GRAPH

PERMUTATION

```
#include <bits/stdc++.h>
int main () {
  int perm [5], n = 5;
  for (int i = 0; i < n; i++)
    perm [i] = i;
  for (int i = 0; i < (1 << n); i++) {
    //printf ("i: %d\n", i);
    for (int j = 0; j < n; j++) {
    //printf ("i: %d, (1 << %d): %d -- ", i, j, (1 << j));
      if (i & (1 << j))
  printf ("%d", perm [j]);</pre>
      //puts ("");
   puts ("");
  return 0;
QUEEN
#include <bits/stdc++.h>
const int MAXN = 8; // board size
// X == column | Y == row
// row [X] stores which row the queen is placed in the column X
int row [MAXN], lc, x, y;
bool check (int r, int c) {
  // for until column == check placed queens
  for (int i = 0; i < c; i++) {
    // if no two queens are in the same row
    // && no two queens share the same diagonal
    if (row [i] == r || (abs (c - i)) == (abs (r - row [i])))
      return false;
  return true;
void backtrack (int column = 0) {
  if (column == MAXN && row [x] == y) {
    // all the queens are place == possible solution
    printf ("%2d
                  ", lc++);
    for (int i = 0; i < MAXN; i++) {
      if (i + 1 < MAXN)
        printf ("%d ", row [i] + 1);
      else
        printf ("%d\n", row [i] + 1);
  // which row from the column X the queen will be place
  for (int i = 0; i < MAXN; i++) {
   if (check (i, column)) {
      row [column] = i;
      // advance a column and calls the recursion
      backtrack (column + 1);
    }
  }
```

```
}
int main () {
  int n; scanf ("%d", &n);
  while (n--) {
    scanf ("%d%d", &x, &y);
    std::swap (x, y);
    x--; y--;
    memset (row, 0, sizeof (row));
                  COLUMN");
1 2 3 4 5 6 7 8\n");
    puts ("SOLN
    puts (" #
    1c = 1;
    backtrack ();
    if (n)
     puts ("");
  return 0;
BELLMAN-FORD
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::pair <int, int> pi;
typedef std::vector <pi> vpi;
typedef std::vector <vpi> vvpi;
const int MAXN = 1e2 + 1;
int n, m;
vvpi g;
int dst [MAXN], INF = 0x3f3f3f3f;
void bl (int s) {
      dst [s] = 0;
      for (int i = 0; i < n - 1; i++)
            for (int j = 0; j < n; j++)
                  for (pi v : g [j])
                        dst [v.first] = std::min (dst [v.first], dst [j] +
v.second);
}
void input () {
      scanf ("%d%d", &n, &m);
      g.resize (n);
      memset (dst, 0x3f, sizeof dst);
      for (int i = 0; i < m; i++) {
            int a, b, c; scanf ("%d%d%d", &a, &b, &c);
            g [a].push_back ({b, c});
      }
      solve ();
void solve () {
```

```
bl (0);
      for (int i = 0; i < n; i++)
            printf ("%d ", dst [i]);
      puts ("");
}
int main () {
      input ();
      return 0;
BFS
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
typedef std::queue <int> qi;
const int MAXN = 1e3;
int n;
vvi g;
int visited [MAXN];
void bfs (int x) {
      printf ("x: %d", x);
      qi q;
      q.push(x);
      //memset (visited, -1, sizeof visited);
      visited [x] = 1;
      while (!q.empty ()) {
             int nd = q.front (); q.pop ();
for (int v : g [nd]) {
                   if (!visited [v]) {
                          visited [v] = visited [nd] + 1;
                          q.push (v);
             }
      }
void input () {
      scanf ("%d", &n);
      g.resize (n + 1);
      for (int i = 0; i <= n; i++) {
             int a, b; scanf ("%d", &a);
             for (int j = 0; j < a; j++) {
    scanf ("%d", &b);</pre>
                   g [i].push_back (b);
             }
      }
}
void solve () {
      for (int i = 0; i < g.size (); i++) {
             for (int j = 0; j < g [i].size (); <math>j++)
                   printf ("%d ", g [i][j]);
             puts ("");
      bfs (5);
      for (int i = 0; i < g.size (); i++) {
             printf ("i: %d => ", i);
```

```
for (int j = 0; j < g.size (); j++)
    if (visited [j] == i)</pre>
                          printf ("%d ", j);
             puts ("");
      }
}
int main () {
      input ();
solve ();
      return 0;
}
BIPARTIDE CHECK
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
const int MAXN = 2e2 + 1;
int n, m;
vvi g;
int visited [MAXN];
bool bfs (int s) {
      int ans = 1;
      std::queue <int> q; q.push (s);
      visited [s] = 0;
      while (!q.empty () && ans) {
             int x = q.front(); q.pop();
             for (int v : g [x]) {
                   if (visited [v] == -1) {
                          visited [v] = 1 - visited [x];
                          q.push (v);
                   else if (visited [v] == visited [x])
                          ans = 0;
      return ans;
bool dfs (int x, int f) {
      visited [x] = 1 - visited [f];
      int ans = 1;
      for (int v : g [x]) {
             if (visited [v] == -1)
                   dfs(v, x);
             else if (visited [v] == visited [x])
                   return false;
      return true;
}
void input () {
      while (scanf ("%d", &n) && n != 0) {
             scanf ("%d", &m);
             g.clear ();
             g.resize (n);
             memset (visited, -1, sizeof visited); for (int i = 0; i < m; i++) {
                   int a, b; scanf ("%d%d", &a, &b);
```

```
g [a].push_back (b);
                   g [b].push_back (a);
            solve ();
      }
}
void solve () {
      if (!dfs (0, 0))
            puts ("NOT BICOLORABLE.");
      else
            puts ("BICOLORABLE.");
int main () {
      input ();
      return 0;
BIPARTIDE KUHN
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::pair <int, int> pi;
typedef std::vector <pi> vpi;
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
int n, m;
int match [251], vis [251];
vvi g;
vpi ans;
bool dfs (int x) {
      if (vis [x])
            return 0;
      vis [x] = 1;
      for (auto v : g [x]) {
             if (match [v] == -1 || dfs (match [v])) {
                   match [v] = x;
                   return 1;
             }
      return 0;
}
void input () {
      scanf ("%d%d", &n, &m);
      g.resize (n);
      memset (match, -1, sizeof match); for (int i = 0; i < n; i++) {
            while (1) {
                   int a; scanf ("%d", &a);
                   if (a)
                         g [i].push_back (a - 1);
                   else
                         break;
             }
      solve ();
}
```

```
void solve () {
      for (int i = 0; i < n; i++) {
            memset (vis, 0, sizeof vis);
            dfs (i);
      for (int i = 0; i < m; i++)
            if (match [i] != -1)
                  ans.push_back ({match [i], i});
      printf ("%d\n", (int) ans.size ());
      for (int i = 0; i < ans.size (); i++)
            printf ("%d %d\n", ans [i].first + 1, ans [i].second + 1);
}
int main () {
      input ();
      return 0;
BRIDGE ARTICULATION CHECK
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
const int MAXN = 1e2 + 1;
int n, m, rch, root;
vvi g;
vi stk;
int num [MAXN], low [MAXN], visited [MAXN];
// if num [x] \le low [v] it means that V cannot reach a vertex
// with num [w] <= num [x] so by removing vertex V the graph become
// disconect because V cannot reach X, so X is an articulation point.
