

Aula 06 – Filtragem espacial I

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Roteiro



- Convolução e correlação
- Exemplo: Convolução



CONVOLUÇÃO E CORRELAÇÃO

Convolução e Correlação



Correlação

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$

	f(x,y)					
	0	1	2	3		
0	f(0, 0)	f(0, 1)	f(0, 2)			
1	f(1, 0)	f(1, 1)	f(1, 2)			
2	f(2, 0)	f(2, 1)	f(2, 2)			
3						

		w(s,t)	
	-1	0	1
-1	w(-1,-1)	w(-1, 0)	w(-1, 1)
0	w(0, -1)	w(0, 0)	w(0, 1)
1	w(1, -1)	w(1, 0)	w(1, 1)

Convolução e correlação





$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

Convolução

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$

f(x,y)

0

1

2

3

f(0, 0)	f(0, 1)	f(0, 2)	
---------	---------	---------	--

f(1, 0)	f(1, 1)	f(1, 2)	
---------	---------	---------	--

f(2, 0)	f(2, 1)	f(2, 2)	

|--|--|--|--|--|

w(s,t)

w(-1,-1) w(-1, 0) w(-1, 1)

w(0,-1) w(0,0) w(0,1)

w(1, -1) | w(1, 0) | w(1, 1

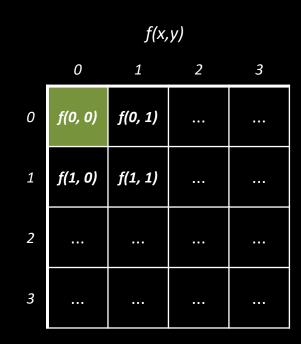
Convolução e correlação



Correlação

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$



		w(s,t)	
	-1	0	1
-1	w(-1,-1)	w(-1, 0)	w(-1, 1)
0	w(0, -1)	w(0, 0)	w(0, 1)
1	w(1, -1)	w(1, 0)	w(1, 1)

Convolução e correlação

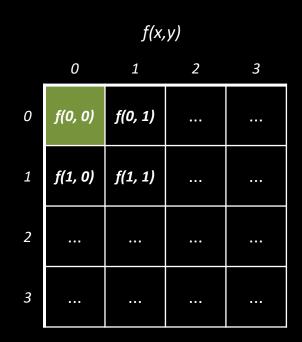


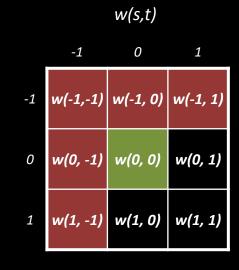
Correlação

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

Convolução

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$





padding



EXEMPLO: CONVOLUÇÃO



f(x,y)

	0	1	2	3
)	1	0	6	4
1	2	1	7	2
2	5	0	2	3
3	5	0	3	2

	,	w(s,t,)
	-1	0	1
-1	1	2	3
0	4	5	6
1	7	8	9



	f(x,y)					
		0	1	2	3	
	0	0	0	0	0	0
0	0	1	0	6	4	0
1	0	2	1	7	2	0
2	0	5	0	2	3	0
3	0	5	0	3	2	0
	0	0	0	0	0	0

	w(s,t)				
	-1	0	1		
1	1	2	3		
0	4	5	6		
1	7	8	9		

padding

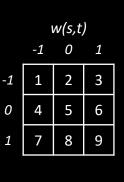


	f(x,y)					
		0	1	2	3	
	0	0	0	0	0	0
0	0	1	0	6	4	0
1	0	2	1	7	2	0
2	0	5	0	2	3	0
3	0	5	0	3	2	0
	0	0	0	0	0	0

	١	w(s,t,)
	-1	0	1
1	1	2	3
)	4	5	6
1	7	8	9



			f(x,	.y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	1	0	6	4	0
1	0	2	1	7	2	0
2	0	5	0	2	3	0
3	0	5	0	3	2	0
	0	0	0	0	0	0



			g(x	,y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	0	0	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

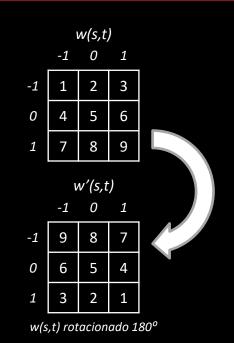


$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$

convolução



			f(x,	<i>y)</i>		
		0	1	2	3	
	0	0	0	0	0	0
0	0	1	0	6	4	0
1	0	2	1	7	2	0
2	0	5	0	2	3	0
3	0	5	0	3	2	0
	0	0	0	0	0	0

