

Teambook Sindicato de Transporte 2880

Universidad Mayor de San Simón



2880

March 3, 2023

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Chapter 1

Introduction

The following document represents the Teambook for the team Sindicato de Transporte 2880. This version was elaborated for the Latin American Regional phase of 2022's ICPC.

The template for the C++ code is presented:

```
#include <bits/stdc++.h>
// #include <ext/pb_ds/assoc_container.hpp>
// #include <ext/pb_ds/assoc_container.hpp>
// #include <ext/pb_ds/tree_policy.hpp>
// #include <ext/rope>
#define int ll
#define mp      make_pair
#define pb      push_back
#define all(a)   (a).begin(), (a).end()
#define sz(a)    (int)a.size()
#define eq(a, b) (fabs(a - b) < EPS)
#define md(a, b) ((a) % b + b) % b
#define mod(a)   md(a, MOD)
#define _max(a, b) ((a) > (b) ? (a) : (b))
#define srt(a)   sort(all(a))
#define mem(a, h) memset(a, (h), sizeof(a))
#define f        first
#define s        second
#define forn(i, n) for(int i = 0; i < n; i++)
#define fore(i, b, e) for(int i = b; i < e; i++)
#define forg(i, b, e, m) for(int i = b; i < e; i+=m)
#define index   int mid = (b + e) / 2, l = node * 2 + 1, r = l + 1;
#define DBG(x) cerr<<#x<<"_ _"<<(x)<<endl
#define RAYA cout<<"===== "<<'\\n'
```

```
// int in(){int r=0,c;for(c=getchar();c<=32;c=getchar());if(c=='-')
return -in();for(;c>32;r=(r<<1)+(r<<3)+c-'0',c=getchar());
return r;}
```

```
using namespace std;
// using namespace __gnu_pbds;
// using namespace __gnu_cxx;

// #pragma GCC target ("avx2")
// #pragma GCC optimization ("O3")
// #pragma GCC optimization ("unroll-loops")

typedef long long ll;
typedef long double ld;
typedef unsigned long long ull;
typedef pair<int, int> ii;
typedef pair<pair<int, int>, int> iii;
typedef vector<int> vi;
typedef vector<ii> vii;
typedef vector<ll> vll;
// typedef tree<int,null_type,less<int>,rb_tree_tag,
// tree_order_statistics_node_update> ordered_set;
// find_by_order kth largest order_of_key <
// mt19937 rng(chrono::steady_clock::now().time_since_epoch().count
// ());
// rng
const int tam = 200010;
const int MOD = 1000000007;
```

```
const int MOD1 = 998244353;
const double DINF=1e100;
const double EPS = 1e-9;
const long double PI = acos(-1.0L);

signed main()
{
    ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
    // freopen("asd.txt", "r", stdin);
    // freopen("qwe.txt", "w", stdout);

    return 0;
}
```

../Template.cpp

Chapter 2

Mathematics

This chapter is about some useful mathematical tools needed in order to solve problems.

2.1 GCD and LCM

In order to find the greatest common divisor (GCD) of two numbers, the Euclidean algorithm can be used. The implementation is as follows:

```
11 gcd(11 a, 11 b){return b==0? a:gcd(b,a%b);}

int x, y, d;
void extendedEuclid(int a, int b)//ecuacion diofantica ax + by = d
{
    if(b==0) {x=1; y=0; d=a; return;}
    extendedEuclid(b,a%b);
    int x1=y;
    y = x-(a/b)*y;
    x=x1;
}
```

../Mathematics/Euclid.cpp

Another (and faster) way to find the GCD is by using the following code:

```
int gcd(int a, int b) {
    if (!a || !b)
        return a | b;
    unsigned shift = __builtin_ctz(a | b);
    a >>= __builtin_ctz(a);
```

```
do {
    b >>= __builtin_ctz(b);
    if (a > b)
        swap(a, b);
    b -= a;
} while (b);
return a << shift;
}
```

