

My Project

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Chapter 1

Class Index

1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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Chapter 2

File Index

2.1 File List

Here is a list of all documented files with brief descriptions:

matrix_math.hpp	
Linear algebra and matrix mathematics library	19

Chapter 3

Class Documentation

3.1 Linear_Solvers Class Reference

Class containing static methods for solving linear systems.

```
#include <matrix_math.hpp>
```

3.1.1 Detailed Description

Class containing static methods for solving linear systems.

using various methods including LU and QR decomposition

The documentation for this class was generated from the following file:

- [matrix_math.hpp](#)

3.2 LUResult Struct Reference

Result of LU decomposition of a matrix.

```
#include <matrix_math.hpp>
```

Public Attributes

- `std::vector< std::vector< double > > L`
Lower triangular matrix.
- `std::vector< std::vector< double > > U`
Upper triangular matrix.
- `std::vector< int > P`
Permutation vector.

3.2.1 Detailed Description

Result of LU decomposition of a matrix.

Stores the lower triangular (L), upper triangular (U) matrices, and the permutation vector (P) from the decomposition

The documentation for this struct was generated from the following file:

- [matrix_math.hpp](#)

3.3 LUResult_to_pass Struct Reference

Collaboration diagram for LUResult_to_pass:

Public Attributes

- [Matrix](#) **L**
- [Matrix](#) **U**
- `std::vector< int >` **P**

The documentation for this struct was generated from the following file:

- [matrix_math.hpp](#)

3.4 Matrix Class Reference

[Matrix](#) class implementation for mathematical operations.

```
#include <matrix_math.hpp>
```

Public Member Functions

- [Matrix](#) (int rs=1, int cs=1)
Constructor for [Matrix](#).
- [Matrix](#) (const [Matrix](#) &other)
Copy constructor for [Matrix](#).
- [Matrix](#) & **operator=** (const [Matrix](#) &other)
Assignment operator for [Matrix](#).
- [Matrix](#) **operator+** (const [Matrix](#) &other) const
[Matrix](#) addition operator.
- [Matrix](#) **operator-** (const [Matrix](#) &other) const
[Matrix](#) subtraction operator.
- [LUResult](#) **L_U** () const
Computes the LU Decomposition of the matrix.
- [QRresult](#) **QR_fact** () const
Computes the QR Decomposition of the matrix.
- [Matrix](#) **operator*** (const [Matrix](#) &other) const
[Matrix](#) multiplication operator.
- [My_Vec](#) **multiply** (const [My_Vec](#) &x) const
Multiplies the matrix with a vector.
- [Matrix](#) **Transpose** () const
Transposes the matrix.
- [Matrix](#) **Scalar_Mul** (double k) const
Scalar multiplication of the matrix.

Static Public Member Functions

- static [My_Vec UV](#) (int i, int L)
Creates a unit vector with a 1 at position i.
- static [Matrix Embed](#) (const [Matrix](#) &Householder, const [Matrix](#) &A)
Embeds a Householder matrix into a larger identity matrix.
- static [Matrix Outer_Product](#) (const [My_Vec](#) &u, const [My_Vec](#) &v)
Static method to compute the outer product of two vectors.
- static [Matrix eye](#) (int a)
Static method to create an identity matrix of size a.
- static [Matrix Ones](#) (int a, int b)
Static method to create a matrix of ones.
- static [Matrix Zeros](#) (int a, int b)
Static method to create a matrix of zeros.

Public Attributes

- int **rows**
Number of rows in the matrix.
- int **cols**
Number of columns in the matrix.
- std::vector< std::vector< double > > **MyMAT**
Internal matrix storage.

3.4.1 Detailed Description

[Matrix](#) class implementation for mathematical operations.

Provides basic matrix operations including addition, subtraction, multiplication, and various matrix factorizations (LU, QR)

3.4.2 Constructor & Destructor Documentation

3.4.2.1 [Matrix\(\)](#) [1/2]

```
Matrix::Matrix (
    int rs = 1,
    int cs = 1 ) [inline]
```

Constructor for [Matrix](#).