//
// if num [x] < low [v] it means that edge \{X, V\} is a bridge becouse
// when that edge \{X,\ V\} is removed an ancestor os X is still reachable // by V.
int dfs (int x, int f) {
      num [x] = ++rch;
      low [x] = num [x];
      for (int v : q [x]) {
            if (!num [v])
                  low [x] = std::min (dfs (v, x), low [x]);
            if (v != f) {
                  low [x] = std::min (low [v], low [x]);
                  low [f] = std::min (low [x], low [f]);
            // if can be chanced so that never prints more than one time
            // the same articulation vertex
            if (num [x] \le low [v]) {
                  if (x != root)
                        printf ("%d is an articulation vertex.\n", x);
                  if (num [x] != low [v])
                        printf ("{%d, %d} is a bridge.\n", x, v);
      return num [x];
}
```

```
int dfsSCC (int x, int f) {
      num [x] = ++rch;
      low [x] = num [x];
      visited [x] = 1;
      stk.push_back (x);
      for (int v : g [x]) {
            if (!visited [v])
                  dfs(v, x);
            if (visited [v])
                  low [x] = std::min (low [v], low [x]);
      if (low [x] == num [x]) {
            nmb++;
            while (true) {
                  int t = stk.back();
                  stk.pop_back ();
                  visited [t] = 0;
                  if (x == t)
                        break;
      }
      return num [x];
void cp3_dfs (int u, int f) {
      low [u] = num [u] = ++rch;
      for (int v : q [u]) {
            if (!num [v]) {
                  dfs (v, u);
                  if (num [u] \le low [v]) {
                        if (u != root)
                              printf ("%d is an articulation vertex.\n", u);
                        if (num [u] != low [v])
                              printf ("\{%d, %d\} is a bridge.\n", u, v);
                  low [u] = std::min (low [u], low [v]);
            else if (v != f)
                  low [u] = std::min (low [u], num [v]);
      }
void input () {
      scanf ("%d%d", &n, &m);
      g.clear ();
      g.resize (n);
      for (int i = 0; i < m; i++) {
            int a, b; scanf ("%d%d", &a, &b);
            g [a].push_back (b);
            g [b].push_back (a);
      solve ();
void solve () {
      cp3_dfs (root, root);
      for (int i = 0; i < n; i++)
            printf ("%d = {%d, %d}\n", i, num [i] - 1, low [i] - 1);
}
int main () {
```

```
input ();
      return 0;
EDMOND KARP
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::pair <int, int> pi;
typedef std::vector <pi> vpi;
typedef std::vector <vpi> vvpi;
typedef std::vector <int> vi;
const int MAXN = 1e3, INF = 0x3f3f3f3f3f;
int n, m, f, s, t;
vvpi g;
int res [MAXN][MAXN];
vi bst;
void augmented_path (int v, int min) {
      if (v == s) f = min;
      else if (bst [v] != -1) {
            // augmented_path (father of V, (min_edge (maximum flow) between the
current MIN and the edge {bst [v] -> v}));
            augmented_path (bst [v], std::min (min, res [bst [v]][v]));
            // F is a global variable which stores the min_edge (maximum_flow) on
the
            // bsf spanning tree
            res [bst [v]][v] -= f;
            res [v][bst [v]] += f;
      }
void ek () {
      int ans = 0;
      while (1) {
            f = 0;
            vi dst (n, INF); dst [s] = 0;
            std::queue <int> q;
            q.push (s);
            bst.assign (n, -1);
            // run bfs
            // bst [X] stores the father of {\tt X}
            // on the bfs spanning tree
            while (!q.empty ()) {
                  int u = q.front(); q.pop();
                  if (u == t) break;
                  for (int v = 0; v < n; v++) {
                        // if there is unused capacity and // v was not visited yet
                        if (res [u][v] > 0 && dst [v] == INF) {
                               dst [v] = dst [u] + 1;
                               q.push (v);
                               bst [v] = u;
                         }
            // find a augmented path if exists
            augmented_path (t, INF);
            if (f == 0) break;
            ans += f;
```

```
printf ("ans: %d\n", ans);
void input () {
      scanf ("%d%d", &n, &m);
      scanf ("%d%d", &s, &t);
      g.clear ();
      g.resize (n);
      for (int i = 0; i < m; i++) {
             int a, b, c; scanf ("%d%d%d", &a, &b, &c);
             g [a].push_back ({b, c});
             res [a][b] = c;
      solve ();
void solve () {
      ek ();
int main () {
      input ();
      return 0;
DIJKSTRA
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::pair <int, int> pi;
typedef std::vector <int> vi;
typedef std::vector <pi> vpi;
typedef std::vector <vpi> vvpi;
const int MAXN = 1e3, INF = 0x3f3f3f3f3f;
int n, m;
vi dst;
vvpi g;
std::priority_queue <pi> pq;
void bfs (int x) {
      pq.push ({0, x});
      dst[x] = 0;
      while (!pq.empty ()) {
    pi top = pq.top (); pq.pop ();
printf ("{%d, %d}\n", top.first, top.second);
             if (top.first > dst [top.second]) continue;
             for (pi i : g [top.second]) {
                    if (dst [top.second] + i.first < dst [i.second]) {
          dst [i.second] = dst [top.second] + i.first;</pre>
                           pq.push ({dst [i.second], i.second});
                    }
             }
      }
void input () {
      scanf ("%d%d", &n, &m);
      g.resize (n);
      dst.assign (n, INF);
```

```
for (int i = 0; i < m; i++) {
            int a, b, c; scanf ("%d%d%d", &a, &b, &c);
            g[a].push_back ({c, b});
            g[b].push_back ({c, a});
      solve ();
void solve () {
  puts ("calling dijkstra");
      bfs (0);
      for (int i = 0; i < dst.size (); i++)
            printf ("0 -> %d = %d\n", i, dst [i]);
}
int main () {
      input ();
      return 0;
}
FLOYD WARSHALL
#include <bits/stdc++.h>
void input ();
void solve ();
const int MAXN = 1e3, INF = 0x3f3f3f3f3f;
typedef std::pair <int, int> pi;
typedef std::vector <pi> vpi;
typedef std::vector <vpi> vvpi;
int n, m;
vvpi q;
int arr [MAXN] [MAXN], p [MAXN] [MAXN];
void fw () {
      for (int k = 0; k < n; k++)
            for (int i = 0; i < n; i++)
                   for (int j = 0; j < n; j++) {
                         printf ("{%d, %d} => {%d, %d} {%d, %d}\n", i, j, i, k, k,
j);
                         if (arr [i][j] > arr [i][k] + arr [k][j]) {
                               printf ("\{ d, d \} = \{ d, d \} = d n", i, j, k, j, p
[k][j]);
                               arr [i][j] = std::min (arr [i][j], arr [i][k] + arr
[k][j]);
                               p[i][j] = p[k][j];
                         }
                   }
}
void path (int i, int j) {
      if (i != j)
            path (i, p [i][j]);
      printf ("%d ", j);
void input () {
      scanf ("%d%d", &n, &m);
      g.resize (n);
      memset (arr, 0x3f, sizeof arr);
for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++)
```

```
p[i][j] = i;
             arr [i][i] = 0;
      for (int i = 0; i < m; i++) {
             int a, b, c; scanf ("%d%d%d", &a, &b, &c);
             g [a].push_back ({b, c});
             arr [a][b] = c;
      solve ();
}
void solve () {
      fw ();
      for (int i = 0; i < n; i++) {
             for (int j = 0; j < n; j++)
                    printf ("%d ", arr [i][j]);
             puts ("");
      puts ("shortest path");
      path (3, 4);
      puts ("");
int main () {
      input ();
      return 0;
EDGE PROPERTIE CHECK
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
const int MAXN = 2e2 + 1, explored = 2;
int n, m;
vvi g;
int visited [MAXN];
void dfs (int x, int f) {
      visited [x] = explored;
      for (int v : g [x]) {
             if (!visited [v]) {
                    printf ("Tree-edge: \{%d, %d\} \setminus n", x, v);
                    dfs(v, x);
             else if (visited [v] == explored && v != x)
                    printf ("Back-edge: \{%d, %d\}\n", x, v);
             else
                    printf ("Forward/cross: {%d, %d}\n", x, v);
      visited [x] = 1;
}
void input () {
      scanf ("%d%d", &n, &m);
      g.clear ();
      g.resize (n);
      g.lesize (ii),
memset (visited, 0, sizeof visited);
for (int i = 0; i < m; i++) {
    int a, b; scanf ("%d%d", &a, &b);</pre>
             g [a].push_back (b);
```

```
g [b].push_back (a);
      solve ();
void solve () {
      dfs(0, 0);
int main () {
      input ();
      return 0;
MAXFLOW DINIC
#include <bits/stdc++.h>
struct flow_edge {
      int v, u_i // flow from 'v' to 'u'
      long long cap, flow = 0; // cap is the max flow in this edge
      flow_edge (int v, int u, long long cap) : v (v), u (u), cap (cap) {}
};
void input ();
void solve ();
typedef long long 11;
typedef std::pair <int, int> pi;
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
typedef std::vector <pi> vpi;
typedef std::vector <vpi> vvpi;
typedef std::vector <flow_edge> vf;
typedef std::queue <int> qi;
const long long flow_inf = 0x3f3f3f3f3f3f3f3f3f3f;
int n, pos;
int s, t;
vf edges;
vvi adj;
vi level, ptr;
qi q;
// init
void dinic (int n1, int s1, int t1) {
      n = n1; s = s1; t = t1;
      adj.clear ();
      level.clear ();
      ptr.clear ();
      adj.resize (n);
      level.resize (n);
      ptr.resize (n);
// add an edge to the residual graph
void add_edge (int v, int u, long long cap) {
      // add an edge V -> U with CAP
      // add an back-edge U -> V with 0
      edges.push_back (flow_edge (v, u, cap));
      edges.push_back (flow_edge (u, v, 0));
      // undirected graph which represents
      // the residual graph without any capacity
      adj [v].push_back (pos);
      adj [u].push_back (pos + 1);
      pos += 2;
```

```
}
bool bfs () {
      while (!q.empty ()) {
            int v = q.front();
            q.pop ();
            for (int id : adj [v]) {
                   // if there is no capacity left and
                   // the vertex is already visited just continue
                   if (edges [id].cap - edges [id].flow < 1)</pre>
                         continue;
                   if (level [edges [id].u] !=-1)
                         continue;
                   // normal bfs
                   level [edges [id].u] = level [v] + 1;
                   q.push (edges [id].u);
      // return true if the sink T is reached
      return level [t] !=-1;
}
long long dfs (int v, long long pushed) {
      if (pushed == 0)
            return 0;
      if (v == t)
            return pushed;
      // for all neightbors of v
      for (int &cid = ptr [v]; cid < (int)adj [v].size (); cid++) {
            // ID is the id of edge which connects V -> U
            int id = adj [v][cid];
            // u is the back-edge of V -> U
            int u = edges [id].u;
            // if V -> U isnt on the bfs spanning tree
            // or it doesnt have capacity left just continue
if (level [v] + 1 != level [u] || edges [id].cap - edges [id].flow < 1)</pre>
                   continue;
            // find the min_edge capacity on the bfs spanning tree using dfs
            long long tr = dfs (u, std::min (pushed, edges [id].cap - edges
[id].flow));
            // if there isnt flow left, continue
            if (tr == 0)
                   continue;
            // else update the flow residual graph
            edges [id].flow += tr;
            edges [id ^ 1].flow -= tr;
            // return TR
            return tr;
      // return 0 if there isnt capacity left
      return 0;
}
long long flow () {
      long long f = 0;
      while (true) {
            // all level are -1
            std::fill (level.begin (), level.end (), -1);
            // source level is 0
            level [s] = 0;
            q.push (s);
            if (!bfs ())
                   break;
            // all ptr are 0
            std::fill (ptr.begin (), ptr.end (), 0);
```

```
// pushed will be the min-edge or max-flow in the
            // bfs spanning tree, which was found by the dfs
            while (long long pushed = dfs (s, flow_inf)) {
                  f += pushed;
      return f;
void input () {
void solve () {
int main () {
      // necessary to add the (S)ource and the (T)sink using add_edge ();
      return 0;
MST KRUSKAL
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::pair <int, int> pi;
typedef std::pair <int, pi> pipi;
typedef std::vector <int> vi;
typedef std::vector <pipi> vpi;
const int MAXN = 1e2 + 1;
vpi edges;
vi p, rank, size;
int n, m;
int visited [MAXN];
std::priority_queue <pi> pq;
int find (int i) {
      return (p [i] == i) ? i : p [i] = find (p [i]); // path compression
int same (int i, int j) {
    return find (i) == find (j);
int add (int i, int j) {
      if (!same (i, j)) {
            int x = find (i);
            int y = find (j);
            if (rank [x] > rank [y]) {
                  p [y] = x;
                   size [x] += size [y];
            else {
                  p[x] = y;
                  size [y] += size [x];
                   if (rank [x] == rank [y])
                        rank [y]++;
            return 1;
      return 0;
}
```

```
void kruskal () {
      std::sort (edges.begin (), edges.end ());
      long long ans = 0;
      for (int i = 0; i < m; i++) {
            if (add (edges [i].second.first, edges [i].second.second)) {
                  //printf ("{%d, %d}\n", edges [i].second.first, edges
[i].second.second);
                  ans += edges [i].first;
      printf ("%lld\n", ans);
void aux (int s) {
      visited [s] = 1;
      for (int i = 0; i < m; i++)
            if (edges [i].second.first == s && !visited [edges [i].second.second])
                  pq.push ({-edges [i].first, -edges [i].second.second});
            else if (edges [i].second.second == s && !visited [edges
[i].second.first])
                  pq.push ({-edges [i].first, -edges [i].second.first});
}
void prim (int s) {
      long long ans = 0;
      aux(s);
      while (!pq.empty ()) {
            pi top = pq.top (); pq.pop ();
            printf ("{%d, %d}\n", -top.first, -top.second);
            if (!visited [-top.second]) {
                  ans += -top.first;
                  aux (-top.second);
      printf ("%lld\n", ans);
void input () {
      scanf ("%d%d", &n, &m);
      // n++; if starts from 1
      edges.clear ();
      size.clear ();
      rank.clear ();
      p.clear ();
      size.assign (n, 1);
      rank.assign (n, 0);
      p.assign (n, 0);
      for (int i = 0; i < n; i++)
            p[i] = i;
      for (int i = 0; i < m; i++) {
            int a, b, c; scanf ("%d%d%d", &a, &b, &c);
            edges.push_back ({c, {a, b}});
      solve ();
void solve () {
      prim (0);
int main () {
      input ();
      return 0;
}
```

TOPOLOGICAL SORT DAG

```
#include <bits/stdc++.h>
void input ();
void solve ();
typedef std::vector <int> vi;
typedef std::vector <vi> vvi;
const int MAXN = 1e3;
int n, m;
int visited [MAXN];
int inc [MAXN], out [MAXN];
vi ans;
vvi g;
// the idea of topological sort is to always remove the TOP first, which could be
more than 1
// but everytime that a TOP is removed we get the next TOP
// TOP == vertices which has no incoming edges
void dfs (int x) {
      visited [x] = 1;
      for (int v : g [x])
            if (!visited [v])
                  dfs (v);
      ans.push_back (x);
}
void bfs () {
      std::queue <int> q;
for (int i = 0; i < n; i++)</pre>
            if (!inc [i])
                  q.push (i);
      while (!q.empty ()) {
            int x = q.front (); q.pop ();
            ans.push_back (x);
            for (int v : g [x])
                   if (--inc [v] == 0)
                        q.push (v);
      }
}
void input () {
      scanf ("%d%d", &n, &m);
      g.clear ();
      g.resize (n);
      for (int i = 0; i < m; i++) {
            int a, b; scanf ("%d%d", &a, &b);
            g [a].push_back (b);
            out [a]++;
            inc [b]++;
      }
}
void solve () {
      for (int i = 0; i < n; i++)
            if (!visited [i])
                  dfs (i);
      for (int i = ans.size () - 1; i >= 0; i--)
            printf ("%d ", ans [i]);
```

```
puts ("");
      bfs ();
      for (int i = 0; i < ans.size (); i++)
            printf ("%d ", ans [i]);
      puts ("");
int main () {
      input ();
      solve ();
      return 0;
SEGMENT TREE
#include <bits/stdc++.h>
const int MAXN = 1e5 + 1;
int n;
int arr [MAXN * 2];
// **** RANGE SUM QUERY ****
// use arr as the seg_tree and the input array
// all positions from N to 2 ^{\star} N are already filled with the leaf values
void build () {
  for (int i = n - 1; i > 0; i--)
    arr [i] = arr [i << 1] + arr [(i << 1) + 1];
void update (int p, int value) {
  p += n; // p + n == leaf nodes indexs
  // arr [p] = value == updating the leaf index
  // arr [p >> 1] == father node
  // arr [p] + arr [p ^ 1] == pair that have the same father (odd and even number) for (arr [p] = value; p > 1; p >>= 1)
    arr [p >> 1] = arr [p] + arr [p ^ 1];
int rq (int 1, int r) { // [L, R[
  int res = 0;
  1 += n;
  r += n;
  for (; 1 < r; 1 >>= 1, r >>= 1) {
    if (1 & 1)
      res += arr [l++];
    if (r & 1)
      res += arr [--r];
  return res;
int main () {
  scanf ("%d", &n);
  for (int i = 0; i < n; i++)
    scanf ("%d", arr + i + n);
  build ();
  puts ("printing the tree:");
  for (int i = 1; i < 2 * n; i++)
printf ("%d ", arr [i]);
  puts ("");
```

```
printf ("rq [1, 2]: %d\n", rq (3, 8));
  return 0;
FENWICK TREE
#include <bits/stdc++.h>
\#define LSOne(x) (x & (-x))
typedef std::vector <int> vi;
vi ft;
int n;
int q;
void insert (int num, int freq) {
  int x = num;
  // o num vai de num e se atualiaza com num += (LSOne (num))
  // ate que preencher todas as posicoes possiveis com
  // ft [num] += freq
  for (; num < ft.size (); num += (num & (-num))) {</pre>
   ft [num] += freq;
    printf ("num: %d, freq: %d, ft: %d\n", num, freq, ft [num]);
  }
int rsq(int num) { // returns RSQ(1, b)
  int sum = 0;
  // o num faz o processo inverso do insert assim,
  // como no insert ele vai crescendo, na busca ele
  // diminui
  for (; num; num -= LSOne(num)) {
    printf ("num: %d, ft[num]: %d\n", num, ft[num]);
    sum += ft[num];
  return sum;
int rsq(int a, int b) { // returns RSQ(a, b)
 // se a == 1 retorna rsq (b) - 0
  // se a != 1 retorna rsq (b) - rsq (a - 1)
  // assim "excluindo" a parte do range antes de 'a'
 return rsq(b) - (a == 1 ? 0 : rsq(a - 1));
int main () {
  scanf ("%d", &n);
  ft.assign (n + 1, 0);
  for (int i = 1; i \le n; i++) {
    int a;
    puts ("NEW");
    scanf ("%d", &a);
    insert (i, a);
  }
  for (int i = 1; i < ft.size (); i++)
   printf ("%d ", ft [i]);
  puts ("");
  printf ("rsq : %d\n", rsq (3, 3));
  return 0;
```

COMPUTATIONAL GEOMETRY

BASIC

```
#include <bits/stdc++.h>
struct Point {
 int x = 0, y = 0;
 Point operator- (Point a) {
   Point ans;
   ans.x = x - a.x;
   ans.y = y - a.y;
   return ans;
  // lexographically
  bool operator< (Point a) {</pre>
   if (x == a.x)
     return y < a.y;
   return x < a.x;
  }
};
Point center;
// which quarter
int quarter (Point a) {
 if (a.x >= 0 \&\& a.y >= 0)
   return 1;
  if (a.x <= 0 \&\& a.y >= 0)
   return 2;
  if (a.x <= 0 && a.y <= 0)
   return 3;
  return 4;
// cros product
int cross (Point a, Point b) {
 return a.x * b.y - a.y * b.x;
// return a point which represents a vector
Point toVector (Point a, Point b) {
 Point ans;
 ans.x = b.x - a.x;
 ans.y = b.y - a.y;
 return ans;
// positive == left, 0 == colinear, negative == right
int checkTurn (Point a, Point b, Point c) {
 return cross (toVector (a, b), toVector (a, c));
// compare function by polar angle
bool cmp (Point a, Point b) {
 a = a - center; b = b - center; // relative points from a pivot
 if (quarter (a) == quarter (b))
   return cross (a, b) > 0;
 return quarter (a) < quarter (b);
// convex hull Andrew`s monotone chain
std::vector <Point> ch_monotone (std::vector <Point> pts) {
 int k = 0;
  std::vector <Point> ans (pts.size () * 2);
```

```
std::sort (pts.begin (), pts.end ());
  puts ("SORTED:");
  for (int i = 0; i < pts.size (); i++)
    printf ("{%d, %d} ", pts [i].x, pts [i].y);
  puts ("");
  // lower hull
  for (int i = 0; i < pts.size (); i++) {
    // more than 2 points and while notConvex remove last point
    while (k \ge 2 \&\& \text{checkTurn (ans } [k-2], \text{ ans } [k-1], \text{ pts } [i]) < 0)
      k--;
    ans [k++] = pts [i];
  printf ("k: %d\n", k);
for (int i = 0; i < k; i++)</pre>
    printf ("{%d, %d} ", ans [i].x, ans [i].y);
  puts ("");
  // upper hull
  for (int i = (int)pts.size () - 2, t = k + 1; i >= 0; i--) {
    // k >= t to not erase the lower hull ans while notConvex remove last point
    while (k \ge t \&\& checkTurn (ans [k - 2], ans [k - 1], pts [i]) < 0)
    ans [k++] = pts [i];
  ans.resize (k);
  return ans;
int main () {
  std::vector <Point> input, hull;
  input.resize (7);
  input [0].x = 0; input [0].y = 0;
  input [1].x = 0; input [1].y = 8;
  input [2].x = 1; input [2].y = 6;
  input [3].x = 3; input [3].y = 1;
  input [4].x = 6; input [4].y = 6;
  input [5].x = 8; input [5].y = 0;
  input [6].x = 8; input [6].y = 8;
  puts ("INPUT:");
  for (int i = 0; i < input.size (); i++)
  printf ("{%d, %d} ", input [i].x, input [i].y);</pre>
  puts ("");
 hull = ch_monotone (input);
  puts ("CH:");
  for (int i = 0; i < hull.size (); i++)
    printf ("{%d, %d} ", hull [i].x, hull [i].y);
  puts ("");
  return 0;
}
INTEGER LINE
#include <bits/stdc++.h>
typedef long long 11;
struct point {ll x, y;};
struct line {
```

```
ll a, b, c; //ax - by = c
  bool operator <(const line& rhs) const {</pre>
    return std::make_tuple(a, b, c) < std::make_tuple(rhs.a, rhs.b, rhs.c);</pre>
};
ll gcd(ll a, ll b) {
  while (b) {
    a %= b;
    std::swap(a, b);
  return a;
line pointsToLine(point p1, point p2) {
  11 a = p1.y - p2.y;
  ll b = p1.x - p2.x;
ll c = p1.y * p2.x - p2.y * p1.x;
  11 d = gcd(gcd(a, b), c);
  a/=d, b/=d, c/=d;
  if (a < 0) a^*=-1, b^*=-1, c^*=-1;
  return {a, b, c};
bool areParallel(line 11, line 12) {
  return (11.a == 12.a) && (11.b == 12.b);
bool areSame(line 11, line 12) {
  return areParallel(11, 12) && (11.c == 12.c);
INTERSECT
struct point {int x, y;};
struct segment {point a, b;};
point tovec(point a, point b) {
  return {b.x-a.x, b.y-a.y};
int cross(point a, point b) {
  return a.x*b.y - a.y*b.x;
bool ccw(point p, point q, point r) {
  return cross(tovec(p, q), tovec(p, r)) > 0;
bool collinear(point p, point q, point r) {
  return cross(tovec(p, q), tovec(p, r)) == 0;
bool in_bouding_box(point p, point q, point r) {
  int maxX = std::max(q.x, r.x), minX = std::min(q.x, r.x);
  int maxY = std::max(q.y, r.y), minY = std::min(q.y, r.y);
  return p.x <= \max X \&\& p.x >= \min X \&\& p.y <= \max Y \&\& p.y >= \min Y;
bool segment_intersect(segment s, segment t) {
  if (collinear(s.a, t.a, t.b) && in_bouding_box(s.a, t.a, t.b)) return true; if (collinear(s.b, t.a, t.b) && in_bouding_box(s.b, t.a, t.b)) return true;
  if (collinear(t.a, s.a, s.b) && in_bouding_box(t.a, s.a, s.b)) return true;
```

```
if (collinear(t.b, s.a, s.b) && in_bouding_box(t.b, s.a, s.b)) return true;
  if (ccw(s.a, s.b, t.a) != ccw(s.a, s.b, t.b)
      && ccw(t.a, t.b, s.a) != ccw(t.a, t.b, s.b))
    return true;
  return false;
CALOPSITA
#define EPS 1e-9
struct point {
      double x, y;
      point() { x = y = 0.0; }
      point(double _x, double _y) : x(_x), y(_y) {}
double norm() { return hypot(x, y); }
      point normalized() {
            return point (x,y)*(1.0/norm());
      }
      double angle() { return atan2(y, x); }
      double polarAngle() {
            double a = atan2(y, x);
            return a < 0 ? a + 2*acos(-1.0) : a;
      bool operator < (point other) const {</pre>
            if (fabs(x - other.x) > EPS) return x < other.x;
            else return y < other.y;</pre>
      bool operator == (point other) const {
            return (fabs(x - other.x) < EPS && (fabs(y - other.y) < EPS));
      point operator +(point other) const {
            return point(x + other.x, y + other.y);
      point operator -(point other) const {
            return point(x - other.x, y - other.y);
      point operator *(double k) const {
            return point(x*k, y*k);
};
double dist(point p1, point p2) {
      return hypot (p1.x - p2.x, p1.y - p2.y);
double inner(point p1, point p2) {
      return p1.x*p2.x + p1.y*p2.y;
double cross(point p1, point p2) {
     return p1.x*p2.y - p1.y*p2.x;
bool ccw(point p, point q, point r) {
      return cross (q-p, r-p) > 0;
bool collinear(point p, point q, point r) {
     return fabs(cross(p-q, r-p)) < EPS;
}
point rotate(point p, double rad) {
      return point(p.x * cos(rad) - p.y * sin(rad),
                  p.x * sin(rad) + p.y * cos(rad));
double angle(point a, point o, point b) {
      return acos(inner(a-o, b-o) / (dist(o,a)*dist(o,b)));
}
```

```
point proj(point u, point v) {
      return v*(inner(u,v)/inner(v,v));
bool between(point p, point q, point r) {
      return collinear(p, q, r) && inner(p - q, r - q) \leq 0;
}
point lineIntersectSeg(point p, point q, point A, point B) {
      double c = cross(A-B, p-q);
      double a = cross(A, B);
      double b = cross(p, q);
      return ((p-q)*(a/c)) - ((A-B)*(b/c));
bool parallel(point a, point b) {
      return fabs(cross(a, b)) < EPS;
bool segIntersects(point a, point b, point p, point q) {
      if (parallel(a-b, p-q)) {
            return between(a, p, b) || between(a, q, b)
                  || between (p, a, q) || between (p, b, q);
      point i = lineIntersectSeg(a, b, p, q);
      return between(a, i, b) && between(p, i, q);
point closestToLineSegment(point p, point a, point b) {
      double u = inner(p-a, b-a) / inner(b-a, b-a);
      if (u < 0.0) return a;
      if (u > 1.0) return b;
      return a + ((b-a)*u);
struct circle{
      point c;
      double r;
      circle() { c = point(); r = 0; }
      circle(point _c, double _r) : c(_c), r(_r) {}
      double area() { return acos(-1.0)*r*r; }
      double chord(double rad) { return 2*r*sin(rad/2.0); }
      double sector(double rad) { return 0.5*rad*area()/acos(-1.0); }
      bool intersects (circle other) {
            return dist(c, other.c) < r + other.r;</pre>
      bool contains(point p) { return dist(c, p) <= r + EPS; }</pre>
      pair<point, point> getTangentPoint(point p) {
            double d1 = dist(p, c), theta = asin(r/d1);
            point p1 = rotate(c-p, -theta);
            point p2 = rotate(c-p, theta);
            p1 = p1*(sqrt(d1*d1-r*r)/d1)+p;
            p2 = p2*(sqrt(d1*d1-r*r)/d1)+p;
            return make_pair(p1,p2);
      vector< pair<point, point> > getTangentSegs(circle other) {
            vector<pair<point, point> > ans;
            double d = dist(other.c, c);
            double dr = abs(r - other.r), sr = r + other.r;
            if (dr >= d) return ans;
            double u = a\cos(dr / d);
            point dc1 = ((other.c - c).normalized())*r;
point dc2 = ((other.c - c).normalized())*other.r;
            ans.push_back(make_pair(c + rotate(dc1, u), other.c + rotate(dc2, u)));
            ans.push_back(make_pair(c + rotate(dc1, -u), other.c + rotate(dc2, -
u)));
            if (sr >= d) return ans;
            double v = acos(sr / d);
            dc2 = ((c - other.c).normalized()) * other.r;
            ans.push_back(\{c + rotate(dc1, v), other.c + rotate(dc2, v)\});
            ans.push_back({c + rotate(dc1, -v), other.c + rotate(dc2, -v)});