../Mathematics/FastGCD.cpp

The way Halim suggests to find the GCD and the LCM is given by the following code:

```
int gcd(int a, int b) { return b == 0 ? a : gcd(b, a%b); }
int lcm(int a, int b) { return a / gcd(a, b) * b; }
```

../Mathematics/HalimGCD.cpp

2.2 Prime Numbers

The fastest way to check the primality of a number is by using Erathostenes' sieve. The typical implementation is as follows:

```
bitset<100000> bi;
vi primos; //primos
vector<ll> pric; //primos al cuadrado
void criba()
{
    bi.set();
```

```

for(int i=2;i<100000;i++)
    if(bi[i])
    {
        for(int j=i+i;j<100000;j+=i)
            bi[j]=0;
        primos.push_back(i);
        pric.push_back((ll)i*(ll)i);
    }
}
int euler(int n)
{
    int res=n;
    for(int i=0;pric[i]<=n;i++)
    {
        if(n%primos[i]==0)
        {
            res-= res/primos[i];
            while(n%primos[i]==0) n/=primos[i];
        }
    }
    if(n!=1) res-=res/n;
    return res;
}

```

../Mathematics/Erathostenes.cpp

Nevertheless, the following implementation is faster, since the statement `if (i % prime[j] == 0) break;` terminates the loop when `p` divides `i`. The inner loop is executed only once for each composite. Hence, the code performs in $O(n)$ complexity, resulting in the 'linear' sieve:

```

// This algorithm allows to find Eratosthenes sieve in  $O(n \log n)$ 
// time.

std::vector<int> prime;
bool is_composite[MAXN];

void sieve (int n) {
    std::fill (is_composite, is_composite + n, false);
    for (int i = 2; i < n; ++i) {
        if (!is_composite[i]) prime.push_back (i);

```

```

        for (int j = 0; j < prime.size () && i * prime[j] < n; ++j) {
            is_composite[i * prime[j]] = true;
            if (i % prime[j] == 0) break;
        }
    }

    // An application of this linear sieve is to find the Euler
    // totient function of a number in  $O(n \log n)$  time.
    std::vector<int> prime;
    bool is_composite[MAXN];
    int phi[MAXN];

    void sieve (int n) {
        std::fill (is_composite, is_composite + n, false);
        phi[1] = 1;
        for (int i = 2; i < n; ++i) {
            if (!is_composite[i]) {
                prime.push_back (i);
                phi[i] = i - 1; //i is prime
            }
            for (int j = 0; j < prime.size () && i * prime[j] < n; ++j) {
                is_composite[i * prime[j]] = true;
                if (i % prime[j] == 0) {
                    phi[i * prime[j]] = phi[i] * prime[j]; //prime[j]
                    divides i
                    break;
                } else {
                    phi[i * prime[j]] = phi[i] * phi[prime[j]]; //prime[j]
                    does not divide i
                }
            }
        }
    }
}

```

../Mathematics/LinearSieve.cpp

2.3 Modular Arithmetic

The modular inverse is defined by the following equation:

$$a \cdot a^{-1} \equiv 1 \pmod{m} \quad (2.1)$$

The following code shows how to find the modular inverse of a number:

```
int ModPow(int a, int b, int m) {
    int res = 1;
    while (b > 0) {
        if (b & 1) res = (res * a) % m;
        a = (a * a) % m;
        b >>= 1;
    }
    return res;
}

// Language: java
public static int modPow(int a, int b, int m) {
    int res = 1;
    while (b > 0) {
        if ((b & 1) == 1) res = (res * a) % m;
        a = (a * a) % m;
        b >>= 1;
    }
    return res;
}

int ModInverse(int a, int m) {
    return ModPow(a, m - 2, m);
}
```

../Mathematics/ModularInverse.cpp

Some other useful relationships in modular arithmetic are:

