

**Question 1**

Review the following graph heuristics, (shown in dotted red) and classify each graph according to the heuristics given here. Pick one classification from each list.

**choose one from this classification**

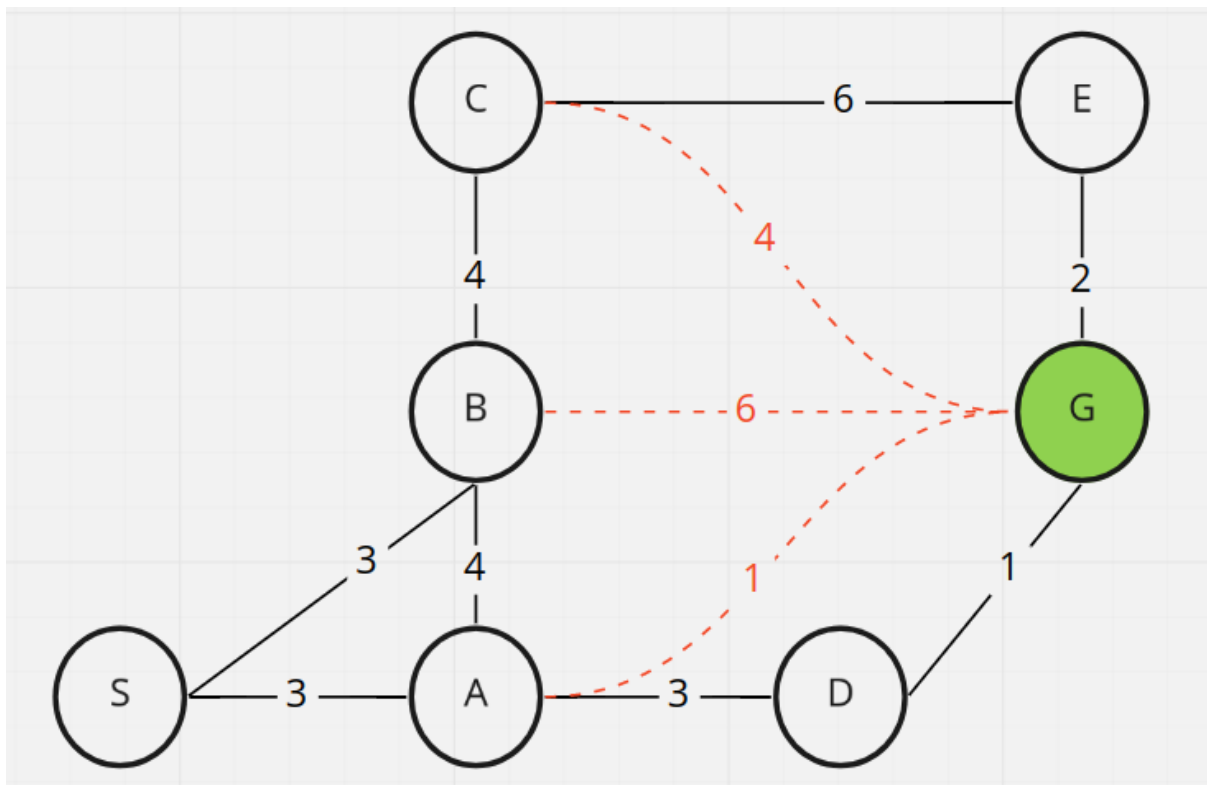
1. All admissible
2. Some admissible, some inadmissible
3. All inadmissible

