



# Optimising Load Flexibility for the Day Ahead in Distribution Networks with Photovoltaics

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- In recent years a massive integration of renewable-based DERs (Distributed Energy Resources) has been taken place in Low Voltage (LV) distribution systems
- This is positive since DERs can contribute to the reduction of Greenhouse emissions and the increase of renewable energy consumption
- However, DER can lead to contingencies (such as over-voltages, overloadings, etc.) if the hosting capacity of the circuits they are connected to is exceeded
- In this context, Demand Flexibility, becomes a well suited solution to efficiently integrate those DERs avoiding those technical problems.







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- A methodology to calculate load flexibility schedule for the next 24 hours
- Objective: minimise the flexibility quantity used to alleviate the contingencies

- Unbalance operation of LV distribution system
- Presence of Photovoltaics (PV) panels as DER technology
- Customers participating in a Demand Response (DR) program
- Forecast of the demand, PV generation and weather conditions







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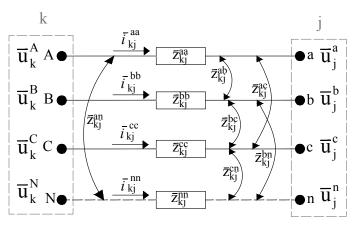






# System Modelling

 $\bullet$  Unbalance operation of the LV systems  $\Rightarrow$  three phase modelling









# Power flow modelling

• Minimise mismatch between power injections specified and calculated for each node and phase.

$$F(\mathcal{X}) = 0 = \begin{bmatrix} F_p(\mathcal{X}) \\ F_q(\mathcal{X}) \end{bmatrix} = \begin{bmatrix} p_{i,k}^{p,sp} + p_{i,k}^{p,cal} \\ q_{i,k}^{p,sp} + q_{i,k}^{q,cal} \end{bmatrix}$$

Decomposition in real and imaginary part of the electrica magnitudes

$$\mathcal{X} = \begin{bmatrix} \begin{bmatrix} u_1^{a,re} u_1^{b,re} u_1^{c,re} \dots u_N^{a,re} u_N^{b,re} u_N^{c,re} \end{bmatrix}^T \\ \begin{bmatrix} u_1^{a,im} u_1^{b,re} u_1^{c,im} \dots u_N^{a,im} u_N^{b,im} u_N^{c,im} \end{bmatrix}^T \end{bmatrix}$$





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Case study

# PV Modelling

• PV panels model which depends on the temperature  $T_{cell,t}$ and the solar irradiation  $\hat{G}_t$ .

$$p_{g,k,t}^{p,sp} = \frac{P_{PV_k}}{S_B} \left( \frac{\hat{G}_t}{1000} \left[ 1 + \gamma \left( T_{cell,t} + 25 \right) \right] \right)$$

Forecast of the weather conditions ⇒ ARIMA model

$$\hat{y}_{t+\tau} = \delta + \sum_{i=1}^{p_a + d_a} \phi_i y_{t+\tau-i} + \varepsilon_{t+\tau} - \sum_{i=1}^{q_a} \theta_i \varepsilon_{t+\tau-i}$$







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# Load Modelling

• To account for the voltage dependency of the demand, is considered a load ZIP model, tuning with smart meters data.

$$p_{d,k,t}^{p,sp} = \hat{p}_{d,k,t}^{p} \left[ c_{p,k}^{p,1} \left( u_{k,t}^{p} \right)^{2} + c_{p,k}^{p,2} \left( u_{k,t}^{p} \right) + c_{p,k}^{p,3} \right]$$

$$q_{d,k,t}^{p,sp} = \hat{q}_{d,k,t}^{p} \left[ c_{q,k}^{p,1} \left( u_{k,t}^{p} \right)^{2} + c_{q,k}^{p,2} \left( u_{k,t}^{p} \right) + c_{q,k}^{p,3} \right]$$







# Load Flexibility

 Load shifting mechanism is considered for managing the flexibility of the load demand of the customers participating in the DR program.

$$p_{i,k,t}^{p,sp} = p_{g,k,t}^{p,sp} - \left(p_{d,k,t}^{p} + \Delta p_{d,k,t}^{p}\right), \forall k \in \tilde{\Omega}_{c}$$

$$p_{d,k,t}^{p} + \Delta p_{d,k,t}^{p} \geqslant \beta_{k} \cdot p_{ctd,k}$$
$$\sum_{t \in \{t_{0},...,t_{n}\}} \Delta p_{d,k,t}^{p} = 0$$

$$-\alpha_k \cdot p_{ctd,k} \leq \Delta p_{d,k,t}^p \leq \alpha_k \cdot p_{ctd,k}$$







# Load Flexibility

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$$\begin{split} p_{i,k,t}^{p,sp} &= p_{g,k,t}^{p,sp} - \left( p_{d,k,t}^{p} + \Delta p_{d,k,t}^{p} \right), \forall k \in \tilde{\Omega}_{c} \\ \\ p_{d,k,t}^{p} &+ \Delta p_{d,k,t}^{p} \geqslant \beta_{k} \cdot p_{ctd,k} \\ \\ \sum_{t \in \{t_{0}, \dots, t_{n}\}} \Delta p_{d,k,t}^{p} = 0 \\ \\ -\alpha_{k} \cdot p_{ctd,k} \leqslant \Delta p_{d,k,t}^{p} \leqslant \alpha_{k} \cdot p_{ctd,k} \end{split}$$







