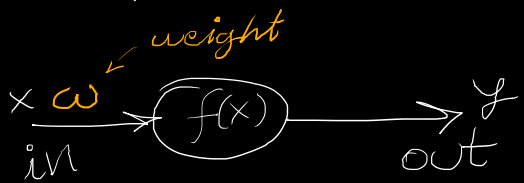
Ann Basic

* artificial Neural Network

①

* An: artificial Neuron

Perceptron

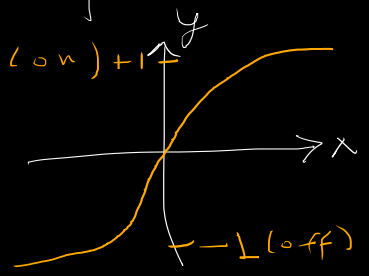


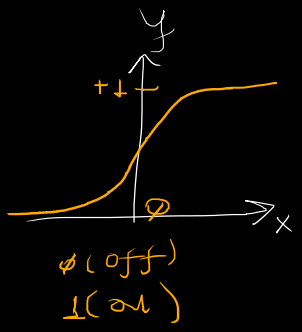
* Neuron's math model

- in = x (numbers) ← known data
- out = y (numbers) ←
- w = weight (number) ← unknown data!
- f(x): activation function

②

* f(x):





$$y = f(x \cdot w)$$

$$y(x) = f(x \cdot w)$$

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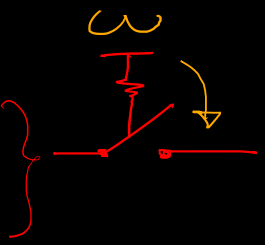
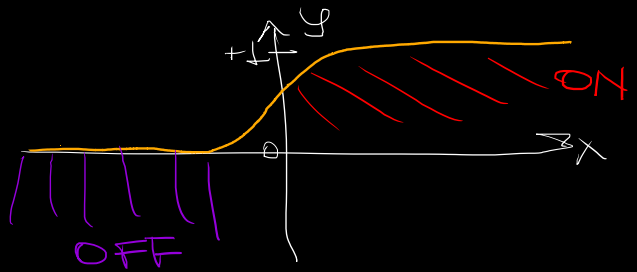
③ f(x) Example

Sigmoid:

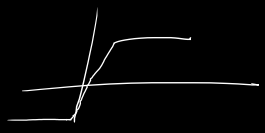
$$f(x) = \frac{1}{1 - e^{-x}}$$

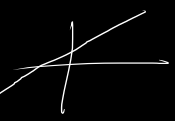




④ what is else?

* Sigmoide

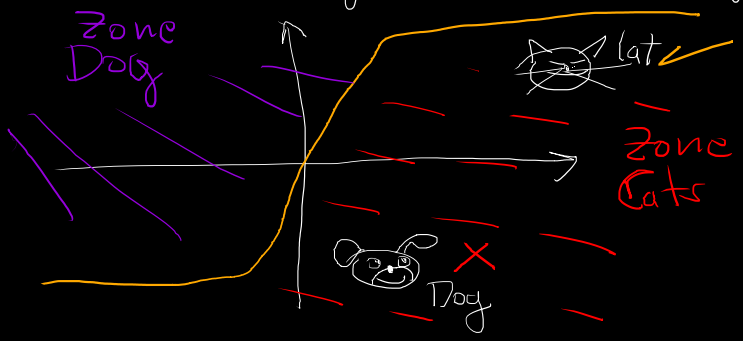
* tanh 

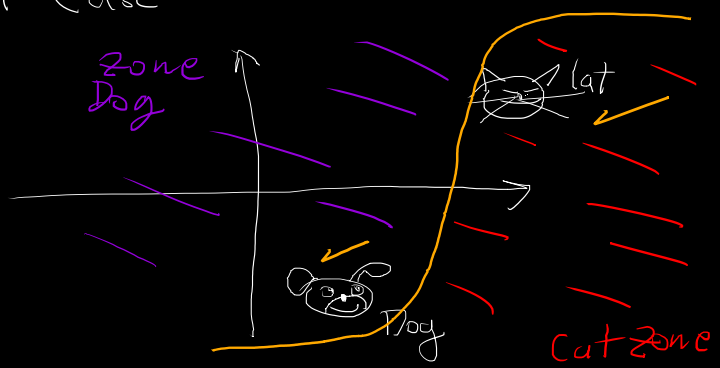
* ReLU 

* maxout ....

etc !!

