

The impact of gas bulk rotation on the Lyman- α line

Nicolas Garavito-Camargo¹, Jaime E. Forero-Romero¹ and Mark Dijkstra²

¹*Departamento de Física, Universidad de los Andes, Cra. 1 No. 18A-10, Edificio Ip, Bogotá, Colombia*

²

3 October 2013

ABSTRACT

Rotation is present in the gas kinematics of galaxies up to the highest redshifts. In this paper we present for the first time radiative transfer calculations that show the impact of gas bulk rotation on the morphology of the Lyman α line. To this end we model a galaxy as an homogeneous sphere composed as an homogeneous mixture of dust and hydrogen at a constant temperature. These spheres have a solid-body rotation with linear velocities at the surface in the range $0 - 300 \text{ km s}^{-1}$ and neutral hydrogen optical depths in the range $\tau_{\text{H}} = 10^5 - 10^7$. We consider radiation sources both in the center of the rotating cloud and also homogeneously distributed in the volume. We find that higher rotational velocities increase the width of each peak in the outgoing line profile while it also increases the amount of Lyman alpha photons escaping in the line center. This trends makes that for high rotational velocities and large Hydrogen optical depths the double peak of the line tends to be erased and be replaced by a single peak at the line center. This trend is more pronounced for radiation sources homogeneously distributed. Concerning the escape fraction we find that rotation does not have any effect, provided that all the sources are centrally emitted. However, in the case of homogeneously emitted sources we measure an increase of about a factor of 2 in the escape fraction for higher rotational velocity values. This work shows that gas bulk rotation has a non negligible impact on the shape of the Lyman α line.

Key words: galaxies: high-redshift - galaxies: star formation - line: formation

1 INTRODUCTION

The detection of strong Ly α emission lines has become an essential method in extragalactic astronomy to find distant star-forming galaxies (?????). The galaxies detected using this method receive the name of Ly α emitters (LAEs). A detailed examination of this galaxy population has diverse implications for galaxy formation, reionization and the large scale structure of the Universe. Attempts to fully exploit the physical information included in the Ly α line require an understanding of all the physical factors involved in shaping the line. Due to the resonant nature of this line, these physical factors include temperature, density and bulk velocity field of the neutral Hydrogen in the emitting galaxy and its surroundings.

A basic understanding for the quantitative behaviour of the Ly α line has been reached through analytical studies in the case of a static configurations, such as uniform slabs (??) and uniform spheres (?). Analytical studies of configurations including some kind of bulk flow only include the case of a sphere with a Hubble like expansion flow (?).

A more detailed quantification of the Ly α line has been reached using Monte Carlo simulations (???). In the last two decades these studies have become more popular due to

the availability of computing power. Early into the 21st century the first studies focused on on homogeneous and static media (???). Later on the effects of clumpy media (?) and expanding/contracting shell/spherical geometries started to be studied (??). Similar codes have applied these results to semi-analytical models of galaxy formation (?) and results of large hydrodynamical simulations (???). Recently Monte Carlo codes have also been applied to the results of high resolution hydrodynamical simulations (????). Recent developments have been focused on the study of clumpy outflows (?) and anisotropic velocity configurations (?).

The recent studies of galaxies in hydrodynamical simulations (????) have all shown systematic variations in the Ly α line with the viewing angle. These variations are a complex superpositions of anisotropic density configurations (i.e. edge-on vs. face-on view of a galaxy), the inflows observed by gas cooling and the outflows included in the supernova feedback process of the simulation. These bulk flows physically correspond to the circumgalactic and intergalactic medium (CGM and IGM). These effects have been systematically studied different anisotropic models of hydrogen clouds varying the density and wind characteristics (?).

However, in all these systematics efforts the effect of

rotation, which is an ubiquitous feature in galaxies, has not been systematically studied. The processing of the Ly α photons in a rotating interstellar medium (ISM) must have an impact in the line morphology. It is necessary to investigate to what extent bulk gas rotation has an measurable impact in the Ly α alpha line.

Performing that study is the main goal of this paper. We investigate for the first time the impact of rotation on the morphology of the Lyman α line. We focus on a simplified system, a spherical gas cloud with homogeneous density and solid body rotation. We focus our study on the line morphology, anisotropic integrated emission and the escape fraction in the presence of dust. We base our work on two independent Monte Carlo based radiative transfer codes CLARA (?) and XX (?) .

This paper is structured as follows. In §2 we present the implementation of bulk rotation into the Monte Carlo codes, paying special attention to coordinate definitions. There we also list the different physical parameters in the simulated grid of models. In the next section we present the results of the simulations, with special detail to quantities in the line that show a clear evolution as a function of the cloud's rotational velocity. In §?? we discuss the implications of our results in the interpretation of LAEs observations and further refinements that can be implemented in the theoretical modelling of the Ly α line. In the last section we present our conclusions.

