BDA Project: Hurricane forecasting in Stan

José Miguel Ramírez & Jonas Lindblad Aalto University

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- They can cause extreme levels of flooding and destroy many buildings.
- Monetary damages and loss of lives increase with an almost exponential character as a function of storm intensity.



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- Rapid intensification: forecasted better by dynamical models
- This project: a statistical model for intensity

The US government forecasting agency, the National Hurricane Center (NHC), uses a large number of models operationally. The models (together: the *model ensemble*) are used together with experienced meteorologists' judgment to provide the official forecast.

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- SHIPS: ~140 covariates, many calculated from data sources more easily available to the NHC
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- ... but the documentation is terrible
- SHIPS: only a point estimate; our project: a predictive distribution

The SHIPS developmental data is confusing!

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We are making synoptic models.

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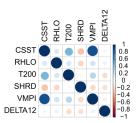
We are making synoptic models and choosing variables.

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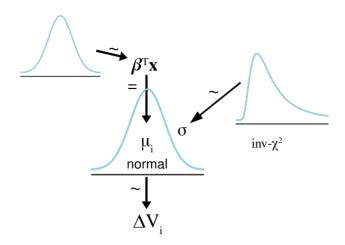
We have not done statistical variable selection. Choice of variable subset is based on theory.

- CSST: (climatological) sea surface temperature
- RHLO: low-altitude relative humidity
- **T200**: air temperature at 200 mb (very high altitude)
- SHRD: wind shear between 850 and 200 mb
- VMPI: maximum potential intensity



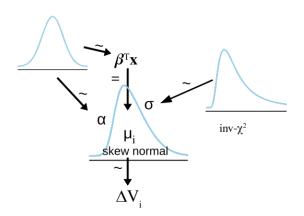
- for testing, we have variable sets A, B, C
- A: LAT/LON, VMAX, CSST, SHRD
- B: LAT/LON, VMAX, CSST, SHRD, VMPI
- C: LAT/LON, VMAX, CSST, SHRD, VMPI, RHLO, T200

The SHIPS Blunder: a simple linear regression



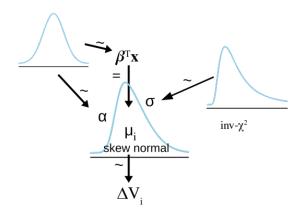
Model 2: regression with skewness

errors not symmetric around the mean prediction!



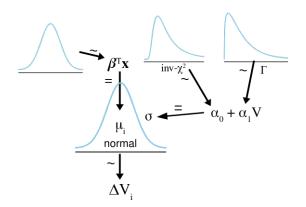
Model 2: regression with skewness

- errors not symmetric around the mean prediction!
- rapid intensification!



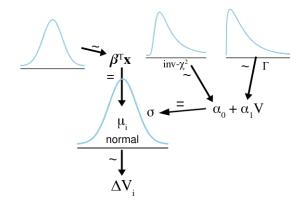
Model 3: regression with a linear model for standard deviation

fewer storms reach higher values of VMAX



Model 3: regression with a linear model for standard deviation

- fewer storms reach higher values of VMAX
- allow for higher variance to account for larger historical uncertainty



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Models: some remarks

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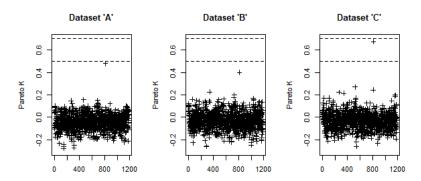
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- SHIPS data: 1982-2019; our restriction: 2017-2019
- poor problem setup! True model is the laws of physics, but we are fitting a regression
- models were programmed in Stan; sampling with rstan resulted in no divergences or issues except for the skew model and the issue was solved by increasing max tree depth to 15

Forecasting: Model Comparison

Forecasting: Model Comparison

Dataset comparison for the linear regression model (LOOCV)

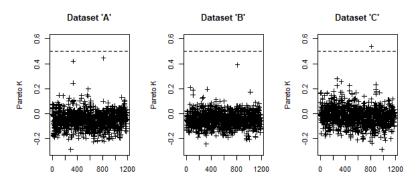
Dataset	elpd_diff	se_diff
С	0.0	0.0
В	-25.0	6.5
Α	-27.4	6.3



Forecasting: Model Comparison (2)

Dataset comparison for the skewed regression model (LOOCV)

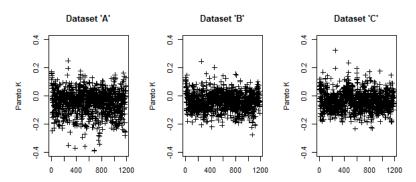
Dataset	elpd_diff	se_diff
С	0.0	0.0
В	-23.2	6.2
Α	-28.7	6.2



Forecasting: Model Comparison (3)

Dataset comparison for the **Changing variance model** (LOOCV)

