Lab 4

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TODO: As this is a policy exercise, you should do your best to address the campaign's questions from a causal perspective. At the same time, you should clearly explain the limitations of your analysis, and provide discussion around whether your estimates suffer from endogeneity bias.

Introduction

\$ year

TODO: A brief introduction

Exploratory Data Analysis

TODO: An initial exploratory analysis. Detect any anomalies, including missing values, top-coded or bottom-coded variables, etc.

```
library(car) # lm
library(ggplot2) # ggplot
library(lmtest) # bptest
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
library(plm) # vcovHC
## Loading required package: Formula
library(sandwich)
library(stargazer) # stargazer
##
## Please cite as:
  Hlavac, Marek (2015). stargazer: Well-Formatted Regression and Summary Statistics Tables.
  R package version 5.2. http://CRAN.R-project.org/package=stargazer
library(tidyr) # gather
data <- read.csv("crime.csv")</pre>
str(data)
## 'data.frame':
                    90 obs. of 26 variables:
              : int 1 2 3 4 5 6 7 8 9 10 ...
## $ county : int 1 3 5 7 9 11 13 15 17 19 ...
```

: int 87 87 87 87 87 87 87 87 87 87 ...

```
$ crmrte : num
                    0.0356 0.0153 0.013 0.0268 0.0106 ...
##
                    0.298 0.132 0.444 0.365 0.518 ...
   $ prbarr : num
   $ prbconv : num
                    0.528 1.481 0.268 0.525 0.477 ...
   $ prbpris : num
                    0.436 0.45 0.6 0.435 0.443 ...
##
   $ avgsen : num
                     6.71 6.35 6.76 7.14 8.22 ...
##
   $ polpc
                     0.001828 0.000746 0.001234 0.00153 0.00086 ...
            : num
                     2.423 1.046 0.413 0.492 0.547 ...
   $ density : num
##
   $ taxpc
              : num
                     31 26.9 34.8 42.9 28.1 ...
##
   $ west
              : int
                     0 0 1 0 1 1 0 0 0 0 ...
##
                     1 1 0 1 0 0 0 0 0 0 ...
   $ central : int
   $ urban
             : int
                     0 0 0 0 0 0 0 0 0 0 ...
##
                     20.22 7.92 3.16 47.92 1.8 ...
   $ pctmin80: num
##
   $ wcon
                     281 255 227 375 292 ...
              : num
##
                     409 376 372 398 377 ...
   $ wtuc
              : num
##
   $ wtrd
                     221 196 229 191 207 ...
              : num
##
   $ wfir
                     453 259 306 281 289 ...
              : num
##
                     274 192 210 257 215 ...
   $ wser
              : num
##
   $ wmfg
                     335 300 238 282 291 ...
              : num
                     478 410 359 412 377 ...
##
   $ wfed
              : num
##
   $ wsta
              : num
                     292 363 332 328 367 ...
##
   $ wloc
              : num
                     312 301 281 299 343 ...
                     0.0802 0.0302 0.4651 0.2736 0.0601 ...
              : num
                     0.0779 0.0826 0.0721 0.0735 0.0707 ...
   $ pctymle : num
```

summary(data)

```
##
          Х
                        county
                                         year
                                                     crmrte
##
   Min. : 1.00
                    Min. : 1.0
                                    Min.
                                           :87
                                                        :0.005533
   1st Qu.:23.25
                    1st Qu.: 51.5
                                    1st Qu.:87
                                                 1st Qu.:0.020604
##
   Median :45.50
                    Median :103.0
                                    Median:87
                                                 Median :0.030002
##
         :45.50
                                           :87
   Mean
                    Mean :100.6
                                    Mean
                                                 Mean
                                                        :0.033510
##
   3rd Qu.:67.75
                    3rd Qu.:150.5
                                    3rd Qu.:87
                                                 3rd Qu.:0.040249
##
   Max.
           :90.00
                    Max. :197.0
                                    Max.
                                           :87
                                                 Max.
                                                         :0.098966
##
       prbarr
                         prbconv
                                           prbpris
                                                             avgsen
##
           :0.09277
                      Min.
                             :0.06838
                                        Min.
                                               :0.1500
                                                         Min. : 5.380
   Min.
    1st Qu.:0.20495
                      1st Qu.:0.34422
                                        1st Qu.:0.3642
                                                         1st Qu.: 7.375
##
   Median : 0.27146
                      Median :0.45170
                                        Median :0.4222
                                                         Median: 9.110
##
   Mean :0.29524
                      Mean :0.55086
                                        Mean
                                              :0.4106
                                                         Mean : 9.689
##
    3rd Qu.:0.34487
                      3rd Qu.:0.58513
                                        3rd Qu.:0.4576
                                                         3rd Qu.:11.465
   Max.
          :1.09091
                      Max.
                            :2.12121
                                        Max.
                                               :0.6000
                                                         Max.
                                                                :20.700
##
       polpc
                           density
                                             taxpc
                                                               west
##
          :0.0007459
                       Min.
                               :0.2034
                                         Min. : 25.69
                                                                  :0.0000
   Min.
                                                          Min.
                                         1st Qu.: 30.73
##
   1st Qu.:0.0012378
                        1st Qu.:0.5472
                                                          1st Qu.:0.0000
                        Median :0.9792
##
   Median :0.0014897
                                         Median : 34.92
                                                          Median :0.0000
##
   Mean :0.0017080
                        Mean :1.4379
                                         Mean : 38.16
                                                          Mean :0.2333
   3rd Qu.:0.0018856
                        3rd Qu.:1.5693
                                         3rd Qu.: 41.01
                                                          3rd Qu.:0.0000
##
##
   Max.
          :0.0090543
                        Max.
                              :8.8277
                                         Max. :119.76
                                                          Max. :1.0000
##
       central
                         urban
                                          pctmin80
                                                             wcon
##
   Min.
           :0.0000
                     Min.
                            :0.00000
                                       Min. : 1.284
                                                        Min.
                                                               :193.6
##
   1st Qu.:0.0000
                     1st Qu.:0.00000
                                       1st Qu.:10.024
                                                        1st Qu.:250.8
   Median :0.0000
                     Median :0.00000
                                       Median :24.852
                                                        Median :281.2
##
   Mean
                                              :25.713
         :0.3778
                     Mean
                           :0.08889
                                       Mean
                                                        Mean :285.4
                                       3rd Qu.:38.183
   3rd Qu.:1.0000
                     3rd Qu.:0.00000
                                                        3rd Qu.:315.0
   Max.
                     Max.
##
           :1.0000
                            :1.00000
                                       Max.
                                              :64.348
                                                        Max.
                                                               :436.8
##
         wtuc
                         wtrd
                                         wfir
                                                         wser
```

```
## Min.
          :187.6
                    Min.
                           :154.2
                                    Min. :170.9
                                                    Min. : 133.0
##
   1st Qu.:374.3
                    1st Qu.:190.7
                                    1st Qu.:285.6
                                                    1st Qu.: 229.3
                    Median :203.0
   Median :404.8
                                    Median :317.1
                                                    Median: 253.1
         :410.9
                         :210.9
                                          :321.6
##
  Mean
                    Mean
                                    Mean
                                                    Mean : 275.3
##
   3rd Qu.:440.7
                    3rd Qu.:224.3
                                    3rd Qu.:342.6
                                                    3rd Qu.: 277.6
##
   Max.
           :613.2
                   Max.
                           :354.7
                                    Max.
                                          :509.5
                                                           :2177.1
                                                    Max.
                         wfed
                                                         wloc
##
         wmfg
                                         wsta
##
   Min.
          :157.4
                    Min.
                           :326.1
                                    Min.
                                           :258.3
                                                    Min.
                                                           :239.2
##
   1st Qu.:288.6
                    1st Qu.:398.8
                                    1st Qu.:329.3
                                                    1st Qu.:297.2
   Median :321.1
                    Median :448.9
                                    Median :358.4
                                                    Median :307.6
##
  Mean
         :336.0
                    Mean
                          :442.6
                                    Mean
                                          :357.7
                                                    Mean
                                                           :312.3
   3rd Qu.:359.9
##
                    3rd Qu.:478.3
                                    3rd Qu.:383.2
                                                    3rd Qu.:328.8
##
   Max.
           :646.9
                   Max.
                           :598.0
                                    Max.
                                          :499.6
                                                    Max.
                                                           :388.1
##
        mix
                         pctymle
##
  Min.
          :0.01961
                      Min.
                           :0.06216
##
  1st Qu.:0.08060
                      1st Qu.:0.07437
## Median :0.10095
                      Median :0.07770
## Mean :0.12905
                     Mean :0.08403
## 3rd Qu.:0.15206
                      3rd Qu.:0.08352
## Max.
           :0.46512
                      Max.
                             :0.24871
# sample size n = 90
nrow(data)
## [1] 90
# number of variables = 26
ncol(data)
## [1] 26
# number of prbarr where probability is greater than 1
sum(data$prbarr > 1)
## [1] 1
# number of prbconv where probability is greater than 1
sum(data$prbconv > 1)
## [1] 10
# verify number of missing values = 0
colSums(sapply(data, is.na))
##
          X
              county
                         year
                                crmrte
                                         prbarr prbconv prbpris
                                                                     avgsen
##
          0
                   0
                            0
                                     0
                                              0
                                                       0
                                                                0
                                                                          0
##
     polpc
             density
                        taxpc
                                  west
                                        central
                                                   urban pctmin80
                                                                       wcon
##
                                                                          0
         0
                   0
                            0
                                     0
                                              0
                                                       0
                                                                0
##
       wtuc
                wtrd
                         wfir
                                  wser
                                           wmfg
                                                    wfed
                                                             wsta
                                                                       wloc
##
          0
                   0
                            0
                                     0
                                                       0
                                                                0
                                                                          0
                                              0
##
        mix
            pctymle
##
          0
                   0
# plot every variable except x, county, year
plot.data <- data[!(names(data) %in% c("X", "county", "year"))]</pre>
ggplot(gather(plot.data), aes(value)) +
       facet_wrap(~key, scales="free") +
       geom histogram()
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

crmrte

0.0000025505000755100

density

0.0 2.5 5.0 7.5

mix

0.00.10.20.30.4

15 -

10

central

0.000.250.500.751.00

40 -

20

20

avgsen

10 15

