                  69.000000
                                                 9.000000
                                                             104.000000
                                                                             1.000000
         50%
                   39.000000
                                 444.000000
                                                16.000000
                                                             185.000000
                                                                             2.000000
         75%
                   49.000000
                                1480.000000
                                                21.000000
                                                             329.000000
                                                                             3.000000
                   87.000000
                               71188.000000
         max
                                                31.000000
                                                            3025.000000
                                                                            50.000000
                       pdays
                                  previous
                               4521.000000
                 4521.000000
         count
         mean
                   39.766645
                                  0.542579
         std
                  100.121124
                                  1.693562
                   -1.000000
                                  0.000000
         min
         25%
                   -1.000000
                                  0.000000
         50%
                   -1.000000
                                  0.000000
         75%
                   -1.000000
                                  0.000000
         max
                  871.000000
                                 25.000000
In [13]: bank.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4521 entries, 0 to 4520
Data columns (total 17 columns):
             4521 non-null int64
age
job
             4521 non-null object
             4521 non-null object
marital
             4521 non-null object
education
default
             4521 non-null object
             4521 non-null int64
balance
             4521 non-null object
housing
             4521 non-null object
loan
contact
             4521 non-null object
day
             4521 non-null int64
month
             4521 non-null object
```

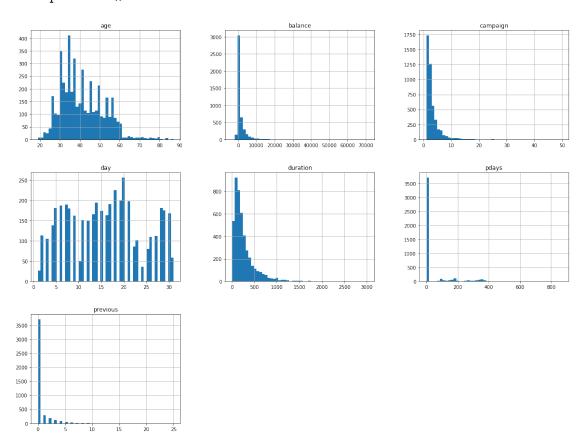
4521 non-null int64

duration

campaign 4521 non-null int64
pdays 4521 non-null int64
previous 4521 non-null int64
poutcome 4521 non-null object
response 4521 non-null object
dtypes: int64(7), object(10)

memory usage: 600.5+ KB

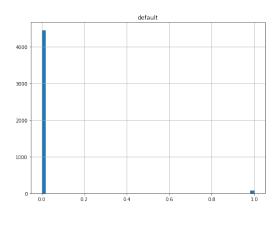
In [14]: %matplotlib inline
 bank.hist(bins=50, figsize=(20,15))
 plt.savefig('bank_hist.pdf')
 plt.show()

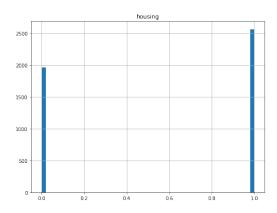


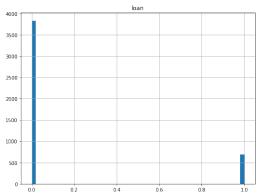
(4521, 17)

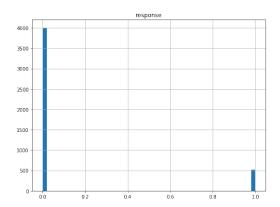
```
In [16]: # look at the list of column names, note that y is the response
         list(bank.columns.values)
Out[16]: ['age',
          'job',
          'marital',
          'education',
          'default',
          'balance',
          'housing',
          'loan',
          'contact',
          'day',
          'month',
          'duration',
          'campaign',
          'pdays',
          'previous',
          'poutcome',
          'response']
In [17]: # look at the beginning of the DataFrame
         bank.head()
Out[17]:
            age
                         job marital education default balance housing loan
         0
             30
                  unemployed married
                                          primary
                                                               1787
                                                       no
                                                                        no
                                                                              no
         1
             33
                    services
                              married secondary
                                                       no
                                                              4789
                                                                        yes
                                                                             yes
         2
             35
                  management
                               single
                                         tertiary
                                                               1350
                                                       no
                                                                        yes
                                                                              no
         3
             30
                  management married
                                         tertiary
                                                       no
                                                               1476
                                                                        yes
                                                                             yes
             59 blue-collar married secondary
                                                                 0
                                                                        yes
                                                       no
                                                                              no
                                 duration campaign pdays previous poutcome response
                      day month
             contact
                                       79
         0 cellular
                       19
                                                         -1
                                                                    0 unknown
                            oct
                                                   1
                                                                                      no
         1 cellular
                                       220
                                                        339
                       11
                            may
                                                   1
                                                                    4 failure
                                                                                      no
         2 cellular
                                                        330
                                                                       failure
                       16
                            apr
                                       185
                                                   1
                                                                    1
                                                                                      no
         3
             unknown
                        3
                            jun
                                       199
                                                   4
                                                         -1
                                                                       unknown
                                                                                      no
             unknown
                        5
                                       226
                                                   1
                                                         -1
                                                                       unknown
                            may
                                                                                      no
In [18]: # mapping function to convert text no/yes to integer 0/1
         convert_to_binary = {'no' : 0, 'yes' : 1}
         # define binary variable for having credit in default
         default = bank['default'].map(convert_to_binary)
         # define binary variable for having a mortgage or housing loan
         housing = bank['housing'].map(convert_to_binary)
         # define binary variable for having a personal loan
         loan = bank['loan'].map(convert_to_binary)
```

