

From HW1, the inductor ripple was found

$$\frac{2 \Delta i_L}{D T_S} = \frac{V_g}{L}$$

$$\Delta i_L = \frac{V_g}{L} \frac{D T_S}{2}$$

DCM Boundary occurs when inductor current ripple equals the average inductor current

from HW1,

$$\langle i(t) \rangle = \frac{-V}{R} \frac{1}{D'}$$

Therefore DCM boundary occurs when

$$\langle i(t) \rangle = \Delta i_L$$

$$\frac{-V}{R} \frac{1}{D'} = \frac{V_g}{L} \frac{D T_S}{2}$$

Find $R = R_{crit}$

$$\frac{-V}{R_{crit}} \frac{1}{D'} = \frac{V_g}{L} \frac{D T_S}{2}$$

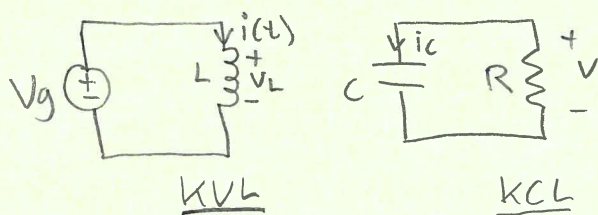
$$R_{crit} = \frac{-V}{D'} \frac{L}{V_g D T_S} \quad (1)$$

$$\text{we know } V = \frac{-V_g D}{1-D} \quad (2)$$

Solve (1) and (2) for R_{crit} and V where $D' = 1-D$

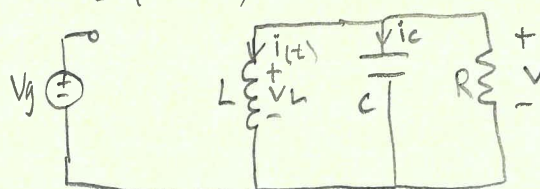
$$\underline{R_{crit} = \frac{2L}{T_S(1-D)^2} + 3}$$

(b) DCM

 Q_1 ON, D_1 OFF "1"

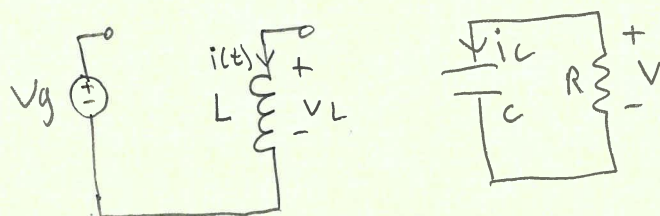
$$V_L(t) = V_g$$

$$i_c(t) = -\frac{V(t)}{R}$$

 Q_1 OFF, D_1 ON "2"

$$V_L(t) = V(t)$$

$$i_c(t) = -i_L(t) - \frac{V(t)}{R}$$

 Q_1 OFF, D_1 OFF "3"

$$V_L(t) = 0$$

$$i_c(t) = -\frac{V(t)}{R}$$

Small Ripple Approximation

"1"

$$V_L(t) = V_g$$

$$i_c(t) = -\frac{V}{R}$$

"2"

$$V_L(t) = V$$

$$i_c(t) = -i_L(t) - \frac{V}{R}$$

"3"

$$V_L(t) = 0$$

$$i_c(t) = -\frac{V}{R}$$

(b) cont

Volt-second Balance

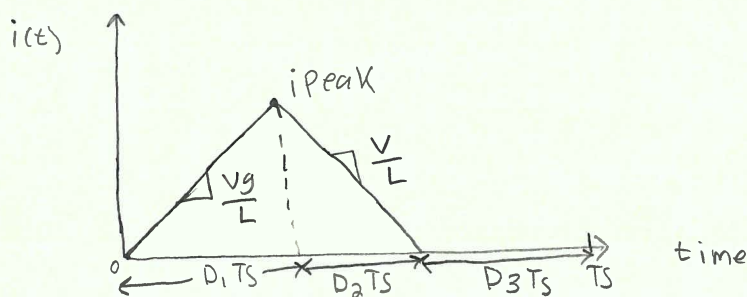
$$\langle V_L(t) \rangle = V_g D_1 + V D_2 + 0 D_3 = 0 \quad (1)$$

capacitor charge balance

$$\langle i_c(t) \rangle = -\frac{V}{R} D_1 + (-i(t) - \frac{V}{R}) D_2 + \frac{V}{R} D_3 = 0$$

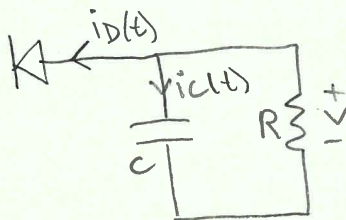
notice not a DC quantity \rightarrow need another relationship

Consider the inductor current



$$i_{peak} = \frac{V_g}{L} D_1 T_s \quad (2)$$

Consider diode current



$$i_D(t) = -i_c(t) + \frac{V(t)}{R}$$

$$\text{or} \quad i_c(t) = -i_D(t) - \frac{V(t)}{R}$$

$$\langle i_c(t) \rangle = \frac{1}{T_s} \int_{T_s} (-i_D(t) - \frac{V(t)}{R}) dt \quad \begin{matrix} \text{by s.r.A. } \approx V \\ \text{"capacitor charge" balance} \end{matrix}$$

$$\langle i_c(t) \rangle = \frac{1}{T_s} \int_{T_s} -i_D(t) dt - \frac{1}{T_s} \int_{T_s} \frac{V}{R} dt$$