- $(a + b) \pmod{m} = (a \pmod{m} + b \pmod{m}) \pmod{m}$
- $(a - b) \pmod{m} = (a \pmod{m} - b \pmod{m}) \pmod{m}$
- $(a * b) \pmod{m} = (a \pmod{m} * b \pmod{m}) \pmod{m}$
- $(a/b) \pmod{m} = (a \pmod{m} * b^{-1} \pmod{m}) \pmod{m}$
- $(a^b) \pmod{m} = (a \pmod{m})^b \pmod{m}$
- $(a^b) \pmod{m} = (a \pmod{m})^{b \pmod{\phi(m)}} \pmod{m}$

- $(a^b) \pmod{m} = (a \pmod{m})^{b \pmod{m-1}} \pmod{m}$
- $\frac{a}{k} \equiv \frac{a}{k} \pmod{m} \iff a \equiv k \pmod{m}$
- $\frac{a}{k} \equiv \frac{a}{k} \pmod{\frac{n}{\gcd(n,k)}}$

2.4 Matrix Exponentiation

The following code shows how to find the nth power of a *mat*, noting that a data structure of type matrix is defined as follows:

```
typedef vector<vector<ll>> mat;
mat ans;
void mult(mat m1, mat m2)
{
    assert(m1[0].size() == m2.size());
    ans.clear();
    ll answer = 0;
    for(i, 0, m1.size())
    {
        vector<ll> fila;
        for(j, 0, m2[0].size())
        {
            answer = 0;
            for(k, 0, m2.size())
                answer = (answer + m1[i][k] * m2[k][j]) % MOD;
            fila.pb(answer);
        }
        ans.pb(fila);
    }
}

void pot(mat base, ll exp)
{
    mat res(base.size(), vector<ll>(base.size(), 0));
    for(i, 0, base.size())
        res[i][i] = 1;
    while(exp)
    {
        if(exp & 1)
        {
            mult(res, base);
        }
    }
}
```

```
        res = ans;  
    }  
    mult(base, base);  
    base = ans;  
    exp /= 2;  
}  
ans = res;  
}
```

../Mathematics/MatrixPower.cpp

Chapter 3

Graphs

This chapter shows some of the basic algorithms and implementations required to solve problems that include graphs.

3.1 Depth First Search (DFS)

The DFS algorithm is a recursive algorithm that visits all the nodes of a graph. It is used to find connected components, topological sorting, and to find bridges and articulation points. The algorithm is as follows:

The implementation can be done as follows:

```
vector<vector<int>> g(tam);
vector<bool> vis(tam);

void dfs(int u){
    vis[u]=true;
    ans++;
    for(int v: g[u]){
        if(!vis[v]){
            dfs(v);
        }
    }
}

signed main()
{
    int n,m;
    cin>>n>>m; // n nodes, m edges
    g.assign(tam,vector<int>());
```

```
    vis.assign(tam, false);
    for(int i=0; i<m;i++){
        int u,v;
        cin>>u>>v;
        g[u].push_back(v);
        g[v].push_back(u);
    }
    ll res = 0;
    for(int i=1; i<=n;i++){
        if(!vis[i]){
            ans=0;
            dfs(i);
            res = max(res,ans);
        }
    }
    g.clear();
    vis.clear();
    return 0;
}
```

../Graphs/DFS.cpp

An application of this algorithm in order to find the shortest path between two nodes can be done as follows:

```
// The following code represents the implementation of a DFS
// algorithm
// to find the shortest path between two nodes in a graph.
// The graph is represented as an adjacency list.
// The algorithm is implemented using a stack.
```