⑤ Training an AN : Dog vs Cat Case





now - trained on "w" is random

trained AN "w" was computed

What is "train" ? = Solve ω !!

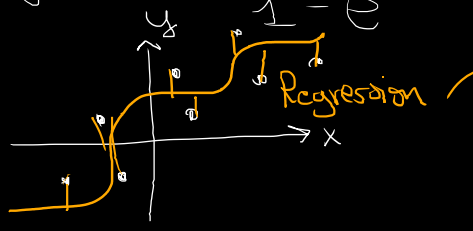
⑥ How to Solve ?

$$y = f(x \cdot \omega) = y = \frac{1}{1 - e^{-x \cdot \omega}}$$

$$y = \frac{1}{1 - e^{-x \cdot \omega}} \qquad y(x, \omega) = \frac{1}{1 - e^{-x \omega}}$$

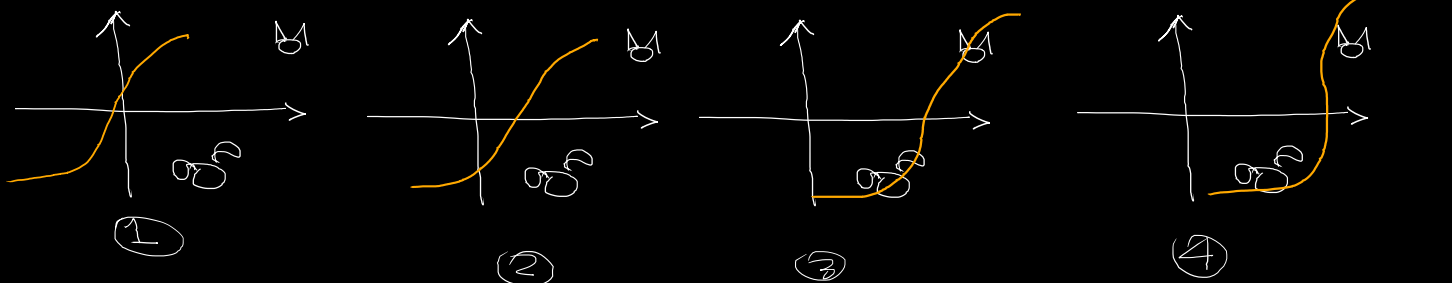
Input(x)	Output(y)
1	Cat
2	Dog
3	Cat
4	Dog
5	.
6	.

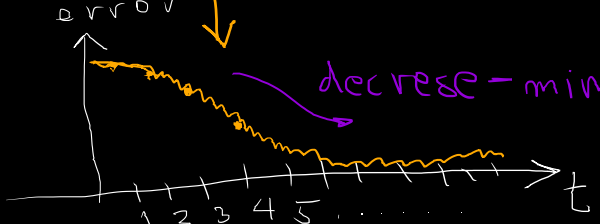
$$x = [\,\cdot\ \cdot\ \cdot\ \cdot\ \cdot\ \cdot\,]$$
$$y = [\,\cdot\ \cdot\ \cdot\ \cdot\ \cdot\ \cdot\,]$$



$$\text{Error} = \| \underbrace{y(x, \omega)}_{\text{real}} - \underbrace{f(x \cdot \omega)}_{\text{prediction}} \|$$

* Error → Loss ⇨ Training is an iterative process





Training process :

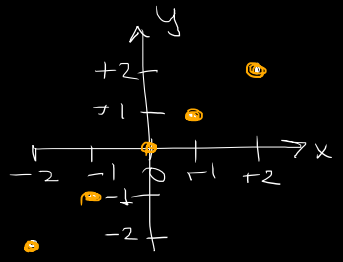
$$\| \text{Loss}(\omega) \|_{\min} = \| \text{error}(\omega) \|_{\min}$$

