$$\underbrace{\begin{bmatrix} \mathbf{H} & -\mathbf{J}_c^{\top} \\ -\mathbf{J}_c & 0 \end{bmatrix}}_{\mathbf{K}} \underbrace{\begin{bmatrix} \ddot{\mathbf{q}} \\ \boldsymbol{\lambda} \end{bmatrix}}_{\boldsymbol{\nu}} = \underbrace{\begin{bmatrix} \mathbf{S}^{\top} \boldsymbol{\tau} + \mathbf{h} \\ \dot{\mathbf{J}}_c \dot{\mathbf{q}} \end{bmatrix}}_{\Psi}$$

$$| \boldsymbol{
u} = \mathbf{K}^{-1} \Psi |$$

AD tools once:
$$\frac{\partial \boldsymbol{\nu}}{\partial \mathbf{q}}$$
 $\mathcal{O}(n^2)$

III Conventional DDP

AD tools once: $\frac{\partial^2 \boldsymbol{\nu}}{\partial \mathbf{q}^2}$ $\mathcal{O}(n^3)$

Contraction: $\boldsymbol{\gamma}^{\top} \frac{\partial^2 \boldsymbol{\nu}}{\partial \mathbf{q}^2}$ $\mathcal{O}(n^3)$