Load demand flexibility methodology is formulated as an unbalance optimal power flow (OPF) which results in a non-linear programming problem (NLP)

Minimise:

$$OF = \sum_{t \in T} \sum_{p \in \{a,b,c\}} \sum_{k \in \tilde{\Omega}_c} \left( \Delta p_{d,k,t}^p \right)^2$$

Subject to:

$$(i_{kj,t}^{p,re})^2 + (i_{kj,t}^{p,im})^2 \leqslant (i_{kj}^{max,p})^2$$
 
$$(u^{min})^2 \leqslant (u_{k,t}^{p,re})^2 + (u_{k,t}^{p,im})^2 \leqslant (u^{max})^2$$

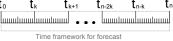






## Rolling optimisation

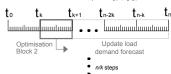




Stage 1: Optimisation process
Optimisation Block 1: Load demand shift for period  $t_0 \rightarrow t_k$ Update load demand short-term forecast for period  $t_k \rightarrow t_k$ 



Optimisation Block 2: Load demand shift for period  $t_{k-}$   $t_{k+1}$  Update load demand short-term forecast for period  $t_{k+1}$   $t_n$ 



Optimisation Block n/k: Load demand shift for period  $t_{n-k} \rightarrow t_k$ 









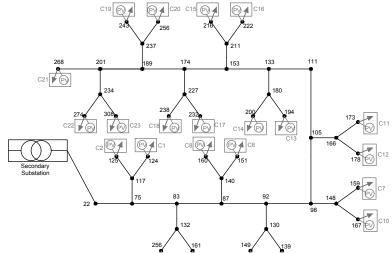
- Real medium-size LV distribution system (LVNS project)
- 23 single-phase residential customers
  - $P_{ctd} = \{3, 15\} \ kW$
- 23 PV facilities
  - $\bullet$   $P_{PV} = 4 kW$
- Load flexibility control parameters:
  - $\beta_k \in (0.05, 0.1)$
  - $\alpha_k \in (0.1, 0.5)$







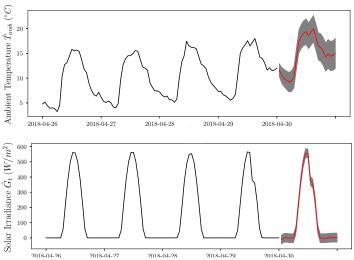
# Case Study







# Case study: forecast weather conditions

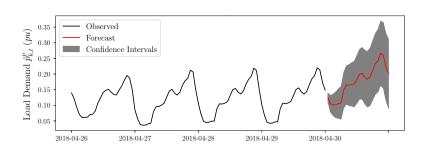








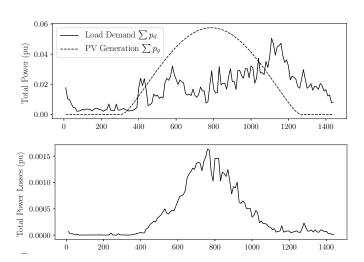
# Case study: forecast demand







# Case study: Demand, PV generation and losses

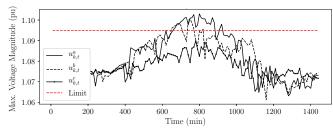


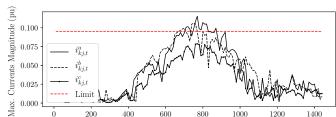






# Case study: Over-voltages, Over-currents



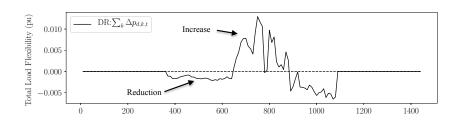








# Flexibility Results: Load flexibility

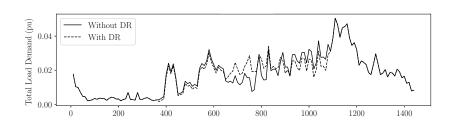








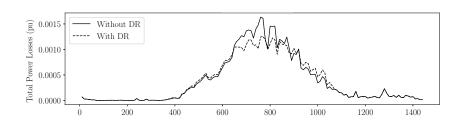
# Flexibility Results: Change in demand







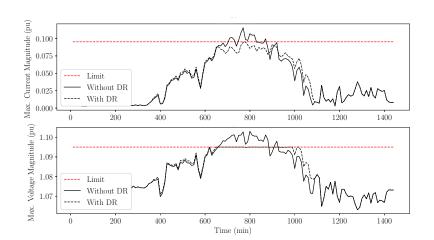
# Flexibility Results: Losses







# Flexibility Results: Maximum voltage and current









- A simple and efficient optimisation methodology was presented to obtain the load flexibility schedule in LV systems with high PV penetration
- The problem is solved in a rolling optimisation fashion, updating the forecast after completing each optimisation block
- load shift is used as flexibility enabler
- Simulation results show the capability of the load shift mechanism to reduce the over-voltages and over-loading's of the system and even a reduction of the power losses has been achieved
- Future work:
  - Include other DERs: Flectric Vehicles Energy Storage etc.
  - Include temperature dependant component of demand







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# Thank you very much for your attention Q?

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