Parameters

<i>rs</i>	Number of rows (defaults to 1)
<i>cs</i>	Number of columns (defaults to 1)

3.4.2.2 Matrix() [2/2]

```
Matrix::Matrix (
    const Matrix & other ) [inline]
```

Copy constructor for [Matrix](#).

Parameters

<i>other</i>	The matrix to copy
--------------	--------------------

3.4.3 Member Function Documentation

3.4.3.1 Embed()

```
static Matrix Matrix::Embed (
    const Matrix & Householder,
    const Matrix & A ) [inline], [static]
```

Embeds a Householder matrix into a larger identity matrix.

Parameters

<i>Householder</i>	The Householder matrix to embed
<i>A</i>	The original matrix

Returns

The embedded matrix

3.4.3.2 eye()

```
static Matrix Matrix::eye (
    int a ) [inline], [static]
```

Static method to create an identity matrix of size a.

Parameters

<i>a</i>	Size of the matrix (number of rows and columns)
----------	---

Returns

Identity matrix of size a

3.4.3.3 L_U()

```
LUResult Matrix::L_U ( ) const [inline]
```

Computes the LU Decomposition of the matrix.

Returns

[LUResult](#) structure containing L, U matrices and P vector

Exceptions

<code>std::invalid_argument</code>	if the matrix is not square
<code>std::runtime_error</code>	if the matrix is singular or nearly singular

3.4.3.4 multiply()

```
My_Vec Matrix::multiply (  
    const My_Vec & x ) const [inline]
```

Multiplies the matrix with a vector.

Parameters

<code>x</code>	The vector to multiply with
----------------	-----------------------------

Returns

Resulting vector after multiplication

Exceptions

<code>std::invalid_argument</code>	if dimensions are not compatible
------------------------------------	----------------------------------

3.4.3.5 Ones()

```
static Matrix Matrix::Ones (  
    int a,  
    int b ) [inline], [static]
```

Static method to create a matrix of ones.

Parameters

<code>a</code>	Number of rows
<code>b</code>	Number of columns

Returns

[Matrix](#) of size a x b with all elements set to 1

3.4.3.6 operator*()

```
Matrix Matrix::operator* (
    const Matrix & other ) const [inline]
```

Matrix multiplication operator.

Parameters

<i>other</i>	The matrix to multiply with
--------------	-----------------------------

Returns

Resulting matrix after multiplication

Exceptions

<i>std::invalid_argument</i>	if dimensions are not compatible
------------------------------	----------------------------------

3.4.3.7 operator+()

```
Matrix Matrix::operator+ (
    const Matrix & other ) const [inline]
```

Matrix addition operator.

Parameters

<i>other</i>	The matrix to add
--------------	-------------------

Returns

Resulting matrix after addition

Exceptions

<i>std::invalid_argument</i>	if matrices have different dimensions
------------------------------	---------------------------------------

3.4.3.8 operator-()

```
Matrix Matrix::operator- (
    const Matrix & other ) const [inline]
```

Matrix subtraction operator.

Parameters

<i>other</i>	The matrix to subtract
--------------	------------------------

Returns

Resulting matrix after subtraction

Exceptions

<code>std::invalid_argument</code>	if matrices have different dimensions
------------------------------------	---------------------------------------

3.4.3.9 operator=()

```
Matrix & Matrix::operator= (
    const Matrix & other ) [inline]
```

Assignment operator for [Matrix](#).

Parameters

<i>other</i>	The matrix to assign
--------------	----------------------

Returns

Reference to this matrix

3.4.3.10 Outer_Product()

```
static Matrix Matrix::Outer_Product (
    const My_Vec & u,
    const My_Vec & v ) [inline], [static]
```

Static method to compute the outer product of two vectors.

