A Tour of the Haskell Prelude

(and a few other basic functions)

Authors: <u>Bernie Pope</u> (original content), <u>Arjan van IJzendoorn</u> (HTML-isation and updates), <u>Clem Baker-Finch</u> (updated for Haskell 98 hierarchical libraries organisation).

This webpage is a HTML version of most of Bernie Pope's paper "A Tour of the Haskell Prelude": http://www.cs.mu.oz.au/~bjpop/papers.html.

To make searching easy I've included a list of functions below. Otherwise, when you look for "map" using your browser, you'll not only find the definition but all its uses, too.

This is not a complete reference for the Haskell Prelude. It focuses on some of the more basic functions that may be of most use to beginningstudents. Type classes are not covered.

abs, all, and, any, atan, break, ceiling, chr, compare, concat, concatMap, const, cos, digitToInt, div, drop, dropWhile, elem, error, even, exp, filter, flip, floor, foldl, foldl1, foldr1, fromIntegral, fst, gcd, head, id, init, isAlpha, isDigit, isLower, isSpace, isUpper, iterate, last, lcm, length, lines, log, map, max, maximum, min, minimum, mod, not, notElem, null, odd, or, ord, pi, pred, putStr, product, quot, rem, repeat, replicate, reverse, round, show, sin, snd, sort, span, splitAt, sqrt, subtract, succ, sum, tail, take, takeWhile, tan, toLower, toUpper, truncate, undefined, unlines, until, unwords, words, zip, zipWith, (!!), (.), (*), (**), (^\infty), (^\infty), (^\infty), (^\infty), (-), (:), (+), (++), (/=), (==), (<), (<=), (>), (>=), (&&), (||)

```
abs
            abs :: Num a => a -> a
type:
description: returns the absolute value of a number.
definition:
            abs x
                x >= 0 = x
                otherwise = -x
            Prelude > abs (-3)
usage:
all
            all :: (a -> Bool) -> [a] -> Bool
type:
description: applied to a predicate and a list, returns True if all elements of the list satisfy the predicate, and
            False otherwise. Similar to the function any.
            all p xs = and (map p xs)
definition:
usage:
            Prelude > all (<11) [1..10]
            Prelude > all isDigit "123abc"
            False
and
            and :: [Bool] -> Bool
type:
description: takes the logical conjunction of a list of boolean values (see also `or').
definition:
            and xs = foldr (&&) True xs
```

Prelude> and [True, True, False, True]

Prelude > and [True, True, True, True]

usage:

False

```
True
            Prelude> and []
            True
any
            any :: (a -> Bool) -> [a] -> Bool
type:
description: applied to a predicate and a list, returns True if any of the elements of the list satisfy the
            predicate, and False otherwise. Similar to the function <u>all</u>.
definition:
            any p xs = or (map p xs)
usage:
            Prelude> any (<11) [1..10]
            True
            Prelude> any isDigit "123abc"
            Prelude > any isDigit "alphabetics"
            False
atan
            atan :: Floating a => a -> a
type:
description: the trigonometric function inverse tan.
definition:
            defined internally.
usage:
            Prelude> atan pi
            1.26263
break
            break :: (a -> Bool) -> [a] -> ([a],[a])
type:
description: given a predicate and a list, breaks the list into two lists (returned as a tuple) at the point where
            the predicate is first satisfied. If the predicate is never satisfied then the first element of the
            resulting tuple is the entire list and the second element is the empty list ([]).
definition:
            break p xs
               = <u>span</u> p' xs
                 where
                 p' x = \underline{not} (p x)
usage:
            Prelude> break isSpace "hello there fred"
            ("hello", " there fred")
            Prelude> break isDigit "no digits here"
            ("no digits here","")
ceiling
            ceiling :: (RealFrac a, Integral b) => a -> b
type:
description: returns the smallest integer not less than its argument.
            Prelude> ceiling 3.8
usage:
            Prelude> ceiling (-3.8)
            -3
see also:
            floor
chr
            chr :: Int -> Char
type:
description: applied to an integer in the range 0 -- 255, returns the character whose ascii code is that integer. It
            is the converse of the function ord. An error will result if chr is applied to an integer outside the
            correct range. [Import from Data.Char]
definition:
```

