



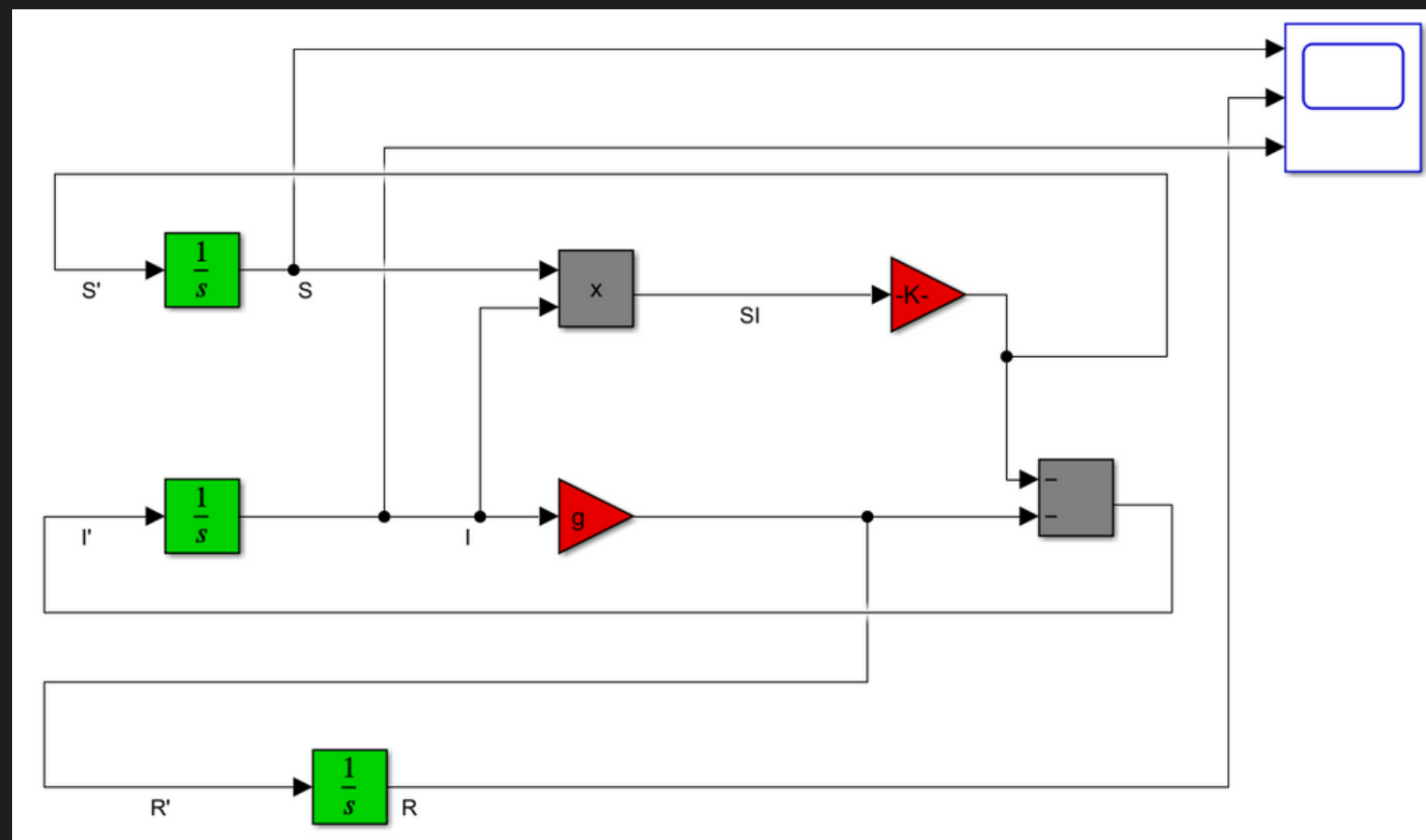
# OPT IMPLEMENTATION AND ANALYSIS OF A DYNAMICAL COVID-19 MODEL

