

I Dynamics

$$\boxed{\boldsymbol{\nu} = \mathbf{K}^{-1} \boldsymbol{\Psi}} \xrightarrow{\text{AD}} \frac{\partial \boldsymbol{\nu}}{\partial \mathbf{q}} \quad \mathcal{O}(n^2)$$

II mRNEAc DDP

$$\text{tmp}_1 = \text{mRNEAc}(\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}}, \mathbf{a}_g, \boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\pi}) \quad \mathcal{O}(n)$$

$$\text{tmp}_2 = \frac{\partial}{\partial \mathbf{q}} [\text{tmp}_1] \quad \mathcal{O}(n) \xleftarrow{\text{Reverse-Mode AD}}$$

$$\mathbf{T}_1 = \frac{\partial}{\partial \mathbf{q}} [\text{tmp}_2] \quad \mathcal{O}(n^2) \xleftarrow{\text{AD}}$$

$$\text{tmp}_3 = \text{mRNEAc} \left(\mathbf{q}, 0, \frac{\partial \ddot{\mathbf{q}}}{\partial \mathbf{q}}, 0, \frac{\partial \boldsymbol{\lambda}}{\partial \mathbf{q}}, \boldsymbol{\mu}, \boldsymbol{\pi} \right) \quad \mathcal{O}(n^2)$$

$$\mathbf{T}_2 = \frac{\partial}{\partial \mathbf{q}} [\text{tmp}_3] \quad \mathcal{O}(n^2) \xleftarrow{\text{Reverse-Mode AD}}$$

$$\boldsymbol{\gamma}^\top \frac{\partial^2 \boldsymbol{\nu}}{\partial \mathbf{q}^2} = \mathbf{T}_1 + \mathbf{T}_2 + \mathbf{T}_2^\top$$

Substitute