In this paper we express a photon's frequency in terms of the dimensionless variable $x \equiv (\nu - \nu_a)/\Delta\nu_\alpha$, where $\nu_\alpha = 2.46 \times 10^{15}$ Hz is the Ly α resonance frequency, $\Delta\nu_\alpha \equiv \nu_\alpha \sqrt{2kT/m_p c^2} \equiv \nu_a v_{th}$ is the doppler broadening of the line which depends on the neutral gas temperature T scattering the radiation or equivalently the thermal velocity v_{th} of the atoms.

2 MODELS OF BULK GAS ROTATION

Describing the kinematics of gas rotation in all generality is a complex task, specially at high redshifts where there is still missing a thorough observational account of rotation in galaxies beyond $z > 1.0$. Furthermore, at low redshifts it has been observed a great variation in the shape of the rotation curve as observed in HI emission as a function of the distance to the galaxy center. However there are two features that are observed very often. First, in the central region the velocity increases proportional to the radius, following the behaviour in a body with solid rotation. Second, beyond a certain radius the rotation curve tends to flatten.

An ab-initio description of realistic rotation curves in simulations depends on having access to the dynamic evolution of all mass components in the galaxy: stars, gas and dark matter. Such level of realism is extremely complex to achieve, specially if one wants to get a systematic description based on statistics of simulated objects.

Following the tradition of studies of Lyman α emitting systems, we implement a model with a simplified geometry and gas distribution. We assume that the gas is homogeneously distributed in a sphere that rotates as a solid body with constant angular velocity. This simple model will contain only one parameter: the linear velocity at the sphere's surface, V_{max} .

Physical Parameter (units)	Symbol	Values
Velocity (km s ⁻¹)	V_{max}	0, 50, 100, 200, 300
Hydrogen Optical Depth	τ_H	10 ⁵ , 10 ⁶ , 10 ⁷
Dust Optical Depth	τ_a	0,1
Photons Distributions		Central, Homogeneous

Table 1. List of the physical parameters that define the spherical models simulated in our Monte Carlo calculations. For each parameter we vary the values in the range listed in the last column. Taking into account all the possible combinations we end up with 60 different models.

2.1 Detailed Implementation of Rotation

In the MonteCarlo code we define a cartesian coordinate system to describe the position of each photon. The origin of this system coincides with the center of the sphere and the rotation axis is defined to be z -axis. With this choice, the components of the gas bulk velocity field, $\vec{v} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$, can be written as

$$v_x = -\frac{y}{R} V_{max}, \quad (1a)$$

$$v_y = \frac{x}{R} V_{max}, \quad (1b)$$

$$v_z = 0, \quad (1c)$$

where R is the radius of the sphere and V_{max} is the linear velocity at the sphere's surface. The minus/plus sign in the x/y -component of the velocity indicates the direction of rotation. In this case we take the angular velocity in the same direction as the \hat{k} unit vector. With these definitions we can write the angular velocity as $\omega = V_{max}/R$.

For each photon in the simulation we have its initial position inside the sphere, direction of propagation \hat{k}_{in} and reduced frequency x_{in} . The photon's propagation stops once they cross the surface of the sphere. At this point we store the position, the outgoing direction of propagation \hat{k}_{out} and the reduced frequency x_{out} . We define the angle Θ by $\cos \Theta = \hat{k} \cdot \hat{k}_{out}$, that is the polar angle of the outgoing photon with respect to the z axis. Following ? we make the study of the anisotropic emission in terms of this angle Θ .

2.2 Grid of Simulated Galaxies

In the Monte Carlo calculations we follow the propagation of $N_\gamma = 10^5$ numerical photons through different spherical galaxies. For each galaxy we vary at least one of the following parameters: the maximum rotational velocity V_{max} , the hydrogen optical depth τ_H , the dust optical depth τ_a and the initial distribution of photons with respect to the gas. There are in total 60 models combining all the input parameters. Table 1 presents a summary of all the models.

Additionally, we have used two independently developed Monte Carlo codes (??) to perform the calculations of the non-dusty models. The results we report here are robust in the sense that they are obtained by both codes.