            return ans;
      }
```

```
pair<point, point> getIntersectionPoints(circle other) {
            assert(intersects(other));
            double d = dist(c, other.c);
            double u = acos((other.r*other.r + d*d - r*r) / (2*other.r*d));
            point dc = ((other.c - c).normalized()) * r;
            return make_pair(c + rotate(dc, u), c + rotate(dc, -u));
      }
};
circle circumcircle(point a, point b, point c) {
      circle ans;
      point u = point((b-a).y, -(b-a).x);
      point v = point((c-a).y, -(c-a).x);
      point n = (c-b)*0.5;
      double t = cross(u,n)/cross(v,u);
      ans.c = ((a+c)*0.5) + (v*t);
      ans.r = dist(ans.c, a);
      return ans;
int insideCircle(point p, circle c) {
      if (fabs(dist(p , c.c) - c.r) < EPS) return 1;</pre>
      else if (dist(p , c.c) < c.r) return 0;
      else return 2;
} //0 = inside/1 = border/2 = outside
circle incircle( point p1, point p2, point p3 ) {
      double m1=dist(p2, p3);
      double m2=dist(p1, p3);
      double m3=dist(p1, p2);
      point c = (p1*m1+p2*m2+p3*m3)*(1/(m1+m2+m3));
      double s = 0.5*(m1+m2+m3);
      double r = sqrt(s*(s-m1)*(s-m2)*(s-m3))/s;
      return circle(c, r);
POLYGON AREA
#include <bits/stdc++.h>
void input ();
void solve ();
struct Point {
  int x = 0, y = 0;
  Point operator- (Point a) {
    Point ans;
    ans.x = x - a.x;
   ans.y = y - a.y;
    return ans;
  }
  // lexographically
  bool operator< (Point a) {
    if (x == a.x)
     return y < a.y;
    return x < a.x;
  }
};
typedef std::pair <float, float> pi;
typedef std::vector <Point> vpi;
int n;
vpi arr;
```

```
Point center;
int quarter (Point a) {
  if (a.x >= 0 \&\& a.y >= 0)
   return 1;
  if (a.x <= 0 \&\& a.y >= 0)
  return 2;
if (a.x <= 0 && a.y <= 0)
    return 3;
  return 4;
// cros product
int cross (Point a, Point b) {
 return a.x * b.y - a.y * b.x;
// compare function by polar angle
bool cmp (Point a, Point b) {
  a = a - center; b = b - center; // relative points from a pivot
  if (quarter (a) == quarter (b))
    return cross (a, b) > 0;
  return quarter (a) < quarter (b);
}
void input () {
    scanf ("%d", &n);
      for (int i = 0; i < n; i++) {
            int a, b; scanf ("%d%d", &a, &b);
            arr.push_back ({a, b});
      solve ();
}
void solve () {
      //std::random_shuffle (arr.begin (), arr.end ());
      std::sort (arr.begin (), arr.end (), cmp);
      arr.push_back ({arr [0].x, arr [0].y});
      float ans = 0;
      for (int i = 0; i < n; i++) {
            ans += (float)arr [i].x * (float)arr [i + 1].y;
            ans -= (float)arr [i].y * (float)arr [i + 1].x;
      printf ("%f\n", ans / 2.0);
int main () {
      input ();
      return 0;
SEGMENT INTERSECTION
#include <bits/stdc++.h>
void input ();
void solve ();
typedef long long 11;
typedef long double ld;
const double EPS = 1e-9;
typedef struct point {
      ld x, y;
```

```
point () {}
      point (ld x, ld y) : x (x), y (y) {}
      point operator- (point& a) {
            return \{x - a.x, y - a.y\};
      bool operator< (point& a) {</pre>
            if (x == a.x)
                  return y < a.y;
            return x < a.x;
      }
      bool operator> (point& a) {
            if (x == a.x)
                  return y > a.y;
            return x > a.x;
      bool operator== (point &a) {
            return x == a.x && y == a.y;
      bool operator>= (point &a) {
            if (x == a.x)
                  return y > a.y || y == a.y;
            return x > a.x \mid \mid x == a.x;
      bool operator<= (point &a) {</pre>
            if (x == a.x)
                 return y < a.y \mid \mid y == a.y;
            return x < a.x \mid \mid x == a.x;
      }
} point;
typedef struct segment {
     point a, b;
      segment () {}
      segment (point a, point b) : a (a), b (b) {}
} segment;
typedef struct line {
      ld a, b, c;
      line () {}
      line (ld a, ld b, ld c) : a (a), b (b), c (c) {}
} line;
line pointsToLine(point p1, point p2) {
      line 1;
      if (fabs(p1.x-p2.x) < EPS)
            1 = \{1.0, 0.0, -p1.x\};
      else {
            double a = -(double)(p1.y-p2.y) / (p1.x-p2.x);
            l = \{a, 1.0, -(double)(a*p1.x) - p1.y\};
      return 1;
}
point to_vec (const point& a, const point& b) {
      return {a.x - b.x, a.y - b.y};
```

```
ld dot (point a, point b) {
     return a.x*b.x + a.y*b.y;
ld cross (point a, point b) {
      return a.x*b.y - a.y*b.x;
int check_turn (point a, point b, point c) {
 return cross (to_vec (a, b), to_vec (a, c)) > 0;
bool collinear(point p, point q, point r) {
  return cross(to_vec(p, q), to_vec(p, r)) == 0;
bool in_bouding_box(point p, point q, point r) {
  ld maxX = std::max(q.x, r.x), minX = std::min(q.x, r.x);
  ld maxY = std::max(q.y, r.y), minY = std::min(q.y, r.y);
  return p.x <= maxX && p.x >= minX && p.y <= maxY && p.y >= minY;
bool segment_intersect(segment s, segment t) {
  if (collinear(s.a, t.a, t.b) && in_bouding_box(s.a, t.a, t.b)) return true;
  if (collinear(s.b, t.a, t.b) && in_bouding_box(s.b, t.a, t.b)) return true;
  if (collinear(t.a, s.a, s.b) && in_bouding_box(t.a, s.a, s.b)) return true;
  if (collinear(t.b, s.a, s.b) && in_bouding_box(t.b, s.a, s.b)) return true;
  if (check_turn(s.a, s.b, t.a) != check_turn(s.a, s.b, t.b)
      && check_turn(t.a, t.b, s.a) != check_turn(t.a, t.b, s.b))
    return true;
  return false;
}
bool areParallel(line 11, line 12) {
                                           // check coefficients a & b
      return (fabs(11.a-12.a) < EPS) && (fabs(11.b-12.b) < EPS);
bool are_same(line 11, line 12) {
                                              // also check coefficient c
      return areParallel(11 ,12) && (fabs(11.c-12.c) < EPS);
point line_intersect (line 11, line 12) {
      point p;
      p.x = (12.b*11.c - 11.b*12.c) / (12.a*11.b - 11.a*12.b);
      if (fabs(l1.b) > EPS)
            p.y = -(11.a*p.x + 11.c);
      else
            p.y = -(12.a*p.x + 12.c);
      return p;
point arr [4];
void input () {
      for (int i = 0; i < 4; i++)
            scanf ("%Lf%Lf", &(arr + i)->x, &(arr + i)->y);
      solve ();
void solve () {
      if (segment_intersect ({arr [0], arr [1]}, {arr [2], arr [3]})) {
    line l1 = pointsToLine (arr [0], arr [1]);
            line 12 = pointsToLine (arr [2], arr [3]);
```

```
//printf ("{%Lf, %Lf, %Lf}\n", l1.a, l1.b, l1.c);
            //printf ("{%Lf, %Lf, %Lf}\n", 12.a, 12.b, 12.c);
            if (are_same (11, 12)) {
                   std::sort (arr, arr + 2);
                   std::sort (arr + 2, arr + 4);
                  point a, b;
                  if (arr [0] <= arr [2]) { // 0---2 if (arr [1] <= arr [3]) { // 0---2-1--3}
                               a = arr [2];
                               b = arr [1];
                         else { // 0---2--3--1
                               a = arr [2];
                               b = arr [3];
                         }
                  else { // 2---0
                         if (arr [1] >= arr [3]) { // 2---0--3--1}
                               a = arr [0];
                               b = arr [3];
                         }
                         else { // 2---0-1--3
                               a = arr [0];
                               b = arr [1];
                         }
                   if (a == b)
                         printf ("%.10Lf %.10Lf\n", a.x, a.y);
                   else {
                         printf ("%.10Lf %.10Lf\n", a.x, a.y);
                         printf ("%.10Lf %.10Lf\n", b.x, b.y);
            else {
                  point p = line_intersect (11, 12);
                  printf ("%.10Lf %.10Lf\n", p.x, p.y);
      else
            puts ("Empty");
}
int main () {
      input ();
      return 0;
}
```

STRINGS

LCS

```
#include <bits/stdc++.h>
void input ();
void solve ();

typedef std::pair <int, int> pi;
typedef std::vector <int> vi;

const int MAXN = 1e2 + 1;

std::string str1, str2;
int dp [MAXN] [MAXN];
pi t [MAXN] [MAXN];
```

```
vi t1, t2;
int lcs (int i, int j) {
      if (i >= str1.size () | | j >= str2.size ())
            return 0;
      if (dp [i][j])
            return dp [i][j];
      if (str1 [i] == str2 [j]) {
            dp[i][j] = lcs(i + 1, j + 1) + 1;
            t [i][j] = std::make_pair (i + 1, j + 1);
      else {
            int a = lcs (i + 1, j), b = lcs (i, j + 1);
            if (a > b) {
                   dp [i][j] = a;
                   t [i][j] = std::make_pair (i + 1, j);
            else {
                   dp [i][j] = b;
                   t [i][j] = std::make_pair (i, j + 1);
             }
      }
      return dp [i][j];
}
void input () {
      std::cin >> str1 >> str2;
      solve ();
}
void solve () {
      printf ("%d\n", lcs (0, 0));
      int a = 0, b = 0;
      while (a < str1.size () && b < str2.size ()) \{
            //printf ("{%d, %d} = {%c, %c}\n", a, b, str1 [a], str2 [b]);
            if (str1 [a] == str2 [b]) {
                   t1.push_back (t [a][b].first);
                   t2.push_back (t [a][b].second);
            pi p = t [a][b];
            a = p.first;
            b = p.second;
      }
      for (int i = 0; i < t1.size (); i++)
            printf ("%d ", t1 [i]);
      puts ("");
      for (int i = 0; i < t2.size (); i++)
printf ("%d ", t2 [i]);
      puts ("");
}
int main () {
      input ();
      return 0;
}
KMP
#include <bits/stdc++.h>
```

```
const int MAXP = 100; // max pattern size
int lsp [MAXP]; // suffix which is a prefix
void build_lps (std::string a) { // a == pattern
  int i = 1, j = 0;
  lps [0] = 0;
  while (i < a.size ()) {
    if (a[i] == a[j]) { // match}
      j++;
      lps [i++] = j;
    else { // missmatch
      // if j == 0 cant go back anymore
// so lps [i] doesnt belongs to a suffix
      // which is a prefix
      // else => can go back so there's still chance
      if (j == 0)
       lps [i++] = 0;
      else
        j = lps [j - 1];
   }
  }
void kmp_search (std::string a, std::string b) { // a == text, b == pattern
  int i = 0; j = 0;
  build_lps (b);
  while (i < a.size () - b.size ()) { // until text.size - pattern.size
    if (a [i] == b [j]) { //match}
      i++; j++;
if (j == b.size ()) { // pattern match
        j = lps [j - 1];
      }
    }
    else {
      if (j == 0)
        i++;
      else
        j = lps [j - 1];
    }
  }
int main () {
 return 0;
                                    MISCELANIA
SIEVE ERASTHOTENES
#include <bits/stdc++.h>
const int MAXN = 1e7 + 1;
std::vector <long long> isp (MAXN, true), p, spf (MAXN);
void sieve () {
  isp [0] = false;
  isp [1] = false;
  for (int i = 2; i <= MAXN; i++) {
    if (isp [i]) {
```

p.push_back (i);

```
spf [i] = i;
}

for (long long j = 0; (j < p.size ()) && (i * p [j] < MAXN) && (p [j] <= spf
[i]); j++) {
    isp [i * p [j]] = false;
        spf [i * p [j]] = p [j];
    }
}

int main () {
    int n; scanf ("%d", &n);
    sieve ();

for (int i = 0; i < n; i++)
        printf ("%d ", p [i]);
    puts ("");

return 0;
}</pre>
```