Parameters

<i>u</i>	First vector
<i>v</i>	Second vector

Returns

[Matrix](#) resulting from the outer product

3.4.3.11 QR_fact()

```
QRresult Matrix::QR_fact ( ) const [inline]
```

Computes the QR Decomposition of the matrix.

Returns

[QRresult](#) structure containing Q, R matrices

3.4.3.12 Scalar_Mul()

```
Matrix Matrix::Scalar_Mul (
    double k ) const [inline]
```

Scalar multiplication of the matrix.

Parameters

k	Scalar value
-----	--------------

Returns

New matrix resulting from scalar multiplication

3.4.3.13 Transpose()

```
Matrix Matrix::Transpose ( ) const [inline]
```

Transposes the matrix.

Returns

New matrix that is the transpose of this matrix

3.4.3.14 UV()

```
static My_Vec Matrix::UV (
    int i,
    int L ) [inline], [static]
```

Creates a unit vector with a 1 at position i.

Parameters

i	Position of the 1 in the unit vector
L	Total length of the vector

Returns

Unit vector with 1 at position i

3.4.3.15 Zeros()

```
static Matrix Matrix::Zeros (
    int a,
    int b ) [inline], [static]
```

Static method to create a matrix of zeros.

Parameters

<i>a</i>	Number of rows
<i>b</i>	Number of columns

Returns

[Matrix](#) of size a x b with all elements set to 0

The documentation for this class was generated from the following file:

- [matrix_math.hpp](#)

3.5 My_Vec Class Reference

Vector class for mathematical operations.

```
#include <matrix_math.hpp>
```

Public Member Functions

- [My_Vec](#) (int l=1)
Construct a new vector.
- [My_Vec operator+](#) (const [My_Vec](#) &other) const
Add two vectors.
- [My_Vec operator-](#) (const [My_Vec](#) &other) const
Vector subtraction operator.
- double [Norm](#) () const
Computes the Euclidean norm (magnitude) of the vector.
- double [dot](#) (const [My_Vec](#) &other) const
Computes the dot product with another vector.
- [My_Vec Scalar_Mul](#) (double k) const
Scalar multiplication of the vector.
- [My_Vec](#) (const [My_Vec](#) &other)
Copy constructor for My_Vec.
- [My_Vec & operator=](#) (const [My_Vec](#) &other)
Assignment operator for My_Vec.

Static Public Member Functions

- static `My_Vec ones` (int a)
Creates a vector of ones.
- static `My_Vec unit_vec` (int i, int L)
Creates a unit vector with a 1 at position i.
- static `My_Vec Zeros` (const int &i)
Creates a zero vector of length i.

Public Attributes

- int **length**
Length of the vector.
- `std::vector< double >` **myvector**
Vector data storage.

3.5.1 Detailed Description

Vector class for mathematical operations.

Implements a mathematical vector with common operations like addition, subtraction, dot product, and scalar multiplication

3.5.2 Constructor & Destructor Documentation

3.5.2.1 `My_Vec()` [1/2]

```
My_Vec::My_Vec (
    int l = 1 ) [inline]
```

Construct a new vector.

Parameters

<i>l</i>	Length of the vector (defaults to 1)
----------	--------------------------------------

3.5.2.2 `My_Vec()` [2/2]

```
My_Vec::My_Vec (
    const My_Vec & other ) [inline]
```

Copy constructor for `My_Vec`.

Parameters

<i>other</i>	The vector to copy
--------------	--------------------

3.5.3 Member Function Documentation

3.5.3.1 dot()

```
double My_Vec::dot (
    const My_Vec & other ) const [inline]
```

Computes the dot product with another vector.

Parameters

<i>other</i>	The other vector
--------------	------------------

Returns

Dot product result

Exceptions

<i>std::invalid_argument</i>	if vectors have different lengths
------------------------------	-----------------------------------

3.5.3.2 Norm()

```
double My_Vec::Norm ( ) const [inline]
```

Computes the Euclidean norm (magnitude) of the vector.

Returns

Norm of the vector

3.5.3.3 ones()

```
static My_Vec My_Vec::ones (
    int a ) [inline], [static]
```

Creates a vector of ones.

Parameters

<i>a</i>	Length of the vector
----------	----------------------

Returns

Vector with all elements set to 1

3.5.3.4 operator+()

```
My_Vec My_Vec::operator+ (
    const My_Vec & other ) const [inline]
```

Add two vectors.

Parameters

<i>other</i>	Vector to add to this one
--------------	---------------------------

Returns

New vector containing the sum

Exceptions

<i>std::invalid_argument</i>	if vectors have different lengths
------------------------------	-----------------------------------

3.5.3.5 operator-()

```
My_Vec My_Vec::operator- (
    const My_Vec & other ) const [inline]
```

Vector subtraction operator.

Parameters

<i>other</i>	The vector to subtract
--------------	------------------------

Returns

Result of vector subtraction

Exceptions

<i>std::invalid_argument</i>	if vectors have different lengths
------------------------------	-----------------------------------

3.5.3.6 operator=()

```
My_Vec & My_Vec::operator= (
    const My_Vec & other ) [inline]
```

Assignment operator for [My_Vec](#).

Parameters

<i>other</i>	The vector to assign
--------------	----------------------

Returns

Reference to this vector

3.5.3.7 Scalar_Mul()

```
My_Vec My_Vec::Scalar_Mul (
    double k ) const [inline]
```

Scalar multiplication of the vector.

Parameters

<i>k</i>	Scalar value
----------	--------------

Returns

New vector resulting from scalar multiplication

3.5.3.8 unit_vec()

```
static My_Vec My_Vec::unit_vec (
    int i,
    int L ) [inline], [static]
```

Creates a unit vector with a 1 at position i.

Parameters

<i>i</i>	Position of the 1 in the unit vector
<i>L</i>	Total length of the vector

Returns

Unit vector with 1 at position i

3.5.3.9 Zeros()

```
static My_Vec My_Vec::Zeros (
    const int & i ) [inline], [static]
```

Creates a zero vector of length i.

Parameters

<i>i</i>	Length of the zero vector
----------	---------------------------

Returns

Zero vector of length *i*

The documentation for this class was generated from the following file:

- [matrix_math.hpp](#)

3.6 QR_result_to_pass Struct Reference

Collaboration diagram for QR_result_to_pass:

Public Attributes

- [Matrix Q](#)
- [Matrix R](#)

The documentation for this struct was generated from the following file:

- [matrix_math.hpp](#)

3.7 QRresult Struct Reference

Result of QR decomposition of a matrix.

```
#include <matrix_math.hpp>
```

Public Attributes

- `std::vector< std::vector< double > > Q`
Orthogonal matrix.
- `std::vector< std::vector< double > > R`
Upper triangular matrix.

3.7.1 Detailed Description

Result of QR decomposition of a matrix.

Stores the orthogonal matrix Q and upper triangular matrix R

The documentation for this struct was generated from the following file:

- [matrix_math.hpp](#)

Chapter 4

File Documentation

4.1 matrix_math.hpp File Reference

Linear algebra and matrix mathematics library.

```
#include <iostream>
#include <vector>
#include <cmath>
```

Include dependency graph for matrix_math.hpp:

4.2 matrix_math.hpp

[Go to the documentation of this file.](#)

```
00001
00008 //gcc (Ubuntu 13.3.0-6ubuntu2~24.04) 13.3.0
00009 // Standard library includes for basic operations
00010 #include <iostream>
00011 #include <vector>
00012 #include <cmath>
00013
00014 #ifndef MATRIX_MATH_HPP
00015 #define MATRIX_MATH_HPP
00016
00023 struct LUResult {
00024     std::vector<std::vector<double>> L;
00025     std::vector<std::vector<double>> U;
00026     std::vector<int> P;
00027 };
00028
00034 struct QRresult {
00035     std::vector<std::vector<double>> Q;
00036     std::vector<std::vector<double>> R;
00037 };
00038
00045 class My_Vec {
00046 public:
00047     int length;
00048     std::vector<double> myvector;
00049
00054     My_Vec(int l=1) {
00055         length = l;
00056         myvector.resize(length);
00057     }
00058
00065     My_Vec operator+ (const My_Vec& other) const {
00066         if(this->length != other.length) {
00067             throw std::invalid_argument("Invalid lengths");
00068         }
00069         My_Vec Vec(this->length);
00070         for (int i=0; i<this->length; i++) {
```

```

00071         Vec.myvector[i] = this->myvector[i] + other.myvector[i];
00072     }
00073     return Vec;
00074 }
00075
00081 static My_Vec ones(int a) {
00082     My_Vec ones_vec(a);
00083     for(int i=0; i<a; i++) {
00084         ones_vec.myvector[i] = 1;
00085     }
00086     return ones_vec;
00087 }
00088
00095 My_Vec operator- (const My_Vec& other) const{
00096
00097     if(this->length != other.length) {
00098         throw std::invalid_argument("Invalid lengths");
00099     }
00100     My_Vec Vec(this->length);
00101
00102     for (int i=0; i<this->length; i++) {
00103         Vec.myvector[i] = this->myvector[i] - other.myvector[i];
00104     }
00105     return Vec;
00106 }
00107
00112 double Norm() const {
00113     double a=0;
00114     for (int i=0; i<this->length; i++) {
00115         a += pow(this->myvector[i], 2.0);
00116     }
00117     return sqrt(a);
00118 }
00119
00126 double dot (const My_Vec& other) const {
00127     if(this->length != other.length) {
00128         throw std::invalid_argument("Invalid lengths");
00129     }
00130
00131     double a=0;
00132     for(int i=0; i<this->length; i++) {
00133         a += this->myvector[i] * other.myvector[i];
00134     }
00135     return a;
00136 }
00137
00143 My_Vec Scalar_Mul(double k) const {
00144     My_Vec New(this->length);
00145     for (int i=0; i<this->length; i++) {
00146         New.myvector[i] = k * this->myvector[i];
00147     }
00148     return New;
00149 }
00150
00155 My_Vec(const My_Vec& other)
00156 : length(other.length), myvector(other.myvector) {};
00157
00163 My_Vec& operator=(const My_Vec& other) {
00164     if (this != &other) {
00165         length = other.length;
00166         myvector = other.myvector;
00167     }
00168     return *this;
00169 }
00170
00177 static My_Vec unit_vec(int i, int L) {
00178     My_Vec unit_vec(L);
00179     for (int j=0; j<L; j++) {
00180         unit_vec.myvector[j] = (j == i) ? 1 : 0;
00181     }
00182     return unit_vec;
00183 }
00184
00190 static My_Vec Zeros(const int& i) {
00191     My_Vec unit_vec(i);
00192     for (int j=0; j<i; j++) {
00193         unit_vec.myvector[j] = 0;
00194     }
00195     return unit_vec;
00196 }
00197 };
00198
00205 class Matrix {
00206 public:
00207     int rows;
00208     int cols;
00209     std::vector<std::vector<double>> MyMAT;

