

# Multinomial Processing Tree with JAGS

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# Multinomial Processing Trees

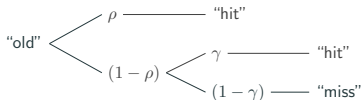
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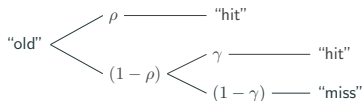
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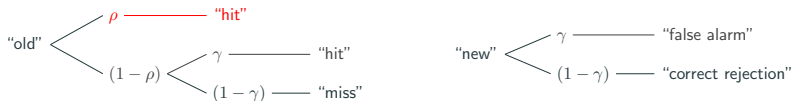
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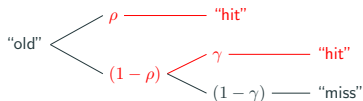
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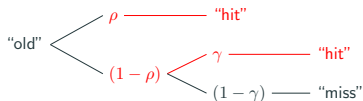
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# One-High Threshold Model

The remembering parameter  $\rho$  and the old-guessing parameter  $\gamma$  can both take any value with equal likelihood:

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Those rates tell us how often old items lead to hits (the data are  $k^h$  hits out of  $n_o$  old items) and how often new items lead to false alarms ( $k^f$  false alarms out of  $n_n$  new items):

$$k^h \sim \text{binomial}(\theta^h, n_o)$$

$$k^f \sim \text{binomial}(\theta^f, n_n)$$



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# One-High Threshold Model

		Amyloid Status	Hits	False Alarms
$\rho$	$\sim$ uniform $(0, 1)$	negative	13	0
$\gamma$	$\sim$ uniform $(0, 1)$	positive	8	4
$\theta^h$	$= \rho + (1 - \rho) \gamma$	negative	12	1
$\theta^f$	$= \gamma$	negative	14	0
$k^h$	$\sim$ binomial $(\theta^h, n_o)$	positive	9	4
$k^f$	$\sim$ binomial $(\theta^f, n_n)$	...	...	...

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$\theta^h = \rho + (1 - \rho) \gamma$	positive	14	0
$\theta^f = \gamma$	positive	14	1
$k^h \sim \text{binomial}(\theta^h, n_o)$	positive	13	2
$k^f \sim \text{binomial}(\theta^f, n_n)$	...	...	...

# One-High Threshold Model

$\rho \sim \text{uniform}(0, 1)$	<code>rho ~ dunif(0, 1)</code>
$\gamma \sim \text{uniform}(0, 1)$	<code>gamma ~ dunif(0, 1)</code>
$\theta^h = \rho + (1 - \rho) \gamma$	<code>thetaHit = rho + (1-rho)*gamma</code>
$\theta^f = \gamma$	<code>thetaFA = gamma</code>
$\forall p \in (1, \dots, P)$	<code>for (p in 1:nPeople){</code>
$k_p^h \sim \text{binomial}(\theta^h, n_o)$	<code>hit[p] ~ dbin(thetaHit, nOld)</code>
$k_p^f \sim \text{binomial}(\theta^f, n_n)$	<code>fa[p] ~ dbin(thetaFA , nNew)</code>
	<code>}</code>
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# Amyloid Positive Inferences

Patients remember around 60-70% of the items, and guess “old” 5-10% of the time when they do not remember

Parameter	Posterior			95% Cred. Int.	
	Mean	Median	SD	Lower	Upper
gamma	0.075	0.074	0.012	0.053	0.100
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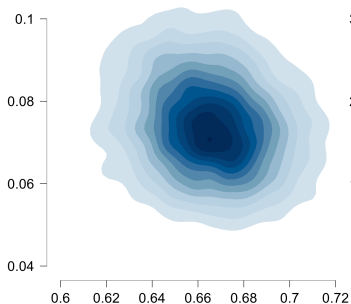
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*“Convergence of the MCMC procedure was good, with all  $\hat{R} < 1.01$ .”*

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