**By**

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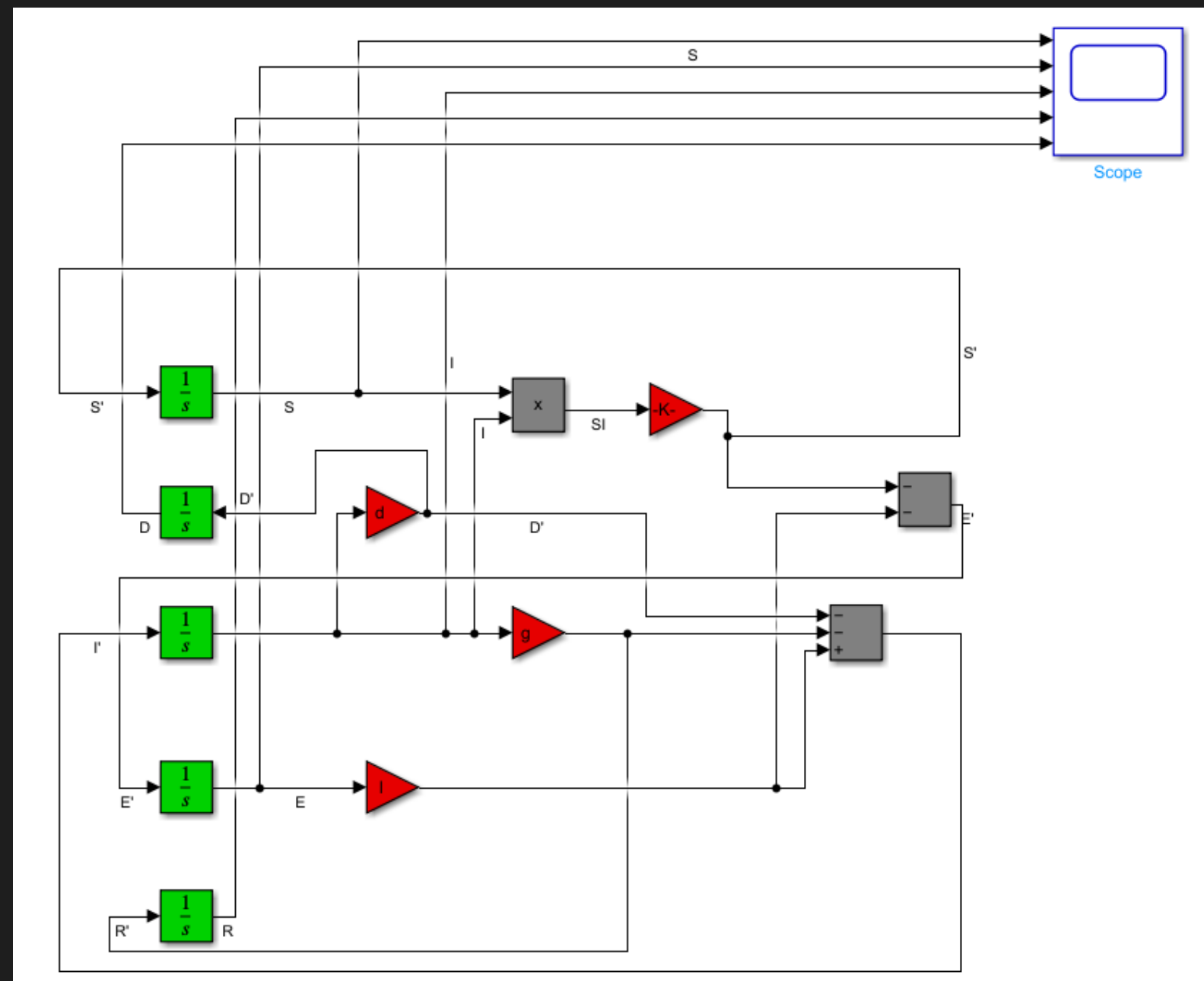
# BASIC MODEL (SIR)

$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta}{N}SI, \\ \frac{dI}{dt} &= \frac{\beta}{N}SI - \gamma I, \\ \frac{dR}{dt} &= \gamma I.\end{aligned}$$



$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta}{N}SI, \\ \frac{dE}{dt} &= \frac{\beta}{N}SI - \lambda E, \\ \frac{dI}{dt} &= \lambda E - \gamma I - \delta I, \\ \frac{dR}{dt} &= \gamma I, \\ \frac{dD}{dt} &= \delta I.\end{aligned}$$