① Example

$x \rightarrow f(x) \rightarrow y$

$$y = \frac{1}{1 - e^{-xw}} = y(x, w)$$

x	y
-1	-1
-2	-2
0	0
+1	1
+2	+2



$$-1 = \frac{1}{1 - e^{-1w}} \qquad -2 = \frac{1}{1 - e^{2w}} \qquad +2 = \frac{1}{1 - e^{-2w}}$$

$$0 = \frac{1}{1 - e^{0w}} \qquad +1 = \frac{1}{1 - e^{1w}}$$

$\forall w$, all eqs are true

$w = 0$ $w = 1$ $w = 2$ $w = -1$ $w = \ldots\ldots$

$y = f(x)$ / suppose $w = 1$

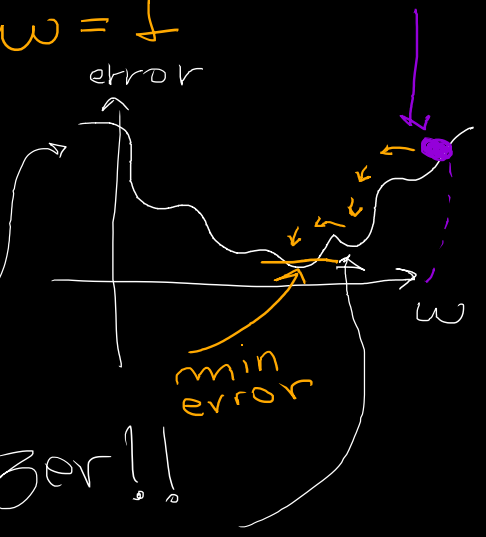
$$-1 = \frac{1}{1 - e^{-1w}} = \frac{1}{1 - e^{1}} = -0.8$$

(-1: i want it; -0.8: predicted) when $w = 1$

$$\text{error} = \|-1 - (-0.8)\| = 0.2$$

For any "w" $\text{error}(w) = y - \frac{1}{1 - e^{xw}}$

$= \|y - f(x, w)\|$



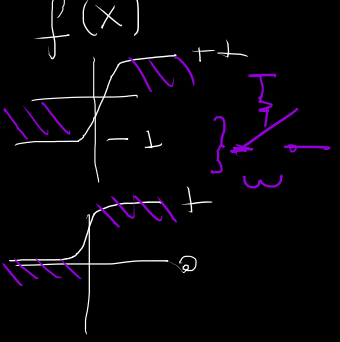
How to find min error? Optimizer!!

* Summary:

: perceptron

variables:

- x, y, f(x): data known
- w: data known



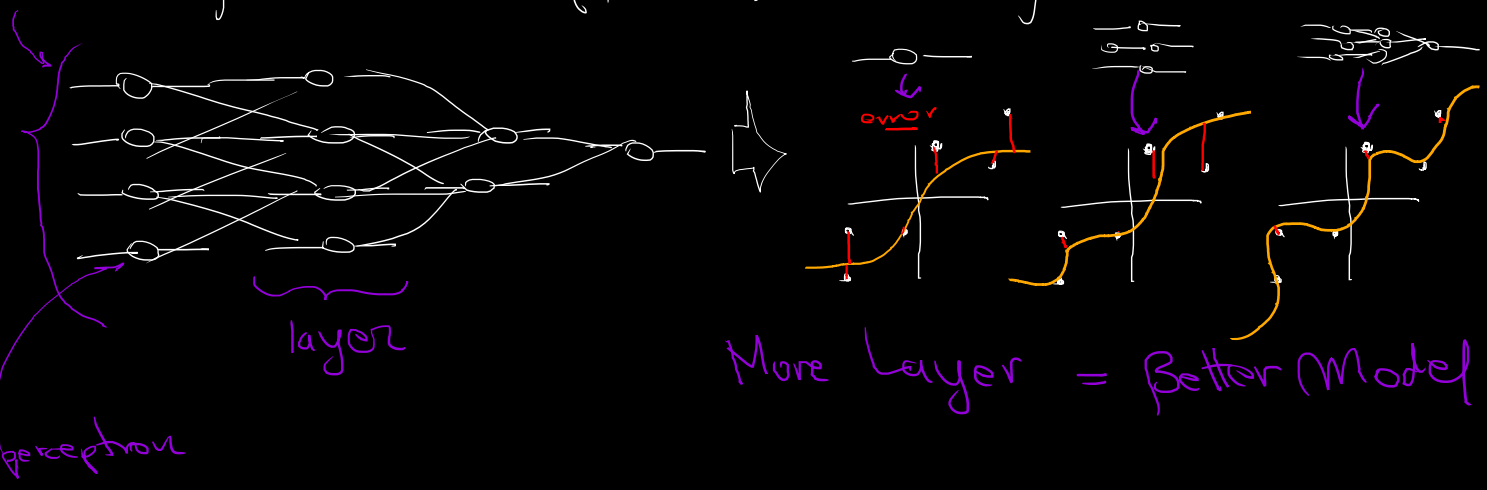
Train: loop iterative

Search w optimo

loss, error } min ↓ decreases!!

MLP

① Multi Layer Perceptron (Math model of Dense Brain)