```



```

00210
00216     Matrix(int rs=1, int cs=1) {
00217         rows = rs;
00218         cols = cs;
00219         MyMAT.resize(rs, std::vector<double>(cs));
00220     }
00221
00226     Matrix(const Matrix& other)
00227     : rows(other.rows), cols(other.cols), MyMAT(other.MyMAT) {}
00228
00234     Matrix& operator=(const Matrix& other) {
00235         if (this != &other) {
00236             rows = other.rows;
00237             cols = other.cols;
00238             MyMAT = other.MyMAT;
00239         }
00240         return *this;
00241     }
00242
00249     Matrix operator+(const Matrix& other) const {
00250         Matrix New_Mat(other.rows, other.cols);
00251         if (this->cols != other.cols || other.rows != this->rows) {
00252             throw std::invalid_argument("Dimension mismatch");
00253         } else {
00254             for (int i=0; i<rows; i++) {
00255                 for (int j=0; j<cols; j++) {
00256                     New_Mat.MyMAT[i][j] = other.MyMAT[i][j] + this->MyMAT[i][j];
00257                 }
00258             }
00259         }
00260         return New_Mat;
00261     }
00262
00269     Matrix operator-(const Matrix& other) const {
00270         Matrix New_Mat(other.rows, other.cols);
00271         if (this->cols != other.cols || other.rows != this->rows) {
00272             throw std::invalid_argument("Dimension mismatch");
00273         } else {
00274             for (int i=0; i<rows; i++) {
00275                 for (int j=0; j<cols; j++) {
00276                     New_Mat.MyMAT[i][j] = this->MyMAT[i][j] - other.MyMAT[i][j];
00277                 }
00278             }
00279         }
00280         return New_Mat;
00281     }
00282
00289     LUResult L_U() const {
00290         // Check for square matrix
00291         if (this->rows != this->cols) {
00292             throw std::invalid_argument("Not square");
00293         }
00294
00295         Matrix L = eye(this->rows);
00296         Matrix U = Zeros(this->rows, this->cols);
00297         std::vector<int> P(this->rows);
00298         for (int i = 0; i < this->rows; i++) {
00299             P[i] = i;
00300         }
00301
00302         Matrix A_work(*this);
00303
00304         for (int j = 0; j < this->cols; j++) {
00305             int pivot_row = j;
00306             double max_val = std::abs(A_work.MyMAT[j][j]);
00307
00308             for (int i = j+1; i < this->rows; i++) {
00309                 if (std::abs(A_work.MyMAT[i][j]) > max_val) {
00310                     pivot_row = i;
00311                     max_val = std::abs(A_work.MyMAT[i][j]);
00312                 }
00313             }
00314
00315             if (pivot_row != j) {
00316                 for (int k = 0; k < this->cols; k++) {
00317                     std::swap(A_work.MyMAT[j][k], A_work.MyMAT[pivot_row][k]);
00318                 }
00319
00320                 std::swap(P[j], P[pivot_row]);
00321
00322                 if (j > 0) {
00323                     for (int k = 0; k < j; k++) {
00324                         std::swap(L.MyMAT[j][k], L.MyMAT[pivot_row][k]);
00325                     }
00326                 }
00327             }
00328