**and choose one from this classification**

1. All consistent
2. Some consistent, some inconsistent
3. All inconsistent

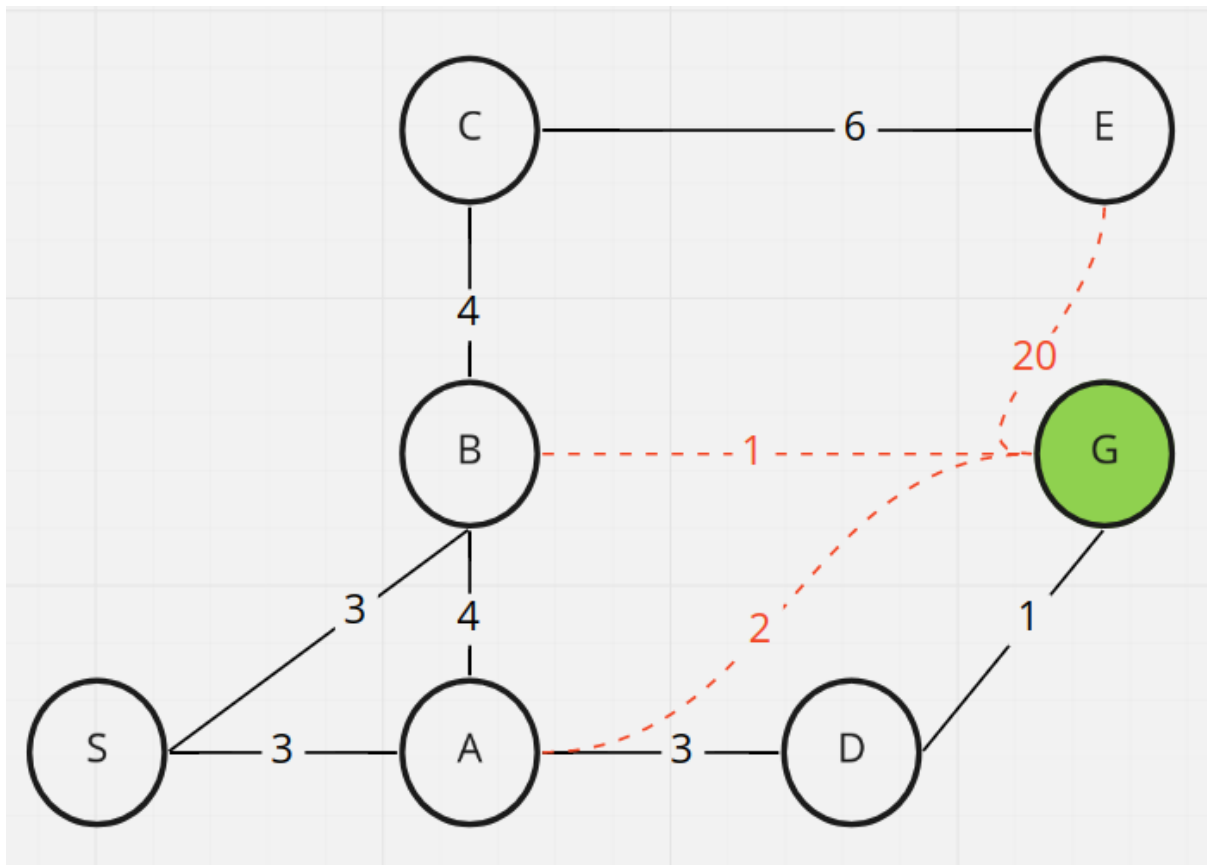
In each graph, show your calculations.

(a)