Algorithm 1 Depth First Search (DFS)

```

1: procedure DFS( $G$ )
2:    $visited \leftarrow \emptyset$ 
3:    $time \leftarrow 0$ 
4:    $parent \leftarrow \emptyset$ 
5:    $low \leftarrow \emptyset$ 
6:    $disc \leftarrow \emptyset$ 
7:    $AP \leftarrow \emptyset$ 
8:    $bridge \leftarrow \emptyset$ 
9:   for all  $v \in V$  do
10:     $visited[v] \leftarrow false$ 
11:     $parent[v] \leftarrow -1$ 
12:     $low[v] \leftarrow \infty$ 
13:     $disc[v] \leftarrow \infty$ 
14:   end for
15:   for all  $v \in V$  do
16:     if  $visited[v] = false$  then
17:       DFSUtil( $G, v, visited, time, parent, low, disc, AP, bridge$ )
18:     end if
19:   end for
20: end procedure
21: procedure DFSUTIL( $G, v, visited, time, parent, low, disc, AP, bridge$ )
22:    $visited[v] \leftarrow true$ 
23:    $disc[v] \leftarrow time$ 
24:    $low[v] \leftarrow time$ 
25:    $time \leftarrow time + 1$ 
26:    $children \leftarrow 0$ 
27:   for all  $u \in Adj(v)$  do
28:     if  $visited[u] = false$  then
29:        $parent[u] \leftarrow v$ 
30:        $children \leftarrow children + 1$ 
31:       DFSUtil( $G, u, visited, time, parent, low, disc, AP, bridge$ )
32:        $low[v] \leftarrow \min(low[v], low[u])$ 
33:       if  $parent[v] = -1$  and  $children > 1$  then
34:          $AP[v] \leftarrow true$ 
35:       end if
36:       if  $parent[v] \neq -1$  and  $low[u] \geq disc[v]$  then
37:          $AP[v] \leftarrow true$ 
38:       end if
39:       if  $low[u] > disc[v]$  then
40:          $bridge[v][u] \leftarrow true$ 
41:       end if
42:     else
43:        $low[v] \leftarrow \min(low[v], disc[u])$ 
44:     end if
45:   end for

```

```

#include <bits/stdc++.h>

using namespace std;

vector<int> DFS(vector<vector<int>> &adj, int s, int t) {
    stack<vector<int>> path_stack;
    vector<int> path;
    vector<int> visited(adj.size(), 0);
    path_stack.push({s});
    while (!path_stack.empty()) {
        path = path_stack.top();
        path_stack.pop();
        int last = path[path.size() - 1];
        if (last == t) {
            return path;
        }
        if (visited[last] == 0) {
            visited[last] = 1;
            for (int i = 0; i < adj[last].size(); i++) {
                if (visited[adj[last][i]] == 0) {
                    vector<int> new_path(path);
                    new_path.push_back(adj[last][i]);
                    path_stack.push(new_path);
                }
            }
        }
    }
    return {};
}

int main() {
    int n, m;
    cin >> n >> m;
    vector<vector<int>> adj(n, vector<int>());
    for (int i = 0; i < m; i++) {
        int x, y;
        cin >> x >> y;
        adj[x - 1].push_back(y - 1);
        adj[y - 1].push_back(x - 1);
    }
}

```

```

}
int x, y;
cin >> x >> y;
x--, y--;
vector<int> path = DFS(adj, x, y);
for (int i = 0; i < path.size(); i++) {
    cout << path[i] + 1 << " ";
}
}

```

../Graphs/DFS-application.cpp

3.2 Breadth First Search (BFS)

The BFS algorithm is a non-recursive algorithm that visits all the nodes of a graph. It is used to find connected components, topological sorting, and to find bridges and articulation points, to better understand it, a propagating fire can be imagined. The algorithm is as follows:

The implementation can be done as follows:

```

#include <bits/stdc++.h>

using namespace std;
signed main()
{
    vector<vector<int>> adj; // adjacency list representation
    int n; // number of nodes
    int s; // source vertex

    queue<int> q;
    vector<bool> used(n);
    vector<int> d(n), p(n);

    q.push(s);
    used[s] = true;
    p[s] = -1;
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        for (int u : adj[v]) {
            if (!used[u]) {

