

I

Dynamics

$$\underbrace{\begin{bmatrix} \mathbf{H} & -\mathbf{J}_c^\top \\ -\mathbf{J}_c & 0 \end{bmatrix}}_{\mathbf{K}} \underbrace{\begin{bmatrix} \ddot{\mathbf{q}} \\ \lambda \end{bmatrix}}_{\boldsymbol{\nu}} = \underbrace{\begin{bmatrix} \mathbf{S}^\top \boldsymbol{\tau} - \mathbf{h} \\ \mathbf{J}_c \dot{\mathbf{q}} \end{bmatrix}}_{\boldsymbol{\Psi}}$$

$$\boldsymbol{\nu} = \mathbf{K}^{-1} \boldsymbol{\Psi}$$

AD

II

Conventional iLQR

AD tools once:  $\frac{\partial \boldsymbol{\nu}}{\partial \mathbf{q}}$   $\mathcal{O}(n^2)$

III

Conventional DDP

$$\frac{\partial^2 \boldsymbol{\nu}}{\partial \mathbf{q}^2} \quad \mathcal{O}(n^3)$$

AD

$$\gamma^\top \frac{\partial^2 \boldsymbol{\nu}}{\partial \mathbf{q}^2} \quad \mathcal{O}(n^3)$$

Contraction