# SEIRD MODEL

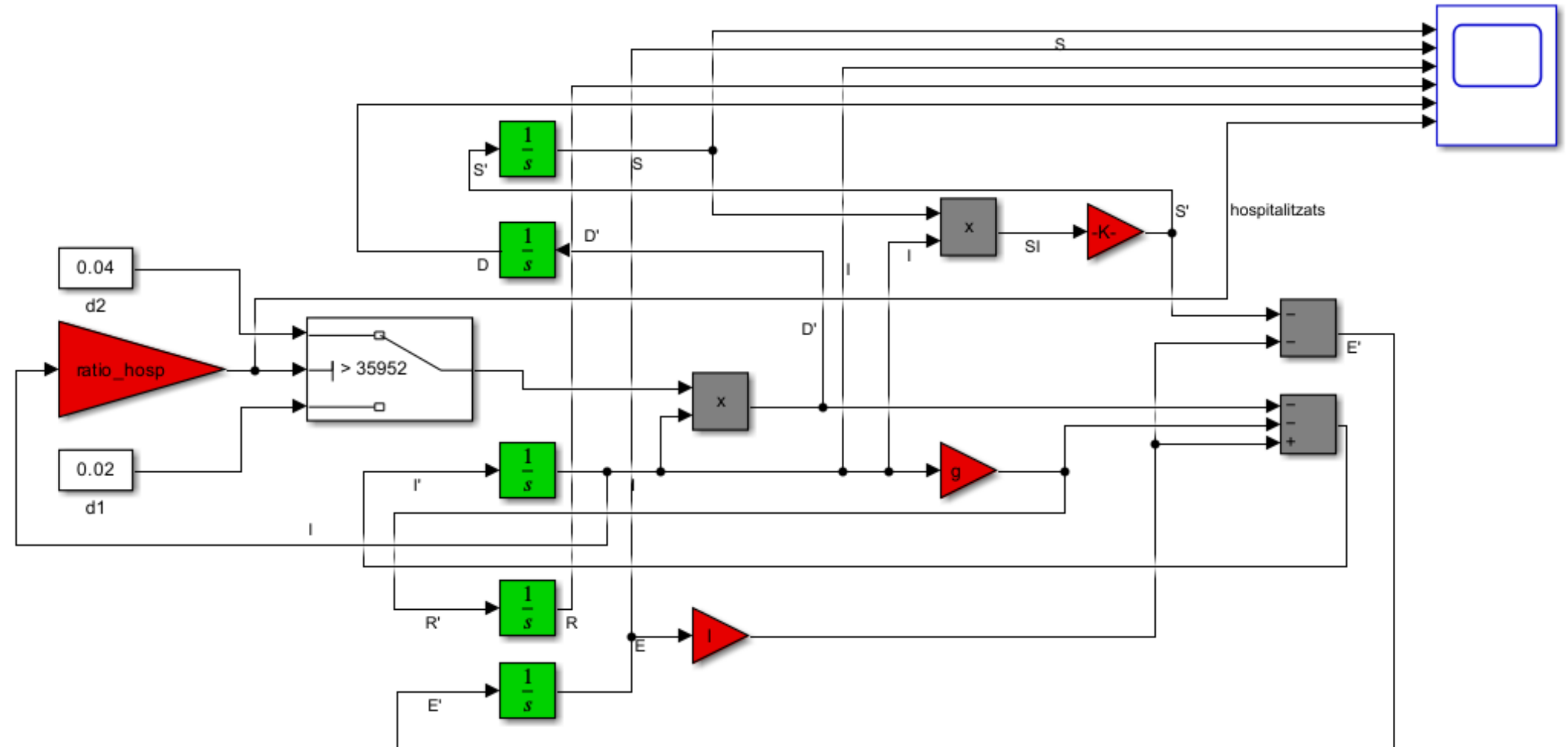


# SEIRD + UCI MODEL

$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta}{N}SI, \\ \frac{dE}{dt} &= \frac{\beta}{N}SI - \lambda E, \\ \frac{dI}{dt} &= \lambda E - \gamma I - \delta' I, \\ \frac{dR}{dt} &= \gamma I, \\ \frac{dD}{dt} &= \delta' I.\end{aligned}$$