```
pctmin80
                              pctymle
                                                   polpc
                                                                      prbarr
                                                                                        prbconv
                                           20 -
                                                               10 -
                                           10 -
            20
               40
                   60
                            0.100.150.200.25
                                              0.002500600075
                                                                    0.3 0.6 0.9
                                                                                   0.00.51.01.52.0
                                                   urban
            prbpris
                               taxpc
                                                                       wcon
                                                                                         west
         0.20.30.40.50.6
                          25 50 75 100125
                                             0.00.250.500.751.00
                                                                  20@5@0@5@40@450 0.0@.2$0.5@.751.00
             wfed
                                wfir
                                                   wloc
                                                                       wmfg
                                                                                         wser
                                         12:5
                                                             13:5
           400 500 600
                           200 300 400 500
                                             240280320360400
                                                                  20304050600
                                                                                    0 500 000 502000
                                wtrd
                                                   wtuc
             wsta
                                         16:5=
5:5=
    10.0
                       10 -
                                              200300400500600
       250300350400450500
                          150200250300350
                                                  value
# just list outliers for variables that are non-categorical
subset.data <- data[!(names(data) %in% c("X", "county", "year", "central", "urban", "west"))]</pre>
# list all outliers
list_all_outliers <- function (var) {</pre>
  outliers <- sort(boxplot.stats(var)$out)</pre>
  return(paste(length(outliers), ": ", paste(outliers, collapse=", ")))
lapply(subset.data, list_all_outliers)
## $crmrte
  [1] "5 :
              0.0729478970170021, 0.0790162980556488, 0.0834982022643089, 0.0883848965167999, 0.09896589
##
## $prbarr
              0.689023971557617, 1.09090995788574"
##
## $prbconv
##
  [1] "11 :
              0.972972989082336, 1.01538002490997, 1.06896996498108, 1.18292999267578, 1.22561001777649
## $prbpris
##
   [1] "1:
              0.150000005960464"
##
## $avgsen
## [1] "1 :
              20.7000007629395"
##
```

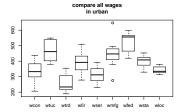
```
## $polpc
## [1] "4 : 0.00316379009746015, 0.00400961982086301, 0.00445923022925854, 0.00905433017760515"
##
## $density
## [1] "8 : 3.93455100059509, 4.38875865936279, 4.8347339630127, 5.12442398071289, 5.6744966506958, 6.°
##
## $taxpc
## [1] "6 : 56.8621063232422, 61.1525115966797, 67.6796340942383, 67.8479766845703, 75.6724319458008,
##
## $pctmin80
## [1] "0 :
##
## $wcon
## [1] "1 : 436.766632080078"
##
## $wtuc
## [1] "9 : 187.617263793945, 202.429153442383, 213.675216674805, 548.323852539062, 548.986511230469, and the control of the c
##
## $wtrd
## [1] "5 : 277.292510986328, 279.227264404297, 306.083526611328, 308.576232910156, 354.676116943359"
##
## $wfir
## [1] "7 : 170.940170288086, 430.069702148438, 435.110717773438, 441.141296386719, 453.172210693359, ·
##
## $wser
## [1] "4 : 133.043060302734, 354.300720214844, 391.308074951172, 2177.06811523438"
##
## $wmfg
## [1] "7 : 157.410003662109, 494.299987792969, 560.780029296875, 567.059997558594, 588.989990234375,
##
## $wfed
## [1] "0 : "
##
## $wsta
## [1] "1 : 499.589996337891"
##
## $wloc
## [1] "5 : 239.169998168945, 246.649993896484, 379.769989013672, 386.119995117188, 388.089996337891"
##
## $mix
## [1] "8 : 0.273622035980225, 0.28078818321228, 0.290488421916962, 0.311355322599411, 0.3195266425609
##
## $pctymle
## [1] "10 : 0.0989191979169846, 0.0993558466434479, 0.106941692531109, 0.114216551184654, 0.122244790
Glaring outliers: 1. Probability > 1 for prbarr and prbconv 2. Outlier 2177 in wser which happens to be in
central instead of urban (weird)
# number of urban
sum(data$urban == 1)
## [1] 8
# number of central
```

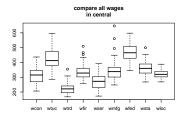
sum(data\$central == 1)

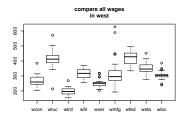
```
## [1] 34
# number of west
sum(data$west == 1)
## [1] 21
# determine if a county can have multiple categorical label: urban, central, west
urban.county <- data[data$urban == 1, ]$county</pre>
central.county <- data[data$central == 1, ]$county</pre>
west.county <- data[data$west == 1, ]$county</pre>
# can a county be labeled as both urban and central?
uc.county <- c(urban.county, central.county)</pre>
uc.county[duplicated(uc.county)]
## [1] 63 67 81 119 183
# can a county be labeled as both urban and west?
uw.county <- c(urban.county, west.county)</pre>
uw.county[duplicated(uw.county)]
## [1] 21
# I have verified that there is no county labeled as both central and west
# counties that have more than one categorical label
all.county <- c(urban.county, central.county, west.county)</pre>
all.county[duplicated(all.county)]
## [1] 63 67 81 119 183 21
# compare all the wages
boxplot(as.vector(data[c(16:24)]), main="compare all wages")
# compare all wages in central
central.data <- data[data$central == 1, ]</pre>
boxplot(as.vector(central.data[c(16:24)]), main="compare all wages\nin central")
                                                                    compare all wages
                   compare all wages
                                                                        in central
   2000
   1500
                                                    1500
   1000
                                                    1000
   200
                                                    500
        wcon wtuc wtrd
                     wfir
                        wser wmfg wfed
                                    wsta
                                                         wcon
                                                                  wtrd
                                                                         wser
                                                                             wmfg wfed wsta
```

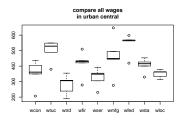
```
# compare all wages in urban
urban.data <- data[data$urban == 1, ]
boxplot(as.vector(urban.data[c(16:24)]), main="compare all wages\nin urban")
# compare all wages in central with outlier removed
central.data[central.data$wser == 2177.06811523438, ]$wser <- mean(central.data$wser)
boxplot(as.vector(central.data[c(16:24)]), main="compare all wages\nin central")
# compare all wages in west
west.data <- data[data$west == 1, ]</pre>
```

```
boxplot(as.vector(west.data[c(16:24)]), main="compare all wages\nin west")
# compare all wages in urban and central
urban.central.data <- data[data$urban == 1 & data$central == 1, ]
boxplot(as.vector(urban.central.data[c(16:24)]), main="compare all wages\nin urban central")
# compare all wages in urban and west
# not worth it because it's only one dataset</pre>
```



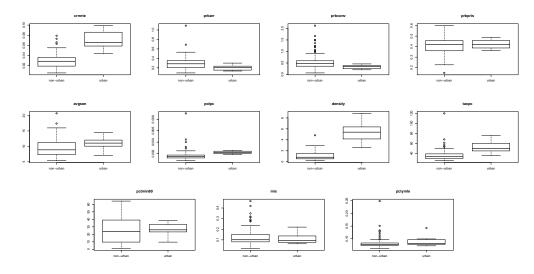






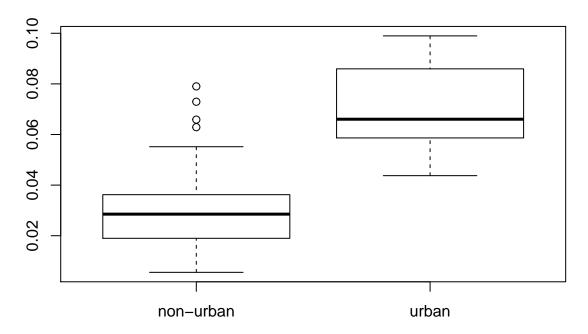
```
# in urban area, is there higher ...?
independents <- c("crmrte", "prbarr", "prbconv", "prbpris", "avgsen", "polpc", "density", "taxpc", "pct
mapply(function(var, var.name) {
   boxplot(var ~ urban, data=data, names=c("non-urban", "urban"), main=var.name)
}, subset(data, select=independents), independents)</pre>
```

```
crmrte
                      prbarr
                                  prbconv
                                               prbpris
                                                           avgsen
## stats Numeric,10
                     Numeric, 10
                                  Numeric, 10
                                              Numeric, 10
                                                           Numeric, 10
## n
         Numeric,2
                      Numeric,2
                                  Numeric,2
                                               Numeric,2
                                                           Numeric, 2
## conf
         Numeric, 4
                      Numeric,4
                                  Numeric,4
                                               Numeric,4
                                                           Numeric, 4
         Numeric,4
                     Numeric,2
                                  Numeric,11
                                                           Numeric,2
## out
                                              0.15
## group Numeric,4
                     Numeric,2
                                  Numeric,11
                                                           Numeric,2
## names Character,2 Character,2 Character,2 Character,2 Character,2
         polpc
                      density
                                  taxpc
                                              pctmin80
## stats Numeric,10
                     Numeric,10
                                  Numeric, 10 Numeric, 10 Numeric, 10
## n
         Numeric,2
                      Numeric,2
                                  Numeric,2
                                              Numeric,2
                                                           Numeric, 2
        Numeric,4
                      Numeric,4
                                  Numeric,4
                                              Numeric,4
                                                           Numeric,4
## conf
         Numeric,5
                      4.834734
                                  Numeric,6
                                              Numeric,0
                                                           Numeric,8
## out
  group Numeric,5
                                  Numeric,6
                                              Numeric,0
                                                           Numeric,8
##
  names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
         pctymle
## stats Numeric, 10
## n
         Numeric, 2
## conf
         Numeric, 4
## out
         Numeric,9
## group Numeric,9
## names Character,2
```

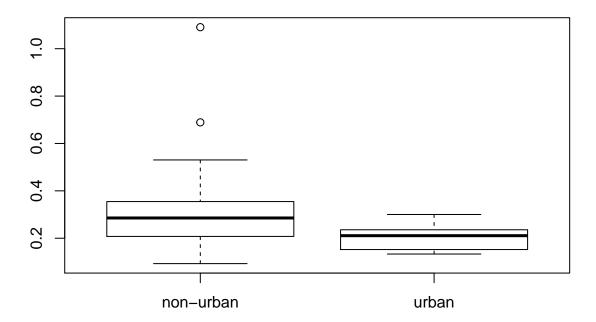