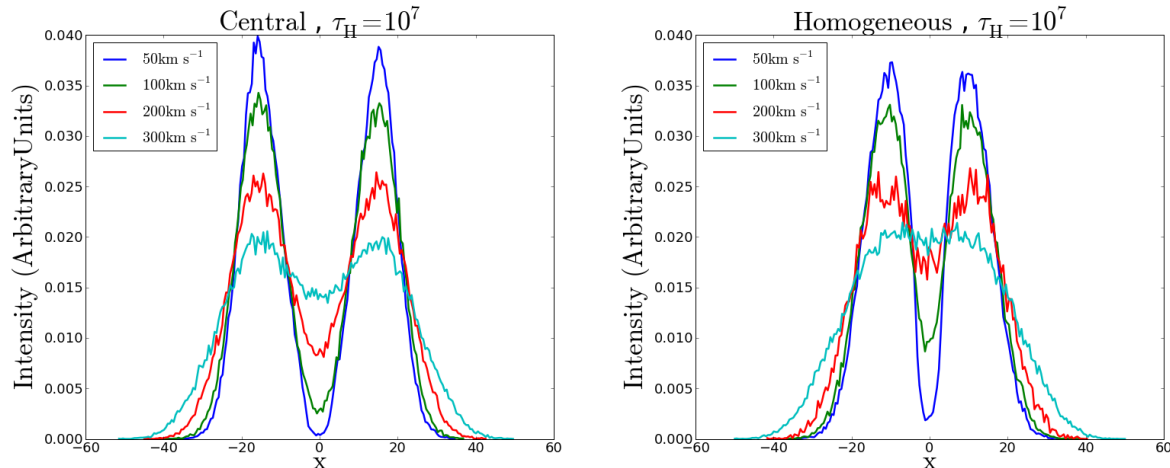


Figure 1. Shape of the Ly α line for different velocities rotational velocities for spherical distributions with $\tau_H = 10^7$. The left (right) panel shows the central (homogeneous) photon distribution. All photons were taken into account regardless of their final direction of propagation.

3 RESULTS

The central result of this paper is summarized in Figure 1. It shows the considerable impact of rotation on the morphology of the emergent Ly α line. Both panels in the Figure focus on the results for $\tau_H = 10^7$, showing that the influence of rotation is present both when the photons are either homogeneously or centrally initialized over the gas volume.

In the following subsections we characterize the line morphology by the half-width at half intensity and the peak maxima. In order to interpret the morphological changes in the line we also report the median number of scatter for each Ly α photon in the simulation. For the models where dust is included we measure the bulk escape fraction as a function of rotational velocity. Finally, we make an estimate of the anisotropic emission of the models in comparison with static spheres.

3.1 Line width and peak maxima

The first quantitative conclusion of the effect of rotation in the Ly α line is that double peaks broaden and reduce their intensity while the line center rises. This produces the impression that, as the rotational velocity increases, the double peaks are merged into a single broad emission peak. This is most evident at the highest rotational velocities for the homogeneously distributed sources (right panel in Figure 1).

To quantify the line broadening we use a modified version of the full width at half maximum (FWHM). We measure it only for half of the line, $W_{1/2}$. This definition allows us to quantify the line width and see the transition from double to single peak emission. In the case of double peaked emission $W_{1/2}$ corresponds to the width of a single peak, while in the extreme case of high rotational velocities, when the double peak is erased, it simply correspond to half FWHM.

Figure 2 shows how $W_{1/2}$ increases with rotational velocity. Continuous (dashed) lines connect the results for homogeneous (central) source distribution. For the tempera-

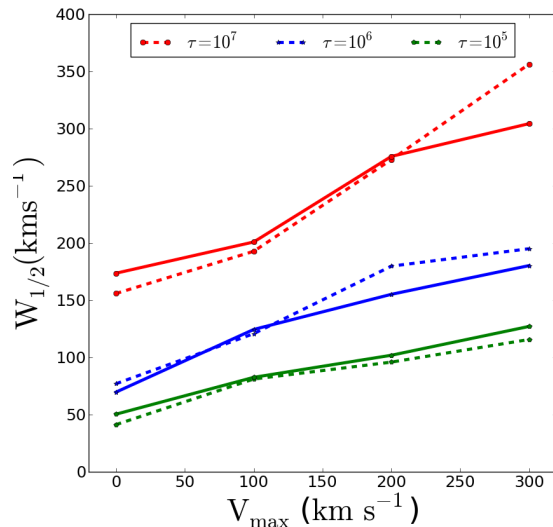


Figure 2. Half-width for the non-dusty models as a function of rotational velocity V_{\max} . Continuous (dashed) lines correspond to homogeneous (central) source distributions.

ture $T = 10^4$ K used in our radiative transfer calculations the thermal velocity is $v_{th} = 12.8$ km s $^{-1}$. For a model with τ_H it means that the half-width can increase up to 350 km s $^{-1}$ (at $V_{\max} = 300$ km s $^{-1}$) compared to a half-width of 150 km s $^{-1}$ in the static case.

Figure 3 shows the position for the peak maxima as a function of the rotational velocity V_{\max} . This Figure clearly shows that in the case of central distributed sources there is barely any change with rotational velocity in the range of explored parameters. However, in the case of homogeneously emitted sources the maxima position remain close to constant until beyond some velocity threshold the line becomes single peaked with $x_{\max} = 0$ km s $^{-1}$.

The transition to a single peak line seems to occur for

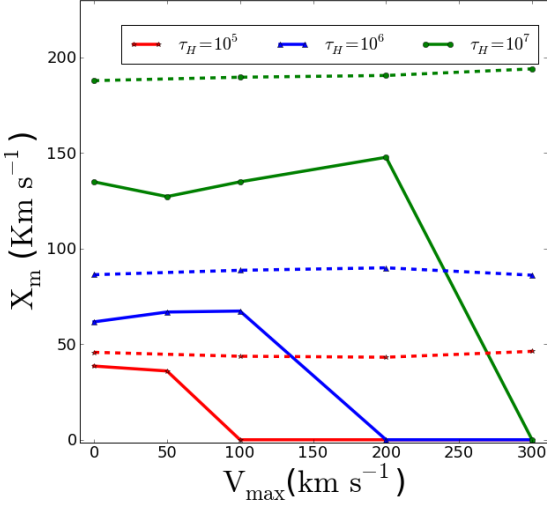


Figure 3. Position of the peak maxima as a function of rotational velocity V_{\max} . Continuous (dashed) lines correspond to homogeneous (central) source distributions. A value of $x_{\max} = 0$ indicates that line becomes single peaked.