defined internally.

```
Prelude> chr 65
usage:
            'A'
            Prelude> (ord (chr 65)) == 65
see also:
            ord
compare
type:
            compare :: Ord a => a -> a -> Ordering
description: applied to to values of the same type which have an ordering defined on them, returns a value of
            type Ordering which will be: EQ if the two values are equal; GT if the first value is strictly
            greater than the second; and LT if the first value is less than or equal to the second value.
definition:
            compare x y
                  x == y = EQ
                  x \le y = LT
                  otherwise = GT
            Prelude > compare "aadvark" "zebra"
usage:
            LT
concat
type:
            concat :: [[a]] -> [a]
description: applied to a list of lists, joins them together using the ++ operator.
definition:
            concat xs = foldr (++) [] xs
            Prelude > concat [[1,2,3], [4], [], [5,6,7,8]]
usage:
            [1, 2, 3, 4, 5, 6, 7, 8]
concatMap
type:
            concatMap :: (a -> [b]) -> [a] -> [b]
description: given a function which maps a value to a list, and a list of elements of the same type as the value,
            applies the function to the list and then concatenates the result (thus flattening the resulting list).
definition:
            concatMap f = concat \cdot map f
usage:
            Prelude concatMap show [1,2,3,4]
            "1234"
const
            const :: const :: a -> b -> a
type:
description: creates a constant valued function which always has the value of its first argument, regardless of
            the value of its second argument.
            const k _ = k
definition:
usage:
            Prelude> const 12 "lucky"
            12
COS
            cos :: Floating a => a -> a
type:
description: the trigonometric cosine function, arguments are interpreted to be in radians.
definition:
            defined internally.
            Prelude> cos pi
usage:
            -1.0
            Prelude > cos (pi/2)
            -4.37114e-08
digitToInt
```

```
digitToInt :: Char -> Int
type:
description: converts a digit character into the corresponding integer value of the digit. [Import from
            Data.Char]
definition:
            digitToInt :: Char -> Int
            digitToInt c
                 isDigit c
                                               fromEnum c - fromEnum '0'
                 c >= 'a' \&\& c <= 'f' = fromEnum c - fromEnum 'a' + 10
                 c >= 'A' \&\& c <= 'F' = fromEnum c - fromEnum 'A' + 10
                                               error "Char.digitToInt: not a digit"
                otherwise
            Prelude > digitToInt '3'
usage:
div
            div :: Integral a => a -> a -> a
type:
description: computes the integer division of its integral arguments.
definition:
            defined internally.
            Prelude> 16 `div` 9
usage:
            Prelude> (-12) `div` 5
            -3
            `div` is integer division such that the result is truncated towards negative infinity.
notes:
drop
            drop :: Int -> [a] -> [a]
type:
description: applied to a number and a list, returns the list with the specified number of elements removed from
            the front of the list. If the list has less than the required number of elements then it returns [].
definition:
            drop 0 xs
                                      = []
            drop _ []
            drop n (:xs) \mid n>0 = drop (n-1) xs
                                      = error "PreludeList.drop: negative argument"
           Prelude> drop 3 [1..10]
usage:
            [4, 5, 6, 7, 8, 9, 10]
            Prelude> drop 4 "abc"
dropWhile
            dropWhile :: (a \rightarrow Bool) \rightarrow [a] \rightarrow [a]
type:
description: applied to a predicate and a list, removes elements from the front of the list while the predicate is
            satisfied.
definition:
           dropWhile p [] = []
            dropWhile p (x:xs)
                p x = dropWhile p xs
                otherwise = (x:xs)
            Prelude > dropWhile (<5) [1..10]
usage:
            [5, 6, 7, 8, 9, 10]
elem
type:
            elem :: Eq a => a -> [a] -> Bool
description: applied to a value and a list returns True if the value is in the list and False otherwise. The
           elements of the list must be of the same type as the value.
definition:
           elem x xs = any (== x) xs
```

```
Prelude> elem 5 [1..10]
usage:
            Prelude> elem "rat" ["fat", "cat", "sat", "flat"]
            False
error
            error :: String -> a
type:
description: applied to a string creates an error value with an associated message. Error values are equivalent
            to the undefined value (undefined), any attempt to access the value causes the program to