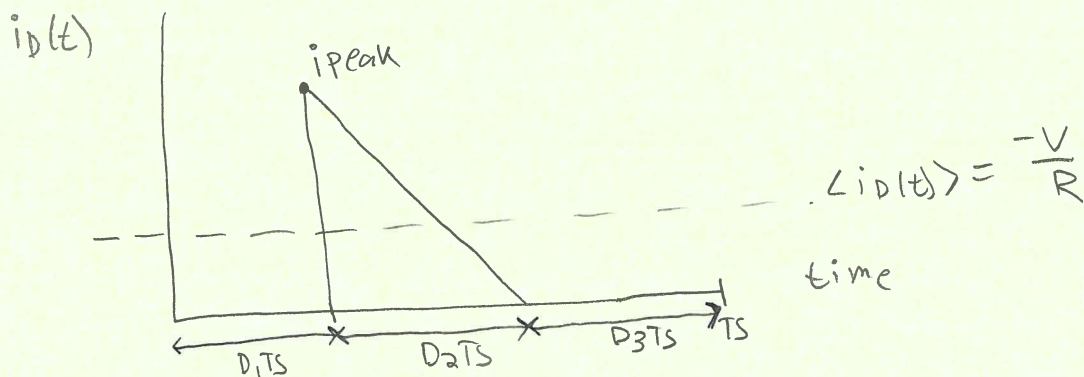
$$\langle i_c(t) \rangle = -\langle i_D(t) \rangle_{T_s} - \frac{1}{T_s} \frac{V}{R} T_s = 0 \quad \langle i_D(t) \rangle = -\frac{V}{R}$$

(b) cont

We showed the dc component of the diode current

$$\langle i_D(t) \rangle = -\frac{V}{R}$$

so we need to sketch the diode current



$$\langle i_D(t) \rangle = \left(\frac{1}{2} i_{peak} D_2 T_s \right) \frac{1}{T_s}$$

$$\frac{1}{2} i_{peak} D_2 = -\frac{V}{R} \quad (3)$$

recall $V_g D_1 + V D_2 = 0 \quad (1)$

$$i_{peak} = \frac{V_g}{L} D_1 T_s \quad (2)$$

Three equations + Three unknowns
- Solve for i_{peak} , D_2 , and V

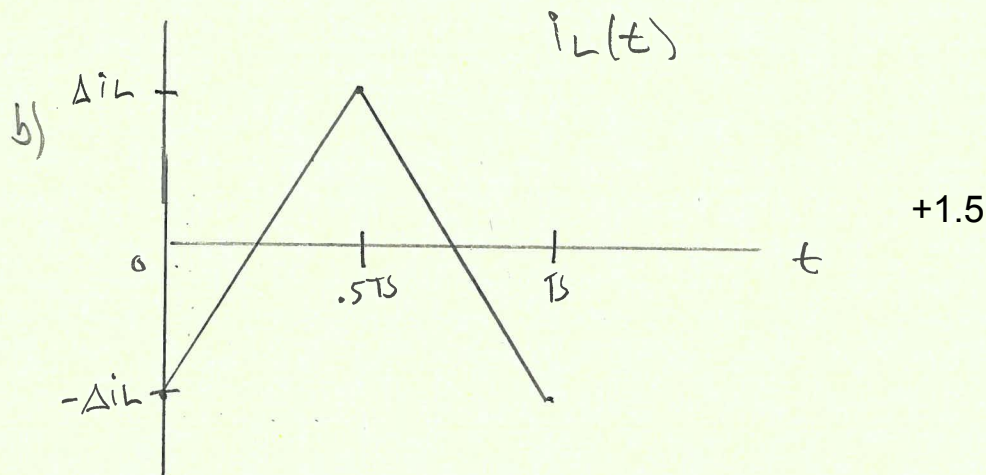
$$D_2 = -\sqrt{\frac{2L}{RT_s}} \quad +2.5$$

$$V = -V_g D_1 \sqrt{\frac{RT_s}{2L}} \quad +2.5$$

c) When R goes to infinity, the output voltage tends to $-\infty$. A voltage regulator is required to drive the duty cycle to zero to prevent damage.

+0.5

- a) No. Synchronous rectification allows inductor current to flow in both directions. The MOSFET allows bidirectional current flow. Since inductor current can go negative, the converter always operates in CCM.



$$\Delta i_L = \frac{V_g - V}{2L} D T_S$$

$$D = 0.5$$

$$\Delta i_L = \frac{(V_g - V)}{4L} T_S = \frac{V_g - DV_g}{4L} T_S$$

$$\Delta i_L = \frac{V_g - 0.5V_g}{4L} T_S$$

$$\underline{\underline{\Delta i_L = \frac{V_g}{8L} T_S}}$$