```
# repeat of above but checking out all the wages
mapply(function(var, var.name) {
   boxplot(var ~ urban, data=data, names=c("non-urban", "urban"), main=var.name)
}, subset.data, names(subset.data))
```

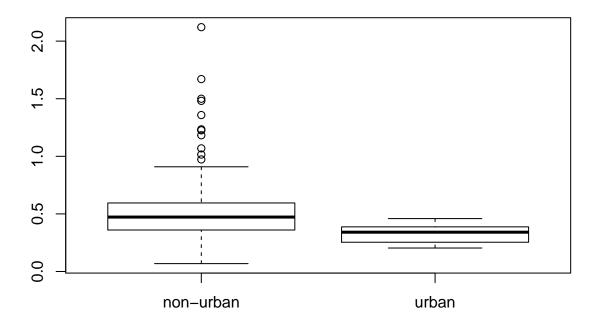
crmrte



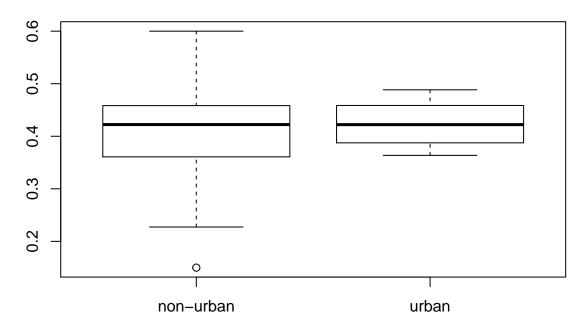
prbarr



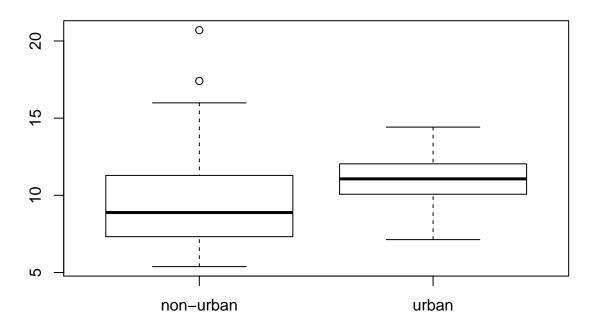
prbconv



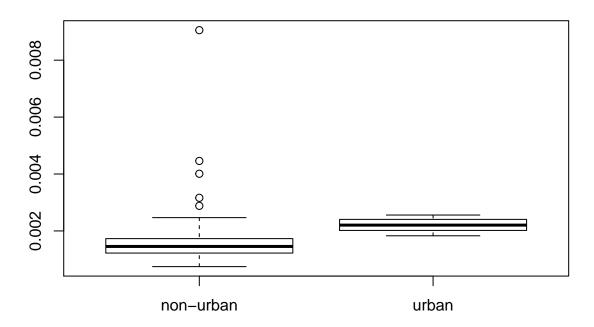
prbpris



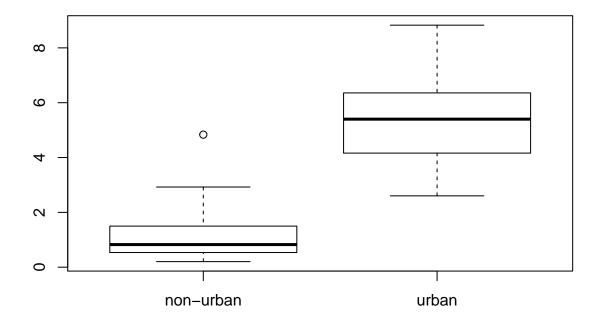
avgsen



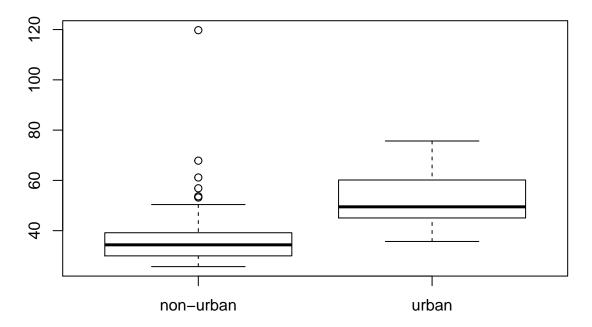
polpc



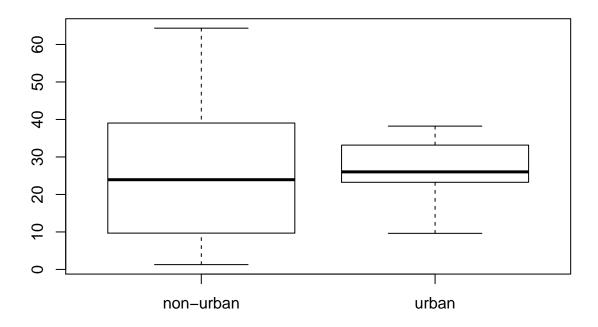
density



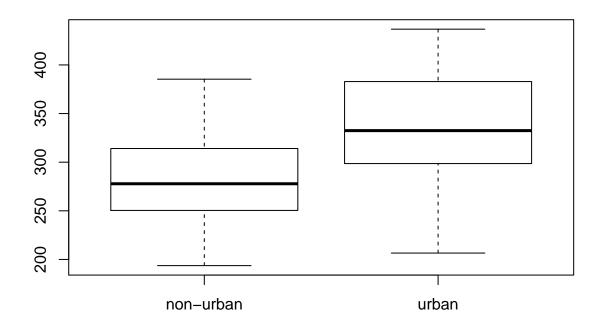
taxpc



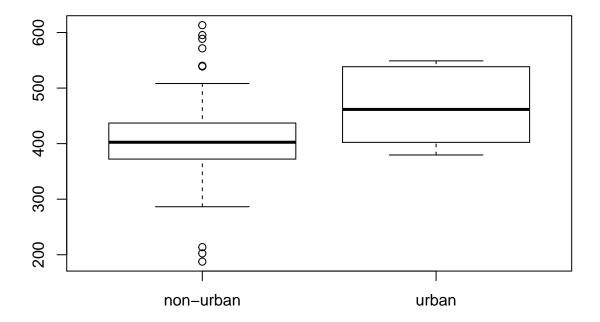
pctmin80



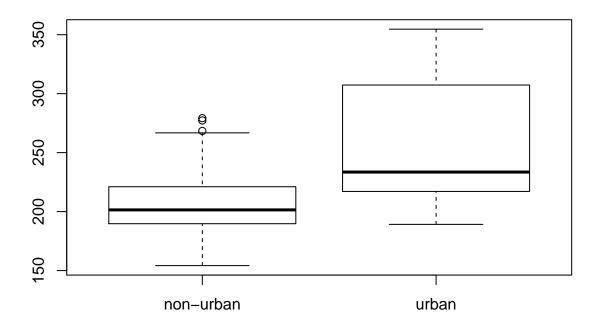
wcon



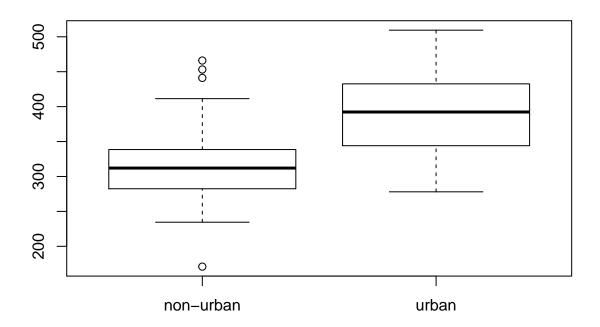
wtuc



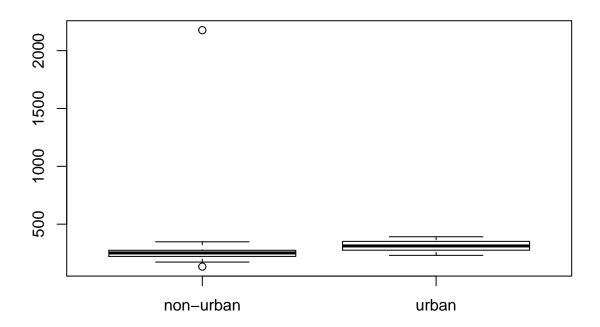
wtrd



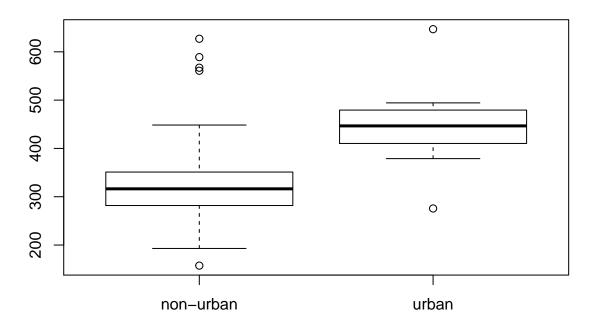




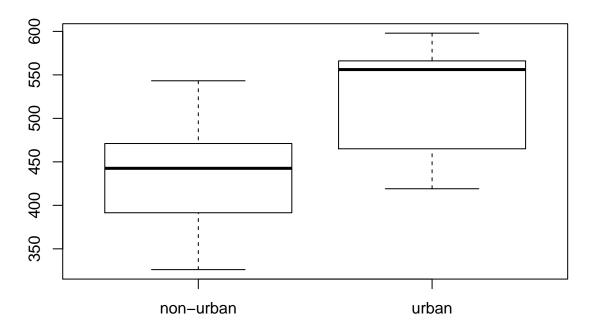
wser



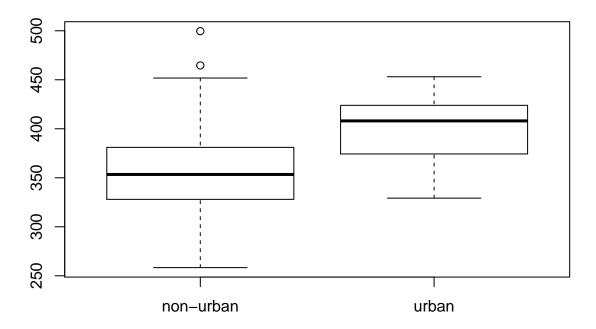
wmfg



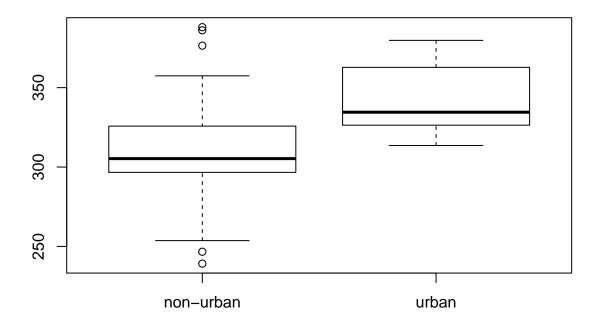
wfed



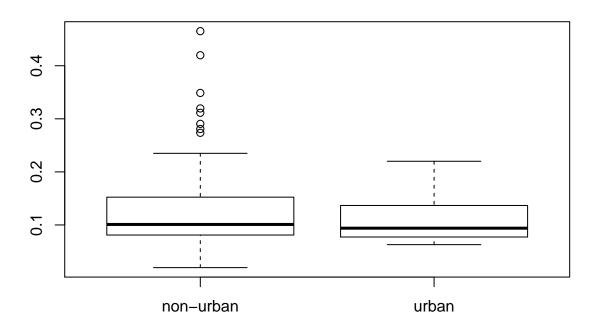
wsta



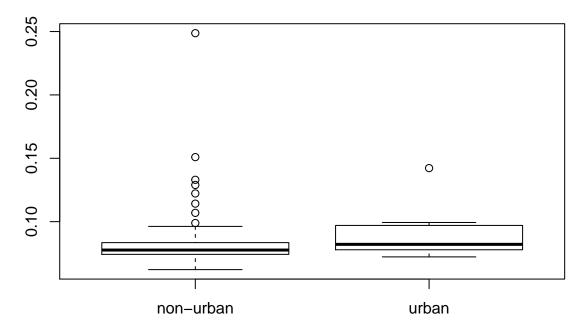
wloc



mix



pctymle



```
##
          crmrte
                       prbarr
                                    prbconv
                                                  prbpris
                                                               avgsen
## stats Numeric,10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                               Numeric, 10
         Numeric,2
                                    Numeric,2
                                                 Numeric,2
                                                               Numeric,2
## n
                       Numeric,2
## conf
         Numeric, 4
                       Numeric, 4
                                    Numeric,4
                                                  Numeric, 4
                                                               Numeric, 4
                                                 0.15
                                                               Numeric, 2
## out
          Numeric, 4
                       Numeric, 2
                                    Numeric, 11
                       Numeric, 2
                                    Numeric, 11
                                                  1
                                                               Numeric, 2
   group Numeric,4
                                    Character, 2 Character, 2 Character, 2
   names Character, 2 Character, 2
##
          polpc
                       density
                                    taxpc
                                                  pctmin80
                                                               wcon
##
   stats Numeric, 10
                       Numeric, 10
                                    Numeric, 10
                                                  Numeric, 10
                                                               Numeric, 10
##
          Numeric, 2
                       Numeric,2
                                    Numeric,2
                                                  Numeric, 2
                                                               Numeric, 2
  n
## conf
         Numeric,4
                       Numeric,4
                                    Numeric,4
                                                  Numeric, 4
                                                               Numeric, 4
##
   out
          Numeric,5
                       4.834734
                                    Numeric,6
                                                 Numeric, 0
                                                               Numeric, 0
   group Numeric,5
                                    Numeric,6
                                                  Numeric,0
                                                               Numeric, 0
##
   names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
                       wtrd
                                    wfir
          wtuc
                                                  wser
                                                               wmfg
                                                               Numeric, 10
## stats Numeric, 10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                               Numeric, 2
## n
          Numeric, 2
                       Numeric, 2
                                    Numeric, 2
                                                 Numeric, 2
## conf
         Numeric, 4
                       Numeric, 4
                                    Numeric,4
                                                  Numeric,4
                                                               Numeric, 4
  out
          Numeric,9
                       Numeric,3
                                    Numeric,4
                                                  Numeric, 2
                                                               Numeric,7
                                                               Numeric,7
   group Numeric,9
                       Numeric,3
                                    Numeric,4
                                                  Numeric, 2
##
   names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
          wfed
                       wsta
                                    wloc
                                                  mix
                                                               pctymle
## stats Numeric,10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                               Numeric, 10
## n
          Numeric, 2
                       Numeric, 2
                                    Numeric,2
                                                  Numeric, 2
                                                               Numeric, 2
## conf
                                    Numeric,4
                                                               Numeric,4
         Numeric, 4
                       Numeric,4
                                                  Numeric,4
## out
          Numeric,0
                       Numeric, 2
                                    Numeric,5
                                                  Numeric,8
                                                               Numeric,9
```

```
## group Numeric,0 Numeric,2 Numeric,5 Numeric,8 Numeric,9
## names Character,2 Character,2 Character,2 Character,2
```

In urban areas, there is higher

- crime rates
- average sentence
- police per capita
- density
- tax revenue per capita
- percentage of minority (slightly higher but not much)
- percentage of young male (slightly higher but not much)
- wages tend to be higher overall

In urban areas, there is lower

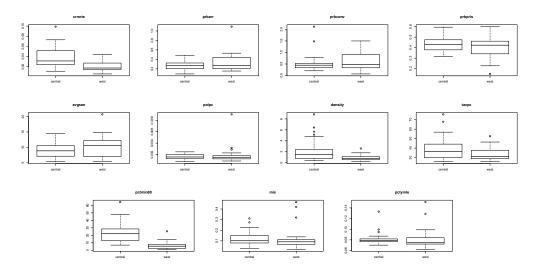
- probability of arrest
- probability of conviction
- face to face confrontation (slightly lower but not much)

In urban areas, there is about the same

• probability of prison sentence

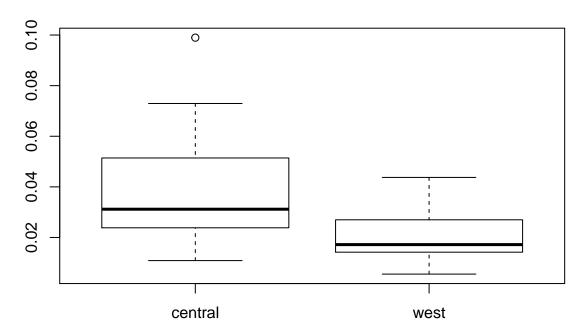
```
# comparing central and west, is there higher ...?
central.data <- data[data$central == 1, ]
subset.central.data <- subset(central.data, select=independents)
west.data <- data[data$west == 1, ]
subset.west.data <- subset(west.data, select=independents)
mapply(function(central.var, west.var, var.name) {
   boxplot(central.var, west.var, names=c("central", "west"), main=var.name)
}, subset.central.data, subset.west.data, independents)</pre>
```