            terminate and print the string as a diagnostic.
definition:
            defined internally.
            error "this is an error message"
usage:
even
            even :: Integral a => a -> Bool
type:
description: applied to an integral argument, returns True if the argument is even, and False otherwise.
            even n = n rem 2 == 0
definition:
            Prelude> even 2
usage:
            True
            Prelude> even (11 * 3)
            False
exp
            exp :: Floating a => a -> a
type:
description: the exponential function (exp n is equivalent to e<sup>n</sup>).
definition:
            defined internally.
usage:
            Prelude> exp 1
            2.71828
filter
type:
            filter :: (a -> Bool) -> [a] -> [a]
description: applied to a predicate and a list, returns a list containing all the elements from the argument list
            that satisfy the predicate.
            filter p xs = [k \mid k < -xs, p k]
definition:
            Prelude> filter isDigit "fat123cat456"
usage:
            "123456"
flip
            flip :: (a \rightarrow b \rightarrow c) \rightarrow b \rightarrow a \rightarrow c
type:
description: applied to a binary function, returns the same function with the order of the arguments reversed.
definition:
            flip f x y = f y x
usage:
            Prelude> flip elem [1..10] 5
            True
floor
            floor :: (RealFrac a, Integral b) => a -> b
type:
description: returns the largest integer not greater than its argument.
            Prelude> floor 3.8
usage:
            Prelude> floor (-3.8)
```

```
-4
see also:
            ceiling
foldl
type:
            foldl :: (a \rightarrow b \rightarrow a) \rightarrow a \rightarrow [b] \rightarrow a
description: folds up a list, using a given binary operator and a given start value, in a left associative manner.
            foldl op r [a, b, c] \rightarrow ((r `op` a) `op` b) `op` c
definition:
            foldl f z [] = z
            foldl f z (x:xs) = foldl f (f z x) xs
            Prelude> foldl (+) 0 [1..10]
usage:
            55
            Prelude > fold1 (flip (:)) [] [1..10]
            [10, 9, 8, 7, 6, 5, 4, 3, 2, 1]
fold11
            foldl1 :: (a \rightarrow a \rightarrow a) \rightarrow [a] \rightarrow a
type:
description: folds left over non-empty lists.
definition:
            foldl1 f (x:xs) = foldl f x xs
            Prelude> foldl1 max [1, 10, 5, 2, -1]
usage:
            10
foldr
            foldr :: (a -> b -> b) -> b -> [a] -> b
type:
description: folds up a list, using a given binary operator and a given start value, in a right associative manner.
            foldr op r [a, b, c] \rightarrow a 'op' (b 'op' (c 'op' r))
definition:
            foldr f z [] = z
            foldr f z (x:xs) = f x (foldr f z xs)
            Prelude> foldr (++) [] ["con", "cat", "en", "ate"]
usage:
            "concatenate"
foldr1
type:
            foldr1 :: (a -> a -> a) -> [a] -> a
description: folds right over non-empty lists.
definition:
            foldr1 f [x] = x
            foldr1 f (x:xs) = f x (foldr1 f xs)
usage:
            Prelude > foldr1 (*) [1..10]
            3628800
fromIntegral
            fromIntegral :: (Integral a, Num b) => a -> b
type:
description: Converts from an Integer or Int to a numeric type which is in the class Num.
            Prelude> (fromIntegral 1000000000)::Float
usage:
            1.0e+10
fst
type:
            fst :: (a, b) -> a
description: returns the first element of a two element tuple.
definition:
            fst(x,) = x
            Prelude> fst ("harry", 3)
usage:
```

```
"harry"
gcd
           gcd :: Integral a => a -> a -> a
type:
description: returns the greatest common divisor between its two integral arguments.
definition:
           gcd 0 0 = error "Prelude.gcd: gcd 0 0 is undefined"
           gcd x y = gcd' (abs x) (abs y)
                        where
                            gcd' x 0 = x
                            gcd' x y = gcd' y (x rem y)
           Prelude> gcd 2 10
usage:
           Prelude> gcd (-7) 13
head
type:
           head :: [a] -> a
description: returns the first element of a non-empty list. If applied to an empty list an error results.
definition:
           head (x:_) = x
           Prelude> head [1..10]
usage:
           Prelude> head ["this", "and", "that"]
           "this"
id
type:
           id :: a -> a
description: the identity function, returns the value of its argument.
definition:
           id x = x
usage:
           Prelude> id 12
           12
           Prelude> id (id "fred")
           "fred"
           Prelude (map id [1..10]) == [1..10]
           True
init
           init :: [a] -> [a]
type:
description: returns all but the last element of its argument list. The argument list must have at least one
           element. If init is applied to an empty list an error occurs.