systems where it becomes easier for the bulk of the photons to escape with the lowest number of scatterings possible, allowing them not to move very far from the center of the line. This might explain how the single peak stage is easily achieved in the homogeneous source distribution. In this case there is a fraction of the photons that are inside a photosphere region with $\tau_{H,r} \ll \tau_H$ where $\tau_{H,r}$ is the optical depth from the radius of emission to the sphere's surface. This conditions allows the photons to escape with much less scatterings compared to the photons emitted at the very center of the sphere. In turn, it gives the photons less scatterings to be placed far from the line center.

Increasing the rotational velocity V_{\max} reduces the optical depth making the photosphere region effectively larger, increasing the number of photons escaping close to the lines's center. In our models we find the following correspondence between the optical depth $\tau_H = \{10^5, 10^6, 10^7\}$ and the transitional velocities $V_{\text{trans}} = \{50 - 100 \text{ km s}^{-1}, 100 - 200 \text{ km s}^{-1}, 200 - 300 \text{ km s}^{-1}\}$ which can only be constrained to be in the range of velocities in the models that gave a $x_{\max} \neq 0$ and $x_{\max} = 0$.

For the central emission the transition to a single peak is never completed in the range of parameters explored here. The nonappearance of a single peak phase can be in part explained to the absence of a photosphere, as is the case in the homogeneous distribution. Nevertheless, there is a rise in the intensity at the line center as the rotational velocity increases. This hints that the encounters with a nonstatic medium are inefficient in changing a photons' frequency out-side the line center.

In the next section we quantify the number of scatterings and explore to what extent this is related to the emergence of single peak.

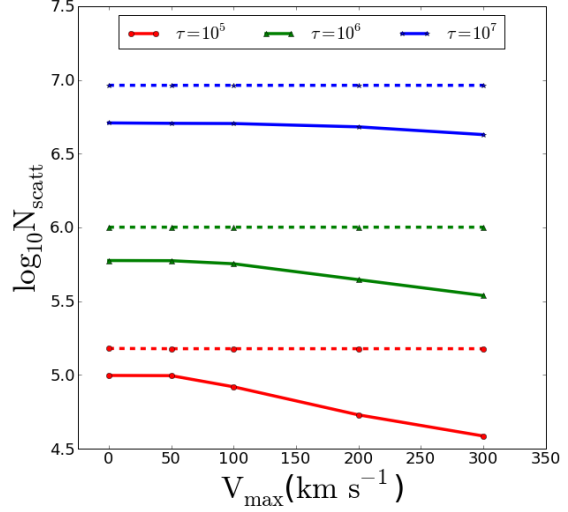


Figure 4. Logarithm of the average number of scatterings as function of the velocity. Continuous/dashed lines represent an homogeneous/central distribution of sources.

3.2 Average Number of Scatterings

The number of times that a Ly α photon is absorbed and re-emitted is connected to the final frequency that it can have after escaping the galaxy. In the case of static gas geometries, a large value of the optical depth is immediately followed by a high number of scatterings. In turn a large optical depth increases the probability that a Ly α photon to be found far from the center of the line. In this case, the peak maxima shift away from the line center as the amount of neutral hydrogen increases.

In Figure 4 we show the average number of scatterings $\langle N_{\text{scatt}} \rangle$ as a function of the rotational velocity V_{\max} . For the central distributions we find that there is not a significant change for increasing rotational velocities, $\langle N_{\text{scatt}} \rangle$ changes less than 0.5% for different velocities. In this case we also find that the average number of scatterings is proportional to the optical depth, as expected in analogy from the analytic result for the homogeneous infinite-slab $\langle N_{\text{scatt}} \rangle = 1.612\tau_H$ (??). In our experiments we find that for the static spheres with centrally distributed sources $\langle N_{\text{scatt}} \rangle = (1.50, 1.00, 0.92)\tau_H$. for optical depths $\tau_H = (10^5, 10^6, 10^7)$

Figure 4 shows that for the homogeneous distribution there is a clear decrease of $\langle N_{\text{scatt}} \rangle$ as the V_{\max} increases. This effect more pronounced for the lower values of the optical depth. For $\tau_H = 10^5$ the average number of scatterings decreases by 61% at $V_{\max} = 300 \text{ km s}^{-1}$ in comparison to the static case.

The analytic expectation for the slab with homogeneously emitted sources is $\langle N_{\text{scatt}} \rangle = 1.16\tau_H$ (?), a factor of 0.72 lower than the case of the centrally emitted photons. In our case we find that for the static, while for homogeneously distributed source $\langle N_{\text{scatt}} \rangle = (0.99, 0.59, 0.51)\tau_H$, this represents a factor of (0.66, 0.59, 0.51) lower than the centrally emitted photons.

