

```

def get_prime(bits):
    num = random.randint(1, bits)
    while num is composite:
        fermat(num)
        num = random.randint(1, bits)
    return num

```

```

p = get_prime(bits)
q = get_prime(bits)

```

$p = 27 \quad q = 11$

```

def extendedEuclid(a, b):
    # a is (p-1)(q-1) and b is e
    if b == 0: return (1, 0, a)
    (x', y', d) = extendedEuclid(b, a mod b)
    return (y', x' - (a/b)y', d)

```

```
def get_prime(bits):  
    num = random.randint(1, bits)  
    while num is composite:  
        fermat(num)  
        num = random.randint(1, bits)  
    return num
```

```
p = get_prime(bits)  
q = get_prime(bits)
```

$p = 27$ $q = 11$

ModExp - Used in Primality Tester

↳ used to find $x^y \pmod N$

modexp(x, y, N)

if $y = 0$:

return 1

$z = \text{modexp}(x, \lfloor y/2 \rfloor, N)$

if y is even:

return $z^2 \pmod N$

else:

return $x \cdot z^2 \pmod N$

%

Fermat: Uses modexp to find if $a^{N-1} \equiv 1 \pmod N$

bool fermat(x, y, N):

if $\text{modexp}(x, y, N) \equiv 1 \pmod N$:

return true

else:

return false

PrimeTest(N):

pick random int $a, < N$:

if fermat($a, N-1, N$):

return yes

else:

return no

> $\frac{1}{2^k}$ times returns correct answer

$1 - \frac{1}{2^k}$

PrimeTest2(N):

for $i = 1$ to k :

if PrimeTest(N) == 'no':

return 'no'

else:

return 'yes'

$$a^{n-1} \not\equiv 1 \pmod N$$

$$a^{n-1} \equiv 1 \pmod N$$

```

MillerRabin(x, y, N):
    if y == N-1 and (modexp(x, y, N) ≡ 1 mod N):
        return true
    if  $\frac{y}{2} \notin \mathbb{R}$ :
        return true
    if modexp(x, y, N) ≠ 1 mod N:
        return false
    return MillerRabin(x,  $\frac{y}{2}$ , N)

```