definition:
           init[x] = []
           init (x:xs) = x : init xs
usage:
           Prelude> init [1..10]
           [1, 2, 3, 4, 5, 6, 7, 8, 9]
isAlpha
type:
           isAlpha :: Char -> Bool
description: applied to a character argument, returns True if the character is alphabetic, and False otherwise.
           [Import from Data.Char]
definition:
           isAlpha c = isUpper c | isLower c
           Prelude> isAlpha 'a'
usage:
           True
           Prelude> isAlpha '1'
```

```
False
isDigit
type:
            isDigit :: Char -> Bool
description: applied to a character argument, returns True if the character is a numeral, and False otherwise.
            [Import from Data.Char]
definition:
            isDigit c = c >= '0' \&\& c <= '9'
            Prelude> isDigit '1'
usage:
            True
            Prelude > isDigit 'a'
            False
isLower
            isLower :: Char -> Bool
type:
description: applied to a character argument, returns True if the character is a lower case alphabetic, and False
            otherwise. [Import from Data.Char]
            isLower c = c >= 'a' && c <= 'z'
definition:
            Prelude> isLower 'a'
usage:
            True
            Prelude> isLower 'A'
            False
            Prelude> isLower '1'
            False
isSpace
type:
            isSpace :: Char -> Bool
description: returns True if its character argument is a whitespace character and False otherwise. [Import from
            Data.Char]
            isSpace c = c == ' ' || c == '\t' || c == '\n' || c == '\r' || c == '\r' || c == '\v'
definition:
            Prelude> dropWhile isSpace " \nhello \n"
usage:
            "hello \n"
isUpper
type:
            isUpper :: Char -> Bool
description: applied to a character argument, returns True if the character is an upper case alphabetic, and
            False otherwise. [Import from Data.Char]
            isUpper c = c >= 'A' && c <= 'Z'
definition:
            Prelude> isUpper 'A'
usage:
            True
            Prelude> isUpper 'a'
            False
            Prelude> isUpper '1'
            False
iterate
            iterate :: (a -> a) -> a -> [a]
type:
description: iterate \sim f \sim x returns the infinite list [x, \sim f(x), \sim f(f(x)), \sim ...].
definition:
            iterate f x = x : iterate f (f x)
usage:
            Prelude> iterate (+1) 1
            [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ....
```

```
last
           last :: [a] -> a
type:
description: applied to a non-empty list, returns the last element of the list.
definition:
           last[x] = x
           last ( :xs) = last xs
           Prelude> last [1..10]
usage:
lcm
           lcm :: Integral a => a -> a
type:
description: returns the least common multiple of its two integral arguments.
           1cm 0 = 0
definition:
           lcm 0 = 0
           lcm x y = abs ((x \cdot quot \cdot gcd x y) * y)
           Prelude> lcm 2 10
usage:
           Prelude> lcm 2 11
           22
length
           length :: [a] -> Int
type:
description: returns the number of elements in a finite list.
           length [] = 0
definition:
           length (x:xs) = 1 + length xs
           Prelude> length [1..10]
usage:
           10
lines
           lines :: String -> [String]
type:
description: applied to a list of characters containing newlines, returns a list of lists by breaking the original
           list into lines using the newline character as a delimiter. The newline characters are removed
           from the result.
definition:
           lines [] = []
           lines (x:xs)
              = 1 : 1s
              where
              (1, xs') = break (== '\n') (x:xs)
                   xs' == [] = []
                   otherwise = lines (tail xs')
           Prelude> lines "hello world\nit's me,\neric\n"
usage:
           ["hello world", "it's me,", "eric"]
log
           log :: Floating a => a -> a
type:
description: returns the natural logarithm of its argument.
definition:
           defined internally.
           Prelude> log 1
usage:
           0.0
           Prelude> log 3.2
           1.16315
```

```
map
            map :: (a \rightarrow b) \rightarrow [a] \rightarrow [b]
type:
description: given a function, and a list of any type, returns a list where each element is the result of applying
            the function to the corresponding element in the input list.
            map f xs = [f x | x < -xs]
definition:
            Prelude > map sqrt [1..5]
usage:
            [1.0, 1.41421, 1.73205, 2.0, 2.23607]
max
            max :: Ord a => a -> a -> a
type:
description: applied to two values of the same type which have an ordering defined upon them, returns the
            maximum of the two elements according to the operator >=.
definition:
