

## Kelvin-Helmholtz Instability

Time development of an inviscid shear layer, as it first wobbles then rolls up into a discrete vortex.

Corresponds to Kelvin-Helmholtz Instability example in paper AIAA-2014-2780, "Using Multi-Dimensional Linear Discretization Over Unsteady Convection Adapted Control Volumes", by Joan G. Moore and John Moore.

750 time step run of example (t=0 to 50) (CPU 42 minutes)

### Unix instructions to run the example

Bring up a terminal window and cd to kh2d.example then

`mkdir out`

`mkdir out/plotcc`

`mkdir out/plotcv`

`mkdir out/plotvort`

`../a.m4d < in.kh2d.2step test > out/print` to run just a 2 timestep test of the input

`../a.m4d < in.kh2d > out/print` to run the full calculation

### Input/Output

The primary input file - `in.kh2d`, uses several other input files for specific tasks.

`inn.grid7x7by.1` - set up a grid covering 0 to 7 in x and -3.5 to 3.5 in y with 0.1 spacing using the master geometry, `geom.cartesian`, set up for block pressure solution, then calculate other geometric arrays.

`inn.init.kh2d.disturb` - set the density(=1). Initialize the velocity as a tanh profile plus a small disturbance. Initialize pressure(=0) and the concentration equal to the vorticity of the initial velocity profile (undisturbed). Set parameters ITER and TIME.

`inn.plotall.bars` - plot initial concentration, vorticity (from velocity gradients) and control volumes together with the corresponding color bars. Gives `out/plotcc/cc0.gif`, `out/plotvort/vort0.gif`, `out/plotcv/fgdv0.gif`, and the corresponding color bars, `out/barcc.gif`, `out/barvort.gif` and `out/barcv.gif`.

Uses `inn.plotcc`, `inn.plotzvort` and `inn.plotcv`.

`inn.plotcc` - plot the current concentration, cc, as color fill. 5 lines of velocity vectors are also included. (Results in dir. `out/plotcc/`)

`inn.plotzvort` - plot the current vorticity calculated from the velocity gradients

as color fill. The grid and 5 lines of velocity vectors are also included. (Results in dir. `out/plotvort`) Note since vorticity is a between-the-points variable it is plotted as uniform between the grid lines. The concentration `cc` is an on-the-points variable so linear interpolation is used when it is plotted. `inn.plotcv` - plot the control volumes (in blue) for the central portion of the grid where the vortex forms. Also on the plot, `cc` as color fill, the grid (magenta) and velocity vectors (black). (Results in dir. `out/plotcv`) `inn.step.inv2d` - take 1 time step using `inn.subiter.inv2d` for the (iterative) procedure to calculate velocity and pressure, then solve the conserved species equation for `cc`, dump convergence info to file `out/converge`, and use `inn.dump` and `inn.plot` for dumping arrays and making plots. `inn.subiter.inv2d` - do 1 iteration for the down-time velocity and mean pressure for the time step. Dumps per-iteration convergence info to file `out/converge`. `inn.dump` - dump current results to `out/u#ITER` `inn.plot` - plot current concentration (`inn.plotcc`), vorticity (`inn.plotzvort`), control volumes (`inn.plotcv`) and convergence (`inn.plotconv`). `inn.plotconv` - gives lineplot file `out/convline`. Then plots `conv.gif` which shows as a function of time, the maximum value of `U2` (y-velocity), the maximum change in `U2` over each timestep, and the estimated error in the maximum change in `U2` over each timestep.

Compare results with those obtained by `jgm`.

### **Post-processing of output by `jgm`**

`mv out out.jgm`. Delete plot files except those at ITERs: 0, 100, 200, 300, 400, 500, 600, 750. Delete dump files (`u2`, etc) except those at ITERs 200, 400, and 750. Rename file `converge` to `converge.reduced` and remove all but the first and last timesteps. (The file `convline` is complete.) Space for results reduced from 15.4Mb to 3.2Mb.

### **Suggestions for variations to try**

Run the calculation with no initial disturbance added to the tanh profile for the velocity. (Set `distmag` in file `in.kh2d` to 0.) But before doing so, look at paper AIAA-2014-2780 and make an estimate of the time it will take (and therefore the number of timesteps) to increase the disturbance from roundoff errors, about  $1.e-13$ , to 0.0001 (the current initial disturbance magnitude). Note that with no set initial disturbance, the vortex may form anywhere, depending on the roundoff errors.

