



## DNHI Homework 2 Solutions

### Recursion

#### Problem 1

**Part A** Write an iterative method that computes a value of  $x^n$  for a positive integer  $n$  and a real number  $x$ .

Answer:

The return value of -1 indicates an error condition.

```
1 public static double powerIter (double x, int n) {
2     double result = 1;
3
4     if (n < 0 ) return -1;
5
6     while (n > 0) {
7         result = result * x;
8         n--;
9     }
10    return result;
11 }
```

**Part B** Write a recursive method that computes a value of  $x^n$  for a positive integer  $n$  and a real number  $x$ . Answer:

The return value of -1 indicates an error condition. X

```
1 public static double powerRecursive (double x, int n) {
2
3     if (n < 0 ) return -1;
4     if (n == 0) return 1;
5     return x * powerRecursive (x, n - 1);
6 }
```

#### Problem 2

Consider the following recursive method

```
1 public int recMethod ( int number ) {
2     if ( number <= 0 )
3         return 0;
4     if ( number % 2 == 0 )
5         return recMethod ( number - 1 );
6     else
7         return number + recMethod ( number - 1 );
8 }
9
```

##### Part A

How many times is this method called (including the initial call) when we run `recMethod(10)` ?

Answer: Called 11 times.

How many times is this method called (including the initial call) when we run `recMethod(-10)` ?

Answer: Called 1 time.



### Part B

What does `recMethod` do (i.e. what does it compute)?

Answer: It computes the sum of odd numbers from zero to `number`.

### Problem 3

Write a recursive method to compute the following series:

$$\frac{1}{3} + \frac{2}{5} + \frac{3}{7} + \frac{4}{9} + \dots + \frac{i}{2i+1}.$$

Answer: The crucial part in this code is casting to `double` so that the fractions do not become all zero. Other than that it should be a straight forward implementation of the recursive method.

```
1 public static double summation ( int num ) {  
2     //base case  
3     if ( num <= 0 ) return 0;  
4     //recursion  
5     return (double)num/(2*num+1) + summation(num-1);  
6 }
```

### Problem 4

Write a recursive method that computes the sum of the digits in an integer. Use the following method header:

```
public static int sumOfDigits ( long n )
```

For example, `sumOfDigits( 234 )` should return 9 (since  $2 + 3 + 4 = 9$ ) and `sumOfDigits( 390 )` should return 12 (since  $3 + 9 + 0 = 12$ ).

Answer: A possible solution could be:

```
1 public static int sumOfDigits ( long n ) {  
2     //base case is when the number is zero  
3     if( n==0 )  
4         return 0;  
5     //recursive case  
6     return ( int)( n%10 ) + sumOfDigits( n/10 );  
7 }
```

### Problem 5

For each of the following recursive methods, rewrite it using iterations instead of recursion. HINT: in order to do so you should first figure out what these methods do.

#### Part A

```
public int recur ( int n ) {  
    if ( n < 0 )  
        return -1;  
    else if ( n < 10 )  
        return 1;  
    else  
        return ( 1 + recur ( n / 10 ) );  
}
```

Answer:

The code above computes the number of digits in the parameter `n`.



```
1 public int recur (int n) {
2     int solution = 0;
3     while (n > 0 ){
4         solution++;
5         n = n/10;
6     }
7     return solution;
8 }
```

## Part B

```
public int recur2 ( int n ){
    if (n < 0 )
        return -1;
    else if ( n < 10 )
        return n;
    else
        return ( n % 10 + recur2 ( n / 10 ) );
}
```

Answer:

This method computes sum of digits in a parameter  $n$ .

```
1 public int recur2 ( int n ){
2     int sum = 0;
3     while (n > 0 ) {
4         sum += n%10;
5         n = n/10;
6     }
7     return sum; fs
8 }
```

