

CSE 331
Assignment 1
Summer 2025

Deadline : 25th July

Submit in google classroom. Don't forget to turn in.

1. Draw DFA's accepting the following languages over the alphabet $\{0,1\}$:
 - a. Draw a DFA for the set of strings that have three consecutive 0s.
 - b. Draw a DFA for the set of strings that doesn't contain 0s. $\Sigma = \{0,1\}$
 - c. Draw a DFA of strings that ends with "0101".
 - d. Construct a DFA defined as $L = \{ w \in \{0,1\}^* : w, \text{ when interpreted as a binary number, is divisible by 5.} \}$
 - e. The set of binary numbers has 0 in all even positions. $\Sigma = \{0,1\}$.
 - f. Draw a DFA which accepts exactly two "00" as a substring.
 - g. Draw a DFA which accepts at most two "00" as a substring.
2. Draw DFA's accepting the following languages over the alphabet $\{0,1\}$:
 - a. $L_1 = \{w \in \text{a string where 1 is followed by at least one 0}\}$, $\Sigma = \{0, 1\}$
 - b. $L_2 = \{w \in \text{a string which contains of odd length}\}$, $\Sigma = \{0, 1\}$
 - c. $L_3 = L_1 \cap L_2$
 - d. $L_4 = \{w \in \text{A string has substring of '010'}\}$, $\Sigma = \{0, 1\}$
 - e. $L_5 = \{w \in \text{start and ends with same symbol}\}$, $\Sigma = \{0, 1\}$
 - f. $L_6 = L_4 \cap L_5$
3. Draw DFA's accepting the following languages over the alphabet $\{a,b\}$:

- a. Construct a DFA that accept the language, $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with different symbols.} \}$
 - b. Construct a DFA that accept the language, $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with the same symbol.} \}$
 - c. Construct a DFA defined as $L = \{ w \mid \text{each "b" is followed by at least one "a"} \}$ $\Sigma = \{a,b\}$ For example: baaa
4. Write regular expressions for the following languages:
 - a. The set of all strings of 0s and 1s such that every pair of adjacent 0s appears before any pair of adjacent 1s
 - b. The set of all strings of 0s and 1s **not containing** 101 as a substring.
 - c. $\{ w \mid w \text{ has an even number of a's and each a is followed by at least one b} \}$
 - d. $\{ w \mid w \text{ is any string that doesn't contain exactly two a's} \}$
 - e. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ contains at least two 1s.} \}$
 - f. $\{ w \mid w \text{ starts with 0 and has odd length, or starts with 1 and has even length} \}$
 - g. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain 00 and 11.} \}$
5. Give english descriptions of the languages of the following regular expressions:
 - a. $(1 + \varepsilon)(00^*1)^*0^*$
 - b. $(0 + 10)^*1^*$
6. Convert the following regular expressions to NFAs with ε - transitions
 - a. 01^*
 - b. $00(0 + 1)^*$
 - c. $0^*(0 + 1)^*010 + 1^*0(10 + 1)^*$