```

Algorithm 2 Breadth First Search (BFS)

```

1: procedure BFS( $G$ )
2:    $visited \leftarrow \emptyset$ 
3:    $time \leftarrow 0$ 
4:    $parent \leftarrow \emptyset$ 
5:    $low \leftarrow \emptyset$ 
6:    $disc \leftarrow \emptyset$ 
7:    $AP \leftarrow \emptyset$ 
8:    $bridge \leftarrow \emptyset$ 
9:   for all  $v \in V$  do
10:     $visited[v] \leftarrow false$ 
11:     $parent[v] \leftarrow -1$ 
12:     $low[v] \leftarrow \infty$ 
13:     $disc[v] \leftarrow \infty$ 
14:   end for
15:   for all  $v \in V$  do
16:     if  $visited[v] = false$  then
17:       BFSUtil( $G, v, visited, time, parent, low, disc, AP, bridge$ )
18:     end if
19:   end for
20: end procedure
21: procedure BFSUtil( $G, v, visited, time, parent, low, disc, AP, bridge$ )
22:    $visited[v] \leftarrow true$ 
23:    $disc[v] \leftarrow time$ 
24:    $low[v] \leftarrow time$ 
25:    $time \leftarrow time + 1$ 
26:    $children \leftarrow 0$ 
27:   for all  $u \in Adj(v)$  do
28:     if  $visited[u] = false$  then
29:        $parent[u] \leftarrow v$ 
30:        $children \leftarrow children + 1$ 
31:       BFSUtil( $G, u, visited, time, parent, low, disc, AP, bridge$ )
32:        $low[v] \leftarrow \min(low[v], low[u])$ 
33:       if  $parent[v] = -1$  and  $children > 1$  then
34:          $AP[v] \leftarrow true$ 
35:       end if
36:       if  $parent[v] \neq -1$  and  $low[u] \geq disc[v]$  then
37:          $AP[v] \leftarrow true$ 
38:       end if
39:       if  $low[u] > disc[v]$  then
40:          $bridge[v][u] \leftarrow true$ 
41:       end if
42:     else
43:        $low[v] \leftarrow \min(low[v], disc[u])$ 
44:     end if
45:   end for

```

```

        used[u] = true;
        q.push(u);
        d[u] = d[v] + 1;
        p[u] = v;
    }
}
return 0;
}

```

../Graphs/BFS.cpp

3.3 Finding Bridges and Articulation Points

3.3.1 Bridges

A bridge is an edge that if it is removed, the graph will be divided into two or more components. The implementation is:

```

int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph

vector<bool> visited;
vector<int> tin, low;
int timer;

void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] > tin[v])
                IS_BRIDGE(v, to);
        }
    }
}
}

```

```

void find_bridges() {
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i) {
        if (!visited[i])
            dfs(i);
    }
}

```

../Graphs/FindBridges.cpp

3.4 Flows

The flow is a concept that is used in many algorithms, it is used to find the maximum flow that could go through a system of nodes.

3.4.1 Dinic

The Dinic algorithm is a useful algorithm to find the maximum flow that could go through a system of nodes. The implementation of this algorithm is:

```

struct flowEdge
{
    int to, rev, f, cap;
};

vector<vector<flowEdge> > G;

void addEdge(int st, int en, int cap) {
    // Anade arista (st --> en) con su capacidad
    flowEdge A = {en, (int)G[en].size(), 0, cap};
    flowEdge B = {st, (int)G[st].size(), 0, 0};
    G[st].pb(A);
    G[en].pb(B);
}

int nodes, S, T; // asignar estos valores al armar el grafo G
                // nodes = nodos en red de flujo. Hacer G.clear();
                G.resize(nodes);

