

3. Read pages 241-242 in the textbook. Using that information, write pseudocode for computing the LCM of an array $A[1..n]$ of integers. You may assume there is a working $\text{gcd}()$ function. (6 points)

ALGORITHM $\text{LCM}(A[1..n])$:

// Computes the least common multiple of all the integer in array A

4. Horner's method:

$$p(x) = 4x^4 + 5x^3 - 2x^2 - 4x + 7$$

- a. Repeatedly factor out x in the following polynomial so that you can apply Horner's method. Write your expression for $p(x)$. (5 points)

$$p(x) = 4x^4 + 5x^3 - 2x^2 - 4x + 7 = (4x^3 + 5x^2 - 2x - 4)x + 7 \quad \text{No } x^4 \text{ terms in } p(x)$$

$$= ((4x^2 + 5x - 2)x - 4)x + 7 = (((4x + 5)x - 2)x - 4)x + 7$$

- b. Show values of the array $P[0..n]$ as needed to apply Horner's method. (3 points)

$$P[] = [4, 5, -2, -4, 7]$$

- c. Apply Horner's method to evaluate the polynomial at $x = 2$. Make a table as we did in class showing the values x , p , n , and i , and then state your final answer for $p(2)$. (5 points)

x	p	n	i	$P[i]$	result
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$$p(2) = 95$$

- d. Use **synthetic** (not long) **division** to divide $p(x)$ by $x - 2$ to check your work. Be sure to show your work. (5 points)

$$\begin{array}{r} 4x^4 + 5x^3 - 2x^2 - 4x + 7 \\ x - 2 \end{array}$$

$$\begin{array}{r} 2 \overline{) 4 \ 5 \ -2 \ -4 \ 7} \\ \underline{\downarrow 8 \ 26 \ 48 \ 88} \\ 4 \ 18 \ 24 \ 44 \ 95 \end{array}$$

$95 = \left(\begin{array}{l} \text{Ans. C} \\ P(2) = 95 \end{array} \right)$

5. Rewrite the *LeftRightBinaryExponentiation* algorithm on page 237 in the textbook to work for $n = 0$ as well as any positive integer. No credit will be given for answers that simply start with an if statement for $n = 0$. (6 points)

ALGORITHM *LeftRightBinaryExponentiation*(a , $b(n)$):

// Computes a^n