

svGPFA analysis 30190367 of MC_MAZE_SMALL with LDA latents

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1 Hyper-parameters

number of latents: 15

number of inducing points: 20

number of trials: 100

number of clusters: 142

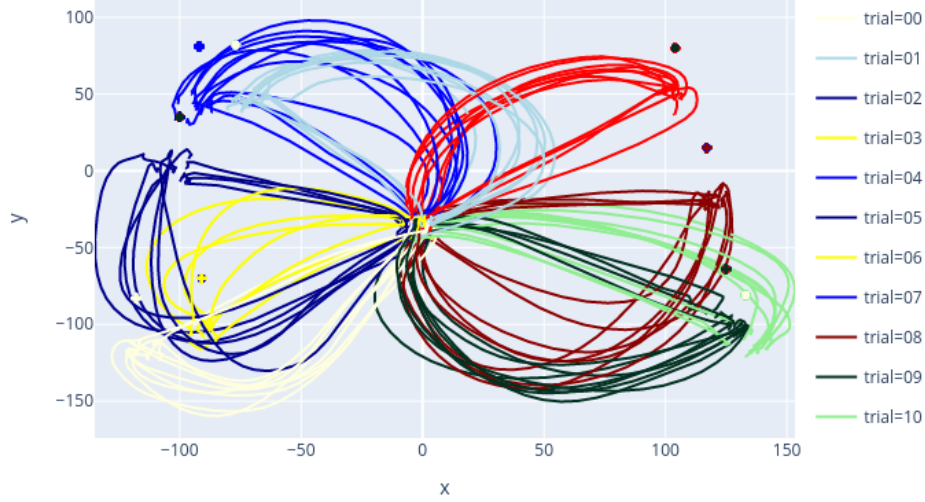


Figure 1: Hand reaching behavior of a monkey. Each trace correspond to a different trial. Trials are colored by target location. There are nine target locations, three to the upper left quadrants, and two to the other quadrants. Click on the figure to get its interactive version.

2 Behavioral data

Figure 1 plots the behavioral data. In every trial monkeys reach to one of the nine target locations.

3 Data for LDA

We provided LDA a matrix of data, $X \in \mathbb{R}^{L \times N}$, and a vector of labels, $\mathbf{y} \in \mathbb{R}^N$. The matrix of data X contains all 15 latents, of all trials, from a 200 ms segment starting at movement onset. A column of X contains the value of the 15 latents corresponding to one sample time point of one trial; thus $L = 15$. The number of columns of X is the number of trials times the number of sample points in the 200 ms segment. The length of \mathbf{y} is the same

as the number of columns of X , and the value of $y[i]$ is the target location corresponding to the trial of the i th column of X .

4 Methods

Our implementation of LDA estimated eight (number of target locations minus one) non-orthogonal directions that maximize a criterion of separability, $J_1(A)$, of the projected data Y , where $Y = AX$, $J_1(A) = \text{Trace}(S_b S_w^{-1})$, and S_b, S_w and the between and within group scatter matrices of Y . Custom code implementing LDA can be found [here](#). Our LDA implementation produced almost identical results as the [scikit-learn](#) one.

The rows of matrix A span the LDA space of dimension number of reach targets minus one. We orthonormalized this space and projected the estimated latents on the orthonormalized space.

5 Results

5.1 First discriminatory direction separates left from right trials

Figure 2 plots histograms of projections of columns of X onto the first discriminatory directions obtained from LDA. There are nine histograms, as many of reaching directions. The histogram for the i th reaching direction contains projections of all columns of X corresponding to trials where the subject reached to the i th direction. The color of the histogram corresponds to the color of the reaching direction in Figure 1. The title of the figure shows the eigenvalue corresponding to this discriminatory direction, which indicates the contribution of this direction to the optimized separability criterion $J_1(A)$ (Section 4). $J_1(A) = \text{Trace}(S_b S_w^{-1}) = \text{eigval}_1 + \text{eigval}_2 + \dots + \text{eigval}_{n_{\text{TargetLocs}}-1}$ (Fukunaga, 1990, Eq. 10.19). This discriminatory direction separates well right (red and green, Figure 1) from left (blue and yellow, Figure 1) trials.

Also, latents corresponding to right and left trials are well separated in the 0.0-0.2 time interval when projected onto the first dimension of the orthonormalised LDA space (see Section 4), as show in Figure 3.

Discriminatory direction 0 (eigenvalue: 14.782824791987471)

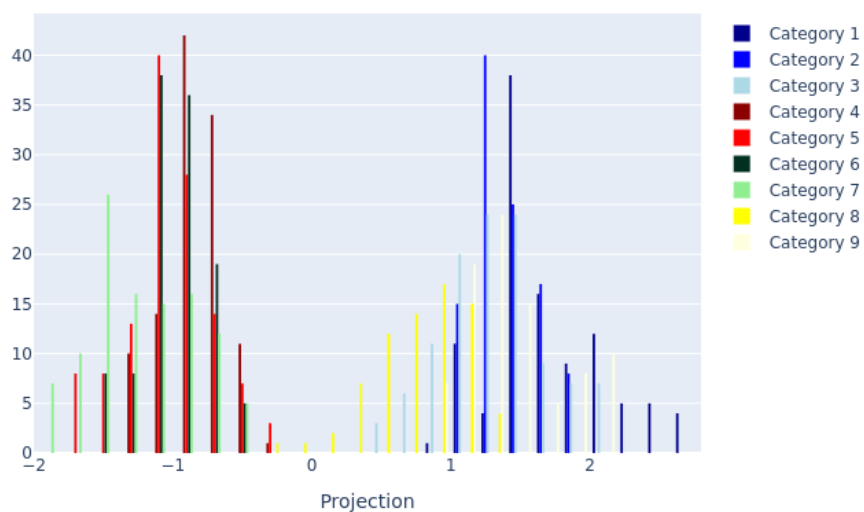


Figure 2: Histograms of projections onto the first LDA direction. Different histograms correspond to the different reach target locations show in Figure 1. This LDA direction separates right (red and green) from left (blue and yellow) trials. Click on the figure to get its interactive version.