```
# define response variable to use in the model
         response = bank['response'].map(convert_to_binary)
In [19]: # gather three explanatory variables and response into a numpy array
         # here we use .T to obtain the transpose for the structure we want
         model_data = np.array([np.array(default), np.array(housing), np.array(loan),
             np.array(response)]).T
         # examine the shape of model_data, which we will use in subsequent modeling
         print(model_data.shape)
         # the rest of the program should set up the modeling methods
         # and evaluation within a cross-validation design
(4521, 4)
In [20]: model_data_df = pd.DataFrame(model_data)
         model_data_df.columns = ['default', 'housing', 'loan', 'response']
In [21]: model_data_df.head()
Out [21]:
            default housing loan response
                           0
         0
                  0
                                 0
                                           0
         1
                  0
                           1
                                 1
         2
                  0
                           1
                                 0
                                           0
         3
                  0
                           1
                                 1
                                           0
         4
                           1
                                 0
                                           0
                  0
In [22]: model_data_df.hist(bins=50, figsize=(20,15))
         plt.savefig('model_data_df_hist.pdf')
        plt.show()
```









```
In [23]: # value counts of the response variable
     # there is a low rate of subscription to a term deposit
     # only 521 clients have a term deposit
     model_data_df.response.value_counts()
```

Out[23]: 0 4000 1 521

Name: response, dtype: int64

In [24]: #split data and response

model_data_df_X = model_data_df.drop('response', axis=1)
model_data_df_y = model_data_df.response.copy()

In [25]: model_data_df_X.head()

default housing Out[25]: loan

```
In [26]: model_data_df_y.head()
Out[26]: 0
              0
              0
         2
              0
         3
              0
              0
         Name: response, dtype: int64
   Split the data into train and test sets
In [27]: #from sklearn.model_selection import train_test_split
         X_train, X_test, y_train, y_test = train_test_split(
             model_data_df_X, model_data_df_y, test_size=0.2, random_state=42)
0.4 Logistic Regression Model, C = 100
In [28]: # Create a logistic regression model on the data
         # C is the hyperparameter controlling the regularization
         # strength of a Scikit-Learn LogisticRegression model.
         # The higher the value of C, the less the model is regularized.
         # Instantiate model
         log_reg100 = LogisticRegression(C=100)
         # Fit the model
         log_reg100.fit(X_train, y_train)
Out[28]: LogisticRegression(C=100, class_weight=None, dual=False, fit_intercept=True,
                   intercept_scaling=1, max_iter=100, multi_class='ovr', n_jobs=1,
                   penalty='12', random_state=None, solver='liblinear', tol=0.0001,
                   verbose=0, warm_start=False)
In [29]: # make predictions for the testing set
         y_predictions100 = log_reg100.predict(X_test)
In [30]: # look at the first 10 entries for predictions
         y_predictions100[0:10]
Out[30]: array([0, 0, 0, 0, 0, 0, 0, 0, 0])
In [31]: # look at the first 10 entries for the true values
         y_test[0:10]
Out[31]: 2398
         800
         2288
                 0
         2344
```