```
##
         crmrte
                      prbarr
                                  prbconv
                                               prbpris
                                                           avgsen
## stats Numeric,10
                     Numeric, 10
                                  Numeric, 10
                                              Numeric, 10
                                                           Numeric, 10
         Numeric,2
                     Numeric,2
                                  Numeric,2
                                              Numeric,2
                                                           Numeric, 2
## conf
        Numeric,4
                     Numeric,4
                                  Numeric,4
                                              Numeric,4
                                                           Numeric,4
## out
         0.0989659
                     1.09091
                                  Numeric,2
                                              0.15
                                                           20.7
## group 1
                      2
                                  Numeric, 2
                                               2
                                                           2
## names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
         polpc
                      density
                                  taxpc
                                               pctmin80
                                                           mix
## stats Numeric,10 Numeric,10
                                  Numeric, 10 Numeric, 10 Numeric, 10
## n
         Numeric,2
                     Numeric,2
                                  Numeric,2
                                              Numeric,2
                                                           Numeric, 2
## conf Numeric,4
                     Numeric,4
                                  Numeric,4
                                              Numeric,4
                                                           Numeric, 4
## out
         Numeric,3
                     Numeric,5
                                  Numeric,3
                                              Numeric,2
                                                           Numeric,5
## group Numeric,3
                     Numeric,5
                                  Numeric, 3
                                              Numeric, 2
                                                           Numeric,5
## names Character,2 Character,2 Character,2 Character,2 Character,2
##
         pctymle
## stats Numeric,10
## n
         Numeric, 2
## conf
        Numeric,4
## out
         Numeric,5
## group Numeric,5
## names Character,2
```

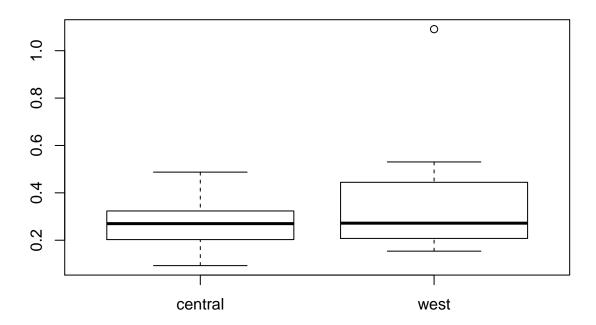


```
# repeat of above but checking out all the wages
central.data <- data[data$central == 1, ]
subset.central.data <- subset(central.data, select=names(subset.data))
west.data <- data[data$west == 1, ]
subset.west.data <- subset(west.data, select=names(subset.data))
mapply(function(central.var, west.var, var.name) {
   boxplot(central.var, west.var, names=c("central", "west"), main=var.name)
}, subset.central.data, subset.west.data, names(subset.data))</pre>
```

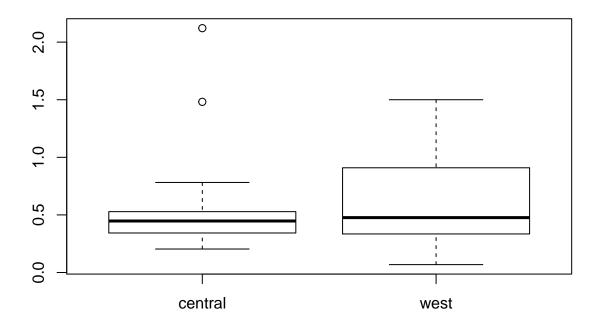
crmrte



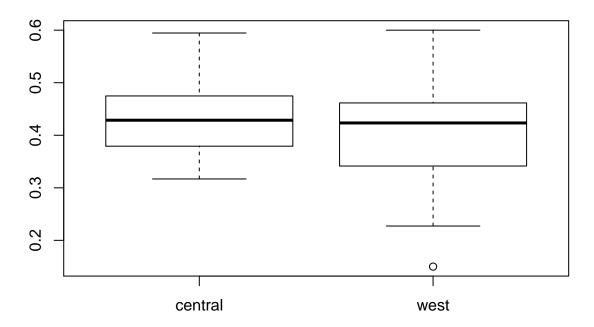
prbarr



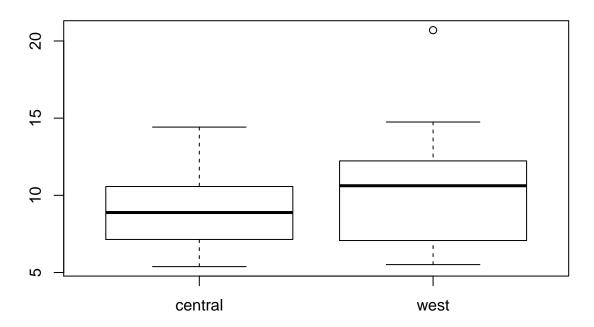
prbconv



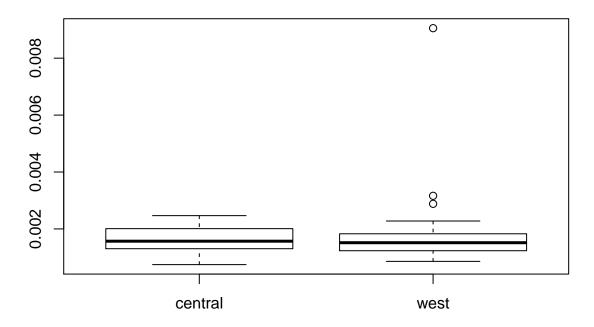
prbpris



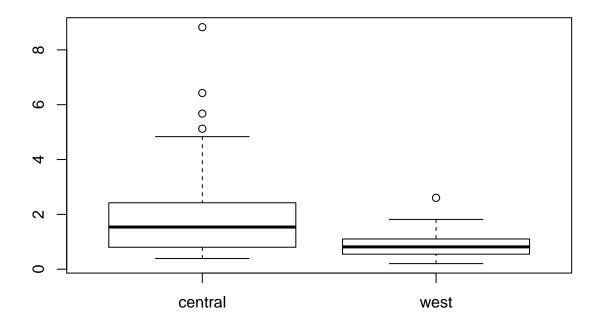
avgsen



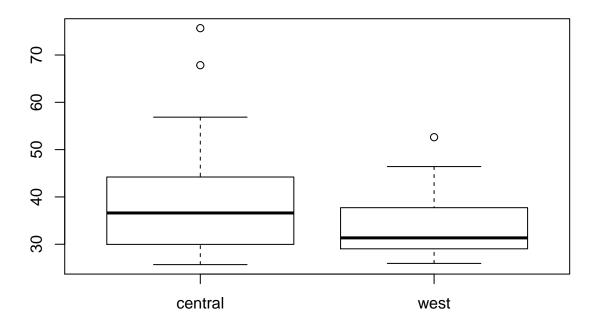
polpc



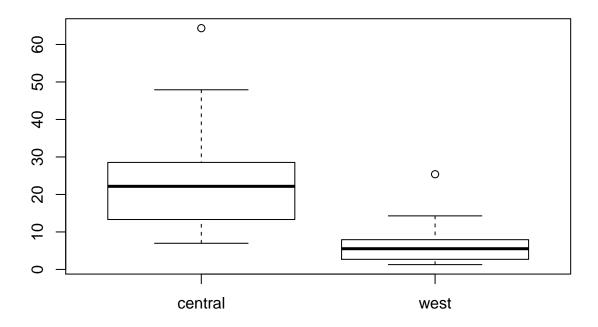
density



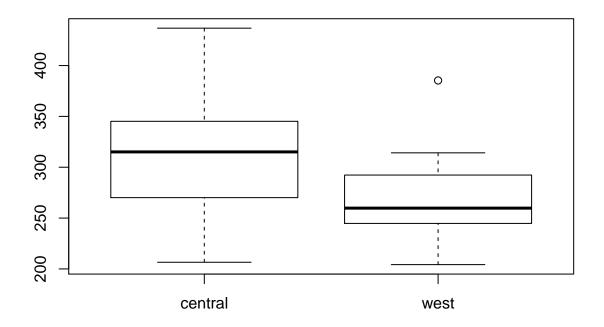
taxpc



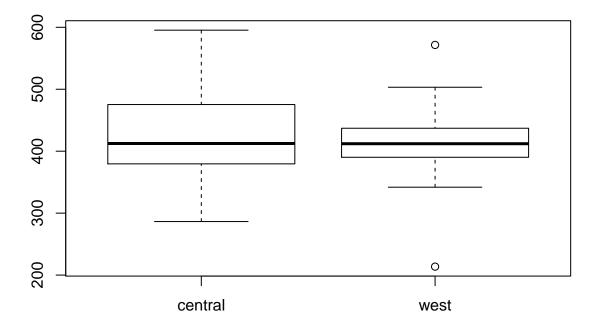
pctmin80



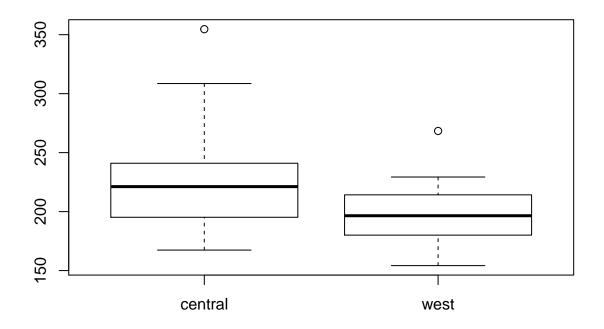
wcon



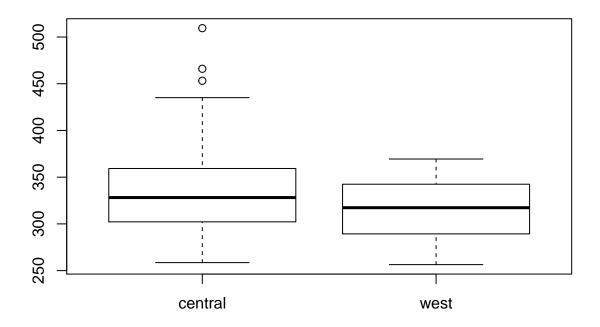
wtuc



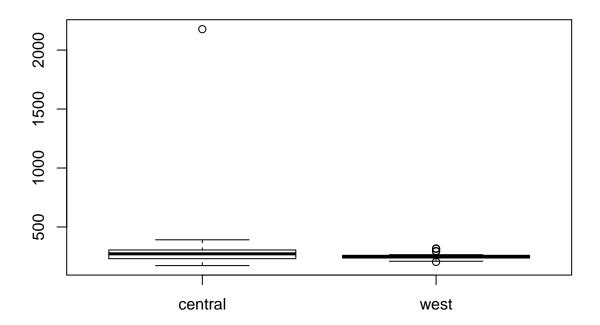
wtrd



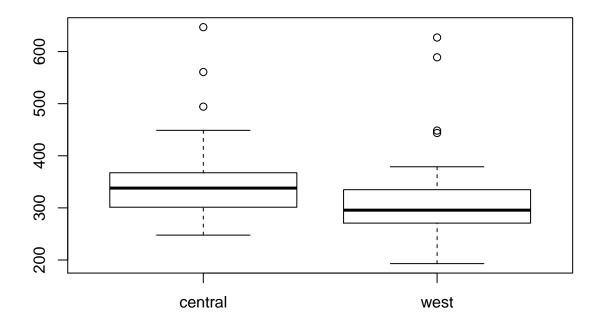
wfir



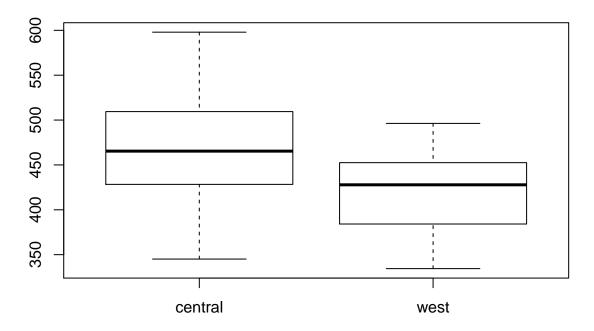
wser



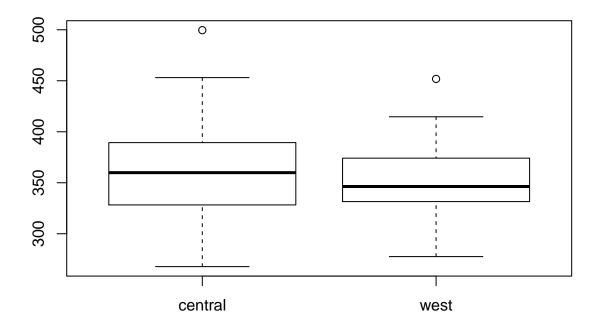
wmfg



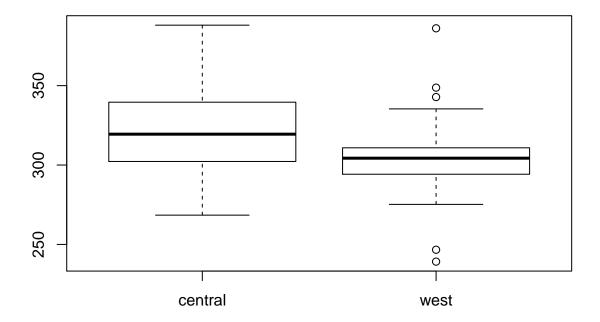
wfed



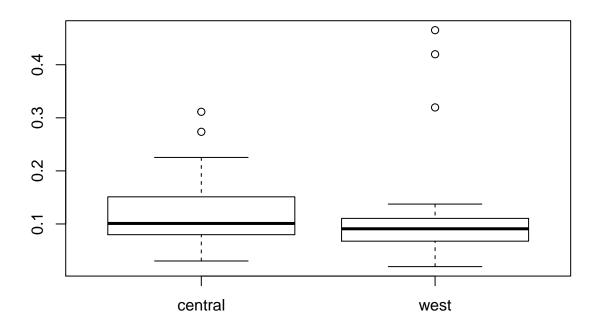




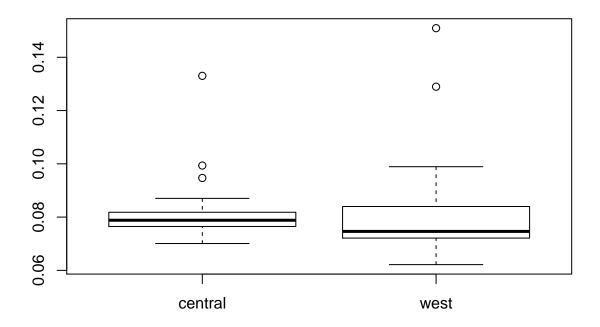
wloc



mix



pctymle



