Deriving Intrinsic Motivation from Uncertainty about Future Goals

https://github.com/jnegrea/csc2541project1

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 - ▶ The learner does not know the reward of each state
 - ▶ The learner does not know the transition mechanics
- ▶ The machine learns the topology of the state space, the transition mechanics, the topography of the reward function, and how to use the mechanics to optimise the specified reward.

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- ► For animal learners, reward signals are recieved by engaging in exploratory, 'fun' behaviours. Can machines be incited to play and explore? To have fun?
- ► Exploratory behaviour is important for animal development human children learn about the world by playing. Can a machine which learns by playing outperform one that does not when performance is integrated over a wide variety of tasks?

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Qualitative Aspects of Intrinsic Motivation

Quantitative Measures for Intrinsic Motivation

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 - An adaptive world model
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 - An intrinsic reward system measuring model improvement
 - A behavioural policy optimising intrinsic reward
- ▶ The kernel of this thesis is that intrinsic motivation is derived from the pursuit of a better model of the dynamics of the world.

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 - ► Task-Independent: The utility is independent of any particular goal or reward function

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- ▶ The learning problem is posed as a two-stage optimisation problem;
 - ► Find the reward function such that an RL agent maximising the reward has highest expected fitness
 - ► Find the RL strategy which maximises the optimal reward function
- ▶ By construction, performs no worse on average than RL using the the natural reward corresponding to fitness.
- ▶ Avoids greedy behaviour in favour of exploratory behaviour (when beneficial).

Quantitative Measures for Intrinsic Motivation II: Empowerment

- Empowerment (metric) aims to achieve the heuristic it is named for
- Quantified as the channel capacity of a state:

$$\mathcal{E}(s) = \max_{\omega \in \Omega_s} \mathcal{I}(A, S_1 | s) = \max_{\omega \in \Omega_s} \mathbb{E}\left[\log \frac{p(S_1, A | s)}{\omega(A | s) p(S_1 | s)}\right] = \max_{\omega \in \Omega_s} \mathbb{E}\left[\log \frac{p(S_1 | s, A)}{p(S_1 | s)}\right]$$

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- ▶ Discussed thoroughly in Singh et al. [13], applied in Mohamed and Rezende [9]
- ▶ Aims to find the state in which an actor is most able to travel to any arbitrary state
- ▶ Not obvious if the information theoretic definition is suitable
- ▶ Does not consider the how rewards may be assigned in the future

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 - Agent learns about distribution of rewards and how to improve heuristic empowerment by computing the posterior distribution of rewards and updating the iER.
- ▶ Originally motivated by goal to show that the empowerment metric was Bayes-optimal the class of problems in Mohamed and Rezende [9]
 - It turns out this is false



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