```

```

00329         if(std::abs(A_work.MyMAT[j][j]) < 1e-10) {
00330             throw std::runtime_error("Matrix is singular or nearly singular");
00331         }
00332
00333         for(int i = 0; i <= j; i++) {
00334             double sum = 0.0;
00335             for(int k = 0; k < i; k++) {
00336                 sum += L.MyMAT[i][k] * U.MyMAT[k][j];
00337             }
00338             U.MyMAT[i][j] = A_work.MyMAT[i][j] - sum;
00339         }
00340
00341         for(int i = j+1; i < this->rows; i++) {
00342             double sum = 0.0;
00343             for(int k = 0; k < j; k++) {
00344                 sum += L.MyMAT[i][k] * U.MyMAT[k][j];
00345             }
00346             L.MyMAT[i][j] = (A_work.MyMAT[i][j] - sum) / U.MyMAT[j][j];
00347         }
00348     }
00349
00350     LUResult result;
00351     result.L = L.MyMAT;
00352     result.U = U.MyMAT;
00353     result.P = P;
00354     return result;
00355 }
00356
00363 static My_Vec UV(int i, int L) {
00364     My_Vec unit_vec(L);
00365     for (int j=0; j<L; j++) {
00366         unit_vec.myvector[j] = (j == i) ? 1 : 0;
00367     }
00368     return unit_vec;
00369 }
00370
00377 static Matrix Embed(const Matrix& Householder, const Matrix& A) {
00378     Matrix Hp = eye(A.rows);
00379     int i = A.rows - Householder.rows;
00380     for (int a = 0; a < Householder.rows; a++) {
00381         for (int b = 0; b < Householder.cols; b++) {
00382             Hp.MyMAT[i+a][i+b] = Householder.MyMAT[a][b];
00383         }
00384     }
00385     return Hp;
00386 }
00387
00392 QRresult QR_fact() const {
00393     Matrix Q = eye(this->rows);
00394     Matrix Aupdate = *this;
00395
00396     for (int i = 0; i < std::min(this->rows-1, this->cols); i++) {
00397         My_Vec vecx(this->rows - i);
00398         for (int row = i; row < this->rows; row++) {
00399             vecx.myvector[row - i] = Aupdate.MyMAT[row][i];
00400         }
00401
00402         double n = vecx.Norm();
00403
00404         My_Vec unit = My_Vec::unit_vec(0, this->rows - i); // Use consistent naming
00405
00406         My_Vec reflec_vec;
00407         if (vecx.myvector[0] < 0) {
00408             reflec_vec = vecx + unit.Scalar_Mul(n);
00409         } else {
00410             reflec_vec = vecx - unit.Scalar_Mul(n);
00411         }
00412
00413         double normalize_ref = reflec_vec.Norm();
00414
00415         // Check for zero vector (avoid division by zero)
00416         if (normalize_ref < 1e-10) {
00417             continue; // Skip this iteration if vector is too small
00418         }
00419
00420         My_Vec V = reflec_vec.Scalar_Mul(1.0 / normalize_ref);
00421
00422         // Create Householder matrix H = I - 2*vv^T
00423         Matrix I = Matrix::eye(V.length);
00424         Matrix vvT = Matrix::Outer_Product(V, V);
00425         Matrix Householder = I - vvT.Scalar_Mul(2.0);
00426
00427         // Embed the Householder matrix into a larger identity matrix
00428         Matrix Hprime = Matrix::eye(this->rows);
00429         for (int r = 0; r < Householder.rows; r++) {
00430             for (int c = 0; c < Householder.cols; c++) {
00431                 Hprime.MyMAT[i + r][i + c] = Householder.MyMAT[r][c];

```

```

00432         }
00433     }
00434
00435     Aupdate = Hprime * Aupdate;
00436     Q = Q * Hprime;
00437 }
00438
00439 QRresult QR;
00440 std::vector<std::vector<double>> Q_n = Q.Transpose().MyMAT;
00441 std::vector<std::vector<double>> R_n = Aupdate.MyMAT;
00442
00443 QR.Q = Q_n;
00444 QR.R = R_n;
00445 return QR;
00446 }
00447
00448 Matrix operator*(const Matrix& other) const {
00449     if (this->cols != other.rows) {
00450         throw std::invalid_argument("Dimension mismatch");
00451     }
00452
00453     Matrix Ans(this->rows, other.cols); // Ensure constructor handles allocation
00454
00455     for (int i = 0; i < this->rows; ++i) {
00456         for (int j = 0; j < other.cols; ++j) {
00457             double sum_of_multiples = 0.0;
00458             for (int k = 0; k < this->cols; ++k) {
00459                 sum_of_multiples += this->MyMAT[i][k] * other.MyMAT[k][j];
00460             }
00461             Ans.MyMAT[i][j] = sum_of_multiples;
00462         }
00463     }
00464
00465     return Ans;
00466 }
00467
00468 My_Vec multiply(const My_Vec& x) const {
00469     if (this->cols != x.length) {
00470         throw std::invalid_argument("Dimension mismatch");
00471     }
00472
00473     My_Vec ans(this->rows);
00474
00475     for (int i=0; i<this->rows; i++) {
00476         double dot_prod = 0;
00477         for(int j=0; j<this->cols; j++) {
00478             dot_prod += this->MyMAT[i][j] * x.myvector[j];
00479         }
00480         ans.myvector[i] = dot_prod;
00481     }
00482
00483     return ans;
00484 }
00485
00486 static Matrix Outer_Product(const My_Vec& u, const My_Vec& v) {
00487     Matrix Output(u.length, v.length);
00488     for(int i=0; i<u.length; i++) {
00489         for(int j=0; j<v.length; j++) {
00490             Output.MyMAT[i][j] = u.myvector[i] * v.myvector[j];
00491         }
00492     }
00493     return Output;
00494 }
00495
00496 Matrix Transpose() const {
00497     Matrix New_Mat(this->cols, this->rows);
00498     for (int i = 0; i < rows; i++) {
00499         for(int j=0; j<cols; j++) {
00500             New_Mat.MyMAT[j][i] = this->MyMAT[i][j];
00501         }
00502     }
00503     return New_Mat;
00504 }
00505
00506 Matrix Scalar_Mul(double k) const {
00507     Matrix new_mat(this->rows, this->cols);
00508
00509     for (int i = 0; i < rows; i++) {
00510         for(int j=0; j<cols; j++) {
00511             new_mat.MyMAT[i][j] = this->MyMAT[i][j] * k;
00512         }
00513     }
00514     return new_mat;
00515 }
00516
00517 static Matrix eye(int a) {