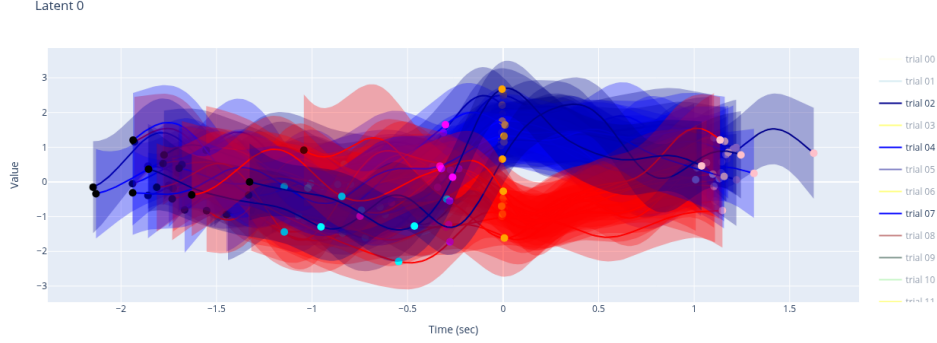


Figure 3: Latents projected onto the first direction of the orthonormalized LDA space. For clarity, the static image on this report displays only latents corresponding to trials where the target was on the top-right and top left. The interactive version of this image shows all latents. Click on the figure to get its interactive version.

5.2 Second discriminatory direction separates top from bottom trials

Figure 4 plots histograms of projections of columns of X onto the second discriminatory directions obtained from LDA. Note that the eigenvalue corresponding to this discriminatory direction is almost 80% smaller than that for the first discriminatory direction, indicating that this direction contributes almost 80% less to the discriminatory criterion $J_1(A)$. This discriminatory direction separates top (red and blue, Figure 1) from bottom (green and yellow, Figure 1) trials. However, this separation is weaker than that with the first discriminative direction (Figure 2).

Also, latents corresponding to top and bottom trials are well separated in the 0.0-0.2 time interval when projected onto the second dimension of the orthonormalised LDA space (see Section 4), as show in Figure 5. However, this separation is weaker than that in Figure 3.

Discriminatory direction 1 (eigenvalue: 2.764695384924153)

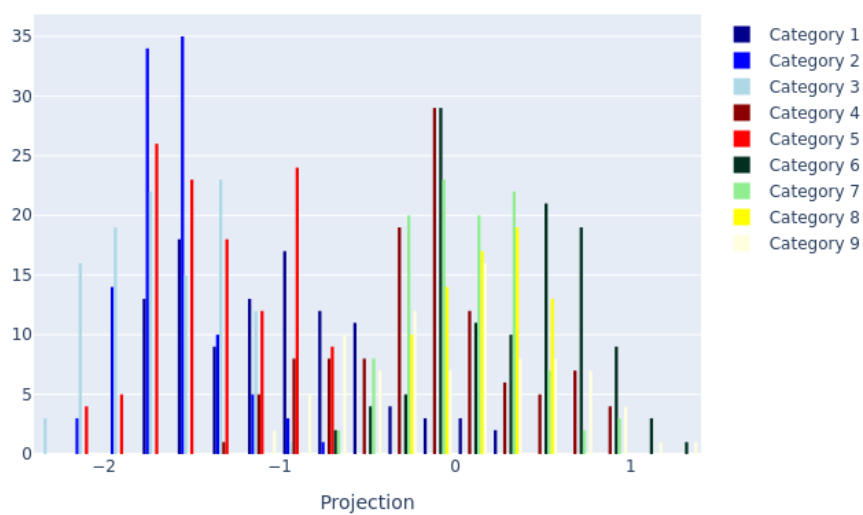


Figure 4: Histograms of projections onto the second LDA direction. Same format as in Figure 2. This LDA direction separates top (red and blue) from bottom (green and yellow) trials. Click on the figure to get its interactive version.

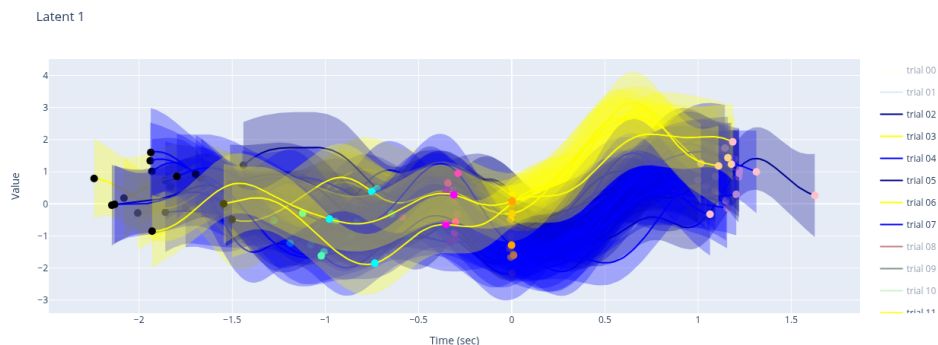


Figure 5: Latents projected onto the second direction of the orthonormalized LDA space. For clarity, the static image on this report displays only latents corresponding to trials where the target was on the top-left and bottom-left. The interactive version of this image shows all latents. Click on the figure to get its interactive version.

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References

Fukunaga, K. (1990). *Introduction to statistical pattern recognition*. Academic Press.