In order to gain a deeper understanding of these results we prepare 2D histograms for the number of scatterings as a

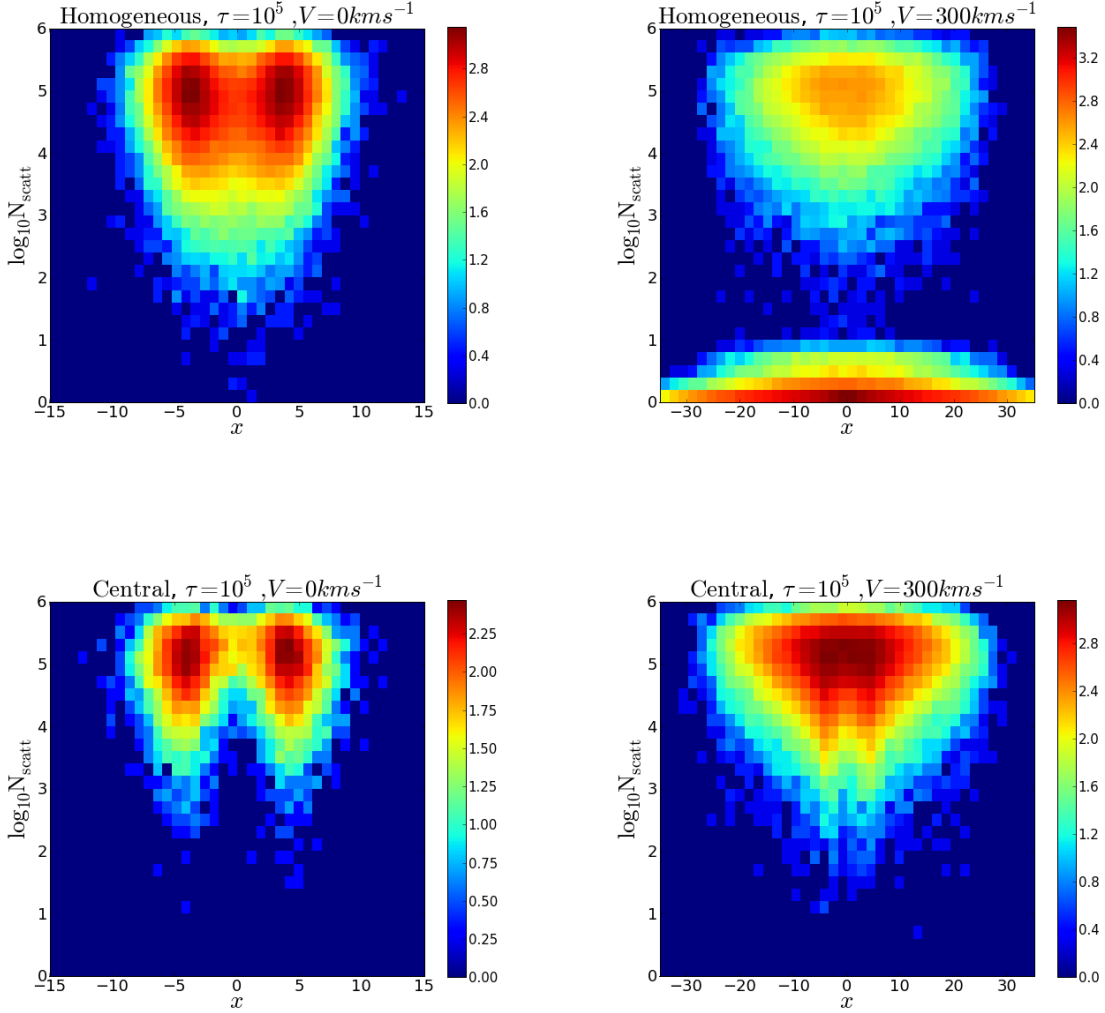


Figure 5. 2D histogram of N_{scatt} vs x . The upper (lower) panels show the homogeneous (central) source distribution. Left corresponds to the static case and the right $V_{\text{max}} = 300 \text{ km/s}$. The colour scale is logarithmic on the number of photons with given values of N_{scatt} and x .

function of the outgoing dimensionless frequency x . In Figure 5 we show the results of such histogram in the case $\tau_{\text{H}} = 10^5$ for the static case and $V_{\text{max}} = 300 \text{ km s}^{-1}$. The upper (lower) panels show the results for the homogeneous (central) source distribution. The color scale is logarithmic in the number of photons at a certain value $x - N_{\text{scatt}}$. This Figure clearly support our hypothesis about the photosphere in the homogeneous distribution, in this case most of the photons that left with $x \sim 0$ have escaped with less than 10 scatterings, explaining the origin of a single central peak. However, for a central distribution the situation is different. In this case the number of scatterings remains high, on the order of the optical depth, but the two peaks do get closer to each other. In this case the physical picture is that each scattering, due to the bulk velocity of the gas, is inefficient in driving the photon outside the line center.

