

Let $H(x)$ be a generating function for the series

$$h_n = 5h_{n-1} - 6h_{n-2}$$

where $h_0 = 1$ and $h_1 = 2$. Find a simple closed formula for $H(x)$.

$$\begin{aligned} H(x) - h_1x - h_0 &= \sum_{n=2}^{\infty} h_n x^n \\ &= \sum_{n=2}^{\infty} 5h_{n-1} x^n + \sum_{n=2}^{\infty} -6h_{n-2} x^n \end{aligned}$$