```
##
         crmrte
                       prbarr
                                    prbconv
                                                 prbpris
                                                              avgsen
## stats Numeric,10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                              Numeric, 10
         Numeric,2
                                                 Numeric,2
                                                              Numeric,2
## n
                       Numeric,2
                                    Numeric,2
                                                              Numeric,4
## conf
         Numeric, 4
                       Numeric, 4
                                    Numeric,4
                                                 Numeric, 4
                                                              20.7
         0.0989659
                       1.09091
                                    Numeric,2
                                                 0.15
## out
                                                              2
                       2
                                    Numeric,2
##
   group 1
   names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
         polpc
                       density
                                    taxpc
                                                 pctmin80
                                                              wcon
## stats Numeric,10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                              Numeric, 10
## n
         Numeric, 2
                       Numeric,2
                                    Numeric,2
                                                 Numeric, 2
                                                              Numeric, 2
## conf
         Numeric,4
                       Numeric, 4
                                    Numeric,4
                                                 Numeric, 4
                                                              Numeric, 4
                                                              385.3424
##
   out
         Numeric,3
                       Numeric,5
                                    Numeric,3
                                                 Numeric, 2
   group Numeric,3
                       Numeric,5
                                    Numeric,3
                                                 Numeric, 2
                                                              2
##
   names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
                                                              wmfg
##
                       wtrd
                                    wfir
         wtuc
                                                 wser
                                                              Numeric, 10
## stats Numeric, 10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                              Numeric, 2
## n
         Numeric, 2
                       Numeric, 2
                                    Numeric, 2
                                                 Numeric, 2
## conf
         Numeric, 4
                       Numeric,4
                                    Numeric,4
                                                 Numeric,4
                                                              Numeric, 4
## out
         Numeric,2
                       Numeric,2
                                    Numeric,3
                                                 Numeric,6
                                                              Numeric,7
   group Numeric,2
                       Numeric,2
                                    Numeric,3
                                                 Numeric,6
                                                              Numeric,7
##
  names Character, 2 Character, 2 Character, 2 Character, 2 Character, 2
##
         wfed
                                    wloc
                       wsta
                                                 mix
                                                              pctymle
## stats Numeric,10
                       Numeric, 10
                                    Numeric, 10
                                                 Numeric, 10
                                                              Numeric, 10
## n
         Numeric, 2
                       Numeric, 2
                                    Numeric,2
                                                 Numeric, 2
                                                              Numeric, 2
## conf
                                    Numeric,4
                                                              Numeric,4
         Numeric, 4
                       Numeric,4
                                                 Numeric,4
## out
         Numeric,0
                       Numeric, 2
                                    Numeric,5
                                                 Numeric,5
                                                              Numeric,5
```