            max x y
                 x >= y = x
                 otherwise = y
            Prelude> max 1 2
usage:
maximum
            maximum :: Ord a \Rightarrow [a] \rightarrow a
type:
description: applied to a non-empty list whose elements have an ordering defined upon them, returns the
            maximum element of the list.
            maximum xs = foldl1 max xs
definition:
usage:
            Prelude > maximum [-10, 0, 5, 22, 13]
min
            min :: Ord a => a -> a -> a
type:
description: applied to two values of the same type which have an ordering defined upon them, returns the
            minimum of the two elements according to the operator <=.
definition:
            min x y
                 x \le y = x
                 otherwise = y
            Prelude> min 1 2
usage:
minimum
type:
            minimum :: Ord a \Rightarrow [a] \rightarrow a
description: applied to a non-empty list whose elements have an ordering defined upon them, returns the
            minimum element of the list.
definition:
            minimum xs = foldl1 min xs
            Prelude > minimum [-10, 0, 5, 22, 13]
usage:
            -10
mod
            mod :: Integral a => a -> a -> a
type:
description: returns the modulus of its two arguments.
definition:
            defined internally.
            Prelude> 16 `mod` 9
usage:
            7
```

```
not
            not :: Bool -> Bool
type:
description: returns the logical negation of its boolean argument.
definition:
            not True = False
            not False = True
            Prelude > not (3 == 4)
usage:
            True
            Prelude > not (10 > 2)
            False
notElem
            notElem :: Eq a \Rightarrow a \rightarrow [a] \rightarrow Bool
type:
description: returns True if its first argument is not an element of the list as its second argument.
            Prelude> 3 `notElem` [1,2,3]
usage:
            False
            Prelude> 4 `notElem` [1,2,3]
null
            null :: [a] -> Bool
type:
description: returns True if its argument is the empty list ([]) and False otherwise.
definition:
            null [] = True
            null (\underline{:}\underline{)} = False
            Prelude> null []
usage:
            True
            Prelude > null (take 3 [1..10])
            False
odd
            odd :: Integral a => a -> Bool
type:
description: applied to an integral argument, returns True if the argument is odd, and False otherwise.
definition:
            odd = not \cdot even
            Prelude> odd 1
usage:
            Prelude > odd (2 * 12)
            False
or
            or :: [Bool] -> Bool
type:
description: applied to a list of boolean values, returns their logical disjunction (see also <u>and</u>).
            or xs = foldr(||) False xs
definition:
usage:
            Prelude> or [False, False, True, False]
            True
            Prelude> or [False, False, False, False]
            False
            Prelude> or []
            False
ord
            ord :: Char -> Int
type:
description: applied to a character, returns its ascii code as an integer. [Import from Data.Char]
```

```
definition:
            defined internally.
            Prelude> ord 'A'
usage:
            Prelude> (chr (ord 'A')) == 'A'
            True
see also:
           chr
pi
           pi :: Floating a => a
type:
description: the ratio of the circumference of a circle to its diameter.
            defined internally.
definition:
usage:
            Prelude> pi
            3.14159
            Prelude > cos pi
            -1.0
pred
type:
           pred :: Enum a => a -> a
description: applied to a value of an enumerated type returns the predecessor (previous value in the
            enumeration) of its argument. If its argument is the first value in an enumeration an error will
            occur.
            Prelude> pred 1
usage:
            Prelude> pred True
            False
putStr
type:
           putStr :: String -> IO ()
description: takes a string as an argument and returns an I/O action as a result. A side-effect of applying
            putStr is that it causes its argument string to be printed to the screen.
definition:
           defined internally.
            Prelude> putStr "Hello World\nI'm here!"
usage:
            Hello World
            I'm here!
product
           product :: Num a => [a] -> a
type:
description: applied to a list of numbers, returns their product.
definition:
           product xs = foldl(*) 1 xs
            Prelude> product [1..10]
usage:
            3628800
quot
            quot :: Integral a => a -> a
type:
description: returns the quotient after dividing the its first integral argument by its second integral argument.
definition:
            defined internally.
            Prelude> 16 `quot` 8
usage:
            Prelude> quot 16 9
            1
```