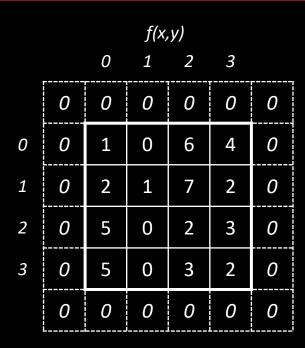


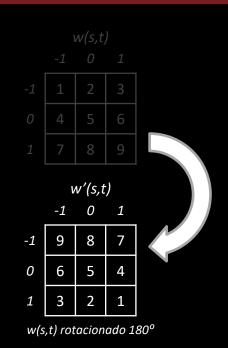
			g(x	(,y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	0	0	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

correlação





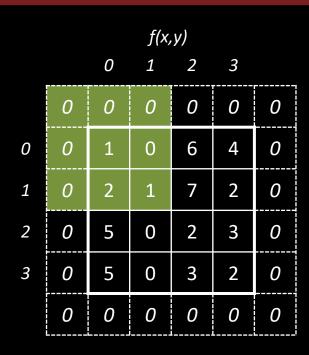


			g(x	,y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	0	0	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

correlação



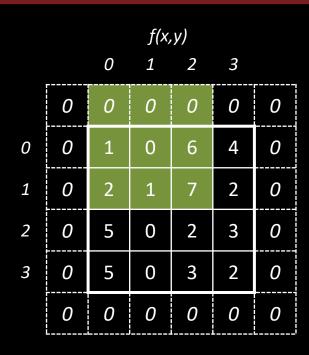


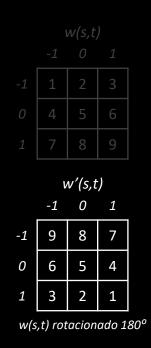
		w(s,t,		
	-1	0		
	1	2	3	
0	4	5	6	
	7	8	9	
	ı	v'(s,t	.)	
	-1	0	1	
-1				
-1 O	-1	0	1	
	-1 9	8	7	

			g(x	,y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	10	0	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t) = 0 \times 9 + 0 \times 8 + 0 \times 7 \\ 0 \times 6 + 1 \times 5 + 0 \times 4 \\ 0 \times 3 + 2 \times 2 + 1 \times 1 = 10$$



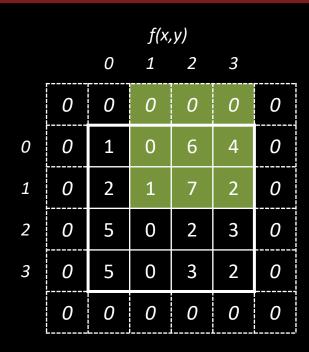




			g(x	,y)		
		0	1	2	3	
	0	0	0	0	0	0
0	0	10	45	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = 0 \times 9 + 0 \times 8 + 0 \times 7 + 1 \times 6 + 0 \times 5 + 6 \times 4 + 2 \times 3 + 1 \times 2 + 7 \times 1 = 45$$



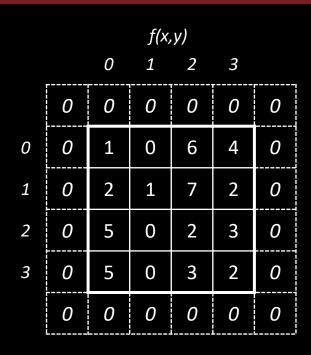


		w(s,t	
	-1	0	1
	1	2	3
0	4	5	6
	7	8	9
	V	v'(s,t)
	-1	0	1
-1	9	8	7
0	6	5	4
0	6	5	4

			g(x	<i>(,y)</i>		
		0	1	2	3	
	0	0	0	0	0	0
)	0	10	45	65	0	0
1	0	0	0	0	0	0
2		0	0	0	0	0
3	0	0	0	0	0	0
	0	0	0	0	0	0

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = 0 \times 9 + 0 \times 8 + 0 \times 7 + 0 \times 6 + 6 \times 5 + 4 \times 4 + 1 \times 3 + 7 \times 2 + 2 \times 1 = 65$$



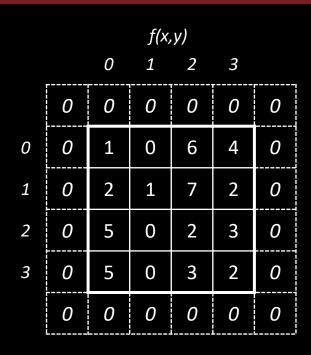


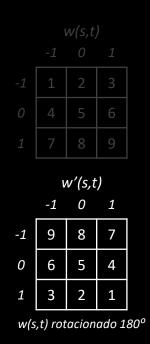
		N(s,t	
	-1	0	1
	1	2	3
0	4	5	6
	7	8	9
	V	v'(s,t)
	-1	0	1
-1	<i>-1</i>	8	7
-1 0			
	9	8	7