```
## group Numeric,0 Numeric,2 Numeric,5 Numeric,5 Numeric,5
## names Character,2 Character,2 Character,2 Character,2
```

Comparing central vs west,

central has higher

- crime rate
- density
- tax revenue per capita
- percentage of minority
- percentage of young male
- wages in general are higher except for wtuc

west has higher

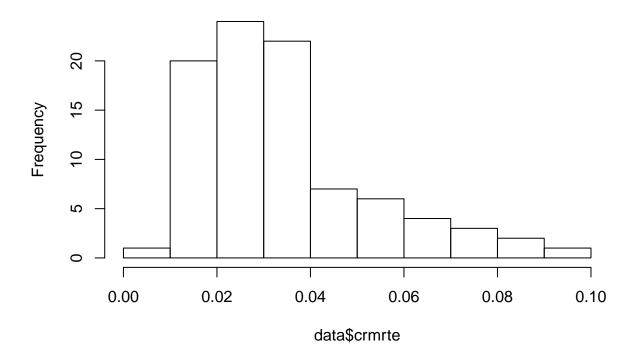
• average sentence

central and west are about the same

- probability of arrest
- probability of conviction
- probability of prison sentence
- police per capita
- face to face confrontation (central has slightly higher)

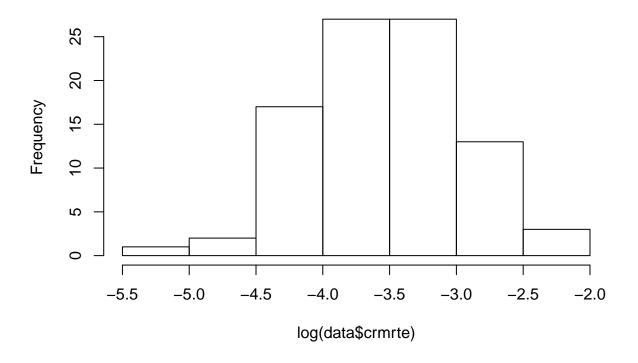
potential dependent variable: crime rate
hist(data\$crmrte)

Histogram of data\$crmrte



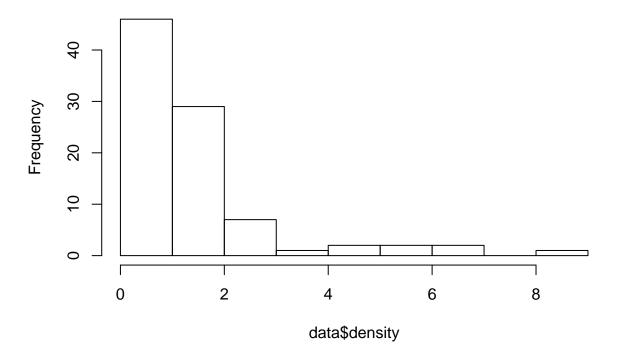
hist(log(data\$crmrte))

Histogram of log(data\$crmrte)



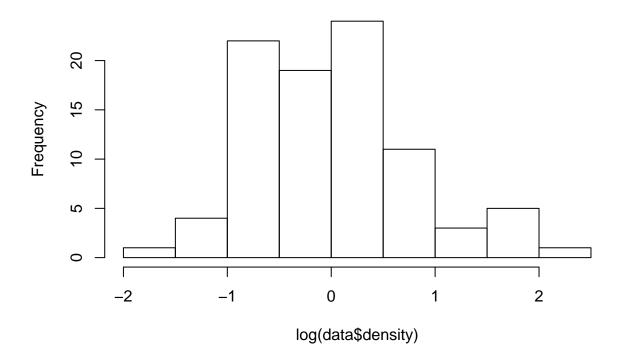
potential independent variables
1. density
hist(data\$density)

Histogram of data\$density



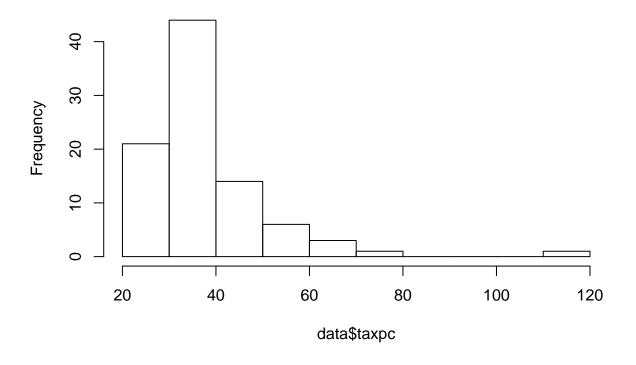
hist(log(data\$density))

Histogram of log(data\$density)



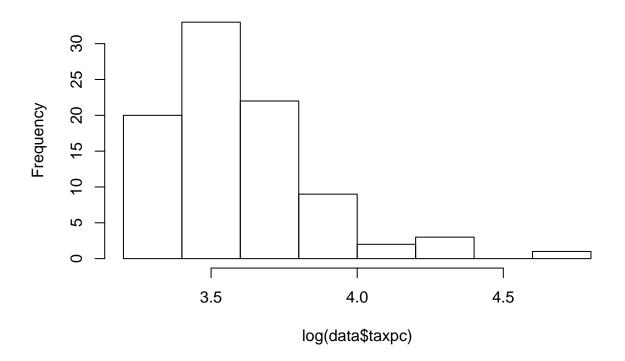
2. taxpc
hist(data\$taxpc)

Histogram of data\$taxpc



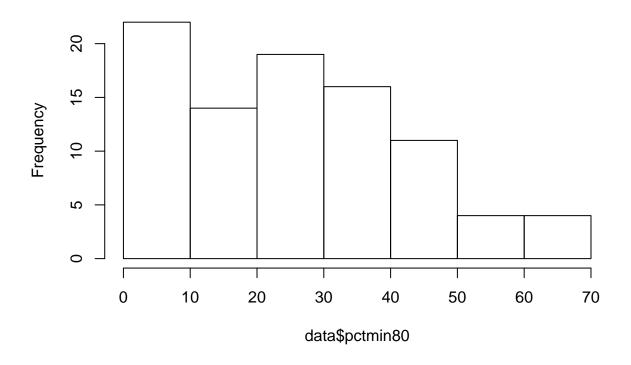
hist(log(data\$taxpc))

Histogram of log(data\$taxpc)



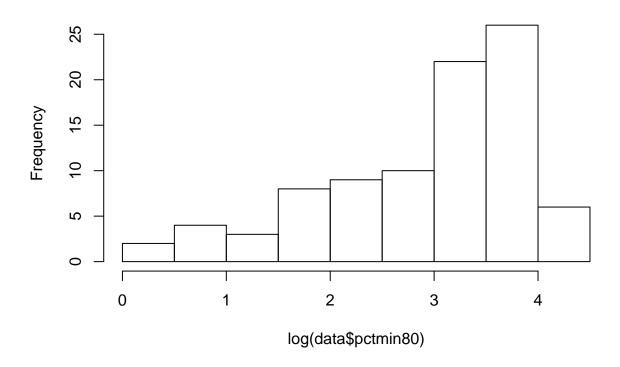
```
# log didn't quite change much because of one outlier
# 3. pctmin80
hist(data$pctmin80)
```

Histogram of data\$pctmin80



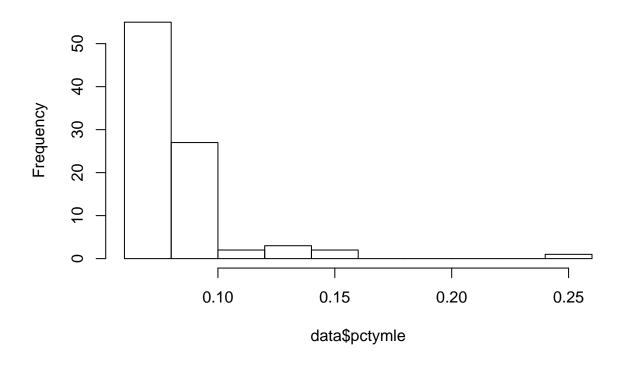
hist(log(data\$pctmin80))

Histogram of log(data\$pctmin80)



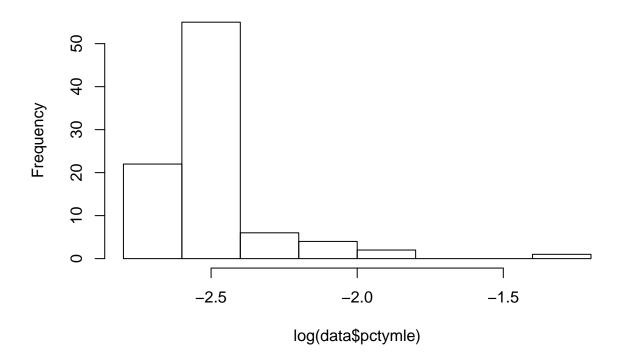
better leave variable as is because applying a log skewed the distribution
4. pctymle
hist(data\$pctymle)

Histogram of data\$pctymle



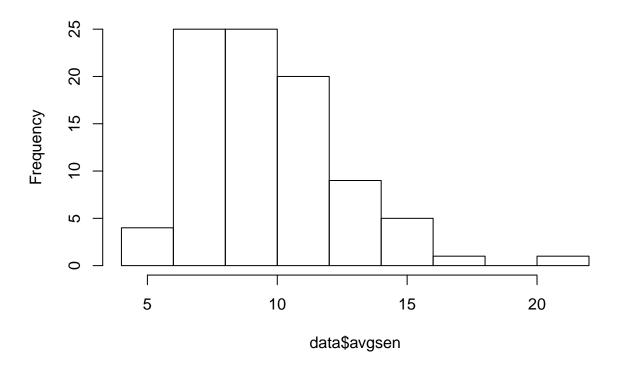
hist(log(data\$pctymle))

Histogram of log(data\$pctymle)



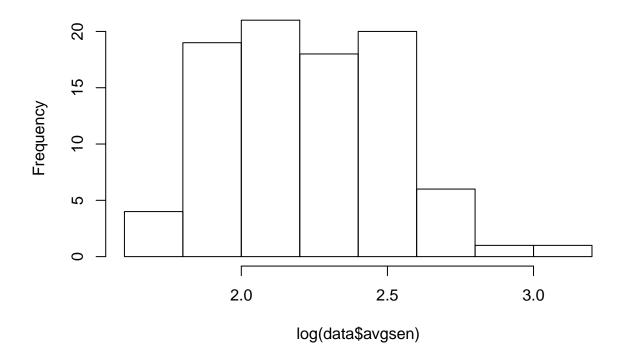
```
# log didn't quite change much because of one outlier
# 5. avgsen
hist(data$avgsen)
```

Histogram of data\$avgsen



hist(log(data\$avgsen))

Histogram of log(data\$avgsen)

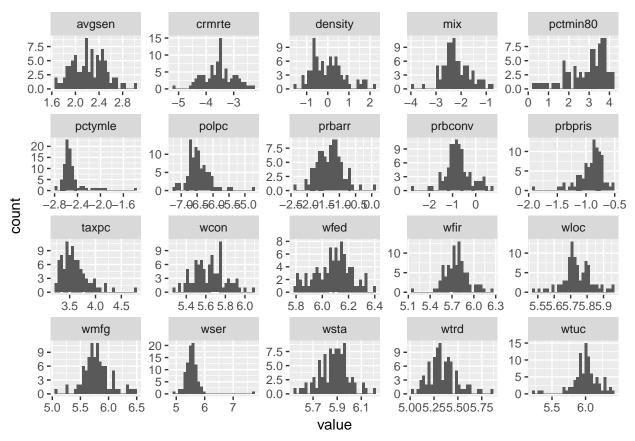


already verified that these variables are not correlated to each other

Observations

- All observations were recorded for the year of 1987.
- urban, central, west are categorical variables.
- Most wages variables (wcon, wfed, wfir, wmfg, wser, wsta, wtrd) have a positively skewed distribution which may be due to few number people getting paid above the average.
- wtuc, wloc appear to be normally distributed.
- prbarr, prbconv appear to be positively skewed while prbpris is more negatively skewed.
- avgsen appears to be positively skewed.
- crmrte, density, polpc, prbconv: The histogram indicates that these variables have positive skews. Given the variables have a meaningful zero-point, we can take the log for a more normal distribution.

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



Observations after taking logs: It looks like the log transformation of variables cmrte, mix, prbconv, wfed, wfir, wmfg, and wsta have made the distributions quite normal. This will help ensure the errors of the model are normal.

Proposed Model Based on the exploratory data analysis and general intution about the potential determinants of crime, an initial proposed model specification and coefficient expectation are:

- Sum of all wages: Summing the wage variables across sectors may identify whether income inequality between counties may explain the difference in crime rates. Initial thoughts are that sum of wages (higher incomes) lead to lower crime rates, so a linear relationship between sum of wages and crimes committed per person is expected with a negative coefficient.
- log(prbarr) Probability of arrest: There is the possibility that the probability of arrest is positively correlated with crime rate, as higher numbers of arrest can increase the number of crimes recorded.
- tax revenue per capita (taxpc): Lack of government-funded resources can take the form of a lack of educational opportunities or employment options, thus leading to rise in crime rates.

Model 1: $log(crmrte) = \beta_0 + \beta_1(allwages) + \beta_2 log(prbarr) + \beta_3(taxrev) + u$

Model Building Process

TODO: A model building process, supported by exploratory analysis. Your EDA should be interspersed with, and support, your modeling decisions. In particular, you should use exploratory techniques to address * What transformations to apply to variables and what new variables should be created. * What variables should be included in each model * Whether model assumptions are met

 $\begin{array}{l} \text{\$density} \ [1] \ "8: 3.93455100059509, \ 4.38875865936279, \ 4.8347339630127, \ 5.12442398071289, \ 5.6744966506958, \\ 6.28648662567139, \ 6.42718458175659, \ 8.82765197753906 \end{array}$

 $\$ taxpc \ [1] \ "6: 56.8621063232422, \ 61.1525115966797, \ 67.6796340942383, \ 67.8479766845703, \ 75.6724319458008, \ 119.761451721191"$

Model Specifications

Model 1

TODO: * One model with only the explanatory variables of key interest (possibly transformed, as determined by your EDA), and no other covariates.

```
log(crmrte) = \beta_0 + \beta_1 \cdot log(density) + \beta_2 \cdot (taxpc) + u m1 <- lm(log(crmrte) ~ log(density) + taxpc, data=data)
```

TODO: For your first model, a detailed assessment of the 6 CLM assumptions. For additional models, you should check all assumptions, but only highlight major differences from your first model in your report.

CLM 1 - A linear model

The model is specified such that the dependent variable is a linear function of the explanatory variables. Is the assumption valid? Yes

Response: No response required.

CLM 2 - Random Sampling

TODO

CLM 3 - Multicollinearity

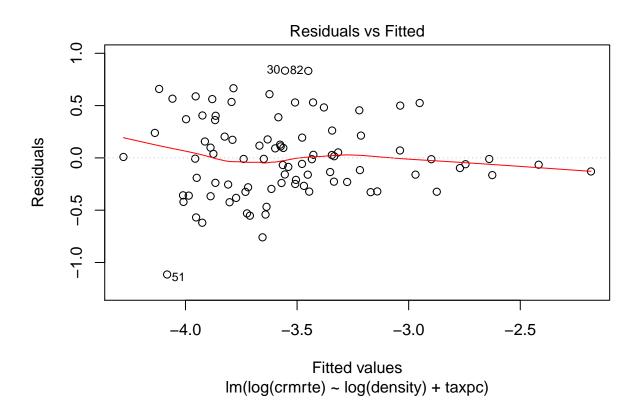
```
# show correlation
data$log.density <- log(data$density)</pre>
cor(data.matrix(subset(data, select=c("density", "log.density", "taxpc"))))
##
                 density log.density
                                           taxpc
## density
               1.0000000
                            0.8896747 0.3204737
## log.density 0.8896747
                            1.0000000 0.1841222
               0.3204737
                            0.1841222 1.0000000
## taxpc
# show vif
vif(m1)
## log(density)
                        taxpc
       1.035091
                    1.035091
```

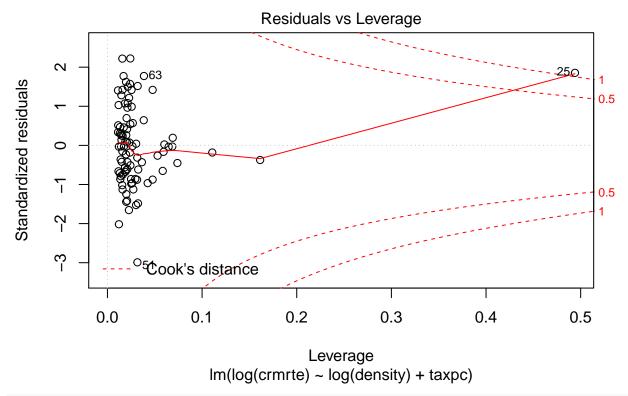
The two explanatory variables (log.density and taxpc) are not perfectly correlated and the VIFs are low (less than 4), so there is no perfect multicollinearity of the independent variables.

Is the assumption valid? Yes

Response: No response required.

plot(m1, which=c(1, 5))





exogenous check
cov(log(data\$density), m1\$residuals)

[1] -8.896016e-18

cov(data\$taxpc, m1\$residuals)

[1] -4.453513e-16

The covariances of the two independent variables with the residuals are very close to zero indicating they are likely exogenous.

There is a data point with a large Cook's distance.

Is the assumption valid?

Response:

CLM 5 - Homoscedasticity

spreadLevelPlot(m1)
plot(m1, which=3)

Scale-Location 051 300820 ιÖ /|Standardized residuals 0 0 1.0 ∞ 0 0 0 0 0.5 0 0 0 0 0 0 0 0 0 0 0 0.0

-3.5

Fitted values Im(log(crmrte) ~ log(density) + taxpc)

-3.0

-2.5

