

Interview Questions: Analysis of Algorithms (ungraded) | Coursera

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Total points 3

1.

Question 1

3-SUM in quadratic time. Design an algorithm for the 3-SUM problem that takes time proportional to n^2 in the worst case. You may assume that you can sort the n integers in time proportional to n^2 or better.

Note: these interview questions are ungraded and purely for your own enrichment. To get a hint, submit a solution.

1 / 1 point

```
public List<List<Integer>> threeSum(int[] nums) {    List<List<Integer>> triplets
= new ArrayList<>();    Arrays.sort(nums);    for(int i = 0; i < nums.length;
i++) {        for(int j = i + 1; j < nums.length; j++) {            int k =
Arrays.binarySearch(nums, (nums[i] + nums[j]) * -1);            if (k >= 0 && k != i
&& k != j){                List<Integer> triplet = new ArrayList<>(List.of(nums[i],
nums[j], nums[k]));                Collections.sort(triplet);                if
(!triplets.contains(triplet)) {                    triplets.add(triplet);                }
            }        }    }    return triplets; }
```



Correct

Hint: given an integer x and a sorted array $a[]$ of n distinct integers, design a linear-time algorithm to determine if there exists two distinct indices i and j such that $a[i] + a[j] == x$.

2.

Question 2

Search in a bitonic array. An array is *bitonic* if it is comprised of an increasing sequence of integers followed immediately by a decreasing sequence of integers. Write a program that, given a bitonic array of n distinct integer values, determines whether a given integer is in the array.

- Standard version: Use $\sim 3 \lg n$ compares in the worst case.
- Signing bonus: Use $\sim 2 \lg n$ compares in the worst case (and prove that no algorithm can guarantee to perform fewer than $\sim 2 \lg n$ compares in the worst case).

1 / 1 point

a = Find longest increasing subsequence
 x = Find longest decreasing subsequence
 ans = number of elements in vector - ($a + x - 1$)
 $a + x - 1$ = gives maximum length of bitonic array we want to find minimum number of removals, so we can subtract maximum length from the size of the vector to get the number of removals.



Correct

Hints: Standard version. First, find the maximum integer using $\sim 1 \lg n$ compares—this divides the array into the increasing and decreasing pieces.

Signing bonus. Do it without finding the maximum integer.

3.

Question 3

Egg drop. Suppose that you have an n -story building (with floors 1 through n) and plenty of eggs. An egg breaks if it is dropped from floor T or higher and does not break otherwise. Your goal is to devise a strategy to determine the value of T given the following limitations on the number of eggs and tosses:

- Version 0: 1 egg, $\leq T \leq T$ tosses.
- Version 1: $\sim 1 \lg n$ eggs and $\sim 1 \lg n$ tosses.
- Version 2: $\sim \lg T$ eggs and $\sim 2 \lg T$ tosses.
- Version 3: 2 eggs and $\sim 2 \sqrt{n}$

tosses.

- Version 4: 222 eggs and $\leq cT$ eggs and $\leq cT$ eggs

tosses for some fixed constant c .

1 / 1 point

One for each floor



Correct

Hints:

- Version 0: sequential search.
- Version 1: binary search.
- Version 2: find an interval containing TTT of size $\leq 2T$ le $2T \leq 2T$, then do binary search.
- Version 3: find an interval of size \sqrt{n}

, then do sequential search. Note: can be improved to $\sim 2n \sin \sqrt{2n} \sim 2n$

tosses.

- Version 4: $1+2+3+\dots+t \sim 12t^{21} + 2 + 3 + \text{ldots} + t$; $\text{sim} ; \text{frac}\{1\}\{2\}$
 $t^{21+2+3+\dots+t-21}t^2$. Aim for $c=22$
 $c = 2 \sqrt{2} c = 22$

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