rem

```
rem :: Integral a => a -> a
type:
description: returns the remainder after dividing its first integral argument by its second integral argument.
definition:
           defined internally.
           Prelude> 16 `rem` 8
usage:
           Prelude> rem 16 9
notes:
           The following equality holds:
           (x \cdot quot \cdot y)*y + (x \cdot rem \cdot y) == x
repeat
type:
           repeat :: a -> [a]
description: given a value, returns an infinite list of elements the same as the value.
definition:
           repeat x
              = xs
              where xs = x:xs
           Prelude> repeat 12
usage:
           replicate
type:
           replicate :: Int -> a -> [a]
description: given an integer (positive or zero) and a value, returns a list containing the specified number of
           instances of that value.
definition:
           replicate n x = \underline{take} n (\underline{repeat} x)
           Prelude> replicate 3 "apples"
usage:
           ["apples", "apples", "apples"]
reverse
           reverse :: [a] -> [a]
type:
description: applied to a finite list of any type, returns a list of the same elements in reverse order.
definition:
           reverse = <u>foldl</u> (flip (:)) []
usage:
           Prelude> reverse [1..10]
           [10, 9, 8, 7, 6, 5, 4, 3, 2, 1]
round
           round :: (RealFrac a, Integral b) => a -> b
type:
description: rounds its argument to the nearest integer.
           Prelude> round 3.2
usage:
           Prelude> round 3.5
           Prelude> round (-3.2)
           -3
show
type:
           show :: Show a => a -> String
description: converts a value (which must be a member of the Show class), to its string representation.
definition:
           defined internally.
usage:
           Prelude> "six plus two equals " ++ (show (6 + 2))
           "six plus two equals 8"
```

```
sin
            sin :: Floating a => a -> a
type:
description: the trigonometric sine function, arguments are interpreted to be in radians.
definition:
            defined internally.
            Prelude> sin (pi/2)
usage:
            Prelude > ((\sin pi)^2) + ((\cos pi)^2)
            1.0
snd
type:
            snd :: (a, b) -> b
description: returns the second element of a two element tuple.
definition:
            snd(_, y) = y
usage:
            Prelude > snd ("harry", 3)
sort
            sort :: Ord a => [a] -> [a]
type:
description: sorts its argument list in ascending order. The items in the list must be in the class Ord. [Import
           from Data.List]
            List> sort [1, 4, -2, 8, 11, 0]
usage:
            [-2,0,1,4,8,11]
span
            span :: (a -> Bool) -> [a] -> ([a],[a])
type:
description: given a predicate and a list, splits the list into two lists (returned as a tuple) such that elements in
            the first list are taken from the head of the list while the predicate is satisfied, and elements in the
            second list are the remaining elements from the list once the predicate is not satisfied.
definition:
            span p [] = ([],[])
            span p xs@(x:xs')
                p x = (x:ys, zs)
                otherwise = ([],xs)
                 where (ys,zs) = span p xs'
            Prelude> span isDigit "123abc456"
usage:
            ("123", "abc456")
splitAt
type:
            splitAt :: Int -> [a] -> ([a],[a])
description: given an integer (positive or zero) and a list, splits the list into two lists (returned as a tuple) at
            the position corresponding to the given integer. If the integer is greater than the length of the list,
            it returns a tuple containing the entire list as its first element and the empty list as its second
            element.
definition:
            splitAt 0 xs = ([],xs)
            splitAt _ [] = ([],[])
            splitAt n (x:xs)
               | n > 0 = (x:xs',xs'')
                 where
                 (xs',xs'') = splitAt (n-1) xs
            splitAt _ _ = error "PreludeList.splitAt: negative argument"
            Prelude> splitAt 3 [1..10]
usage:
            ([1, 2, 3], [4, 5, 6, 7, 8, 9, 10])
```

```
Prelude> splitAt 5 "abc"
            ("abc", "")
sqrt
            sqrt :: Floating a => a -> a
type:
description: returns the square root of a number.
definition:
            sqrt x = x ** 0.5
usage:
            Prelude> sqrt 16
            4.0
subtract
            subtract :: Num a => a -> a -> a
type:
description: subtracts its first argument from its second argument.
definition:
            subtract = flip (-)
            Prelude> subtract 7 10
usage:
succ
            succ :: Enum a => a -> a
type:
description: applied to a value of an enumerated type returns the successor (next value in the enumeration) of
            its argument. If its argument is the last value in an enumeration an error will occur.
definition:
            defined internally.
usage:
            Prelude> succ 'a'
            'b'
            Prelude> succ False
            True
sum
            sum :: Num a => [a] -> a
type:
description: computes the sum of a finite list of numbers.
            sum xs = foldl (+) 0 xs
definition:
usage:
            Prelude> sum [1..10]
            55
tail
            tail :: [a] -> [a]
type:
description: applied to a non-empty list, returns the list without its first element.
definition:
            tail (:xs) = xs
usage:
            Prelude> tail [1,2,3]
            [2,3]
            Prelude> tail "hugs"
            "ugs"
take
type:
            take :: Int -> [a] -> [a]
description: applied to an integer (positive or zero) and a list, returns the specified number of elements from
            the front of the list. If the list has less than the required number of elements, take returns the
            entire list.
            take 0 _ = []
definition:
            take _ []= []
            take n (x:xs)
```

```
| n > 0 = x : take (n-1) xs
            take = error "PreludeList.take: negative argument"
           Prelude> take 4 "goodbye"
usage:
            "good"
           Prelude> take 10 [1,2,3]
            [1,2,3]
takeWhile
           takewhile :: (a \rightarrow Bool) \rightarrow [a] \rightarrow [a]
type:
description: applied to a predicate and a list, returns a list containing elements from the front of the list while
           the predicate is satisfied.
definition:
           takeWhile p [] = []
            takeWhile p (x:xs)
                p x = x : takeWhile p xs
                otherwise = []
           Prelude> takeWhile (<5) [1, 2, 3, 10, 4, 2]
usage:
            [1, 2, 3]
tan
           tan :: Floating a => a -> a
type:
description: the trigonometric function tan, arguments are interpreted to be in radians.
definition:
           defined internally.
           Prelude> tan (pi/4)
usage:
            1.0
toLower
type:
           toLower :: Char -> Char
description: converts an uppercase alphabetic character to a lowercase alphabetic character. If this function is
           applied to an argument which is not uppercase the result will be the same as the argument
           unchanged. [Import from Data.Char]
definition:
           toLower c
                isUpper c = toEnum (fromEnum c - fromEnum 'A' + fromEnum 'a')
                otherwise = c
           Prelude> toLower 'A'
usage:
            'a'
           Prelude> toLower '3'
            '3'
toUpper
type:
           toUpper :: Char -> Char
description: converts a lowercase alphabetic character to an uppercase alphabetic character. If this function is
           applied to an argument which is not lowercase the result will be the same as the argument
           unchanged. [Import from Data.Char]
definition:
           toUpper c
                isLower c = toEnum (fromEnum c - fromEnum 'a' + fromEnum 'A')
                otherwise = c
           Prelude> toUpper 'a'
usage:
            'A'
           Prelude> toUpper '3'
```

