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DNHI Homework 2 Solutions
Recursion

Problem 1

Part A Write an iterative method that computes a value of x^n for a positive integer n and a real number x.

Answer:
The return value of -1 indicates an error condition.

```
public static double powerIter (double x, int n) {
  double result = 1;

  if (n < 0 ) return -1;

  while (n > 0) {
    result = result * x;
    n--;
  }
  return result;
}
```

Part B Write a recursive method that computes a value of x^n for a positive integer n and a real number x. Answer:
The return value of -1 indicates an error condition. X

```
public static double powerRecursive (double x, int n) {

  if (n < 0 ) return -1;
  if (n == 0) return 1;
  return x * powerRecursive (x, n - 1);
}
```

Problem 2

Consider the following recursive method

```
public int recMethod ( int number ) {
  if ( number <= 0 )
    return 0;
  if ( number % 2 == 0 )
    return recMethod ( number - 1 );
  else
    return number + recMethod ( number - 1);
}

```

Part A
How many times is this method called (including the initial call) when we run `recMethod(10)` ?

Answer: Called 11 times.

How many times is this method called (including the initial call) when we run `recMethod(-10)` ?

Answer: Called 1 time.

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Part B

What does **recMethod** do (i.e. what does it compute)?

Answer: It computes the sum of odd numbers from zero to `number`.

Problem 3

Write a recursive method to compute the following series:

$$\frac{1}{3} + \frac{2}{5} + \frac{3}{7} + \frac{4}{9} + \ldots + \frac{i}{2i+1}.$$

Answer: The crucial part in this code is casting to `double` so that the fraction do not become all zero. Other than that it should be a straight forward implementation of the recursive method.

```
public static double summation ( int num ) {
  //base case
  if ( num <= 0 )  return 0;
  //recursion
  return (double)num/(2*num+1) + summation(num-1);
}
```

Problem 4

Write a **recursive** method that computes the sum of the digits in an integer. Use the following method header:

```
    public static int sumOfDigits ( long n )
```

For example, **sumOfDigits(234)** should return 9 (since 2 + 3 + 4 = 9) and **sumOfDigits(390)** should return 12 (since 3 + 9 + 0 = 12).

Answer: A possible solution could be:

```
public static int sumOfDigits ( long n ) {
  //base case is when the number is zero
  if( n==0 )
    return 0;
  //recursive case
  return ( (int)(n%10) + sumOfDigits( n/10 ) );
}
```

Problem 5

For each of the following recursive methods, rewrite it using iterations instead of recursion. HINT: in order to do so you should first figure out what these methods do.

Part A

```
public int recur ( int n ) {
  if (n < 0 )
    return -1;
  else if ( n < 10 )
    return 1;
  else
    return ( 1 + recur ( n / 10 ) );
}
```

Answer:
The code above computes the number of digits in the parameter n.

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```
public int recur (int n) {
  int solution = 0;
  while (n > 0 ){
    solution++;
    n = n/10;
  }
  return solution;
}
```

Part B

```
public int recur2 ( int n ){
  if (n < 0 )
    return -1;
  else if ( n < 10 )
    return n;
  else
    return ( n % 10 + recur2 ( n / 10 ) );
}
```

Answer:
This method computes sum of digits in a parameter n.

```
public int recur2 ( int n ){
  int sum = 0;
  while (n > 0 ) {
    sum += n%10;
    n = n/10;
  }
}
```

Problem 6

What would be printed by the following programs

Part A)

```
public class CatsAndDogs {

  public static void main(String[] args) {
    foo("Cats and Dogs", 4);
  }

  public static void foo ( String s, int n ) {
    if (n <= 1)
      System.out.println("Cats");
    else {
      System.out.println( s ) ;
      foo ( s, n-1 );
    }
  }
}
```

Answer:

```
Cats and Dogs
Cats and Dogs
Cats and Dogs
Cats
```

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Part B)

```
1 public class Numbers {
2
3   public static void main(String[] args) {
4     int [] list = {1, 2, 3, 4, 5};
5     System.out.println( foo (list, 0, list.length-1) );
6   }
7
8   public static int foo ( int [] nums, int begin, int end ) {
9     if ( begin == end )
10      return nums[begin];
11    else
12      return nums[begin] + foo(nums, begin+1, end);
13  }
14 }
```

Answer:
The `foo` method computes the sum of the values in the list from between index `begin` and index `end`. So in this case it computes the sum of all elements in the list. It prints 15

Problem 7

Part A Write a method that generates all sequences of a given length that contain digits 0 through 9 (all ten digits are allowed, repetitions are allowed)? Given length of the sequence equal to n, how many possible sequences are there?

Answer:
With length of n digits, the number of possible sequences is equal to 10^n, for example, with lenght of $n = 4$, we have $10,000$ different sequences.

```
1 /**
2   * Generate all decimal sequences of the specified length.
3   * @param length the length of the sequences to be generated
4   */
5 public static void getAllDecimalSequences ( int length ) {
6   String seq = new String () ;
7   int counter = 0;
8   getAllDecimalSequences( length, seq);
9 }
10
11 /* Generate all decimal sequences of a specified length
12   * using the seq String as storage for partial sequences.
13   * @param length the length of the sequence to be generated
14   * @param seq stores partial sequences between recursive calls
15   */
16 private static void getAllDecimalSequences ( int length, String seq ) {
17   if (seq.length() == length ) {//reached the desired length
18     System.out.printf("%s %n", seq );
19   }
20   else { //add the next digit to the sequence (two possibilities)
21
22     for (int i = 0; i < 10; i++) {
23       //add digit i to the current sequence
24       getAllDecimalSequences( length, seq + Integer.toString(i));
25     }
26   }
27 }
```

Part B Modify the above method so that none of the generated sequences start with zero. How many of those sequences exist, given the length of n digits?

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Answer:
With this restriction, we only have 9 possiblities for the first digit and 10 for all the remaining digits. So there will be total of $9 \times 10^{n-1}$ sequences of length n that do not start with a zero.

```
/**
  * Generate all decimal sequences of the specified length with added
  * constraint that the first digit is never zero.
  * @param length the length of the sequences to be generated
  */
public static void getDecimalSequencesNoLeadingZero ( int length ) {
  String seq = new String () ;
  getDecimalSequencesNoLeadingZero( length, seq);
}

/*
  * Generate all decimal sequences of the specified length with added
  * constraint that the first digit is never zero. seq is used for storage
  * of partial sequences.
  * @param length the length of the sequences to be generated
  * @param seq stores partial sequences between recursive calls
  */
private static void getDecimalSequencesNoLeadingZero ( int length, String seq  ) {
  if (seq.length() == length ) {//reached the desired length
    System.out.printf("%s %n", seq );
  }
  else if (seq.length() == 0 ) { //do not start any sequence with a zero
    for (int i = 1; i < 10; i++) {
      //add digit i to the current sequence
      getAllDecimalSequences( length, seq + Integer.toString(i));
    }
  }
  else {
    for (int i = 0; i < 10; i++) {
      //add digit i to the current sequence
      getAllDecimalSequences( length, seq + Integer.toString(i));
    }
  }
}
```