```
3615
                 0
         3548
                 0
         1115
                 0
         4053
                 0
         838
                 0
         4141
         Name: response, dtype: int64
In [32]: # make predicted probabilities for the predictions
         y_predict_prob100 = log_reg100.predict_proba(X_test)
In [33]: # Look at the first ten rows of predicted probabilities
         # of response class membership.
         # The first column is the predicted probability that the
         # observation is a member of class 0.
         # The second column is the predicted probability that the
         # observation is a member of class 1.
         y_predict_prob100[0:10]
Out[33]: array([[0.871, 0.129],
                [0.831, 0.169],
                [0.831, 0.169],
                [0.909, 0.091],
                [0.831, 0.169],
                [0.831, 0.169],
                [0.909, 0.091],
                [0.831, 0.169],
                [0.831, 0.169],
                [0.831, 0.169]])
In [34]: # the first argument is true values,
         # the second argument is predicted values
         # this produces a 2x2 numpy array (matrix)
         confusion100 = metrics.confusion_matrix(y_test, y_predictions100)
         print(confusion100)
[[807
        0]
 [ 98
        0]]
In [35]: # precision, recall, F1 score, and count of response variable
         # of logistic regression model, C =100 when threshold set to 0.5
         print(classification_report(y_test, y_predictions100))
             precision
                          recall f1-score
                                             support
```

```
0 0.89 1.00 0.94 807
1 0.00 0.00 0.00 98
avg / total 0.80 0.89 0.84 905
```

/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn

0.5 Adjusting the classification threshold

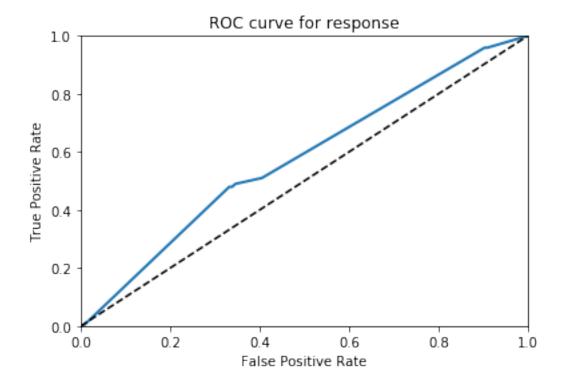
print(confusion100)

```
In [36]: # store the predicted probabilities for class 1 of the response
         # for the logistic regression, C = 100 model
         y_pred_prob100_class1 = log_reg100.predict_proba(X_test)[:,1]
In [37]: # look at the first ten entries for predicted
         # probabilities for class 1
         y_pred_prob100_class1[0:10]
Out[37]: array([0.129, 0.169, 0.169, 0.091, 0.169, 0.169, 0.091, 0.169, 0.169,
                0.169])
In [38]: # the default threshold for predicted probabilities to be classified
         # as 0 or 1 is 0.5
         # let's see what would happen if the default is set to 0.1
         # predict response if the predicted probability is greater than 0.1
         # it will return 1 for all values above 0.1 and 0 otherwise
         # results are 2D so we slice out the first column
         y_pred_class100 = binarize(y_pred_prob100_class1.reshape(-1, 1), 0.1)
In [39]: # print the first 10 predicted classes with the lower threshold
         y pred class100[0:10]
Out[39]: array([[1.],
                [1.],
                [1.],
                [0.],
                [1.],
                [1.],
                [0.],
                [1.],
                [1.],
                [1.]])
In [40]: # previous confusion matrix (default threshold of 0.5)
```