## Problem 6

What would be printed by the following programs

### Part A)

```
1 public class CatsAndDogs {
2
3     public static void main(String[] args) {
4         foo("Cats and Dogs", 4);
5     }
6
7     public static void foo ( String s, int n ) {
8         if (n <= 1)
9             System.out.println("Cats");
10        else {
11            System.out.println( s ) ;
12            foo ( s, n-1 );
13        }
14    }
15 }
```

Answer:

Cats and Dogs  
Cats and Dogs



Cats and Dogs  
Cats

### Part B)

```
1 public class Numbers {
2
3     public static void main(String[] args) {
4         int [] list = {1, 2, 3, 4, 5};
5         System.out.println( foo (list, 0, list.length-1) );
6     }
7
8     public static int foo ( int [] nums, int begin, int end ) {
9         if ( begin == end )
10            return nums[begin];
11        else
12            return nums[begin] + foo(nums, begin+1, end);
13    }
14 }
```

Answer:

The `foo` method computes the sum of the values in the list from between index `begin` and index `end`. So in this case it computes the sum of all elements in the list. It prints 15

### Problem 7

**Part A** Write a method that generates all sequences of a given length that contain digits 0 through 9 (all ten digits are allowed, repetitions are allowed)? Given length of the sequence equal to  $n$ , how many possible sequences are there?

Answer:

With length of  $n$  digits, the number of possible sequences is equal to  $10^n$ , for example, with length of  $n = 4$ , we have 10,000 different sequences.

```
1 /**
2  * Generate all decimal sequences of the specified length.
3  * @param length the length of the sequences to be generated
4  */
5 public static void getAllDecimalSequences ( int length ) {
6     String seq = new String () ;
7     int counter = 0;
8     getAllDecimalSequences( length, seq);
9 }
10
11 /* Generate all decimal sequences of a specified length
12  * using the seq String as storage for partial sequences.
13  * @param length the length of the sequence to be generated
14  * @param seq stores partial sequences between recursive calls
15  */
16 private static void getAllDecimalSequences ( int length, String seq ) {
17     if (seq.length() == length ) { //reached the desired length
18         System.out.printf("%s %n", seq );
19     }
20     else { //add the next digit to the sequence (two possibilities)
21
22         for (int i = 0; i < 10; i++) {
23             //add digit i to the current sequence
24             getAllDecimalSequences( length, seq + Integer.toString(i));
25         }
26     }
27 }
```



**Part B** Modify the above method so that none of the generated sequences start with zero. How many of those sequences exist, given the length of  $n$  digits?

Answer:

With this restriction, we only have 9 possibilities for the first digit and 10 for all the remaining digits. So there will be total of  $9 \times 10^{n-1}$  sequences of length  $n$  that do not start with a zero.

```
1 /**
2  * Generate all decimal sequences of the specified length with added
3  * constraint that the first digit is never zero.
4  * @param length the length of the sequences to be generated
5  */
6 public static void getDecimalSequencesNoLeadingZero ( int length ) {
7     String seq = new String () ;
8     getDecimalSequencesNoLeadingZero( length, seq);
9 }
10
11 /**
12  * Generate all decimal sequences of the specified length with added
13  * constraint that the first digit is never zero. seq is used for storage
14  * of partial sequences.
15  * @param length the length of the sequences to be generated
16  * @param seq stores partial sequences between recursive calls
17  */
18 private static void getDecimalSequencesNoLeadingZero ( int length, String seq ) {
19     if (seq.length() == length ) { //reached the desired length
20         System.out.printf("%s %n", seq );
21     }
22     else if (seq.length() == 0 ) { //do not start any sequence with a zero
23         for (int i = 1; i < 10; i++) {
24             //add digit i to the current sequence
25             getAllDecimalSequences( length, seq + Integer.toString(i));
26         }
27     }
28     else {
29         for (int i = 0; i < 10; i++) {
30             //add digit i to the current sequence
31             getAllDecimalSequences( length, seq + Integer.toString(i));
32         }
33     }
34 }
```