Theorems to Prove

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We introduce the following notation:

$$\vec{x} \triangleq (\hat{\rho}_x \in \mathtt{program}, \hat{\sigma}_x \in \mathtt{stack}, \rho_x \in \mathtt{program}, \sigma_x \in \mathtt{stack})$$

Based on the linear contraints of our stack machine, we have the following property about well-formed closures:

Recall that to reverse Apply, we must split the program and the stack such that we restore the original closure. We define this split by the following:

splits
$$(\rho', \sigma', v, \vec{x}) \triangleq \rho' = \hat{\rho}_x @ \rho_x \wedge \sigma' = \hat{\sigma}_x @ \sigma_x : \text{ wf } (\vec{x}, v)$$

Using the property of the well-formed closure, if we could prove the Unique Splits proposition, then Apply would be injective.

Unique Splits:
$$\forall \rho', \sigma' . \ \exists \ \vec{x} \ \text{splits} \ (\rho', \sigma', \vec{x}) \land \exists \ \vec{y} \ \text{splits} \ (\rho', \sigma', \vec{y}) \Longrightarrow \vec{x} = \vec{y}$$