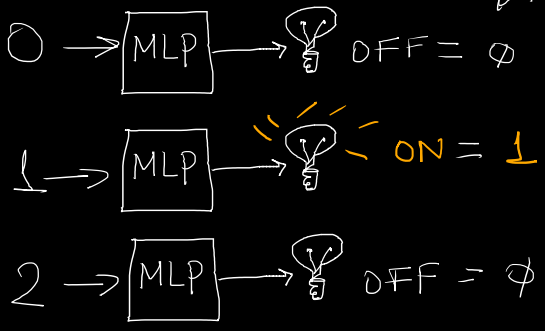
More Layer = Better Model

② Practical Example: Numbers Classifier

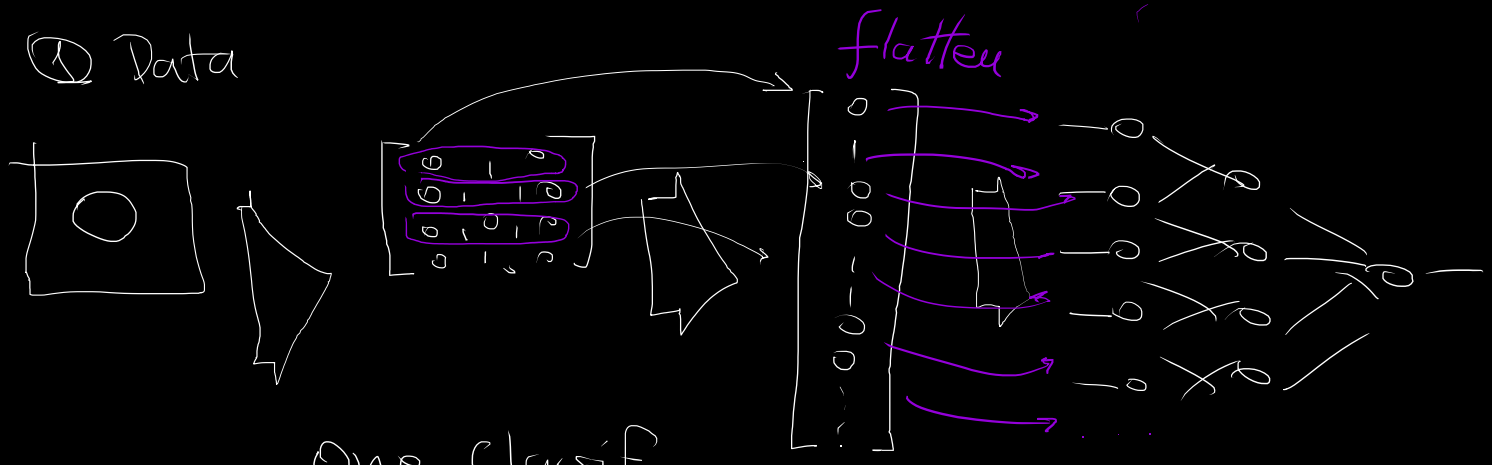
Detects "1" Binary

Input → Output

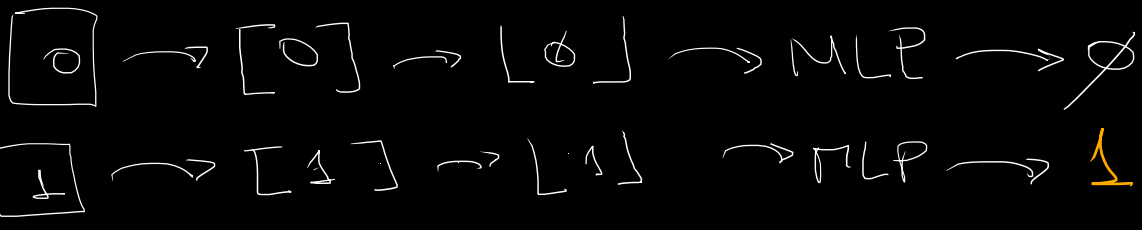
$X \begin{cases} x_1 \\ x_2 \\ x_3 \\ x_4 \end{cases}$ → $\begin{cases} y_1 \\ y_2 \\ y_3 \\ y_4 \end{cases}$ numbers but Labels



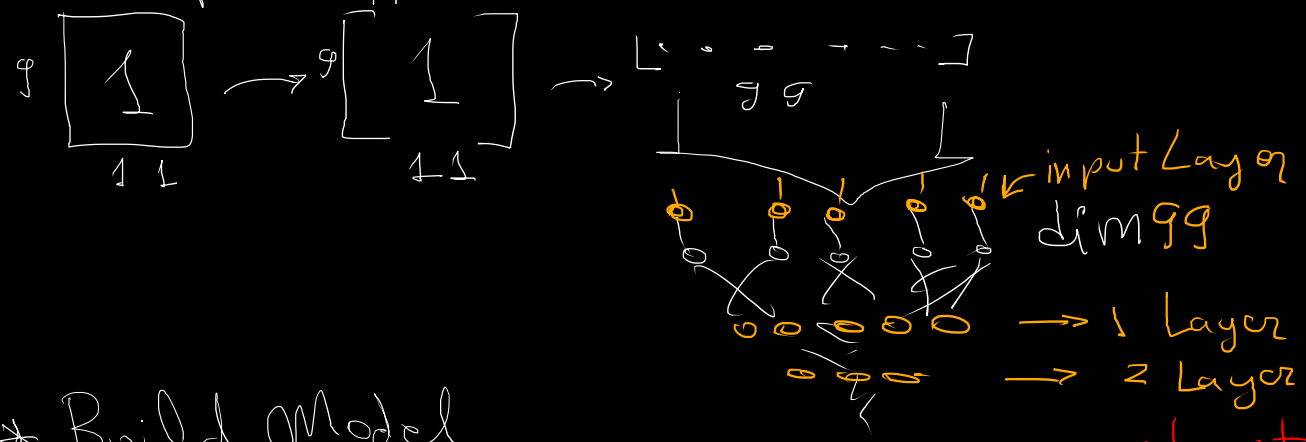
① Data



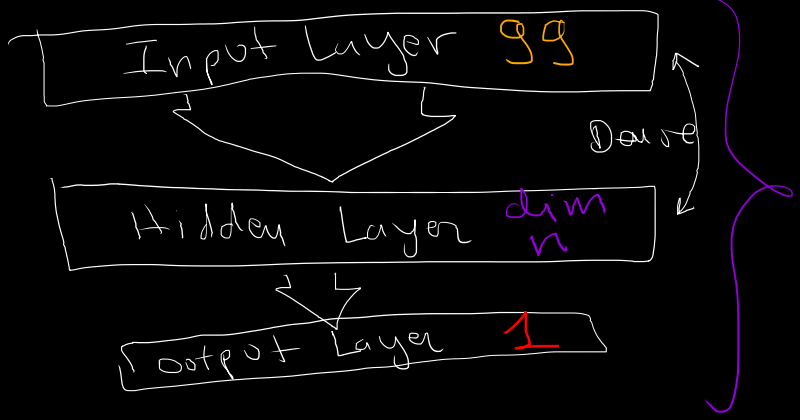
One Classif.



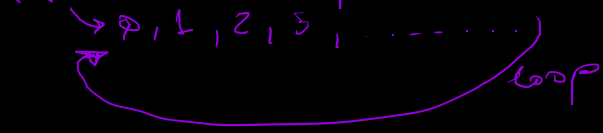
* Implementation:



* Build Model



* Model
* Data In/out
* Optimizer (Gradient)
* iterative process .....



* Python: