

Universidade Federal de Campina Grande - UFCG
Unidade Acadêmica de Matemática - UAMat

Disciplina: *Cálculo II*

Professor: *Jefferson Abrantes*

Lista de Exercícios para a Segunda Avaliação

1. Quais séries convergem? E quais divergem?

a) $\sum_{n=2}^{\infty} \left(\frac{1}{n (\ln n)^2} \right)$

b) $\sum_{n=1}^{\infty} \left(\frac{1}{n^2 - 1} \right)$

c) $\sum_{n=1}^{\infty} \left(\frac{-2}{n\sqrt{n}} \right)^n$

d) $\sum_{n=0}^{\infty} (e^{-n})$

e) $\sum_{n=1}^{\infty} \left(\frac{8 \arctan n}{n^2 + 1} \right)$

f) $\sum_{n=1}^{\infty} \left(\frac{n}{n^2 + 1} \right)$

g) $\sum_{n=1}^{\infty} \left(\frac{n - 2}{n^3 - n^2 + 3} \right)$

i) $\sum_{n=1}^{\infty} \left(\frac{2^n}{3 + 4^n} \right)$

j) $\sum_{n=1}^{\infty} \left(\frac{\sqrt{n} + 1}{\sqrt{n^2 + 3}} \right)$

k) $\sum_{n=1}^{\infty} \left(\ln \left(1 + \frac{1}{n^2} \right) \right)$

l) $\sum_{n=1}^{\infty} \left(\frac{(\ln n)^3}{n^4} \right)$

$$\text{m)} \sum_{n=1}^{\infty} \left(\frac{2^n}{n!} \right)$$

$$\text{n)} \sum_{n=1}^{\infty} \left(\frac{2^n}{n3^{n-1}} \right)$$

$$\text{o)} \sum_{n=2}^{\infty} \left(\frac{3^{n+2}}{\ln n} \right)$$

$$\text{p)} \sum_{n=1}^{\infty} \left(\frac{n}{n^2 + 1} \right)$$

$$\text{q)} \sum_{n=1}^{\infty} \left(1 - \frac{1}{n} \right)^{n^2}$$

$$\text{r)} \sum_{n=1}^{\infty} \left(\sin \left(\frac{1}{\sqrt{n}} \right) \right)^n$$

$$\text{s)} \sum_{n=1}^{\infty} (e^{-n} n^3)$$

$$\text{t)} \sum_{n=1}^{\infty} \left(\frac{(n!)^n}{(n^n)^2} \right)$$

2. **(Questão desafio)** Use o teste da integral para mostrar que a série

$$\sum_{n=0}^{\infty} (e^{-n^2})$$

converge.

Bons Estudos!