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## Problem Set 5

9/4/19

"I pledge my honor that I have abided  
by the Stevens Honor System" Julia Nelson

### Problem 1

$$L = \{0^{2^i} : i \geq 0\}$$

generates

$$\{0, 00, 0000, 000000, \dots\}$$

there exists an int  $n$  such that  $w \in L$

with  $|w| \geq n$

$$xy^iz \in \Sigma^*$$

such that

$$w = xy^iz$$

$$|xy| \geq n$$

$$|x| \geq 1$$

For all  $i \geq 0$

$$w_i = xy^iz \in L$$

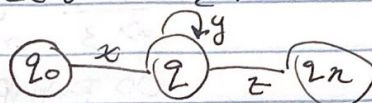
$$w = 0^{2^i}$$

$$w = xy^iz \text{ then } y = 0^k$$

$$w_i = xy^iz$$

$$w_0 = 0^{2^i - k}$$

$w_0$  is Not in  $L$



### Problem 2

Prove  $\text{Lang } B = \{0^i 1^j : i \neq j\}$  is not Regular

Consider how  $B$  is related to Non-reg lang

$$B = \{0^i 1^j : i \neq j\}$$

$$\{0^i 1^j : i \geq 0\}$$

lets assume  $B$  is Reg lang

and gen. strings # of 0's not equal to # of 1's

Complement of  $B$  is

$$\overline{B} = \{0^i 1^j : i = j\} \text{ generates string with equal \# of } i \text{'s and } j \text{'s}$$

if  $B$  is regular, so is  $\overline{B}$  (closed prop)

Since  $\overline{B}$  is of  $B$  (not-reg)

$$\overline{B} = \{0^i 1^j : i = j\} \text{ then}$$

$B = \{0^i 1^j : i \neq j\}$  is Not Regular

### Problem 3

whats min pumping length ~~is~~ for  
the following languages

1.  $0001^*$

Min string length is 000

$$\Rightarrow 3 \rightarrow p' = 3$$

So pumping length can be  
 $p = 2$

~~1~~

$$p' > p$$

$$3 > 2$$

2.  $0^*1^* = \{\epsilon, 00, 11, 01, 001, \dots\}$

min length  $p' = \epsilon$

So can't be pumped  $p = 0$

3.  $0^*1^*0^*1^* \cup 10^*1 = \{\epsilon, 010101, \dots\}$

Min string =  $\epsilon$

So cannot be pumped  $p = 0$

4.  $(01)^* = \{\epsilon, 01, 0101, 010101, \dots\}$

min  $p' = \epsilon$

Cannot be pumped  $p = 0$

5.  $1^*01^*01^* \rightarrow \{00, 100, 10101, \dots\}$

Min string length  $p' = 2$   
 $p$  can = 1

$$p' > p \quad 2 > 1$$



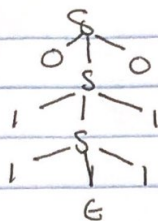
# Problem 4

alphabet  $\{0, 1\}$

1.  $\{w: w = w^R\}$  lang of palindromes

$S \rightarrow 0S0 \mid 1S1 \mid \epsilon$

take string  $\frac{011}{w} \frac{110}{w^R}$

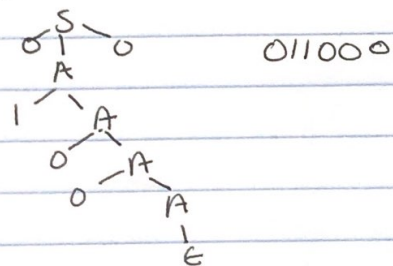


2.  $S \rightarrow 0A0 \mid 1A1$

$\{w: w \text{ starts + ends w/ same symbol}\}$

$A \rightarrow 0A0 \mid 1A1 \mid 1A0 \mid 0A1 \mid \epsilon$

$\Sigma^4 \rightarrow 011000$



3.  $\{w: w \text{ contains more 0's than 1's}\}$

$S \rightarrow AS \mid 0S \mid 0S$

$A \rightarrow AA \mid 0A1 \mid 1A0 \mid \epsilon$

take string 01010