truncate

```
truncate :: (RealFrac a, Integral b) => a -> b
type:
description: drops the fractional part of a floating point number, returning only the integral part.
           Prelude> truncate 3.2
usage:
           Prelude> truncate (-3.2)
undefined
           undefined :: a
type:
description: an undefined value. It is a member of every type.
definition:
           undefined
               | False = undefined
unlines
type:
           unlines :: [String] -> String
description: converts a list of strings into a single string, placing a newline character between each of them. It
           is the converse of the function lines.
definition:
           unlines xs
              = concat (map addNewLine xs)
              where
              addNewLine l = l ++ "\n"
           Prelude> unlines ["hello world", "it's me,", "eric"]
usage:
            "hello world\nit's me,\neric\n"
until
           until :: (a -> Bool) -> (a -> a) -> a -> a
type:
description: given a predicate, a unary function and a value, it recursively re--applies the function to the value
           until the predicate is satisfied. If the predicate is never satisfied until will not terminate.
definition:
            until p f x
              | p x = x
                otheriwise = until p f (f x)
           Prelude> until (>1000) (*2) 1
usage:
            1024
unwords
           unwords :: [String] -> String
type:
description: concatenates a list of strings into a single string, placing a single space between each of them.
definition:
           unwords[] = []
            unwords ws
              = foldr1 addSpace ws
              where
              addSpace w s = w ++ (' ':s)
           Prelude> unwords ["the", "quick", "brown", "fox"]
usage:
            "the quick brown fox"
words
           words :: String -> [String]
type:
description: breaks its argument string into a list of words such that each word is delimited by one or more
            whitespace characters.
definition:
           words s
                findSpace == [] = []
                otherwise = w : words s''
```

```
where
                (w, s'') = break isSpace findSpace
               findSpace = dropWhile isSpace s
             Prelude> words "the quick brown\n\nfox"
usage:
             ["the", "quick", "brown", "fox"]
zip
type:
             zip :: [a] -> [b] -> [(a,b)]
description: applied to two lists, returns a list of pairs which are formed by tupling together corresponding
             elements of the given lists. If the two lists are of different length, the length of the resulting list is
            that of the shortest.
definition:
             zip xs ys
               = zipWith pair xs ys
               where
               pair x y = (x, y)
            Prelude> zip [1..6] "abcd"
usage:
             [(1, 'a'), (2, 'b'), (3, 'c'), (4, 'd')]
zipWith
             zipWith :: (a \rightarrow b \rightarrow c) \rightarrow [a] \rightarrow [b] \rightarrow [c]
type:
description: applied to a binary function and two lists, returns a list containing elements formed be applying
             the function to corresponding elements in the lists.
definition:
             zipWith z (a:as) (b:bs) = z a b : zipWith z as bs
             zipWith _ _ _ = []
            Prelude> zipWith (+) [1..5] [6..10]
usage:
             [7, 9, 11, 13, 15]
(!!)
description: given a list and a number, returns the element of the list whose position is the same as the
            number.
            Prelude> [1..10] !! 0
usage:
             Prelude> "a string" !! 3
            the valid subscripts for a list 1 are: 0 .. (length 1) - 1. Therefore, negative subscripts are not
notes:
             allowed, nor are subsripts greater than one less than the length of the list argument. Subscripts
             out of this range will result in a program error.
(.)
description: composes two functions into a single function.
usage:
             Prelude > (sqrt . sum ) [1,2,3,4,5]
             3.87298
             (f.g.h) x is equivalent to f(g(h x)).
notes:
(**)
description: raises its first argument to the power of its second argument. The arguments must be in the
            Floating numerical type class, and the result will also be in that class.
            Prelude> 3.2**pi
usage:
             38.6345
(\Lambda)
description: raises its first argument to the power of its second argument. The first argument must be a
             member of the Num type class, and the second argument must be a member of the Integral type
```

```
Prelude> 3.2<sup>4</sup>
usage:
             104.858
(\Lambda\Lambda)
description: raises its first argument to the power of its second argument. The first argument must be a
             member of the Fractional type class, and the second argument must be a member of the
             Integral type class. The result will be of the same type as the first argument.
             Prelude> 3.142^^4
usage:
             97.4596
(\%)
description: takes two numbers in the Integral type class and returns the most simple ratio of the two.
             Prelude> 20 % 4
usage:
             5 % 1
             Prelude> (5 % 4)^2
             25 % 16
(*)
description: returns the multiple of its two arguments.
             Prelude> 6 * 2.0
usage:
             12.0
(/)
description: returns the result of dividing its first argument by its second. Both arguments must in the type
             class Fractional.
             Prelude> 12.0 / 2
usage:
             6.0
(+)
description: returns the addition of its arguments.
             Prelude> 3 + 4
usage:
             Prelude> (4 % 5) + (1 % 5)
             1 % 1
(-)
description: returns the substraction of its second argument from its first.
             Prelude> 4 - 3
usage:
             Prelude> 4 - (-3)
(:)
description: prefixes an element onto the front of a list.
usage:
             Prelude> 1:[2,3]
             [1,2,3]
             Prelude> True:[]
             [True]
             Prelude> 'h': "askell"
             "haskell"
(++)
description: appends its second list argument onto the end of its first list argument.
```