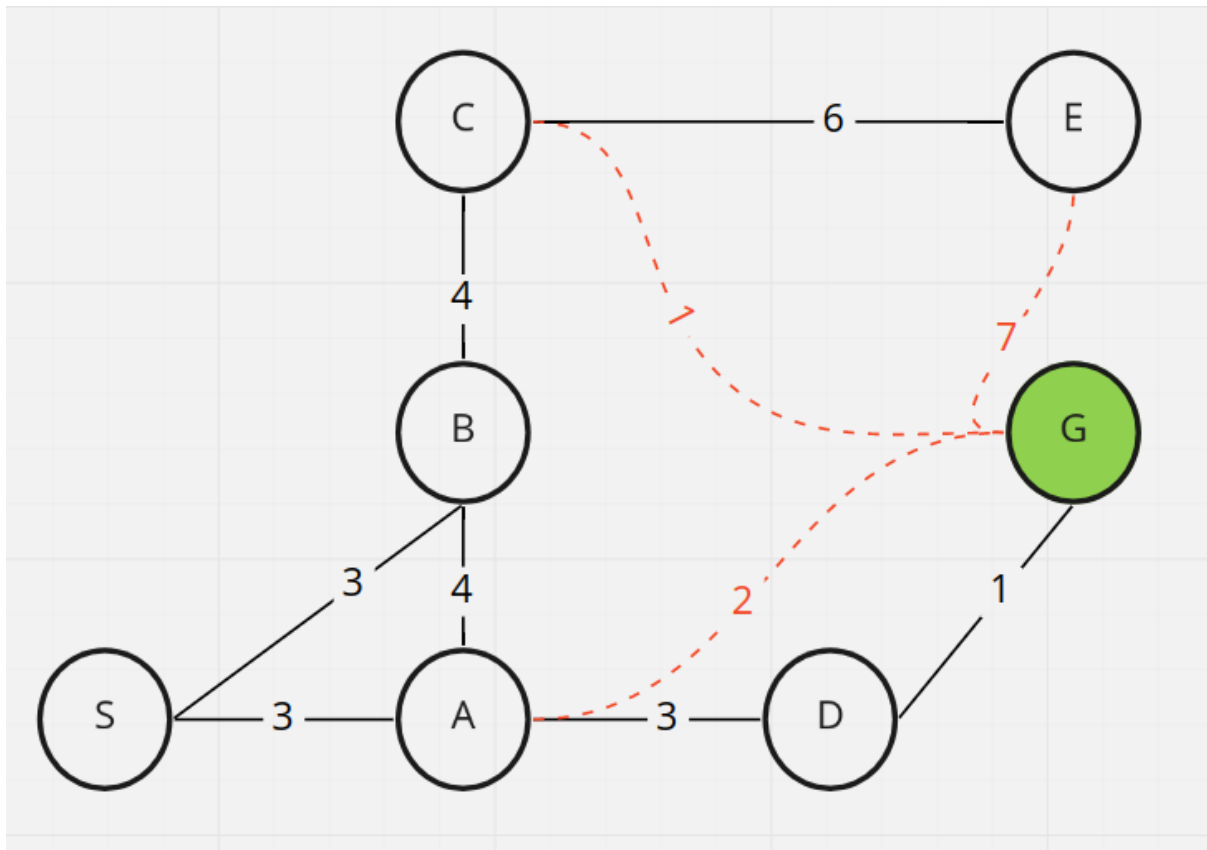
1. All Admissible
2. A-B:  $5 > 4 \Rightarrow$  inconsistent
3. A-C:  $3 < 8 \Rightarrow$  consistent
4. B-C:  $2 < 4 \Rightarrow$  consistent
5. [ = some inconsistent ]

(b)