3.3 Dusty Clouds: Escape Fraction

We also study a dusty cloud configuration to measure the effect of rotation on the escape fraction. We expect that the modified number of scatterings to be reflected in this amount of photons absorbed by dust. Following this line of thought, we do not expect any change in for a dusty cloud with central source of radiation given that the number of scatterings remains close to constant. On the other hand, in the case of an homogeneous radiation source the number of scatterings drops as V_{max} increases, which might be reflected as an increasing escape fraction.

Figure 6 shows the dependence of the escape fraction as a function of the maximum rotational velocity, confirming that our intuitions in this respect is correct. For the central source distribution the escape fraction barely shows any change, while for the homogeneous case there is a clear rise in the escape fraction for high rotational velocities.

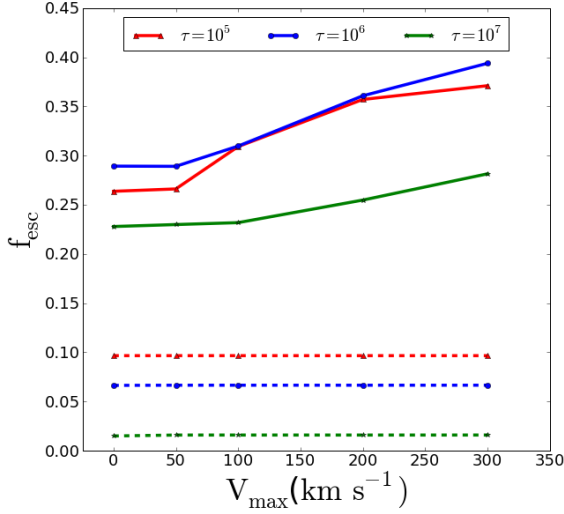


Figure 6. Escape fraction as a function of rotational velocity. The continuous (dashed) lines correspond to homogeneous (central) models.

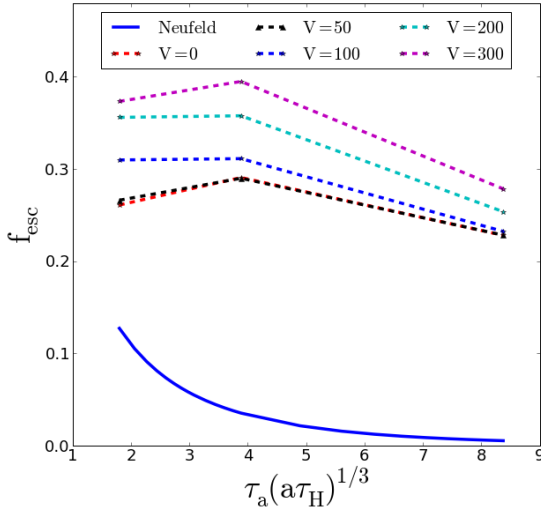


Figure 7. Escape fraction as a function of the product $(a\tau_H)^{1/3}\tau_a$. The analytic solution for the infinite slab shown as a continuous line. Different dashed lines correspond to different rotational velocities.

Rotation has a higher relative impact in the models with low optical depth $\tau_H = 10^5, 10^6$, where it can raise from (0.26, 0.28) respectively in the static case up to (0.37, 0.39) at $V_{\text{rot}} = 300 \text{ km s}^{-1}$.

In Figure 7 we put these results in the context of the analytical solution for the infinite slab (?). In Neufeld's setup the analytic solution depends solely on the product $(a\tau_H)^{1/3}\tau_a$, an approximation that is valid only in the limits $a\tau_H \gg 1$. The dashed lines in Figure 7 correspond to the cases of different velocities. We observe that the escape fraction is higher by factors of 2 – 10 than the expected values for the slab configuration. We also see that for the lower

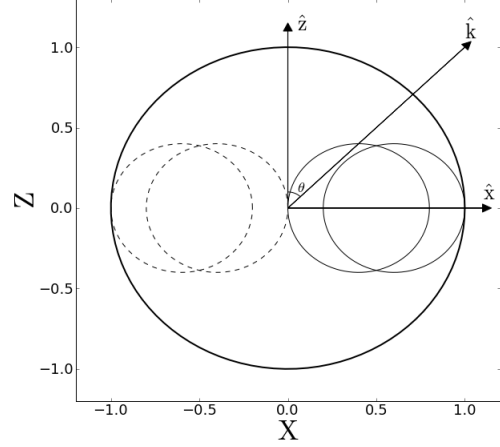


Figure 9. The two solid circles show up the photons we select in order to make the anisotropic emission rotation is defined to be z-axis. we also select photons in the negative side of x (dashed circles) in order to see the complete effect of rotation.

value $\tau_H = 10^5$ the escape fraction does not increase with respect to the solution for $\tau_H = 10^6$ as expected, however we note that we are in a regime where the condition for the analytic expectations ($a\tau_h \gg 1$) does not hold.