class. The result will be of the same type as the first argument.

```
Prelude> [1,2,3] ++ [4,5,6]
usage:
            [1,2,3,4,5,6]
            Prelude> "foo " ++ "was" ++ " here"
            "foo was here"
(/=)
description: is True if its first argument is not equal to its second argument, and False otherwise. Equality is
            defined by the == operator. Both of its arguments must be in the Eq type class.
usage:
            Prelude> 3 /= 4
            True
            Prelude> [1,2,3] /= [1,2,3]
            False
(==)
description: is True if its first argument is equal to its second argument, and False otherwise. Equality is
            defined by the == operator. Both of its arguments must be in the Eq
            Prelude> 3 == 4
usage:
            False
            Prelude> [1,2,3] == [1,2,3]
            True
(<)
description: returns True if its first argument is strictly less than its second argument, and False otherwise.
            Both arguments must be in the type class ord.
            Prelude> 1 < 2
usage:
            True
            Prelude> 'a' < 'z'
            True
            Prelude> True < False
            False
(==)
description: returns True if its first argument is less than or equal to its second argument, and False
            otherwise. Both arguments must be in the type class ord.
            Prelude> 3 <= 4
usage:
            True
            Prelude> 4 <= 4
            True
            Prelude> 5 <= 4
            False
(>)
description: returns True if its first argument is strictly greater than its second argument, and False otherwise.
            Both arguments must be in the type class ord
usage:
            Prelude> 2 > 1
            True
            Prelude> 'a' > 'z'
            False
            Prelude> True > False
            True
(>=)
description: returns True if its first argument is greater than or equal to its second argument, and False
            otherwise. Both arguments must be in the type class ord.
```

usage: Prelude> 4 >= 3 True Prelude> 4 >= 4 True Prelude> 4 >= 5 False (&&)description: returns the logical conjunction of its two boolean arguments. Prelude> True && True usage: True Prelude> (3 < 4) && (4 < 5) && FalseFalse (||)description: returns the logical disjunction of its two boolean arguments. Prelude> True || False usage: True

Prelude> $(3 < 4) \mid \mid (4 > 5) \mid \mid$ False

True