```
bptest(m1)
```

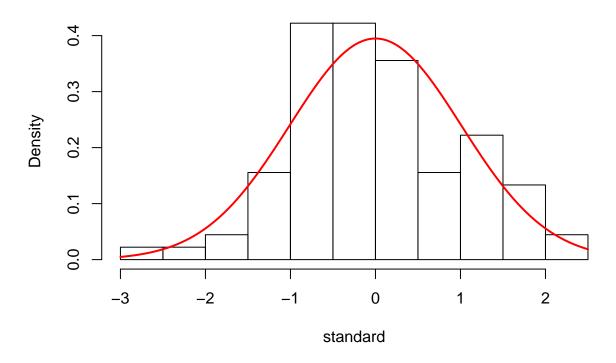
```
##
##
    studentized Breusch-Pagan test
##
## data: m1
## BP = 7.2256, df = 2, p-value = 0.02698
not significant p-value for Breusch-Pagan test -> assumption of homoscedasticity met
ncvTest(m1)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 6.968285
                             Df = 1
                                         p = 0.008296697
significant p-value for Score Test -> assumption of homoscedasticity met
Is the assumption valid? Yes
Response:
```

CLM 6 - Normality of residuals

-4.0

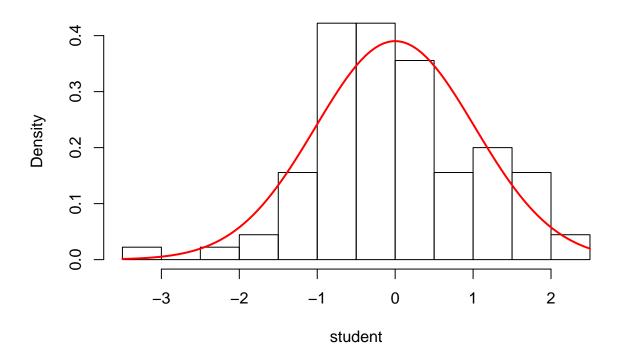
```
# normality of standard residuals
standard <- rstandard(m1)
hist(standard, main="Histogram of standard residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(standard)), col="red", lwd=2, add=TRUE)</pre>
```

Histogram of standard resiudals



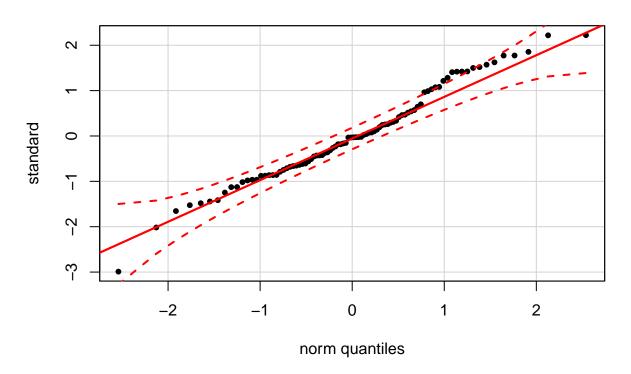
```
# normality of studentized residuals
student <- rstudent(m1)
hist(student, main="Histogram of studentized residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(student)), col="red", lwd=2, add=TRUE)</pre>
```

Histogram of studentized resiudals



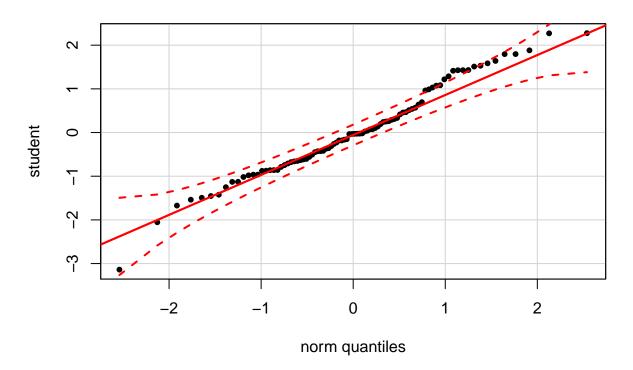
```
# QQ plot standard residuals
qqPlot(standard, distribution="norm", pch=20, main="QQ-Plot standard residuals")
qqline(standard, col="red", lwd=2)
```

QQ-Plot standard residuals



```
# QQ plot studentized residuals
qqPlot(student, distribution="norm", pch=20, main="QQ-Plot studentized residuals")
qqline(student, col="red", lwd=2)
```

QQ-Plot studentized residuals



The histograms in particular appear to be fairly normally distributed, while the Q-Q plot doesn't deviate significantly from normality either, so overall the residuals appear to be fairly normal. Notably the log transformation of views has helped to produce normal errors.

Is the assumption valid? Yes

Response: No response required.

TODO: * One model that includes key explanatory variables and only covariates that you believe increase the accuracy of your results without introducing bias (for example, you should not include outcome variables that will absorb some of the causal effect you are interested in). This model should strike a balance between accuracy and parsimony and reflect your best understanding of the determinants of crime.

m2 <- lm(log(crmrte) ~ log(density) + taxpc + urban, data=data)</pre>

CLM 1 - A linear model

The model is specified such that the dependent variable is a linear function of the explanatory variables. Is the assumption valid? Yes

Response: No response required.

CLM 2 - Random Sampling

TODO

CLM 3 - Multicollinearity

```
# show correlation
data$log.density <- log(data$density)</pre>
cor(data.matrix(subset(data, select=c("density", "log.density", "taxpc", "urban"))))
##
                 density log.density
                                          taxpc
                                                     urban
## density
               1.000000
                           0.8896747 0.3204737 0.8206825
## log.density 0.8896747
                            1.0000000 0.1841222 0.6490078
               0.3204737
                            0.1841222 1.0000000 0.3457462
## taxpc
## urban
               0.8206825
                            0.6490078 0.3457462 1.0000000
# show vif
vif(m2)
## log(density)
                        taxpc
                                     urban
       1.733261
                    1.139396
                                  1.901850
```

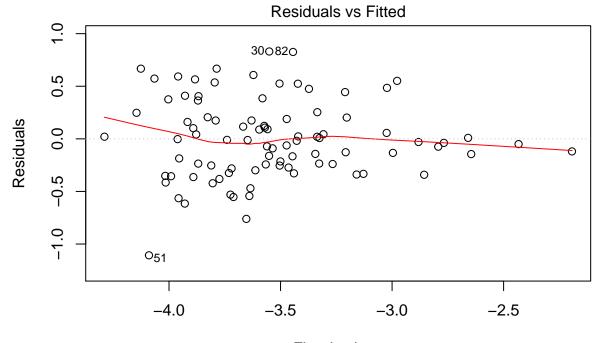
The two explanatory variables (log.density and taxpc) are not perfectly correlated and the VIFs are low (less than 4), so there is no perfect multicollinearity of the independent variables.

Is the assumption valid? Yes

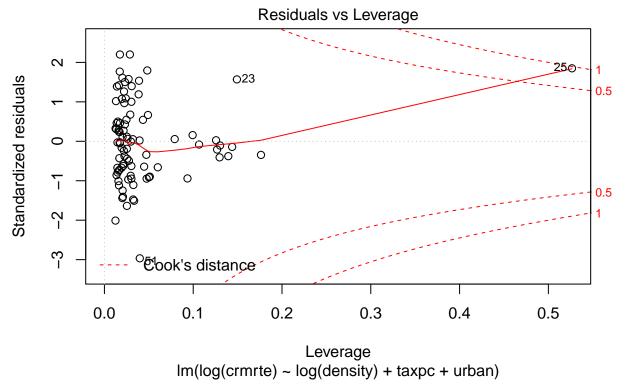
Response: No response required.

CLM 4 - Zero-Conditional Mean

```
plot(m2, which=c(1, 5))
```



Fitted values Im(log(crmrte) ~ log(density) + taxpc + urban)



```
# exogenous check
cov(log(data$density), m2$residuals)
```

```
## [1] -8.492333e-18
cov(data$taxpc, m2$residuals)
```

cov(data\$urban, m2\$residuals)

```
## [1] -3.523097e-16
# TODO: figure out what to do with covariate
```

```
## [1] 9.501997e-19
```

The covariances of the two independent variables with the residuals are very close to zero indicating they are likely exogenous.

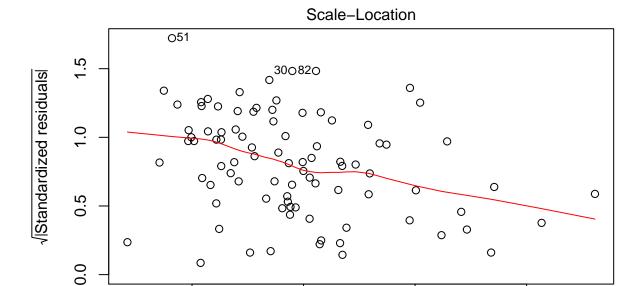
There is a data point with a large Cook's distance.

Is the assumption valid?

Response:

CLM 5 - Homoscedasticity

```
# spreadLevelPlot(m1)
plot(m2, which=3)
```



-3.5

Fitted values Im(log(crmrte) ~ log(density) + taxpc + urban)

-3.0

-2.5

```
bptest(m2)
```

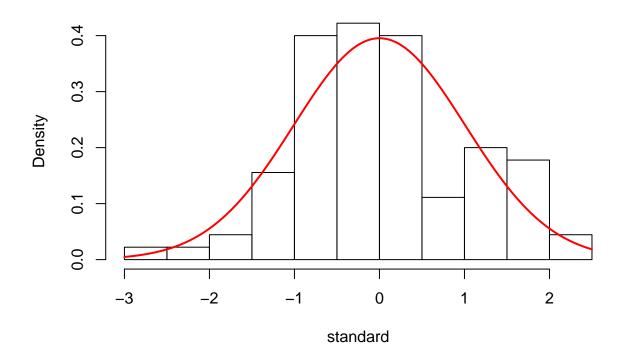
```
##
##
    studentized Breusch-Pagan test
##
## data: m2
## BP = 7.708, df = 3, p-value = 0.05245
not significant p-value for Breusch-Pagan test -> assumption of homoscedasticity met
ncvTest(m2)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 7.064728
                             Df = 1
                                         p = 0.007861626
significant p-value for Score Test -> assumption of homoscedasticity met
Is the assumption valid? Yes
Response:
```

CLM 6 - Normality of residuals

-4.0

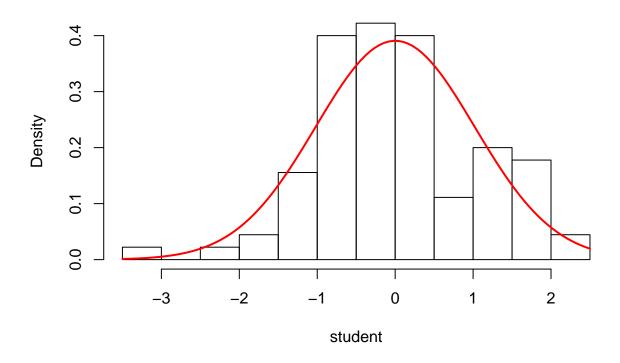
```
# normality of standard residuals
standard <- rstandard(m2)
hist(standard, main="Histogram of standard residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(standard)), col="red", lwd=2, add=TRUE)</pre>
```

Histogram of standard resiudals



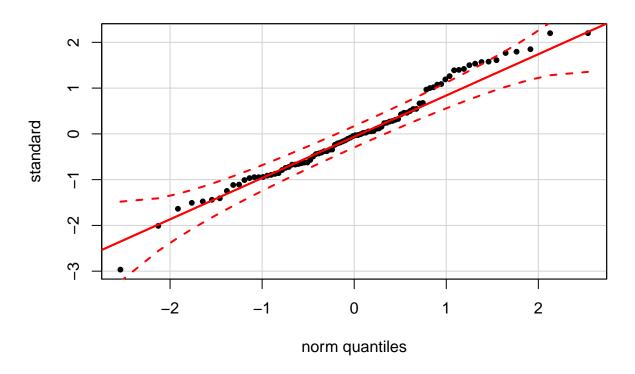
```
# normality of studentized residuals
student <- rstudent(m2)
hist(student, main="Histogram of studentized residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(student)), col="red", lwd=2, add=TRUE)</pre>
```

Histogram of studentized resiudals



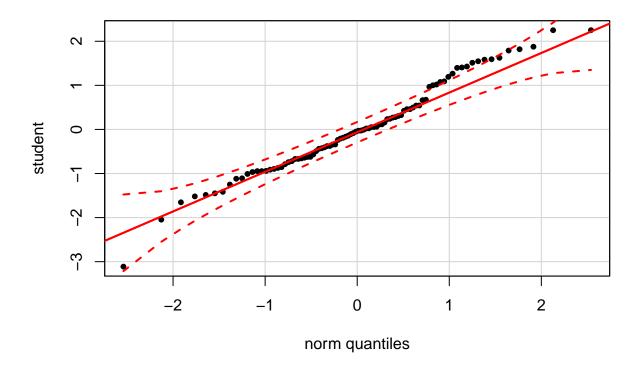
```
# QQ plot standard residuals
qqPlot(standard, distribution="norm", pch=20, main="QQ-Plot standard residuals")
qqline(standard, col="red", lwd=2)
```

QQ-Plot standard residuals



```
# QQ plot studentized residuals
qqPlot(student, distribution="norm", pch=20, main="QQ-Plot studentized residuals")
qqline(student, col="red", lwd=2)
```

QQ-Plot studentized residuals



The histograms in particular appear to be fairly normally distributed, while the Q-Q plot doesn't deviate significantly from normality either, so overall the residuals appear to be fairly normal. Notably the log transformation of views has helped to produce normal errors.

Is the assumption valid? Yes

Response: No response required.

TODO: * One model that includes the previous covariates, and most, if not all, other covariates. A key purpose of this model is to demonstrate the robustness of your results to model specification.