```

```

vi work, lvl;
int Q[200010];

bool bfs() {
    int qt = 0;
    Q[qt++] = S;
    lvl.assign(nodes, -1);
    lvl[S] = 0;
    for (int qh = 0; qh < qt; qh++) {
        int v = Q[qh];
        for (flowEdge &e : G[v]) {
            int u = e.to;
            if (e.cap <= e.f || lvl[u] != -1) continue;
            lvl[u] = lvl[v] + 1;
            Q[qt++] = u;
        }
    }
    return lvl[T] != -1;
}

int dfs(int v, int f) {
    if (v == T || f == 0) return f;
    for (int &i = work[v]; i < G[v].size(); i++) {
        flowEdge &e = G[v][i];
        int u = e.to;
        if (e.cap <= e.f || lvl[u] != lvl[v] + 1) continue;
        int df = dfs(u, min(f, e.cap - e.f));
        if (df) {
            e.f += df;
            G[u][e.rev].f -= df;
            return df;
        }
    }
    return 0;
}

int maxFlow() {
    int flow = 0;
    while (bfs()) {
        work.assign(nodes, 0);
        while (true) {

```

```

            int df = dfs(S, INF);
            if (df == 0) break;
            flow += df;
        }
    }
    return flow;
}

```

../Graphs/Dinic.cpp

This implementation is done in order to do the Dinic algorithm for a graph with a large number of nodes.

This algorithm is based on the idea of the BFS algorithm, it is used to find the shortest path between two nodes, in this case, the shortest path between the source and the sink. The algorithm is as follows:

3.4.2 Ford Fulkerson

The Ford Fulkerson algorithm is a useful algorithm to find the maximum flow that could go through a system of nodes. The implementation of this algorithm is:

```

// This algorithm solves the max flow problem in a directed graph
// in O(max_flow * E)

// Here the graph is represented by an adjacency matrix, but it can
// be easily changed to an adjacency list

// The algorithm is based on the push-relabel algorithm, which is a
// variant of the relabel-to-front algorithm

// Number of vertices in given graph
#define V 6

/* Returns true if there is a path from source 's' to sink
't' in residual graph. Also fills parent[] to store the
path */
bool bfs(int rGraph[V][V], int s, int t, int parent[])
{
    // Create a visited array and mark all vertices as not visited
    bool visited[V];
    memset(visited, 0, sizeof(visited));

```

Algorithm 3 Dinic

```

1: procedure DINIC( $G$ )
2:    $visited \leftarrow \emptyset$ 
3:    $time \leftarrow 0$ 
4:    $parent \leftarrow \emptyset$ 
5:    $low \leftarrow \emptyset$ 
6:    $disc \leftarrow \emptyset$ 
7:    $AP \leftarrow \emptyset$ 
8:    $bridge \leftarrow \emptyset$ 
9:   for all  $v \in V$  do
10:     $visited[v] \leftarrow false$ 
11:     $parent[v] \leftarrow -1$ 
12:     $low[v] \leftarrow \infty$ 
13:     $disc[v] \leftarrow \infty$ 
14:   end for
15:   for all  $v \in V$  do
16:     if  $visited[v] = false$  then
17:       DinicUtil( $G, v, visited, time, parent, low, disc, AP, bridge$ )
18:     end if
19:   end for
20: end procedure
21: procedure DINICUTIL( $G, v, visited, time, parent, low, disc, AP, bridge$ )
22:    $visited[v] \leftarrow true$ 
23:    $disc[v] \leftarrow time$ 
24:    $low[v] \leftarrow time$ 
25:    $time \leftarrow time + 1$ 
26:    $children \leftarrow 0$ 
27:   for all  $u \in Adj(v)$  do
28:     if  $visited[u] = false$  then
29:        $parent[u] \leftarrow v$ 
30:        $children \leftarrow children + 1$ 
31:       DinicUtil( $G, u, visited, time, parent, low, disc, AP, bridge$ )
32:        $low[v] \leftarrow \min(low[v], low[u])$ 
33:       if  $parent[v] = -1$  and  $children > 1$  then
34:          $AP[v] \leftarrow true$ 
35:       end if
36:       if  $parent[v]! = -1$  and  $low[u] \geq disc[v]$  then
37:          $AP[v] \leftarrow true$ 
38:       end if
39:       if  $low[u] > disc[v]$  then
40:          $bridge[v][u] \leftarrow true$ 
41:       end if
42:     else
43:        $low[v] \leftarrow \min(low[v], disc[u])$ 
44:     end if
45:   end for