```
[[807
       0]
 [ 98
       0]]
In [41]: # new confusion matrix (threshold set to 0.1)
         confusion100_threshold1 = metrics.confusion_matrix(y_test, y_pred_class100)
        print(confusion100_threshold1)
[[528 279]
 [ 50 48]]
In [42]: # precision, recall, F1 score, and count of response variable
         # of logistic regression model, C =100 when threshold set to 0.1
        print(classification_report(y_test, y_pred_class100))
            precision
                         recall f1-score
                                             support
          0
                  0.91
                            0.65
                                      0.76
                                                 807
                 0.15
                            0.49
          1
                                      0.23
                                                  98
avg / total
                 0.83
                            0.64
                                      0.70
                                                 905
In [43]: # evaluate logistic regression model, C = 100
         # when threshold set to 0.1
        model_metrics(y_test, y_pred_class100)
The model metrics are:
accuracy: 0.63646408839779
classification error: 0.36353591160221
sensitivity: 0.4897959183673469
specificity: 0.654275092936803
false positive rate: 0.34572490706319703
precision: 0.14678899082568808
F1 score: 0.2258823529411765
confusion matrix:
Out[43]: array([[528, 279],
                [50, 48]])
In [44]: # evaluate logistic regression model, C = 100
```

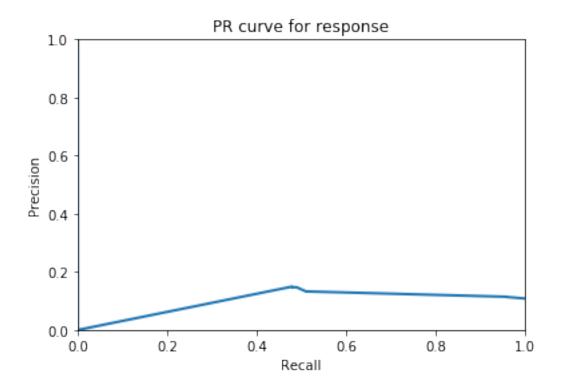
when threshold set to default 0.5

```
model_metrics(y_test, y_predictions100)
                      #y_predictions100 is the predicted response value
The model metrics are:
accuracy: 0.8917127071823204
classification error: 0.10828729281767957
sensitivity: 0.0
specificity: 1.0
false positive rate: 0.0
precision: nan
F1 score: 0.0
confusion matrix:
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/ipykernel_launcher.py:16: RuntimeWarning:
     app.launch_new_instance()
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/p
     'precision', 'predicted', average, warn_for)
Out[44]: array([[807,
                                                           0],
                                        [ 98,
                                                           0]])
0.6 ROC Curve
In [45]: # make predicted probabilities for the predictions
                      # logistic regression, C = 100
                      # store the predicted probabilities for class 1 of response
                      y_pred_prob100_class1 = log_reg100.predict_proba(X_test)[:, 1]
In [46]: # the first argument is true values,
                      # the second argument is predicted probabilities
                      # pass y_test and y_pred_prob
                      # do not use y_pred_class, because it will
                      # give incorrect results without generating an error
                      # roc_curve returns 3 objects fpr, tpr, thresholds
                      # fpr: false positive rate
                      # tpr: true positive rate
                      fpr, tpr, thresholds = roc_curve(y_test, y_pred_prob100_class1)
In [47]: # a check of thresholds
                      thresholds
Out [47]: array([1.229, 0.229, 0.169, 0.129, 0.128, 0.092, 0.091, 0.068, 0.048])
```



```
Specificity: 0.654275092936803
In [51]: # AUC is the percentage of the ROC plot that is underneath the curve
         # first argument is true values, second argument is predicted probabilities
         # AUC for logistic regression, C = 100
         roc_auc_y100_class1 = metrics.roc_auc_score(y_test, y_pred_prob100_class1)
         print('\nThe AUC is:', roc_auc_y100_class1)
The AUC is: 0.5752977771034065
0.7 PR Curve
In [52]: # Given the imbalance of 0 to 1 in the response category
         # let's see what the Precision-Recall curve looks like
         # for the logistic regression model, C = 100
         precision, recall, thresholds = precision_recall_curve(y_test, y_pred_prob100_class1)
In [53]: y_test[:10]
Out[53]: 2398
         800
                 0
         2288
                 0
         2344
                 0
         3615
                 0
         3548
                 0
        1115
                 0
        4053
                 0
         838
                 0
         4141
         Name: response, dtype: int64
In [54]: type(y_test)
Out[54]: pandas.core.series.Series
In [55]: y_pred_prob100_class1[:10]
Out[55]: array([0.129, 0.169, 0.169, 0.091, 0.169, 0.169, 0.091, 0.169, 0.169,
                0.169])
In [56]: # plot the PR curve for logistic regression, C = 100
        plot_pr_curve(recall, precision)
        plt.savefig('PR_logistic_C100_plot.pdf')
```

plt.show()



0.8 Logistic Regression Model, C = 1000

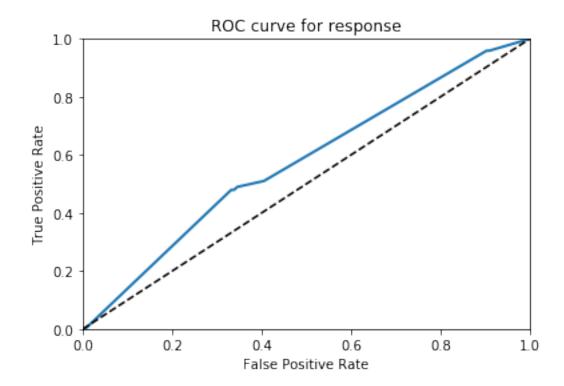
```
In [57]: # Create a logistic regression model on the data
         # C is the hyperparameter controlling the regularization
         # strength of a Scikit-Learn LogisticRegression model.
         # The higher the value of C, the less the model is regularized.
         # Let's see if there is a difference with C = 1000
         # Instantiate model
         log_reg1000 = LogisticRegression(C=1000)
         # Fit the model
         log_reg1000.fit(X_train, y_train)
Out[57]: LogisticRegression(C=1000, class_weight=None, dual=False, fit_intercept=True,
                   intercept_scaling=1, max_iter=100, multi_class='ovr', n_jobs=1,
                   penalty='12', random_state=None, solver='liblinear', tol=0.0001,
                   verbose=0, warm_start=False)
In [58]: # make predictions for the testing set
         y_predictions1000 = log_reg1000.predict(X_test)
In [59]: # make predicted probabilities for the predictions
         y_predict_prob1000 = log_reg1000.predict_proba(X_test)
```