$\delta' = \delta k.$

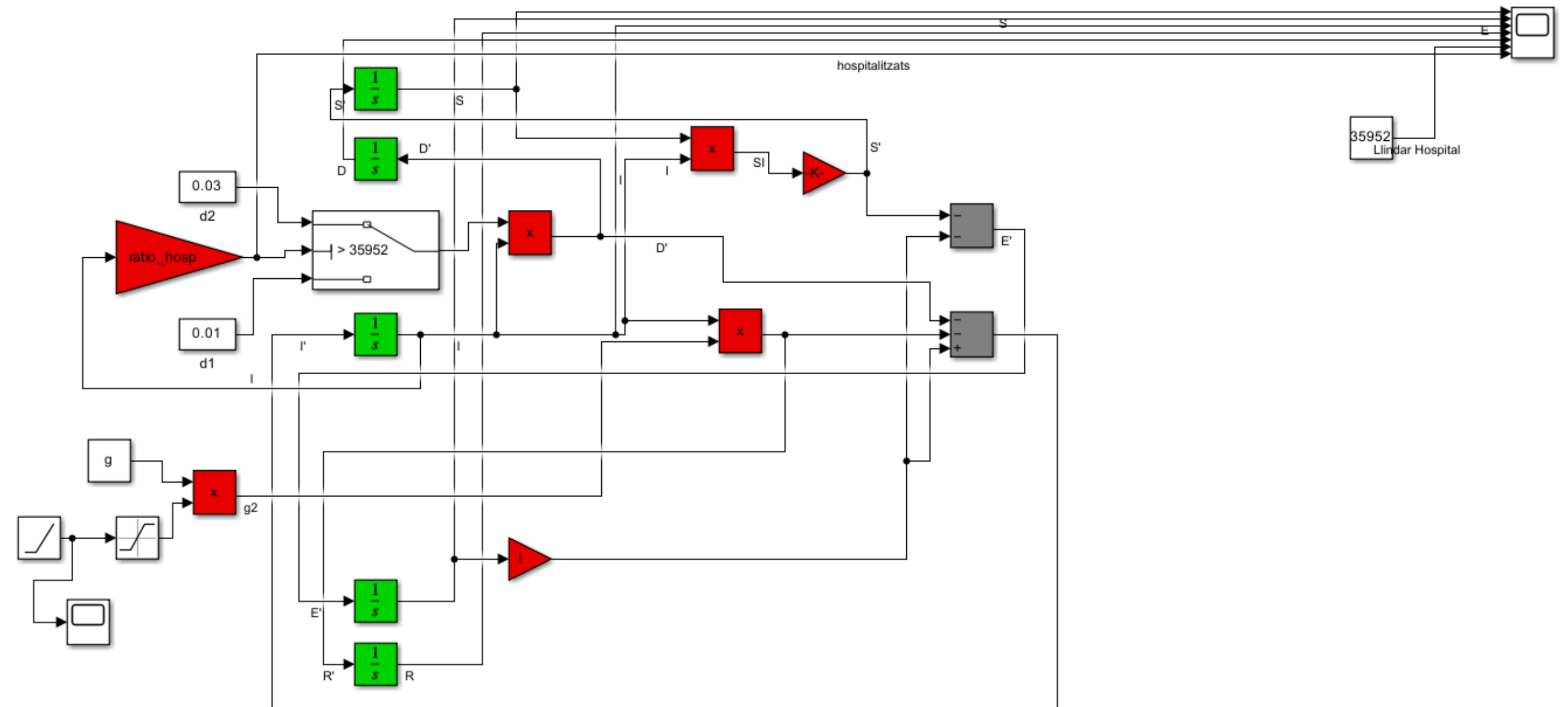
$$k = \begin{cases} 1, & \text{if } 0.05I \leq 35952 \\ 2, & \text{otherwise} \end{cases}$$



# UCI + VACCINATION MODEL

$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta}{N}SI, \\ \frac{dE}{dt} &= \frac{\beta}{N}SI - \lambda E, \\ \frac{dI}{dt} &= \lambda E - \gamma I - \delta' I, \\ \frac{dR}{dt} &= \gamma I, \\ \frac{dD}{dt} &= \delta' I. \\ \delta' &= \delta k.\end{aligned}$$

$$k = \begin{cases} 1, & \text{if } 0.05I \leq 35952 \\ 2, & \text{otherwise} \end{cases}$$