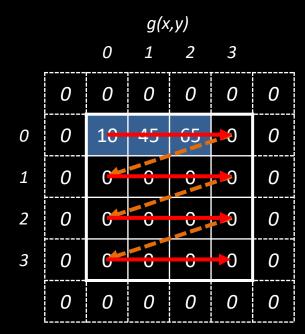
	g(x,y)							
		0	1	2	3			
	0	0	0	0	0	0		
0	0	10	45	65	0	0		
1	0	0	0	0	0	0		
2	0	0	0	0	0	0		
3	0	0	0	0	0	0		
	0	0	0	0	0	0		

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t) =$$









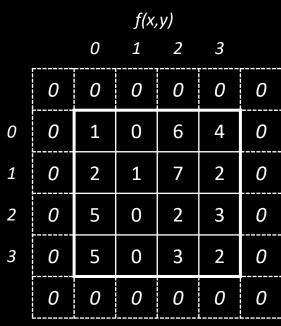
$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t) =$$



132 150

109 119

g(x,y)



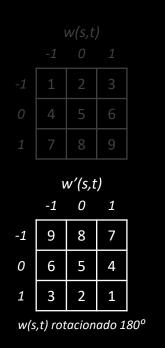
w(s,t)							
	-1	0	1				
	1	2	3				
0	4	5	6				
	7	8	9				
w'(s,t)							
	V	v (S,t)				
	-1	v (s,t 0	1				
-1							
-1 0	-1	0	1				
	-1 9	<i>0</i>	7				



g(x,y)

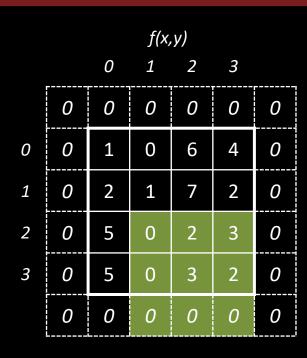
132 150

109 119



$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = \begin{cases} 5 \times 9 + 0 \times 8 + 2 \times 7 + \\ 5 \times 6 + 0 \times 5 + 3 \times 4 + \\ 0 \times 3 + 0 \times 2 + 0 \times 1 \end{cases} = 101$$

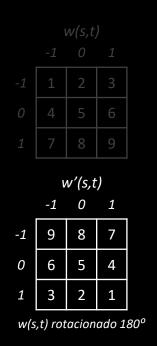




w(s,t)							
	-1	0	1				
	1	2	3				
0	4	5	6				
	7	8	9				
w'(s,t)							
	-1	0	1				
-1	9	8	7				
0	6	5	4				
1	3	2	1				
w(s,t) rotacionado 180°							

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = 0 \times 9 + 2 \times 8 + 3 \times 7 + 0 \times 6 + 3 \times 5 + 2 \times 4 + 0 \times 3 + 0 \times 2 + 0 \times 1 = 60$$





$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = \begin{cases} 2 \times 9 + 3 \times 8 + 0 \times 7 + \\ 3 \times 6 + 2 \times 5 + 0 \times 4 + \\ 0 \times 3 + 0 \times 2 + 0 \times 1 \end{cases} = 70$$



	f(x,y)						
		0	1	2	3		
	0	0	0	0	0	0	
0	0	1	0	6	4	0	
1	0	2	1	7	2	0	
2	0	5	0	2	3	0	
3	0	5	0	3	2	0	
	0	0	0	0	0	0	

w(s,t)							
	-1	0	1				
	1	2	3				
0	4	5	6				
	7	8	9				
w'(s,t)							
	-1	0	1				
-1	9	8	7				
0	6	5	4				
1	3	2	1				
w(s	t) rot	acion	ado 1				

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t)f(x+s,y+t) = \begin{cases} 2 \times 9 + 3 \times 8 + 0 \times 7 + \\ 3 \times 6 + 2 \times 5 + 0 \times 4 + \\ 0 \times 3 + 0 \times 2 + 0 \times 1 \end{cases} = 70$$



	f(x,y)						
		0	1	2	3		
	0	0	0	0	0	0	
0	0	1	0	6	4	0	
1	0	2	1	7	2	0	
2	0	5	0	2	3	0	
3	0	5	0	3	2	0	
	0	0	0	0	0	0	

		N(s,t	
		0	
	1	2	3
0	4	5	6
	7	8	9
		v'(s,t	.)
	V	v (3,1	/
	-1	0	1
-1			
-1 0	-1	0	1
	-1 9	<i>0</i>	7

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$



	w(s,t)						
		0					
		2	3				
0		5	6				
	7	8	9				
	V	v'(s,t)				
	-1	0	1				
-1	<i>-1</i> 9	8	7				
-1 0							

$$g(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x+s,y+t)$$

w(s,t) rotacionado 180º

	0	1	2	3
0	10	45	65	81
1	32	113	132	150
2	58	131	109	119
3	65	101	60	70

Bibliografia



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