```
y_pred_prob1000_class1 = log_reg1000.predict_proba(X_test)[:,1]
In [61]: # predict response if the predicted probability is greater than 0.1
                                  # it will return 1 for all values above 0.1 and 0 otherwise
                                  # results are 2D so we slice out the first column
                                  y_pred_class1000 = binarize(y_pred_prob1000_class1.reshape(-1, 1), 0.1)
In [62]: # precision, recall, F1 score, and count of response variable
                                  # of logistic regression model, C =1000 when threshold set to 0.5
                                  print(classification_report(y_test, y_predictions1000))
                                                                                                   recall f1-score
                                                  precision
                                                                                                                                                                             support
                                      0
                                                                     0.89
                                                                                                           1.00
                                                                                                                                                  0.94
                                                                                                                                                                                             807
                                                                     0.00
                                                                                                           0.00
                                                                                                                                                  0.00
                                                                                                                                                                                                98
                                                                     0.80
                                                                                                           0.89
                                                                                                                                                  0.84
                                                                                                                                                                                             905
avg / total
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/site-packages/sklearn/metrics/classification.python3.6/sit
         'precision', 'predicted', average, warn_for)
In [63]: # evaluate logistic regression model, C = 1000
                                  # when threshold set to default 0.5
                                  # model_metrics(y_known, y_pred):
                                  model_metrics(y_test, y_predictions1000)
The model metrics are:
accuracy: 0.8917127071823204
classification error: 0.10828729281767957
sensitivity: 0.0
specificity: 1.0
false positive rate: 0.0
precision: nan
F1 score: 0.0
confusion matrix:
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/ipykernel_launcher.py:16: RuntimeWarning:
        app.launch_new_instance()
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklea
        'precision', 'predicted', average, warn_for)
```

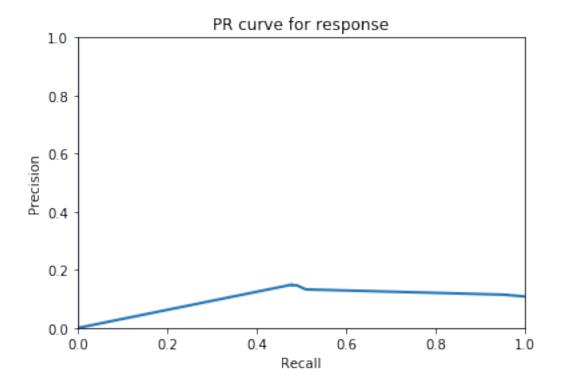
In [60]: # store the predicted probabilities for class 1 of the response

for the logistic regression, C = 1000 model

```
Out[63]: array([[807,
                        0],
                [ 98,
                        0]])
In [64]: # the first argument is true values,
         # the second argument is predicted probabilities
         \# pass y_test and y_pred_prob
         # do not use y_pred_class, because it will give
         # incorrect results without generating an error
         # roc_curve returns 3 objects fpr, tpr, thresholds
         # fpr: false positive rate
         # tpr: true positive rate
         fpr, tpr, thresholds = roc_curve(y_test, y_pred_prob1000_class1)
         plot_roc_curve(fpr, tpr)
         plt.savefig('ROC_logistic_C1000_plot.pdf')
         plt.show()
```