```
m3 <- lm(log(crmrte) ~ log(density) + taxpc + urban + central + west, data=data)
```

CLM 1 - A linear model

The model is specified such that the dependent variable is a linear function of the explanatory variables. Is the assumption valid? Yes

Response: No response required.

CLM 2 - Random Sampling

TODO

CLM 3 - Multicollinearity

```
# show correlation
data$log.density <- log(data$density)</pre>
cor(data.matrix(subset(data, select=c("density", "log.density", "taxpc", "urban"))))
##
                 density log.density
                                          taxpc
                                                     urban
               1.000000
                           0.8896747 0.3204737 0.8206825
## density
## log.density 0.8896747
                            1.0000000 0.1841222 0.6490078
               0.3204737
                            0.1841222 1.0000000 0.3457462
## taxpc
## urban
               0.8206825
                            0.6490078 0.3457462 1.0000000
# show vif
vif(m2)
## log(density)
                        taxpc
                                     urban
       1.733261
                    1.139396
                                  1.901850
```

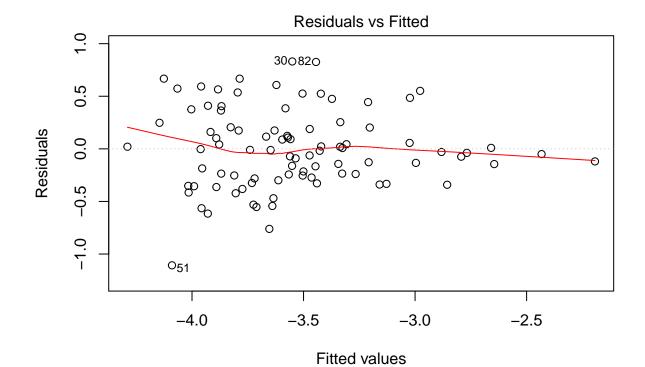
The two explanatory variables (log.density and taxpc) are not perfectly correlated and the VIFs are low (less than 4), so there is no perfect multicollinearity of the independent variables.

Is the assumption valid? Yes

Response: No response required.

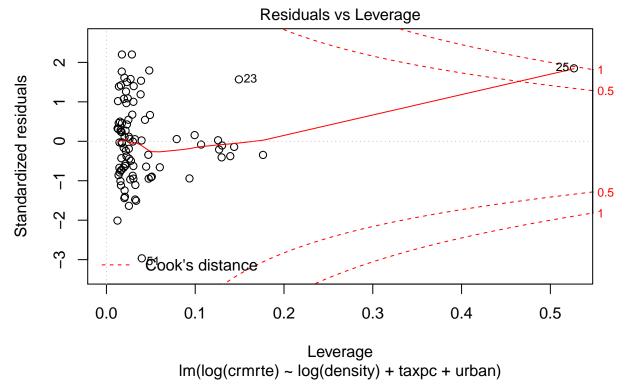
CLM 4 - Zero-Conditional Mean

```
plot(m2, which=c(1, 5))
```



Im(log(crmrte) ~ log(density) + taxpc + urban)

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```
# exogenous check
cov(log(data$density), m2$residuals)
```

```
## [1] -8.492333e-18
```

cov(data\$taxpc, m2\$residuals)

```
## [1] -3.523097e-16
```

```
# TODO: figure out what to do with covariate
cov(data$urban, m2$residuals)
```

[1] 9.501997e-19

The covariances of the two independent variables with the residuals are very close to zero indicating they are likely exogenous.

There is a data point with a large Cook's distance.

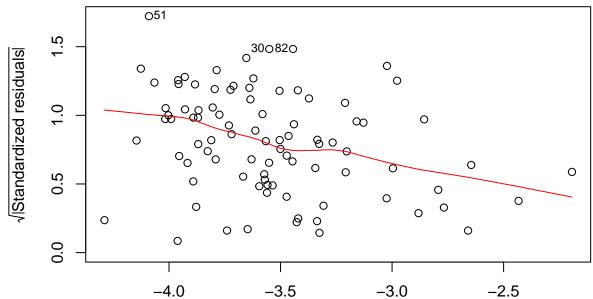
Is the assumption valid?

Response:

CLM 5 - Homoscedasticity

```
# spreadLevelPlot(m1)
plot(m2, which=3)
```

Scale-Location



Fitted values Im(log(crmrte) ~ log(density) + taxpc + urban)

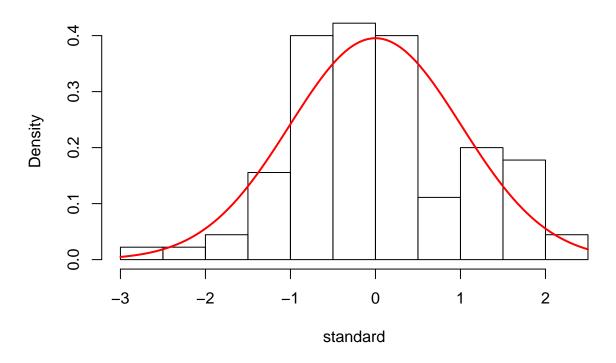
```
bptest(m2)
```

```
##
##
    studentized Breusch-Pagan test
##
## data: m2
## BP = 7.708, df = 3, p-value = 0.05245
not significant p-value for Breusch-Pagan test -> assumption of homoscedasticity met
ncvTest(m2)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 7.064728
                             Df = 1
                                         p = 0.007861626
significant p-value for Score Test -> assumption of homoscedasticity met
Is the assumption valid? Yes
Response:
```

CLM 6 - Normality of residuals

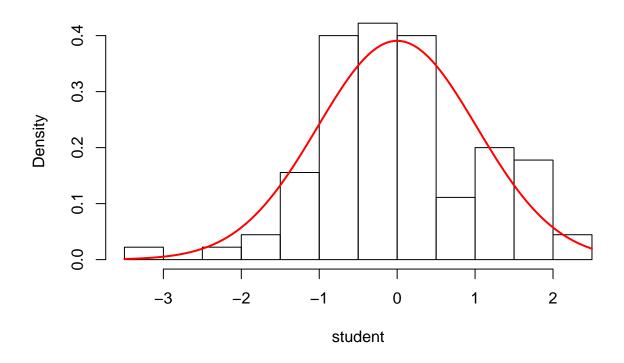
```
# normality of standard residuals
standard <- rstandard(m2)</pre>
hist(standard, main="Histogram of standard residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(standard)), col="red", lwd=2, add=TRUE)
```

Histogram of standard resiudals



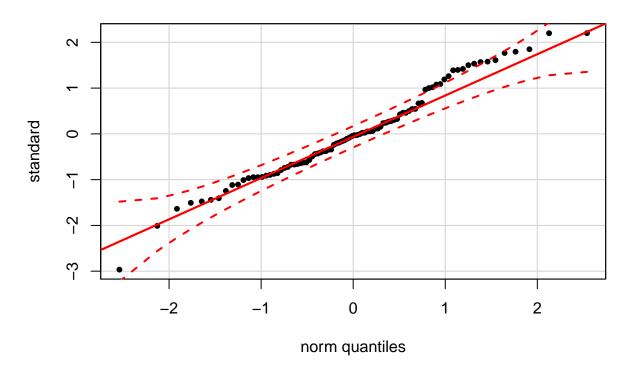
```
# normality of studentized residuals
student <- rstudent(m2)
hist(student, main="Histogram of studentized residuals", freq=FALSE)
curve(dnorm(x, mean=0, sd=sd(student)), col="red", lwd=2, add=TRUE)</pre>
```

Histogram of studentized resiudals



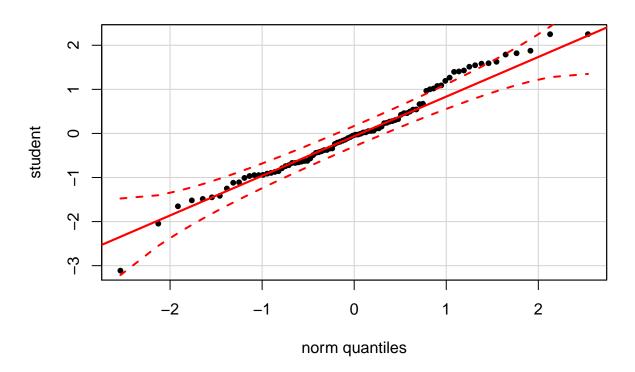
```
# QQ plot standard residuals
qqPlot(standard, distribution="norm", pch=20, main="QQ-Plot standard residuals")
qqline(standard, col="red", lwd=2)
```

QQ-Plot standard residuals



```
# QQ plot studentized residuals
qqPlot(student, distribution="norm", pch=20, main="QQ-Plot studentized residuals")
qqline(student, col="red", lwd=2)
```

QQ-Plot studentized residuals



The histograms in particular appear to be fairly normally distributed, while the Q-Q plot doesn't deviate significantly from normality either, so overall the residuals appear to be fairly normal. Notably the log transformation of views has helped to produce normal errors.

Is the assumption valid? Yes

Response: No response required.

Model Results

TODO: A well-formatted regression table summarizing your model results. Make sure that standard errors presented in this table are valid. Also, be sure to comment on both statistical and practical significance.

```
##
## % Table created by stargazer v.5.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvare
## % Date and time: Wed, Dec 06, 2017 - 03:07:54
## \begin{table}[!htbp] \centering
## \caption{Linear Models Predicting Crime Rates}
## \label{}
```

```
## \begin{tabular}{@{\extracolsep{5pt}}lccc}
## \\[-1.8ex]\hline
## \hline \\[-1.8ex]
## & \multicolumn{3}{c}{\textit{Dependent variable:}} \
## \cline{2-4}
## \\[-1.8ex] & \multicolumn{3}{c}{log(crmrte)} \\
## \\[-1.8ex] & (1) & (2) & (3)\\
## \hline \\[-1.8ex]
   log(density) & 0.455$^{***}$ & 0.464$^{***}$ & 0.488$^{***}$ \\
   & (0.052) & (0.068) & (0.063) \\
##
    & & & \\
## taxpc & 0.010\$^{**}$ & 0.010\$^{**}$ & 0.007\$^{*}$ \\
##
    & (0.003) & (0.003) \\
##
    & & & \\
## urban & & $-$0.043 & $-$0.015 \\
##
    & & (0.195) & (0.168) \\
##
    & & & \\
  central & & & $-$0.306$^{***}$ \\
##
    & & & (0.085) \\
##
    & & & \\
## west & & $-$0.515$^{***}$ \\
    & & & (0.091) \\
    & & & \\
##
## Constant & -33.931^{***} & -33.936^{***} & -33.589^{***} \\
    & (0.125) & (0.128) & (0.125) \\
##
    & & & \\
## \hline \\[-1.8ex]
## Observations & 90 & 90 & 90 \\
## R$^{2}$ & 0.534 & 0.534 & 0.669 \\
## Adjusted R$^{2}$ & 0.523 & 0.518 & 0.649 \\
## \hline
## \hline \\[-1.8ex]
## \textit{Note:} & \multicolumn{3}{r}{$^{*}$p$<$0.05; $^{**}$p$<$0.01; $^{***}$p$<$0.001} \\
## \end{tabular}
## \end{table}
```

Causality

TODO: A detailed discussion of causality. In particular, include a discussion of what variables are not included in your analysis and the likely direction of omitted variable bias. Highlight any coefficients you find that appear to have the wrong sign from a causal perspective, and explain why this is the case.

Conclusion

TODO: A brief conclusion with a few high-level takeaways.