Dataset	elpd_diff	se_diff
С	0.0	0.0
В	-32.6	8.2
Α	-37.1	8.2



Forecasting: Model Comparison (4)

Model comparison using the Dataset C (LOOCV)

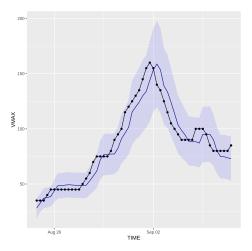
Model	elpd_diff	se_diff
Variance	0.0	0.0
Skew	-176.3	27.8
Linear	-205.5	34.9

Marginal posteriors

- θ_1 : constant term
- θ_2, θ_3 : latitude, longitude
- θ_4 : sea surface temperature (CSST)
- θ_5 : relative humidity (RHLO)
- θ_6 : wind shear (SHRD)
- θ_7 : maximum potential intensity (VMPI)
- θ_8 : air temperature at 200 mb (T200)
- θ_9 : intensity at storm core (VMAX)

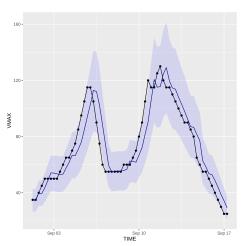
Forecasting: checking predictions

Hurricane Dorian 2019. The image shows a 90% credible interval. Black dotted line: true VMAX



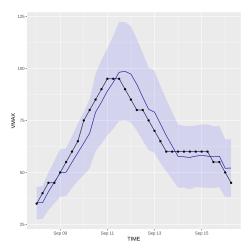
Forecasting: checking predictions

Hurricane Florence 2018. The image shows a 90% credible interval. Black dotted line: true VMAX



Forecasting: checking predictions

Hurricane Helene 2018. The image shows a 90% credible interval. Black dotted line: true VMAX



Further development ideas:

variable selection in full SHIPS dataset

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- variable selection in full SHIPS dataset
- more time series autoregressive components

Further development ideas:

- variable selection in full SHIPS dataset
- more time series autoregressive components
- use LGEM model (will explain)

A final takeaway

"The hurricane will be moving through an environment of low vertical wind shear, a moist mid-level atmosphere, and increasing upper-ocean heat content, and this is ideal for some additional intensification. However, given that the SHIPS models do not show any significant change in the intensity, the NHC forecast keeps Irma a powerful hurricane through five days."

— NHC 5AM advisory Sep. 5th

While the NHC published the advisory, Irma was undergoing rapid intensification from 130 to 175 knots over a span of only a few hours.

Conclusions & contact info

- Takeaway: the SHIPS model is terrible!
- Simple changes to the predictive distribution can improve the model
- Further development using Bayesian methods seems promising and there are several possible directions

More at our Github repo:

https://github.com/jnlb/bda-hurricane-modeling

The SHIPS website: http://rammb.cira.colostate.edu/research/tropical_cyclones/ships/index.asp

Contact info:

José Miguel Ramírez

Jonas Lindblad

rocket-chat: @jnlb

Additional information

The SHIPS model:

$$y_i \sim \mathcal{N}(\alpha + X_i \cdot \beta_{N-1}, \sigma), i = 1, \dots, r,$$

where we let X_i denote the i:th row of the data, β_{N-1} is an N-1-dimensional parameter vector, and r is the number of observations (rows) in the data. Its priors were

$$\begin{bmatrix} \alpha_0 \\ \beta_{N-1,0} \end{bmatrix} \sim \mathcal{N}(\mathbf{0}_N, 10 \cdot \mathbf{I}_N), \sigma_0 \sim \text{Inv-}\chi^2(\frac{1}{10}).$$

The skew-normal regression model:

$$y_i \sim \text{SkewNormal}(\alpha + X_i \cdot \beta_{N-1}, \sigma, \psi), \quad i = 1, \dots, r,$$

with priors

$$\begin{bmatrix} \alpha_0 \\ \beta_{N-1,0} \end{bmatrix} \sim \mathcal{N}(\mathbf{0}_N, 10 \cdot \mathbf{I}_N), \sigma_0 \sim \text{Inv-}\chi^2(\frac{1}{10}), \ \psi_0 \sim \mathcal{N}(0, 1).$$

Additional information

The variance model:

$$y_i \sim \mathcal{N}(\alpha + X_i \cdot \beta_{N-1}, \sigma + \gamma | V_{\max,i} |), i = 1, \dots, r,$$

where, again, we use the same notation as before and let $V_{max,i}$ denote the V_{max} -value of the i:th row. The priors that were fed into Stan were

$$\begin{bmatrix} \alpha_0 \\ \beta_{N-1,0} \end{bmatrix} \sim \mathcal{N}(\mathbf{0}_N, 10 \cdot \mathbf{I}_N), \ \sigma_0 \sim \text{Inv-}\chi^2(\frac{1}{10}), \ \gamma_0 \sim \Gamma(1,1).$$

Additional information

The variance regression was run in rstan with the following options