```
When the threshold is set to 0.5
Sensitivity: 0.0
Specificity: 1.0
In [66]: # evaluate the logistic regression model, C = 1000
         # sensitivity and specificity when the threshold is set to 0.1
         print('When the threshold is set to 0.1')
         evaluate_threshold(0.1)
When the threshold is set to 0.1
Sensitivity: 0.4897959183673469
Specificity: 0.654275092936803
In [67]: # AUC is the percentage of the ROC plot that is underneath the curve
         # first argument is true values, second argument is predicted probabilities
         # AUC for logistic regression, C = 1000
         roc_auc_y100_class1 = metrics.roc_auc_score(y_test, y_pred_prob1000_class1)
         print('\nThe AUC is:', roc_auc_y100_class1)
The AUC is: 0.5752977771034065
In [68]: # Given the imbalance of 0 to 1 in the response category
         # let's see what the Precision-Recall curve looks like
         # for the logistic regression model, C = 1000
         precision, recall, thresholds = precision_recall_curve(y_test, y_pred_prob1000_class1
         # plot the PR curve for logistic regression, C = 1000
         plot_pr_curve(recall, precision)
         plt.savefig('PR_logistic_C1000_plot.pdf')
         plt.show()
```



0.9 Naive Bayes Classifier

```
In [69]: # Create a Naive Bayes Classifier on the data

# Instantiate model
    clf = BernoulliNB()

# Fit the model
    clf.fit(X_train, y_train)

Out[69]: BernoulliNB(alpha=1.0, binarize=0.0, class_prior=None, fit_prior=True)

In [70]: # make predictions for the testing set
    clf_y_predictions = clf.predict(X_test)

In [71]: # make predicted probabilities for the predictions
    clf_y_predict_prob = clf.predict_proba(X_test)

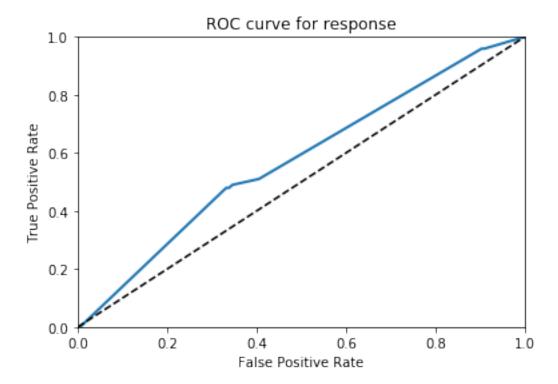
In [72]: # store the predicted probabilities for class 1 of the response
    # for the naive bayes classifier

    clf_y_pred_prob_class1 = clf.predict_proba(X_test)[:,1]
```

```
In [73]: # precision, recall, F1 score, and count of response variable
                                      # of naive bayes classifier
                                      print(classification_report(y_test, clf_y_predictions))
                                                      precision
                                                                                                             recall f1-score
                                                                                                                                                                                               support
                                          0
                                                                            0.89
                                                                                                                      1.00
                                                                                                                                                                  0.94
                                                                                                                                                                                                                 807
                                           1
                                                                            0.00
                                                                                                                      0.00
                                                                                                                                                                  0.00
                                                                                                                                                                                                                    98
avg / total
                                                                            0.80
                                                                                                                      0.89
                                                                                                                                                                  0.84
                                                                                                                                                                                                                905
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklea
          'precision', 'predicted', average, warn_for)
In [74]: # evaluate naive bayes classifier
                                      # when threshold set to default 0.5
                                      # model_metrics(y_known, y_pred):
                                      model_metrics(y_test, clf_y_predictions)
The model metrics are:
accuracy: 0.8917127071823204
classification error: 0.10828729281767957
sensitivity: 0.0
specificity: 1.0
false positive rate: 0.0
precision: nan
F1 score: 0.0
confusion matrix:
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/ipykernel_launcher.py:16: RuntimeWarning:
        app.launch_new_instance()
/Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/classification.py:1135: Users/jmwanat/anaconda3/lib/python3.6/site-packages/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklearn/metrics/sklea
          'precision', 'predicted', average, warn_for)
Out[74]: array([[807,
                                                                                                     0],
                                                                    [ 98,
                                                                                                     0]])
In [75]: # first argument is true values,
                                       # second argument is predicted probabilities
                                      \# pass y\_test and y\_pred\_prob
                                      # do not use y_pred_class, because it will give
```