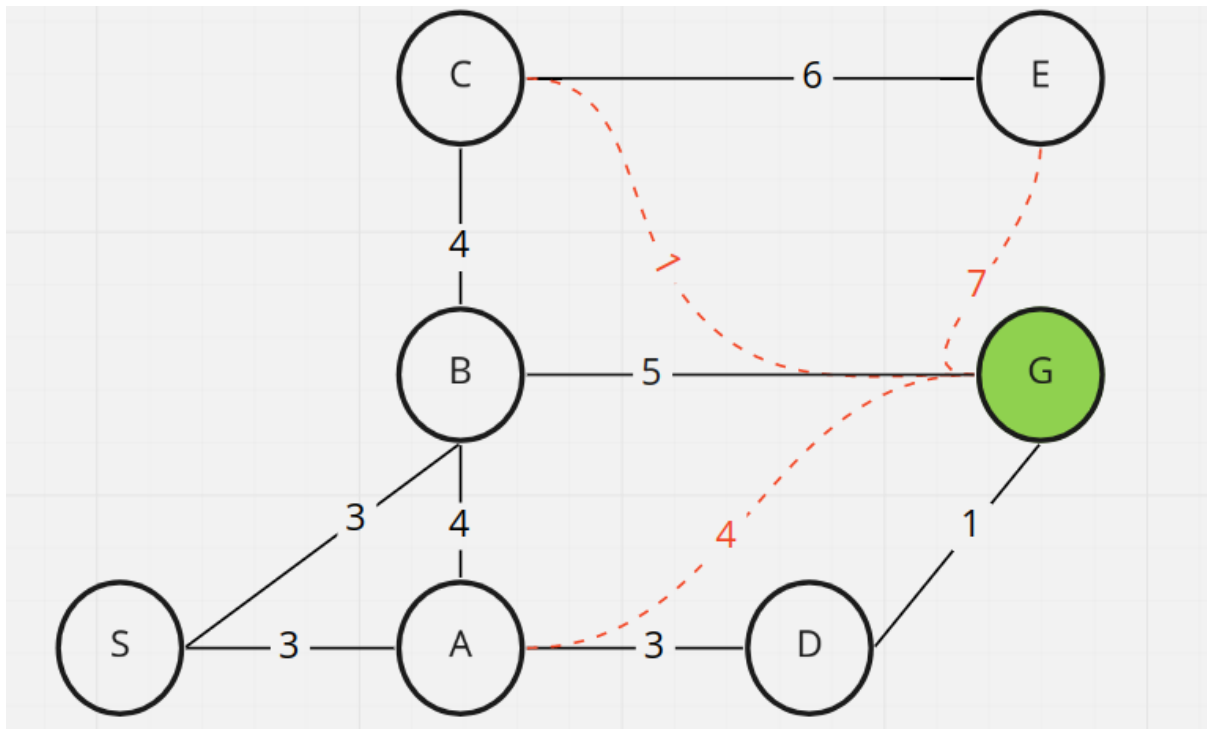
1. Some inadmissible (E)
2. A-B:  $2-1 < 4 \Rightarrow$  consistent
3. B-E:  $19 > 10 \Rightarrow$  inconsistent
4. A-E:  $18 > 14 \Rightarrow$  inconsistent
5. [ = some inconsistent ]

(c)



1. All admissible
2. A-C:  $2-1 < 8 \Rightarrow$  consistent
3. C-E:  $6 < 10 \Rightarrow$  consistent
4. A-E:  $5 < 14 \Rightarrow$  consistent
5. [ = all consistent ]