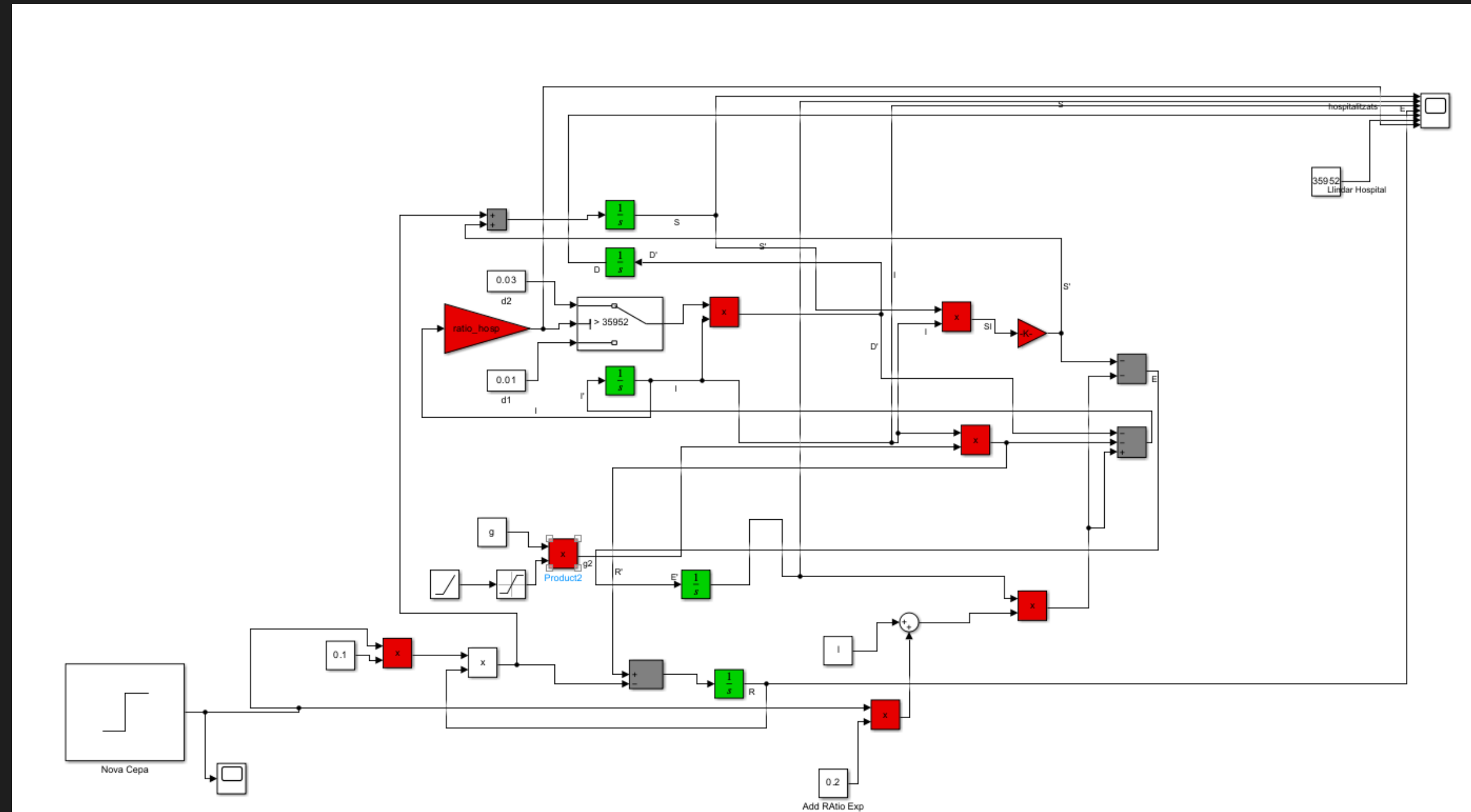


# NEW VARIANT MODEL

$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta}{N}SI, \\ \frac{dE}{dt} &= \frac{\beta}{N}SI - \lambda E, \\ \frac{dI}{dt} &= \lambda E - \gamma' I - \delta' I, \\ \frac{dR}{dt} &= \gamma' I, \\ \frac{dD}{dt} &= \delta' I. \\ \delta' &= \delta k. \\ \gamma' &= \gamma k_2.\end{aligned}$$

$$k = \begin{cases} 1, & \text{if } 0.05I \leq 35952 \\ 2, & \text{otherwise} \end{cases}$$

$$k_2 = \begin{cases} 1, & \text{if } t < 75 \\ 1 + 0.3t, & \text{if } t > 75 \text{ and } 1 + 0.3t < 5 \\ 5, & \text{otherwise} \end{cases}$$



# FINAL CONCLUSIONS

- **Complexity can grow infinitely**
  - **Covid was a complex pandemics with lots of variables taking part on it, modelling it as a whole is impossible but some approximations can be really useful**
- **Hospital capacities played a huge role on the pandemic**
- **Vaccination is the best measure**
- **Being aware of new variants is crucial**