## Tiempo de Ejecución (II)

## **Ejercicio**

```
int c=1;
while (c < n) {
     algo_de_O(1);
     c=2*c;
}</pre>
```

1 Analizar
El bucle termina cuando
c >= n

2 Simular la ejecución del código

$$P_0 c = 1$$

$$P_1 c = 2*1$$

$$P_2 c = 2*2*1$$

$$P_3$$
 c = 2\*2\*2\*1

$$c = 2^k$$
  $\Rightarrow$   $2^k = n$   
 $k = Log_2(n)$ 

El valor de **K** indicará la cantidad de veces que se ejecutó el bucle

$$T(n) = c_1 + \sum_{k=1}^{\log n} (c_2)$$

## Recurrencia

$$T(n) = 8T\left(\frac{n}{2}\right) + n^3, n \ge 2$$

Recurrencia
$$T(n) = \begin{cases} 1, n = \\ 8T\left(\frac{n}{2}\right) + n \end{cases}$$

$$T(n) = \begin{cases} 1, n = 1 \\ 8T\left(\frac{n}{2}\right) + n^3, n \ge 2 \end{cases}$$

$$T(n) = 8 \left[8T\left(\frac{n}{2}\right) + \left(\frac{n}{2}\right)^3\right] + n^3, n \ge 4$$

$$T(n) = 8 \left[ 8T \left( \frac{n}{4} \right) + \frac{n^3}{2^3} \right] + n^3, n \ge 4$$

$$T(n) = 8^2 T \left( \frac{n}{4} \right) + 8 \frac{n^3}{2^3} + n^3, n \ge 4$$

 $T(n) = 8^2 T\left(\frac{n}{2^2}\right) + n^3 + n^3, n \ge 4$ 

 $T(n) = \begin{cases} 1, n = 1 \\ 8T\left(\frac{n}{2}\right) + n^3, n \ge 2 \end{cases}$ 

2  $T(n) = 8^2 T\left(\frac{n}{2^2}\right) + 2|n^3, n \ge 2^2$ 

 $T(n) = 8^{2} \left| 8T \left( \frac{n}{2^{2}} \right) + \left( \frac{n}{2^{2}} \right)^{3} \right| + 2n^{3}, n \ge 2^{3}$ 

 $T(n) = 8^2 \left| 8T\left(\frac{n}{2^3}\right) + \frac{n^3}{2^6} \right| + 2n^3, n \ge 2^3$ 

 $T(n) = 8^3 T\left(\frac{n}{2^3}\right) + 8^2 \frac{n^3}{2^6} + 2n^3, n \ge 2^3$ 

$$T(n) = 8^3 T\left(\frac{n}{2^3}\right) + n^3 + 2n^3, n \ge 2^3$$

$$T(n) = \begin{cases} 1, n = 1 \\ 8T\left(\frac{n}{2}\right) + n^3, n \ge 2 \end{cases}$$

$$T(n) = 8^3 T\left(\frac{n}{2^3}\right) + n^3 + 2n^3, n \ge 2$$

$$T(n) = 8^3 T\left(\frac{n}{2^3}\right) + 3n^3, n \ge 2^3$$

$$T(n) = 8^{i} T\left(\frac{n}{2^{i}}\right) + i n^{3}, n \ge 2^{i}$$

$$n \ge 2^{i} \implies i = L \circ \sigma_{i} (n)$$

$$T(n) = 8^{i} T \left(\frac{n}{2^{i}}\right) + i n^{3}, n \ge 2^{i}$$

$$\frac{n}{2^{i}} = 1 \implies n = 2^{i} \implies i = Log_{2}(n)$$

$$a^{Log_b(c)} = c^{Log_b(a)}$$
$$8^{Log_2(n)} = n^{Log_2(8)}$$

$$\begin{cases} 1, n = 1 \end{cases}$$

$$T(n) = \begin{cases} 1, n = 1 \\ 8T\left(\frac{n}{2}\right) + n^3, n \ge 2 \end{cases}$$

$$T(n) = 8^{Log_2(n)}T\left(\frac{n}{2^{Log_2(n)}}\right) + Log_2(n)n^3$$

$$T(n) = \begin{cases} 1, n = 1 \\ 8T\left(\frac{n}{2}\right) + n^3, n \ge 2 \end{cases} \qquad T(n) = 8^{Log_2(n)}T\left(\frac{n}{2^{Log_2(n)}}\right) + Log_2(n)n^3$$

 $T(n) = n^{Log_2(8)} T\left(\frac{n}{n}\right) + Log_2(n)n^3$ 

 $T(n) = n^3 T(1) + Log_2(n)n^3$ 

 $T(n) = n^3 + Log_2(n)n^3$