```

```

// Create a queue, enqueue source vertex and mark source vertex
// as visited
queue<int> q;
q.push(s);
visited[s] = true;
parent[s] = -1;

// Standard BFS Loop
while (!q.empty()) {
  int u = q.front();
  q.pop();
  for (int v = 0; v < V; v++) {
    if (visited[v] == false && rGraph[u][v] > 0) {
      // If we find a connection to the sink node, then
      // there is no point in BFS anymore We just have to set its parent
      // and can return true
      if (v == t) {
        parent[v] = u;
        return true;
      }
      q.push(v);
      parent[v] = u;
      visited[v] = true;
    }
  }
}

// We didn't reach sink in BFS starting from source, so return
false
return false;
}

// Returns the maximum flow from s to t in the given graph
int fordFulkerson(int graph[V][V], int s, int t)
{
  int u, v;
  // Create a residual graph and fill the residual graph with
  // given capacities in the original graph as residual capacities
  // in residual graph
  int rGraph[V][V]; // Residual graph where rGraph[i][j] indicates
  // residual capacity of edge from i to j (if there is an edge. If

```



```

rGraph[i][j] is 0, then there is not)
for (u = 0; u < V; u++)
    for (v = 0; v < V; v++)
        rGraph[u][v] = graph[u][v];

int parent[V]; // This array is filled by BFS and to store path

int max_flow = 0; // There is no flow initially
// Augment the flow while there is path from source to sink
while (bfs(rGraph, s, t, parent)) {
    // Find minimum residual capacity of the edges along the
    path filled by BFS. Or we can say find the maximum flow through
    the path found.
    int path_flow = INT_MAX;
    for (v = t; v != s; v = parent[v]) {
        u = parent[v];
        path_flow = min(path_flow, rGraph[u][v]);
    }
    // update residual capacities of the edges and reverse
    edges along the path
    for (v = t; v != s; v = parent[v]) {
        u = parent[v];
        rGraph[u][v] -= path_flow;
        rGraph[v][u] += path_flow;
    }
    // Add path flow to overall flow
    max_flow += path_flow;
}
// Return the overall flow
return max_flow;
}

int main()
{
    // Let us create a graph shown in the above example
    int graph[V][V]
        = { { 0, 16, 13, 0, 0, 0 }, { 0, 0, 10, 12, 0, 0 },
            { 0, 4, 0, 0, 14, 0 }, { 0, 0, 9, 0, 0, 20 },
            { 0, 0, 0, 7, 0, 4 }, { 0, 0, 0, 0, 0, 0 } };

    cout << "The maximum possible flow is "

```

```

<< fordFulkerson(graph, 0, 5);

return 0;
}

```

../Graphs/FordFulkerson.cpp

In order to better understand the adjacency matrix in the code Figure 3.1 shows the graph that is used in the code.

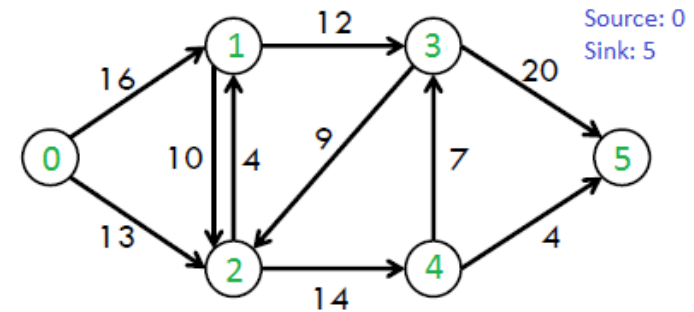


Figure 3.1: Ford Fulkerson