3.4 Anisotropic emission

We study the deviations of the received flux on the surface of the sphere. We follow ? to estimate the flux seen by an observer located at an angle Θ (distant observer angle) normalized to the isotropic flux:

$$F(\mu) = \frac{2\Delta N}{N\Delta\mu}, \quad (2)$$

where $\mu = \cos \Theta$, N is the total number of outgoing photons, ΔN is the number of photons in an angular bin $\Delta\Theta$. This definition satisfies the condition $\int_{-1}^1 F(\mu)d\mu/2 = 1$.

In Figure 8 we show the angular dependency of the flux for the central (left) and homogeneous (right) source distributions. This shows that observers at different directions would infer luminosities different from the isotropical value only at levels $< 3\%$.

3.5 Off-Centered emission

As we know there is unlikely to find galaxies with radiation sources distributed homogeneously. Most of them are in a clumpy distribution (Laursen et al 2013*) which affected the resulting spectra. In order to study an inhomogeneous distribution we set up a model in which we select certain photons that are placed in a specific place but that are not symmetrically distributed Fig. 9 shows the distributions we set up, basically we take photons located in a sphere of $0.5R$ where R is the radii of the homogeneous sphere and we choose two spheres in each side of the \hat{x} axis two at $0.25R$ and the other two at $0.5R$.

As a primer approach we study the angular dependency

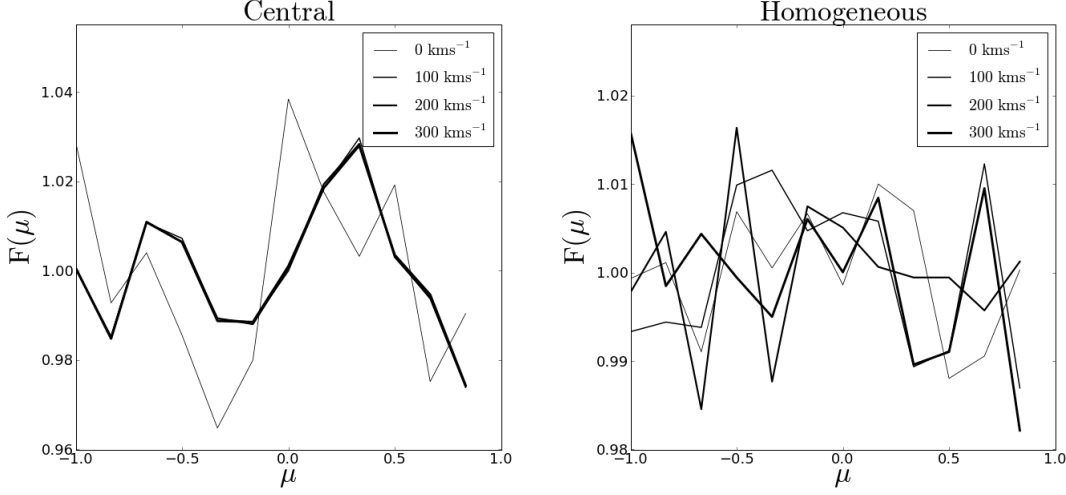


Figure 8. Flux angular dependency for the central (left) and homogeneous (right) source distributions, different line widths illustrate different rotational velocities.

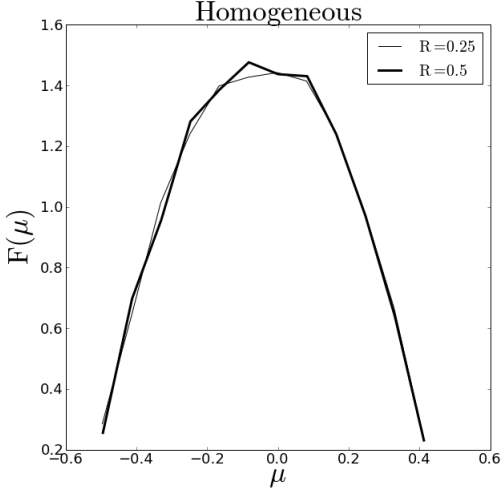


Figure 10. Flux angular dependency for Off-center distribution, different line widths illustrate different off-center positions.

in the same manner as we do in section 3, but with the set up of the off-center models where the galaxy is rotating around the \hat{z} axis and the observer is located at $\theta = \pi/2$. In Fig. 10 the angular dependency for two different off-center distribution are shown. The bold line represents an off-center sphere located at $0.25R$ in the homogeneous sphere, while the narrow line shows a sphere located at $-0.25R$. This is done for the model with $\tau = 10^5$ and $V = 50 \text{ km s}^{-1}$, but results with the rest of models show exactly the same trend. We find a high dependency in the viewing angle in particular the flux at $\theta = \pi/2$ is $\simeq 88\%$ stronger than at $\theta = \pi/3$ this have important consequences in observations when galaxies are oriented in random directions which implies that off-center emission is not going to be observed in all the observed galaxies.

