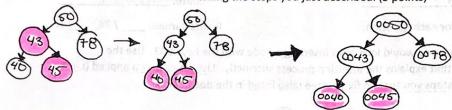
"ipleage my honor that I have avaded by the stevens Honor System."

JULIAN

CS 385, Homework 5: Balanced Trees and Transform-and-Conquer

ame: Julia Nelson	Date: 11/22/19				
int values are assigned for each question.	Points earned:/ 74,%				
Show how the red-black tree would look after inserting a node with the key 0043. Use the document on Moodle that explains the insertion process succinctly. List the case you applied (i.e. 1, 2a, 3b), and write the steps you took to fix the tree (also listed in the document).					
keys. Addrew the tree for each part,	0040 0078 0078 0078 0078 0078 0078 0078				
With the Recognition of	(4) 75 (Figoria)				
a) Draw the tree after a regular binary sea	arch tree insertion. (3 points)				
(0000)					
(0040)					
0045					
b) Which property is violated? (3 points) _ Node is left child, paren	Use and parent are both red				
Case seen after regular binary search to Steps taken to fix the tree: (3 points)					
Draw the tree after taking the steps yo	u just described. (3 points) (27015q E) Et (7				
(0050)					
6040					
6043					
0045	(K) d8 (3 points)				
c) Which property is violated now? (3 point which property is Right child; po	mts) Uode and parent are both redoment is right united				
Case seen after first fixup: (3 points)					
Steps taken to fix the tree: (3 points)	Single Left Rotate.				
Cy I					

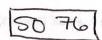
Draw the tree after taking the steps you just described. (3 points)



- 2. Draw the 2-3 tree after inserting each of the following keys. Redraw the tree for each part.
  - a) 50 (1 point)

150

b) 76 (1 point)



c) 23 (3 points)

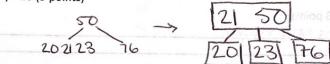
23 50 76 -



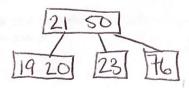
d) 21 (3 points)



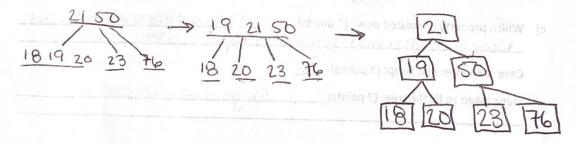
e) 20 (3 points)



f) 19 (3 points)



g) 18 (3 points)



3. Read pages 241-242 in the textbook. Using that information, write pseudocode for computing the LCM of an array A[1..n] of integers. You may assume there is a working gcd() function. (6 points) ALGORITHM LCM(A[1..n]):

// Computes the least common multiple of all the integer in array A

4. Horner's method:

$$p(x) = 4x^4 + 5x^3 - 2x^2 - 4x + 7$$

a. Repeatedly factor out x in the following polynomial so that you can apply Horner's method. Write your expression for p(x). (5 points)

$$P(x) = 4x^{4} + 5x^{3} - 2x^{2} - 4x + 7 = (4x^{3} + 5x^{2} - 2x - 4)x + 7$$

$$= ((4x^{2} + 5x^{2} - 2)x - 4)x + 7 = ((4x + 5)x - 2)x - 4)x + 7$$
bowypluss of the second o

b. Show values of the array P[0..n] as needed to apply Horner's method. (3 points)

c. Apply Horner's method to evaluate the polynomial at x=2. Make a table as we did in class showing the values x, p, n, and i, and then state your final answer for p(2). (5 points)

_	Х	р	n	i	State your in
	. ')	4	4/	1 3 3 7	
	_	5		1	
		- 2		200 2	
		-4		14 3	
		7		4	

$$p(2) = 95$$

d. Use **synthetic** (not long) **division** to divide p(x) by x-2 to check your work. Be sure to show your work. (5 points)

bur work. (5 points)
$$4x^{4}+5x^{3}-2x^{2}-4x+7$$

$$\frac{\sqrt{8264888}}{413244495}$$

$$95 = \begin{pmatrix} Ar6.C \\ P(2)=95 \end{pmatrix}$$

5. Rewrite the LeftRightBinaryExponentiation algorithm on page 237 in the textbook to work for n=0as well as any positive integer. No credit will be given for answers that simply start with an if statement for n = 0. (6 points)

**ALGORITHM** LeftRightBinaryExponentiation(a, b(n)):

// Computes and