Worksheet: temporal time series analysis (part II)

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January 23, 2025

1. The goal of this forecasting exercise is to produce a figure similar to that in slide Example (Forecasting with an AR(1) model) but for an AR(7) model.

Simulate N = 10,000 samples from an AR(7) model with parameters

$$\phi = [5.0/6, -1.0/6, 0.5/6, -0.25/6, 0.5/6, -0.1/6, 0.05/6]$$

$$\sigma = 5.0$$

Use the m = 500 samples before the last sample to forecast h = 50 samples into the future.

You many want to use the script plot_arForecastingYWCor and complete the code for the function forecast in the module tsAnalysisUtils.py.

You should build a plot similar to that in Figure 1.

2. Reproduce the figure in the slide Estimate coefficients of AR(3) model using the Yule-Walker estimators in lecture 2. You may want to use the sample script available here. To run this code, you will need to complete the function estimateCoefsAndNoisVarARpYW in the module tsAnalysisUtils.py, imported in the previous script.

Hints:

- solving the system of equations $A\mathbf{x} = \mathbf{b}$ in Numpy to estimate the vector \mathbf{x} that best approximates the previous equations in Numpy you can use $\mathbf{x} = \text{np.linealg.solve}(\mathbf{A}, \mathbf{x})$.
- computing inner products $x^{T}y$ in Numpy to calculate the previous inner product between vector x and y in Numpy you can use np.inner(x, y).
- computing the inverse A^{-1} of matrix A in Numpy to calculate the previous inverse of matrix A in Numpy you can use np.linalg.inv(A).

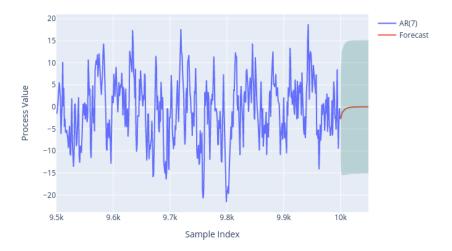


Figure 1: Forecasting result for an AR(7) model