The outgoing spectra for two different spheres located

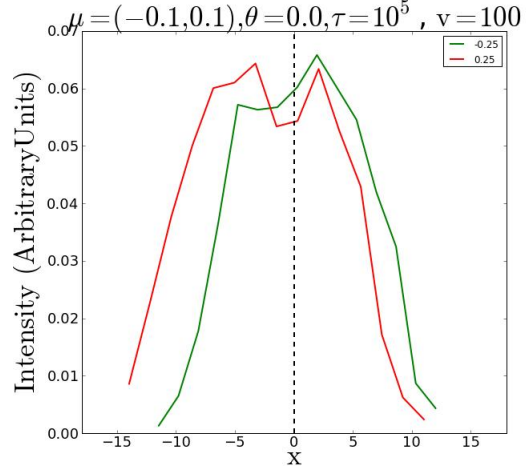


Figure 11. Spectra for two off-center spheres

at $-0.25R$ and $0.25R$ respectively are shown in Fig. 11, we have shown this positions because they are most sensitive to the effect of rotation.

There are two new morphological features that off-center emission in rotating galaxies produces. First in some of our models with specific values of velocity and optical depth an asymmetry in the peak heights is presented, those off-center spheres (*put image reference*) located at the positive side of \hat{x} in Fig.9 present a higher peak in the red-shifted part, while those spheres located at the negative side of \hat{x} present a higher blue shifted peak, we found that the higher asymmetry is for model with $\tau = 10^7$, $V = 200 \text{ km s}^{-1}$ where one peak is 20% higher than the other.

This can be appreciated for both set of spheres at $0.25R$ and $0.5R$, but the effect shows a stronger asymmetry for spheres located at $0.25R$ this due to the fact that photons escaping from this spheres goes through a larger hydrogen medium than photons located in the spheres at $0.5R$.

Also for all the off-center models we found that the $\text{Ly}\alpha$ line width ...

Also for photons located in the spheres at $0.5R$, we found that for some models ($\tau = 10^6$, $V = 100\text{km s}^{-1}$ and $\tau = 10^7$, $V = 200\text{km s}^{-1}$) the line presents three peaks (blue-shifted, centered, red-shifted). In order to gain a better interpretation of this three peaks trend we run this models with $N_\gamma = 10^6$.

4 DISCUSSION

Following the classification of $\text{Ly}\alpha$ profiles made for (Kulas et al, put reference) we divide our results in 3 different groups. Group I represents profiles in which the flux in the red side is stronger than in the blue part, while Group II represents profiles in which the blue side is the stronger. Group III represents single peaked profiles while Group IV represents multi-peaked profiles.

Group I profiles may be explained in our model when off-center emission is present and the location of this photons emission is stronger in the , while Group II profiles correspond to emissions in the ..

Group III profiles are better represented by galaxies rotating at $V > 100\text{km s}^{-1}$

... Comparison with Verhamme et al. results on the rotation (Viewing angle)

... Compare with Kulas et al (Figure 3), Rotation on the Lyman alpha line convert double peak profiles into a single one. comments about rotation with inflows and outflows.

... The results derived in this paper have consequences on the interpretation of galaxy observations in the Lyman alpha line.

..compare steidel et al (2011)

5 CONCLUSIONS

In this paper we have estimated the effects of gas bulk rotation on the emission of the Lyman α line. We based the study on the study of a simplified configuration of an homogeneous sphere rotating as a solid body. We explored a range of models by varying the rotation speed, hydrogen optical depth, dust optical depth and initial distribution of $\text{Ly}\alpha$ photons with respect to the gas density. This was implemented in CLARA, a Monte-Carlo radiative transfer code already used to study the Lyman α line.

As first we see how the width of the line changes using a modified FWHM explained in section 3.1, and we found that as gas bulk rotation increase also the width increase in a factor of 2 – 3 in comparison with the static case. 'We also take into account the influence of the observer viewing angle, we found that observers with a line of sight perpendicular to the axis of rotation measure a 15% larger line width than those aligned with the rotation axis.'

As many observational spectra $\text{Ly}\alpha$ emission line (Kulas et al, Yamada et al) is double peaked, these peaks provide important information concerning gas kinematics and geometry, which can be partially explained with inflows/outflows of gas content. We study the effect of rotation in the position of this peaks, and we find that the position of the max-

ima does change with rotation for the homogeneous models when the double peak merged into a single peak as velocity increase. This effect is not seen for the central distribution when the double peak remains constant as the velocity increase. We also find that there is no dependency in the observer viewing angle with the maxima position.

Concerning the escape fraction under rotational effects on the $\text{Ly}\alpha$ emission line, we found that the escape fraction increase in about 20% – 30% for the homogeneous sphere model. While rotational effects are negligible for the central models and the escape fraction remains constant. Also the observer viewing angle have no effect in the escape fraction neither for the homogeneous and central models. Complementing this analysis we study the average number of scatterings $\langle N_{scatt} \rangle$ that photons perform before escaping of the cloud taking into account rotational effects. The main result here is for the homogeneous models for which as velocity increase photons escape with about $\sim 39\%$ less scatterings than in the static case.

This paper illustrates for the first time the main effects of rotation in the morphology of the $\text{Ly}\alpha$ emission line, we estimate the range of this effects for simplified models.

ACKNOWLEDGEMENTS

APPENDIX A: TABLES