```
# incorrect results without generating an error
# roc_curve returns 3 objects fpr, tpr, thresholds
# fpr: false positive rate
# tpr: true positive rate

fpr, tpr, thresholds = roc_curve(y_test, clf_y_pred_prob_class1)
plot_roc_curve(fpr, tpr)
plt.savefig('ROC_bernoulli_plot.pdf')
plt.show()
```



```
print('When the threshold is set to 0.1')
    evaluate_threshold(0.1)

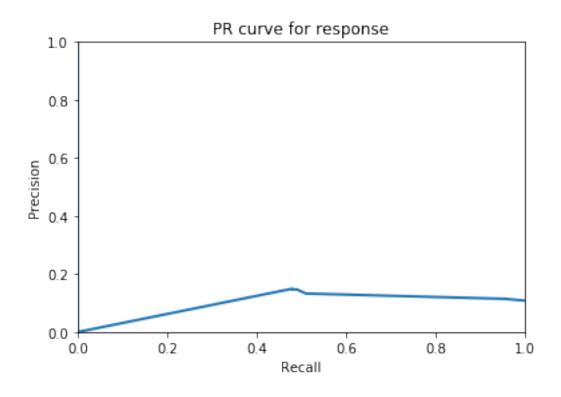
When the threshold is set to 0.1
Sensitivity: 0.4897959183673469
Specificity: 0.654275092936803

In [78]: # AUC is the percentage of the ROC plot that is underneath the curve
    # first argument is true values, second argument is predicted probabilities
    # AUC for naive bayes classifier
```

print('\nThe AUC is:', roc_auc_y100_class1)

The AUC is: 0.5752977771034065

roc_auc_y100_class1 = metrics.roc_auc_score(y_test, clf_y_pred_prob_class1)



0.10 Cross Validation of Logistic Regression Model, C = 100

```
In [80]: # calculate cross-validated AUC for logistic regression model
         #log_reg100 = LogisticRegression(C=100)
         print('Cross validated AUC for Logistic Regression:')
         cross_log_auc = cross_val_score(log_reg100, X_train, y_train, cv=10, scoring='roc_auc
         display_scores(cross_log_auc)
Cross validated AUC for Logistic Regression:
Scores: [0.627 0.606 0.555 0.68 0.632 0.592 0.554 0.599 0.577 0.622]
Mean: 0.6045377265827597
Standard deviation: 0.03632462069250767
0.11 Cross Validation of Naive Bayes Classification
In [81]: # calculate cross-validated AUC for naive Bayes classification
         print('Cross validated AUC for Naive Bayes Classification:')
         cross_clf_auc = cross_val_score(clf, X_train, y_train, cv=10, scoring='roc_auc')
         display_scores(cross_clf_auc)
Cross validated AUC for Naive Bayes Classification:
Scores: [0.627 0.606 0.547 0.68 0.632 0.592 0.554 0.599 0.577 0.622]
Mean: 0.6036947033269457
Standard deviation: 0.03753998048084224
0.12 Interpreting the Logistic Regression Model, C = 100
In [82]: log_reg100.coef_
Out[82]: array([[ 0.382, -0.708, -0.695]])
```

```
In [83]: model_data_df_X.head()
Out [83]:
            default housing loan
                  0
         1
                            1
                                  1
         2
                  0
                            1
                                  0
         3
                                  1
                  0
                            1
         4
                  0
                            1
                                  0
```

```
In [84]: #yes = 1, no = 0
         #response = has the client subscribed to a term deposit?
         #for credit in default = yes, the log of the odds of response increase by 0.382
         #for housing loan = yes, the log of the odds of response decrease by -0.708
         #for personal loan = yes, the log of the odds of response decrease by -0.695
In [85]: clf.coef_
Out[85]: array([[-3.855, -0.905, -2.415]])
In [86]: math.exp(-3.855)
         #for client with credit in default, there is a 2% increase in having a term deposit
Out[86]: 0.02117360331011653
In [87]: math.exp(-0.905)
         #for client with housing loan, there is a 40% decrease in having a term deposit
Out[87]: 0.4045418851030188
In [88]: math.exp(-2.415)
         #for client with personal loan, there is a 8.9% decrease in having a term deposit
Out[88]: 0.08936733892175319
```