```

```

00551         Matrix Identity(a, a);
00552         for(int i=0; i<a; i++) {
00553             Identity.MyMAT[i][i] = 1;
00554         }
00555         return Identity;
00556     }
00557
00564     static Matrix Ones(int a, int b) {
00565         Matrix Ones(a, b);
00566         for(int i=0; i<a; i++) {
00567             for(int j=0; j<b; j++) {
00568                 Ones.MyMAT[i][j] = 1;
00569             }
00570         }
00571         return Ones;
00572     }
00573
00580     static Matrix Zeros(int a, int b) {
00581         Matrix Zeros(a, b);
00582         for(int i=0; i<a; i++) {
00583             for(int j=0; j<b; j++) {
00584                 Zeros.MyMAT[i][j] = 0;
00585             }
00586         }
00587         return Zeros;
00588     }
00589 };
00590
00596 class Linear_Solvers {
00597     static My_Vec SolveLU(const Matrix& A, const My_Vec& b);
00598     static My_Vec SolveQR(const Matrix& A, const My_Vec& b);
00599     static My_Vec Inverse(const Matrix& A);
00600
00601     static My_Vec ForwardSubstitution(const Matrix& L, const My_Vec& b);
00602     static My_Vec BackwardSubstitution(const Matrix& U, const My_Vec& y);
00603 };
00604
00605 struct LUResult_to_pass {
00606     Matrix L;
00607     Matrix U;
00608     std::vector<int> P;
00609 };
00610
00611
00612 struct QR_result_to_pass {
00613     Matrix Q;
00614     Matrix R;
00615 };
00616
00617
00618 LUResult_to_pass conv_LU(const LUResult& LU) {
00619     int a = LU.L.size();
00620     int b = LU.L[0].size();
00621
00622     Matrix L(a, b);
00623     L.MyMAT = LU.L;
00624
00625
00626     int c = LU.U.size();
00627     int d = LU.U[0].size();
00628
00629     Matrix U(c, d);
00630     U.MyMAT = LU.U;
00631
00632     LUResult_to_pass LU_new;
00633
00634     LU_new.L = L;
00635     LU_new.U = U;
00636     LU_new.P = LU.P;
00637     return LU_new;
00638 }
00639
00640
00641 QR_result_to_pass conv_QR(const QRresult& QR) {
00642     int a = QR.Q.size();
00643     int b = QR.Q[0].size();
00644
00645     Matrix Q(a, b);
00646     Q.MyMAT = QR.Q;
00647
00648
00649     int c = QR.R.size();
00650     int d = QR.R[0].size();
00651
00652     Matrix R(c, d);
00653     R.MyMAT = QR.R;
00654

```

```
00655     QR_result_to_pass QR_new;
00656
00657     QR_new.Q = Q;
00658     QR_new.R = R;
00659     return QR_new;
00660 }
00661
00662
00663 #endif
```


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