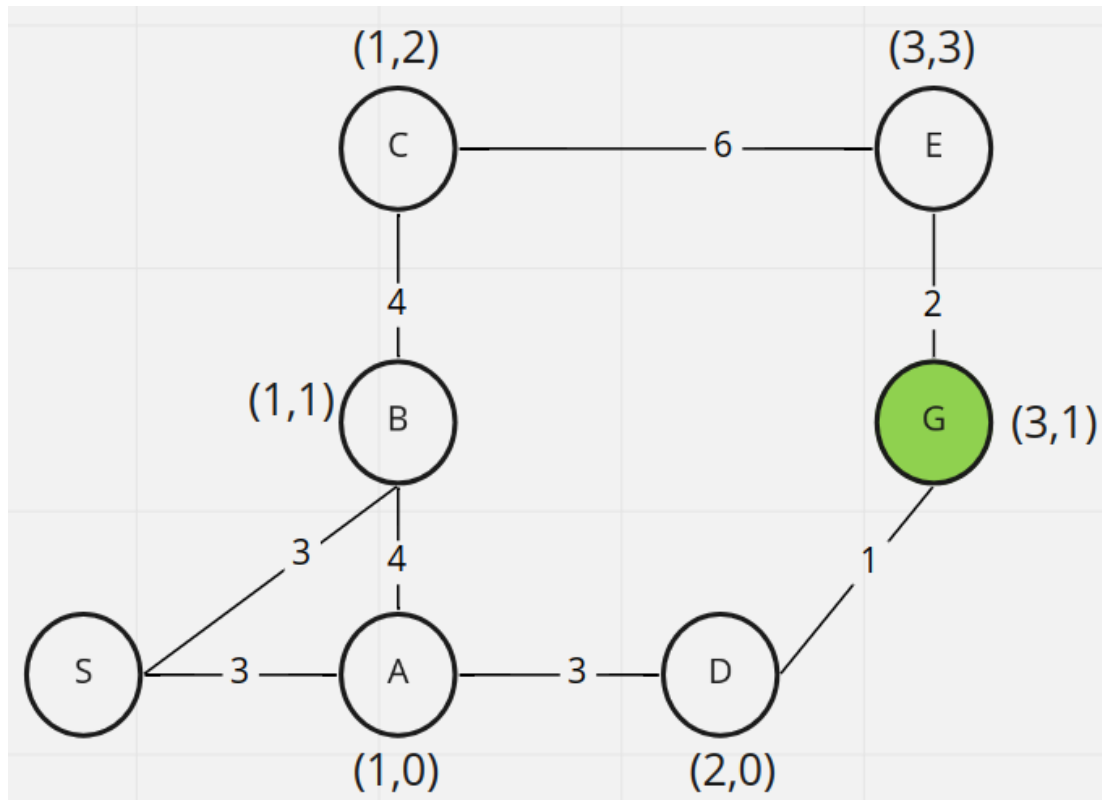
(d)



1. All admissible
  2. A-C:  $4-1 < 8 \Rightarrow$  consistent
  3. C-E:  $6 \leq 6 \Rightarrow$  consistent
  4. A-E:  $3 < 14 \Rightarrow$  consistent
- [ = all consistent ]

## Question 2

Consider the following graph in 2-dimensional Euclidean space. Each node (except the start) has the (x,y) coordinates alongside.



Using the formula from the lecture for Euclidean distance in 2 dimensional space:

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Compute the heuristic distance to G for each node **A,B,C,D,E** using the table here and test each to ensure it is admissible :

| <u>Node Pair</u>  | <u>Heuristic Distance</u>                   | <u>Admissible?</u> |
|-------------------|---|--------------------|
| <b><u>A-G</u></b> | $\text{sqrt}((1-3)^2 + (1-0)^2) = 2.236068$ | yes                |
| <b><u>B-G</u></b> | $\text{sqrt}((1-3)^2 + (1-1)^2) = 2$        | yes                |
| <b><u>C-G</u></b> | $\text{sqrt}((1-3)^2 + (2-1)^2) = 2.236068$ | yes                |
| <b><u>D-G</u></b> | $\text{sqrt}((2-3)^2 + (0-1)^2) = 1.414214$ | yes                |
| <b><u>E-G</u></b> | $\text{sqrt}((3-3)^2 + (3-1)^2) = 2$        | yes                |

### **Question 3**

Consider the following definitions for Admissible and Consistent Heuristics:

$$\textit{Admissible: } |H(x, G)| \leq D(x, G)$$

$$\textit{Consistent: } |H(x, G) - H(y, G)| \leq D(x, y)$$

Write a plain english definition of each of these without the use of mathematics

**Admissible:** “the heuristic distance to the goal must always be less than or equal to the actual distance ”

**Consistent:** “Given two nodes x and y, the heuristic distance from x to the goal minus the heuristic distance from y to the goal must be less than or equal to the actual distance from x to y”

### **Question 4**

Your friend has asked you to explain how the use of the **Already Extended List** in A\* Search enables the algorithm to find the optimal solution.

What do you say?

The **Already Extended List** does not enable the algorithm to find the optimal solution. It enables the algorithm to find the optimal solution more quickly by eliminating re-evaluation of already extended nodes.